1. Find the Z-transform of following sequences and plot their ROC

a)
$$x(n) = -\alpha^n u(-n-1)$$

b)
$$x(n) = \alpha^n u(n)$$

c)
$$x(n) = \alpha^n u(n) + b^n u(-n-1)$$

2. Find the Z-transform of

i)
$$x_1(n) = \cos(\omega_o n)u(n)$$

ii)
$$x_2(n) = \sin(\omega_0 n) u(n)$$

3. Prove *convolution* property of Z-transform

4. Using scaling property, find the Z-transform

i) Z
$$\mathbb{Z}\left\{a^n\cos\left(\omega_o n\right)u(n)\right\}$$

ii)
$$\mathbb{Z}\left\{a^n\sin\left(\omega_o n\right)u(n)\right\}$$

5. Using power series expansion method, find the inverse Z-transform $X(z) = \frac{1}{1 - az^{-1}}$ for case I) ROC -> |z| > |a| and case II ROC -> |z| < |a|