

# THE BINARY HEAP IMPLEMENTATION

THE LOGICAL STRUCTURE OF A BINARY HEAP IS A **TREE** - SO THEORETICALLY WE COULD REPRESENT A HEAP JUST AS WE WOULD A TREE

EACH NODE WOULD HAVE A POINTER TO THE LEFT AND RIGHT CHILD

THE OPERATIONS TYPICALLY PERFORMED ON A HEAP REQUIRES US TO:

1. TRAVERSE DOWNWARDS FROM THE ROOT TOWARDS THE LEAF NODES
2. TRAVERSE UPWARDS FROM THE LEAF NODES TOWARDS THE ROOT

ON A HEAP WE WANT TO BE ABLE TO:

GET LEFT CHILD

GET RIGHT CHILD

GET PARENT

# THE BINARY HEAP IMPLEMENTATION

GET LEFT CHILD

GET RIGHT CHILD

GET PARENT

A NODE WOULD NEED 2 CHILD  
POINTERS AND A PARENT  
POINTER

THIS IS A LOT OF EXTRA SPACE

HEAPS CAN BE REPRESENTED MUCH MORE  
EFFICIENTLY BY USING AN ARRAY AND  
HAVING AN IMPLICIT RELATIONSHIP TO  
DETERMINE THE PARENT, LEFT AND RIGHT  
CHILD OF A NODE

EVERY LEVEL OF THE BINARY  
TREE IN A HEAP IS FILLED EXCEPT  
PERHAPS THE LAST

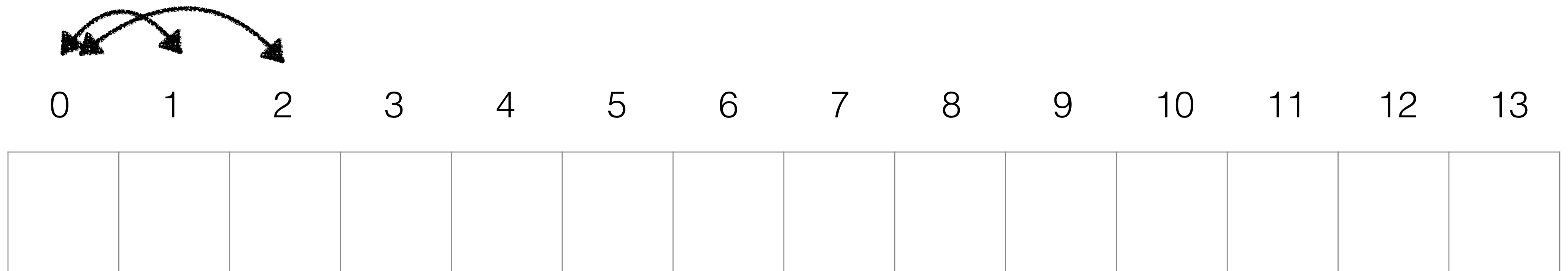
THIS MEANS CONTIGUOUS SLOTS  
IN AN ARRAY CAN BE USED TO  
REPRESENT BINARY TREE LEVELS

# THE BINARY HEAP IMPLEMENTATION

GET PARENT

NODE AT INDEX 0

LEFT CHILD AT INDEX 1  
RIGHT CHILD AT INDEX 2



NODE AT INDEX:  $i$

GET LEFT CHILD HAS A LEFT CHILD AT INDEX:  $2i + 1$

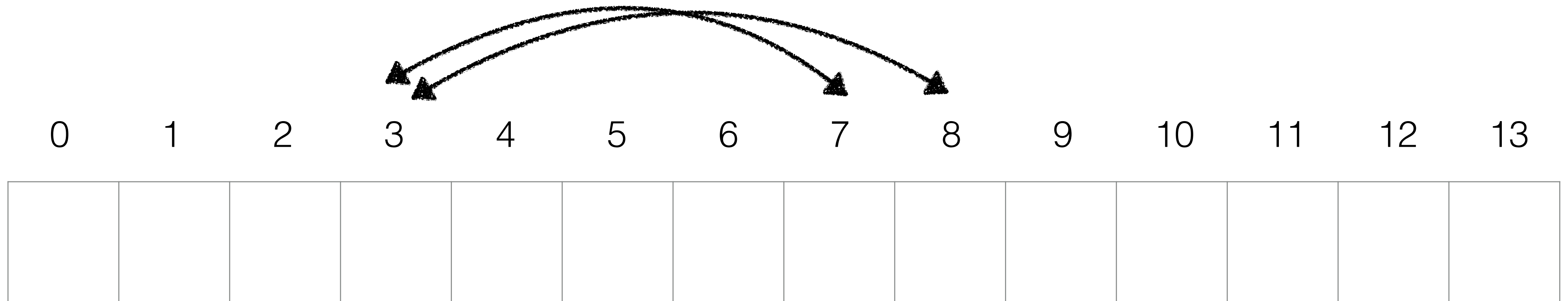
GET RIGHT CHILD HAS A RIGHT CHILD AT INDEX:  $2i + 2$

