On Page 13 of Chapter 7: Survival Models, the course notes states (interpretation of m_x):

the denominator $\int_0^1 t p_x dt$ is interpreted as the expected amount of time spent alive between ages x and t by a life alive at age x...

I am unable to comprehend how can $\int_0^1 {}_t p_x dt$ be thought of as an expectation?