

**Minimize[{x, x^2 + y^2 - 1 == 0}, {x, y}]**

**{-1, {x → -1, y → 0}}**

**Minimize[{Integrate[x^2, x], x^2 + y^2 - 1 == 0}, {x, y}]**

**{-1/3, {x → -1, y → 0}}**

**Minimize[{MarcumQ[1, x, x], x^2 + y^2 - 1 == 0}, {x, y}]**

Minimize::nint: Warning: Minimize used numeric integration to show that the result is a global minimum. >>

**{1/2 (1 + BesselI[0, 1]/e), {x → -1, y → 0}}**

**"Expected Rs"**

Out[3]= Expected Rs

In[5]:= **Simplify[Integrate[Log2[1 + x/nps] \* 1/Gamma[a] \*  
1/b^a x^(-a-1) Exp[-1/(b x)], {x, 0, Infinity}]]**

Out[5]= ConditionalExpression[  

$$\left( b^{-a} \left( \frac{1}{nps} \right)^a \left( \left( -\frac{1}{b nps} \right)^{-a} \pi \operatorname{Csc}[a \pi] \left( \operatorname{Gamma}[a] - \operatorname{Gamma}\left[a, -\frac{1}{b nps}\right] \right) + \right. \\ \left. \left( \frac{1}{b} \right)^{1-a} nps^{-1+a} \operatorname{Gamma}[-1+a] \operatorname{HypergeometricPFQ}\left[\{1, 1\}, \{2, 2-a\}, \frac{1}{b nps}\right] \right) \Bigg) / \\ (\operatorname{Gamma}[a] \operatorname{Log}[2]), \operatorname{Re}[a] > 0 \&\& (\operatorname{Arg}[nps] < \pi \mid \mid (\operatorname{Re}[nps] > 0 \&\& nps \in \operatorname{Reals})) \&\& \\ \left( \left( \frac{1}{nps} \in \operatorname{Reals} \&\& \operatorname{Re}\left[\frac{1}{nps}\right] > 0 \right) \mid \mid \operatorname{Abs}[\operatorname{Arg}[nps]] < \pi \right) \Bigg]$$

**"Density of a Inverse non central chi-squared distribution,  
where lambda is gamma distributed: Bessel function: Density  
of the regulated power at ST:Here the energy (that includes  
path loss, noise power, interference temp, normalization  
constant) is exponetially distributed: Working: Final version"**

In[7]:= **Simplify[Integrate[K \* it \* nc / (2 np x^2)  
Exp[-K / (2 np) (nc it/x + pl g tp)] (nc it / (x pl tp g))^(K/4 - 1/2)  
BesselI[K/2 - 1, sqrt(K^2 pl nc it tp g / (x np^2))] Exp[-g], {g, 0, Infinity}]]**

Out[7]= ConditionalExpression[  

$$\left( e^{-\frac{it K nc}{2 np x + K pl tp x}} (-2 + K) K np pl tp \left( 2 + \frac{K pl tp}{np} \right)^{K/2} \left( \frac{it nc}{pl tp x} \right)^{\frac{2+K}{4}} \left( \frac{it K^2 nc pl tp}{np^2 x} \right)^{\frac{1}{2} - \frac{K}{4}} \right. \\ \left. \left( \operatorname{Gamma}\left[-1 + \frac{K}{2}\right] - \operatorname{Gamma}\left[-1 + \frac{K}{2}, (it K^2 nc pl tp) / (4 np^2 x + 2 K np pl tp x)\right] \right) \right) / \\ \left( 2 (2 np + K pl tp)^2 x \operatorname{Gamma}\left[\frac{K}{2}\right] \right), \operatorname{Re}[K] < 6 \&\& \\ (\operatorname{Im}[\sqrt{((it K^2 nc pl tp) / (np^2 x))}] > 0 \mid \mid \operatorname{Re}[\sqrt{((it K^2 nc pl tp) / (np^2 x))}] > 0) \&\& \\ \operatorname{Re}\left[\frac{K pl tp}{np}\right] > -2 \Bigg]$$

"Determine the Density for power received at PR"

In[13]:=

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Simplify[Integrate[N / (2 np) K it g pl / x^2 Exp[-N pl g / (2 np) (1 / x + tp)]
  (K it / x)^(N/4 - 1/2) BesselI[N/2 - 1, N pl g / np sqrt(K it tp / x)]
  g^(a - 1) Exp[-g/b], {g, 0, Infinity}]]
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Out[13]= ConditionalExpression[

$$\left( 2^{-1+a} b N^2 p l \left( \frac{i t K}{x} \right)^{\frac{2+N}{4}} \left( (b^2 i t K N^2 p l^2 t p x) / (2 n p x + b N p l (1 + t p x))^2 \right)^{\frac{1}{4} (-2+N)} \right. \\ \left. \left( \frac{2}{b} + (N p l (1 + t p x)) / (n p x) \right)^{-a} \Gamma\left[a + \frac{N}{2}\right] \text{Hypergeometric2F1}\left[\frac{1}{4} (2 a + N), \right. \right. \\ \left. \left. \frac{1}{4} (2 + 2 a + N), \frac{N}{2}, (4 b^2 i t K N^2 p l^2 t p x) / (2 n p x + b N p l (1 + t p x))^2 \right] \right) /$$

$$\left( (2 n p x + b N p l (1 + t p x)) \Gamma\left[1 + \frac{N}{2}\right] \right), \text{Re}\left[\frac{N p l \sqrt{\frac{i t K t p}{x}}}{n p}\right] \geq 0 \ \&\&$$

$$\left( \text{Im}\left[\frac{N p l \sqrt{\frac{i t K t p}{x}}}{n p}\right] > 0 \ || \ \text{Re}\left[\frac{N p l \sqrt{\frac{i t K t p}{x}}}{n p}\right] > 0 \ \&\& \text{Re}[a] > -1 \ \&\& \text{Re}\left[a + \frac{N}{2}\right] > 0 \right)$$