# THE BINARY HEAP IMPLEMENTATION

GET PARENT

NODE AT INDEX 3

LEFT CHILD AT INDEX 7  
RIGHT CHILD AT INDEX 8



NODE AT INDEX:  $i$

GET LEFT CHILD HAS A LEFT CHILD AT INDEX:  $2i + 1$

GET RIGHT CHILD HAS A RIGHT CHILD AT INDEX:  $2i + 2$

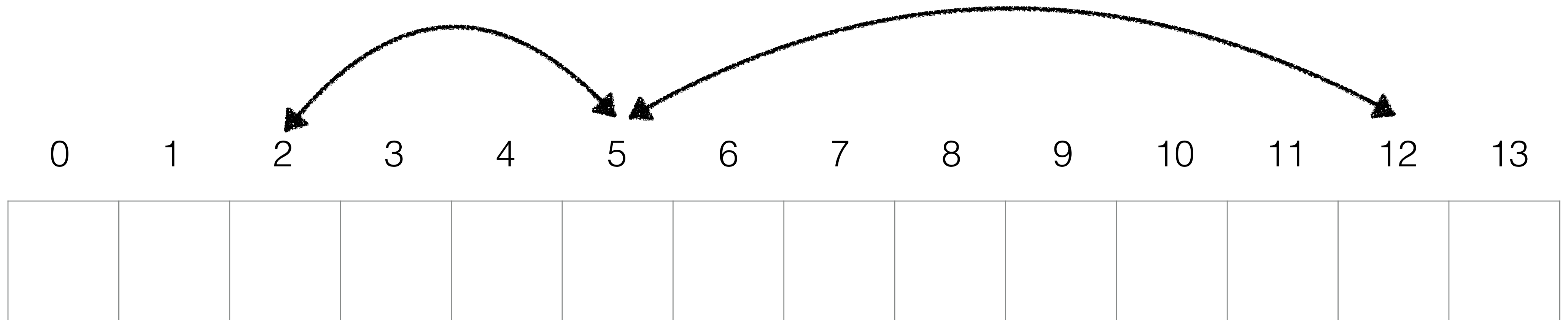
# THE BINARY HEAP IMPLEMENTATION

GET LEFT CHILD

GET RIGHT CHILD

NODE INDEX 5  
PARENT INDEX 2

NODE INDEX 12  
PARENT INDEX 5



NODE AT INDEX:  $i$

GET PARENT HAS PARENT AT INDEX:  $(i - 1) / 2$

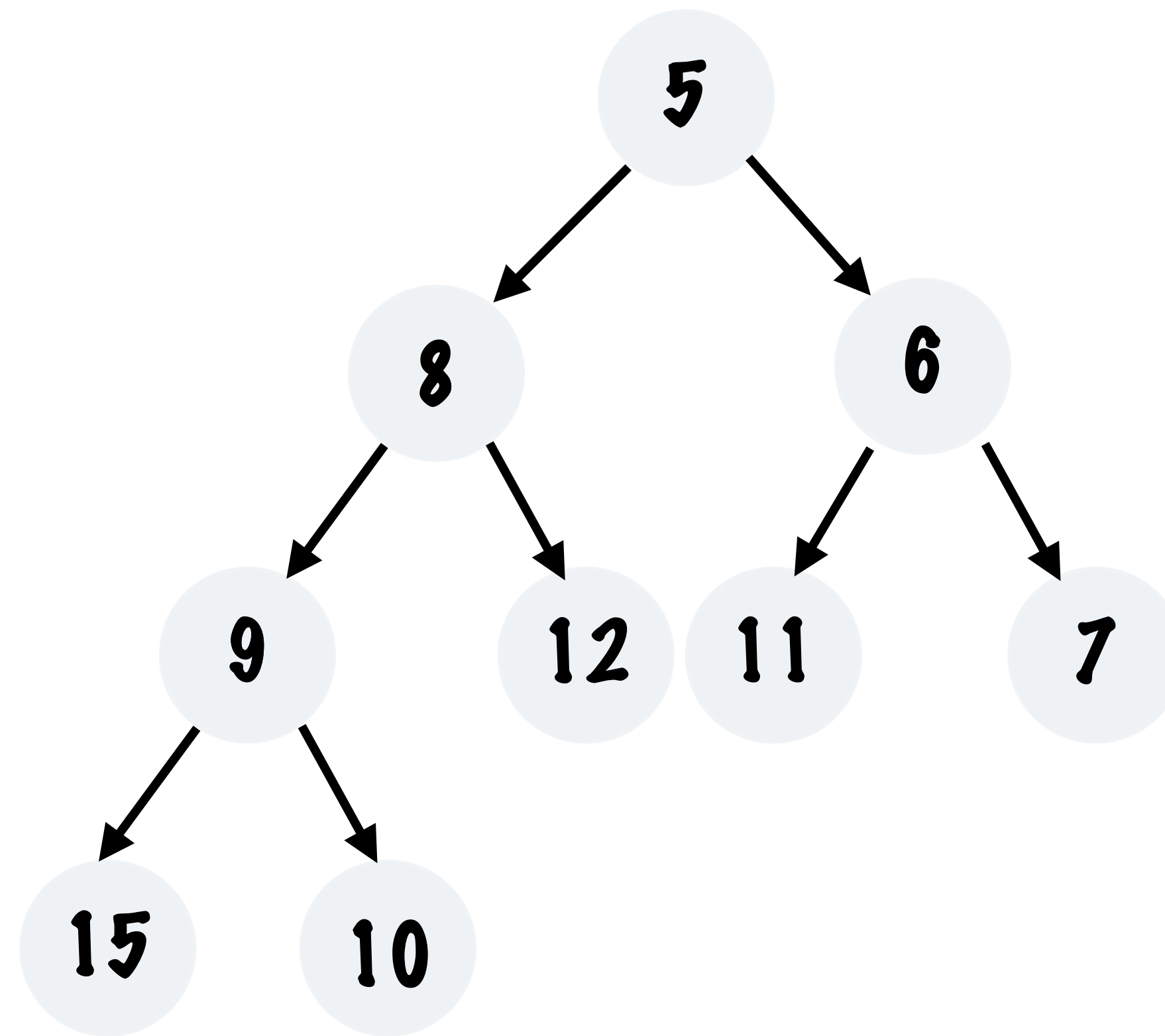


# THE BINARY HEAP IMPLEMENTATION

GET LEFT CHILD

GET RIGHT CHILD

GET PARENT

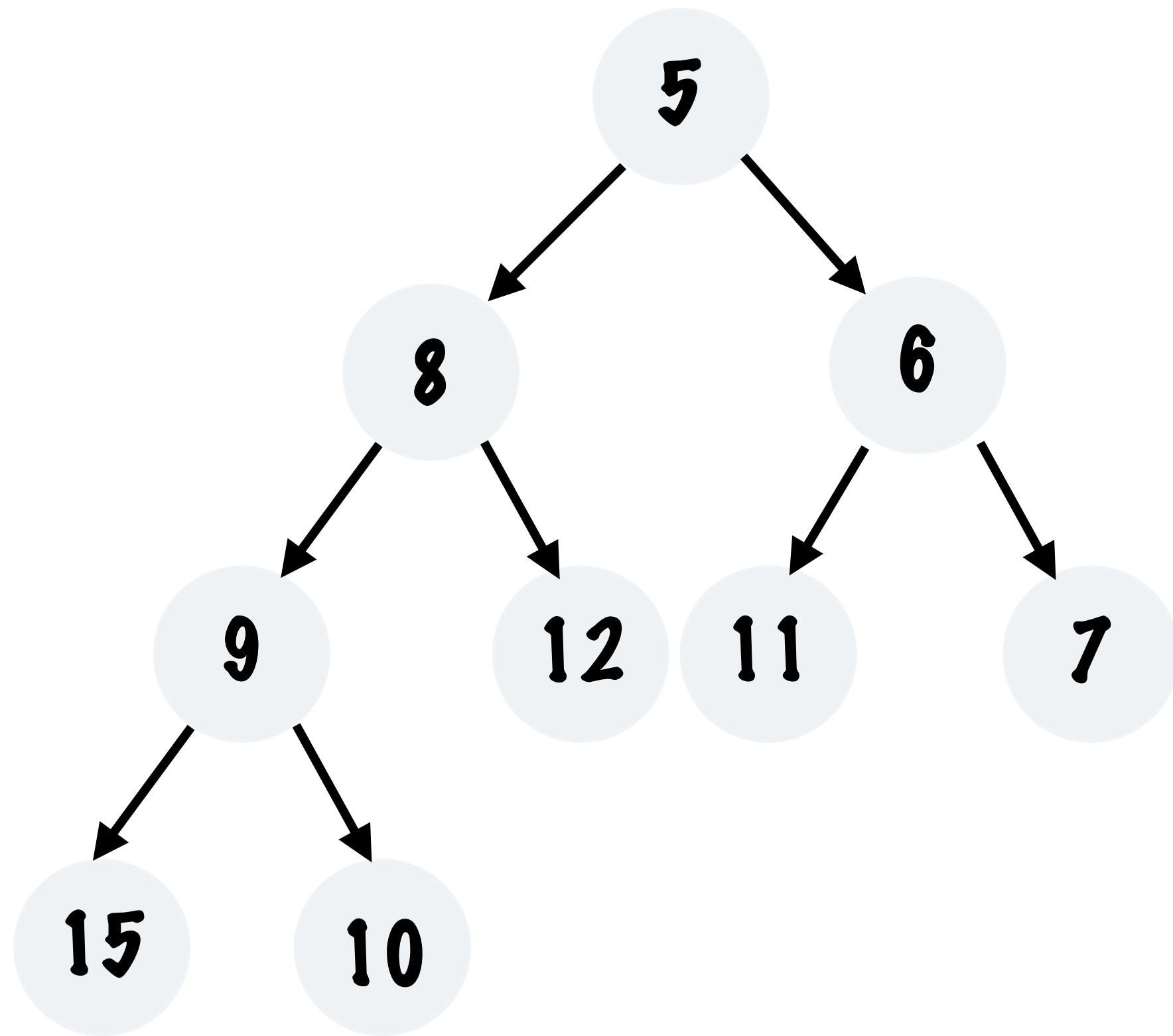


# THE BINARY HEAP IMPLEMENTATION

GET LEFT CHILD

GET RIGHT CHILD

GET PARENT

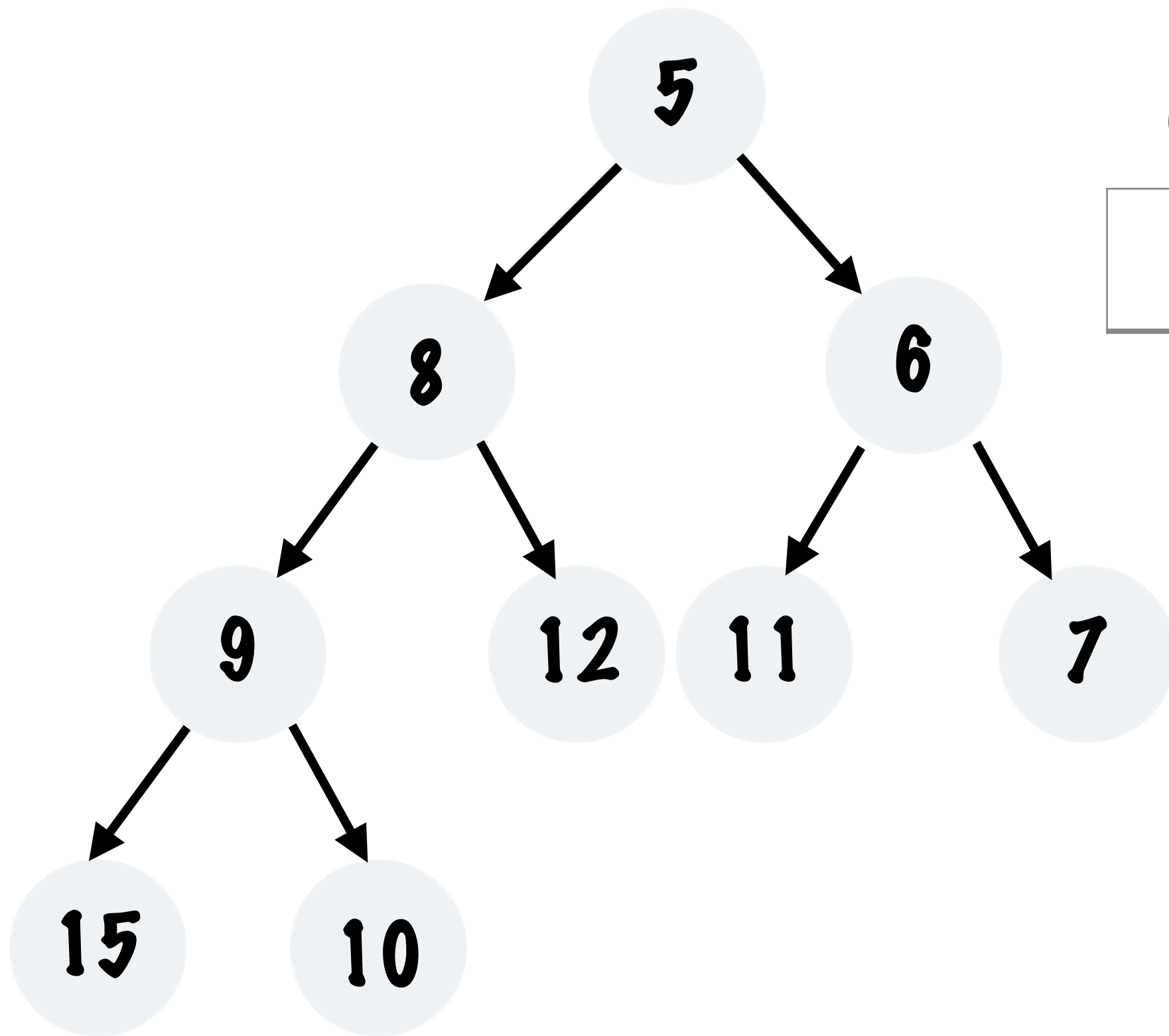


# THE BINARY HEAP IMPLEMENTATION

# GET LEFT CHILD

# GET RIGHT CHILD

# GET PARENT

[illegible]

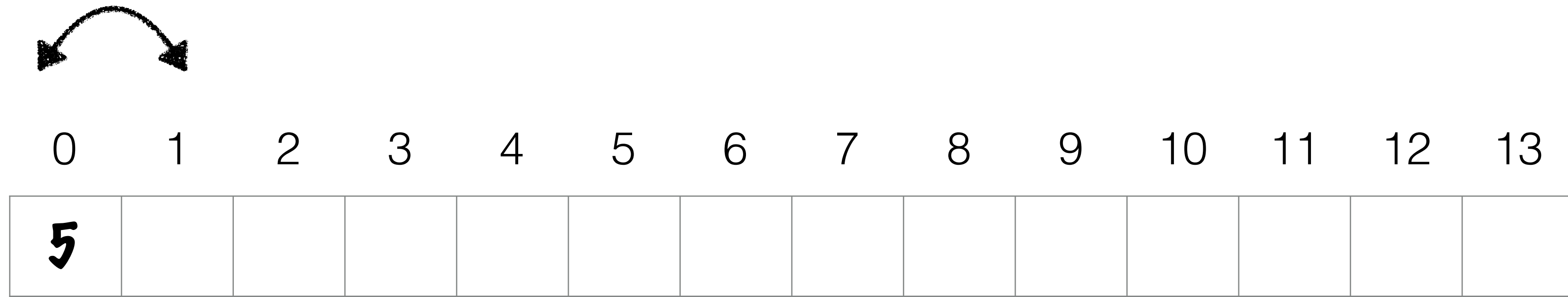
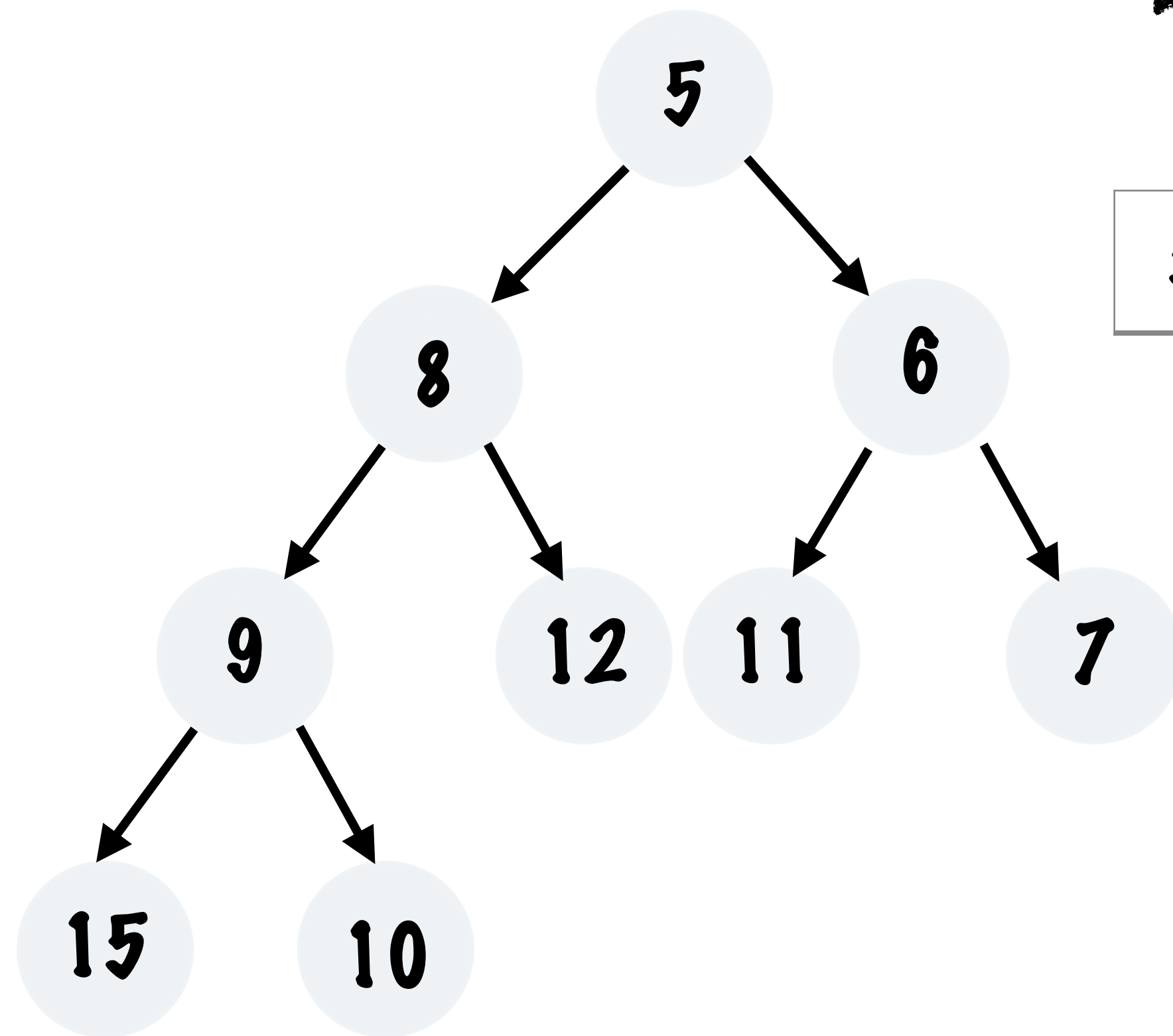


# THE BINARY HEAP IMPLEMENTATION

GET LEFT CHILD

GET RIGHT CHILD

GET PARENT



NODE AT INDEX:  $i$

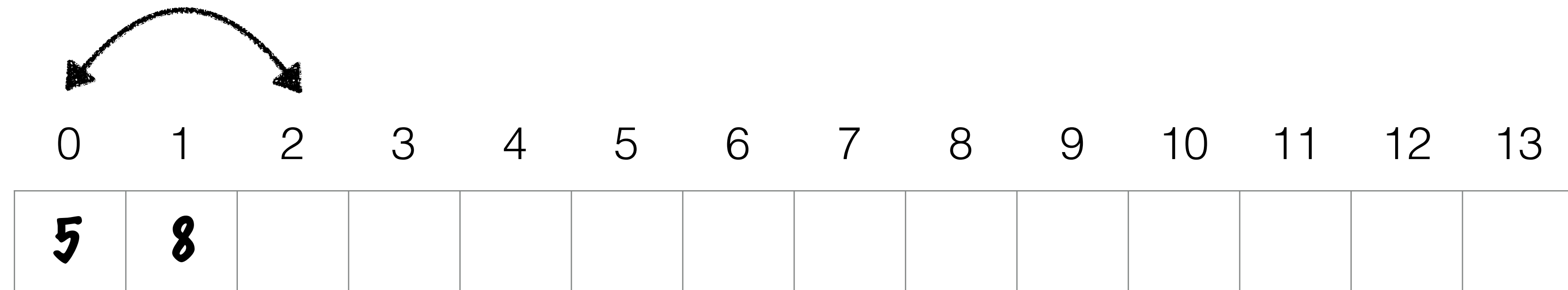
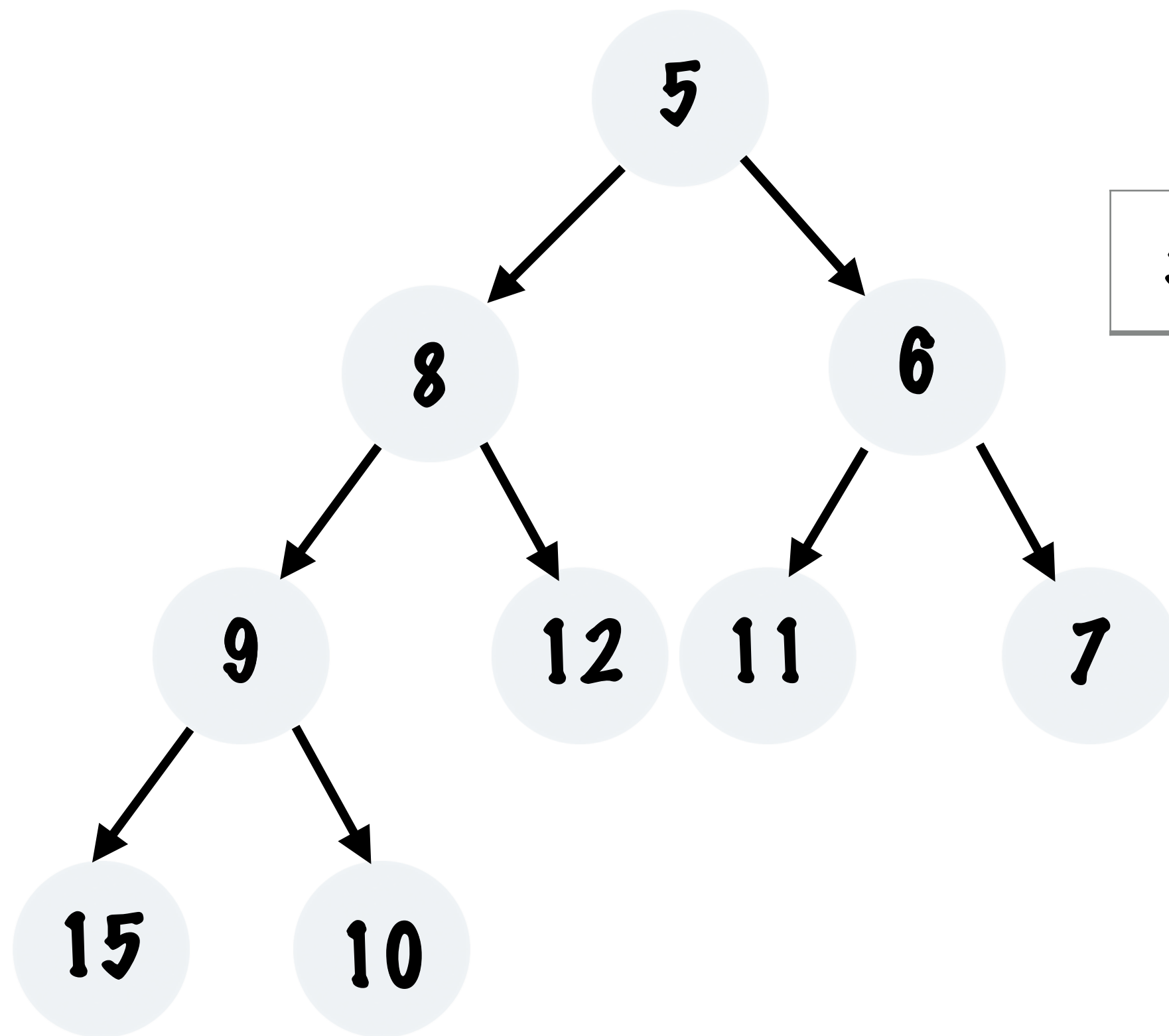
HAS A LEFT CHILD AT INDEX:  $2i + 1$

# THE BINARY HEAP IMPLEMENTATION

GET LEFT CHILD

GET RIGHT CHILD

GET PARENT



NODE AT INDEX:  $i$

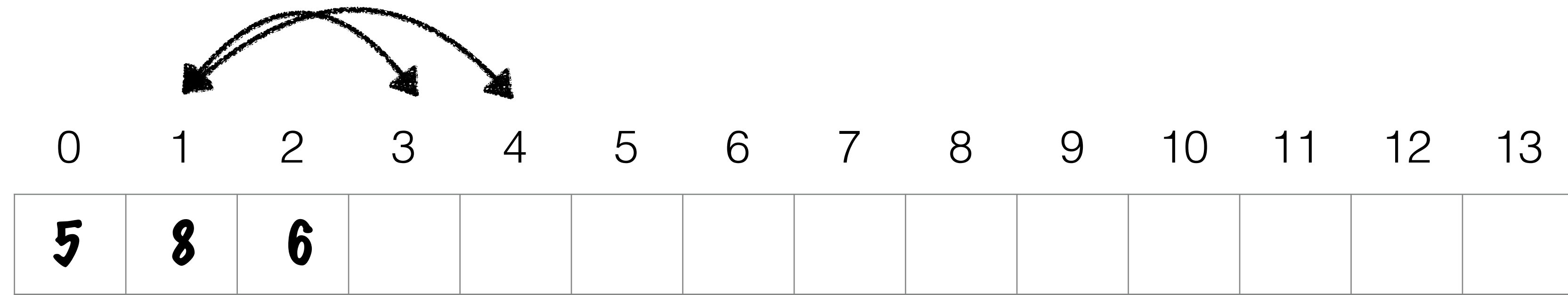
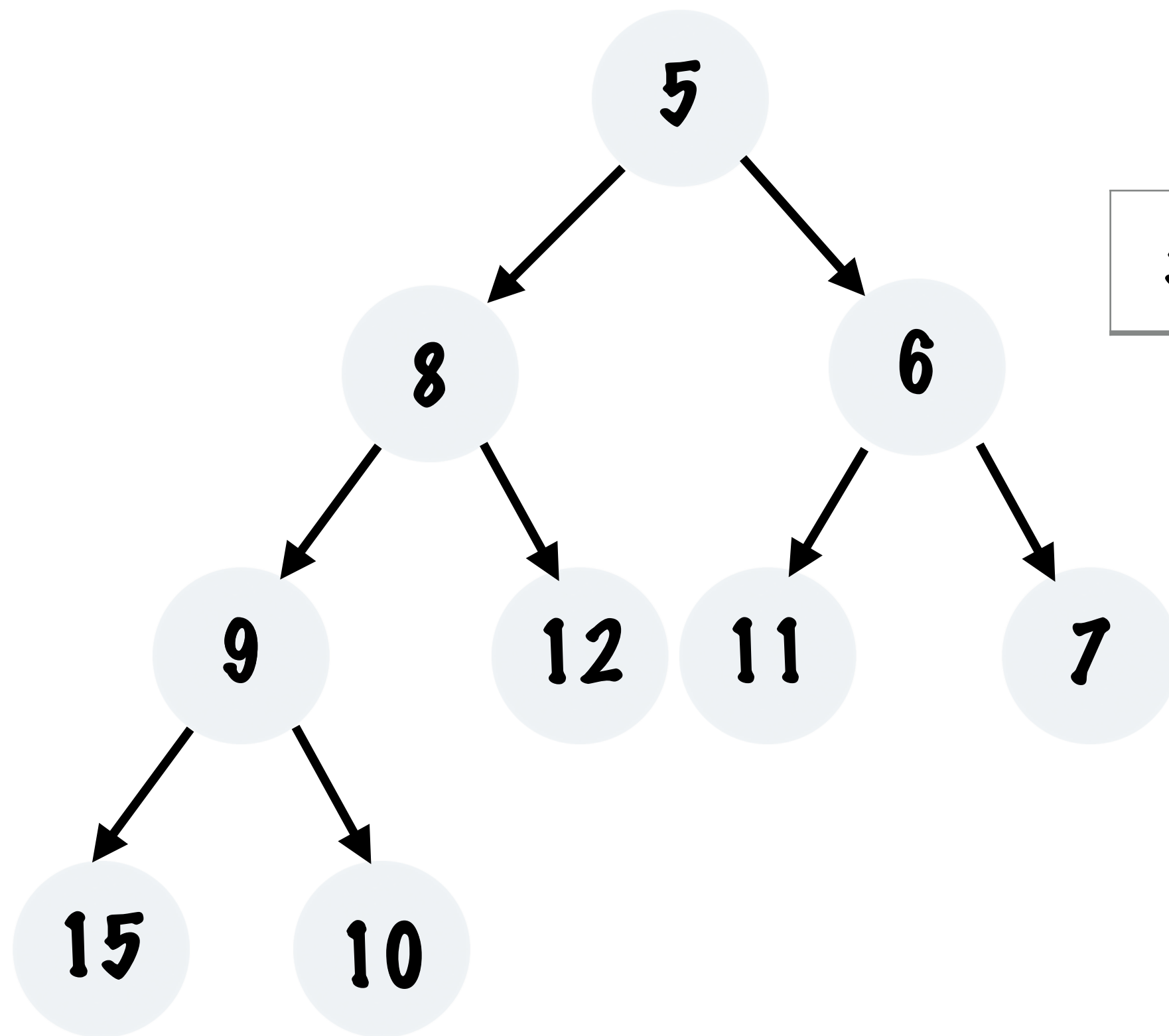
HAS A RIGHT CHILD AT INDEX:  $2i + 2$

# THE BINARY HEAP IMPLEMENTATION

GET LEFT CHILD

GET RIGHT CHILD

GET PARENT



NODE AT INDEX:  $i$

HAS A LEFT CHILD AT INDEX:  $2i + 1$

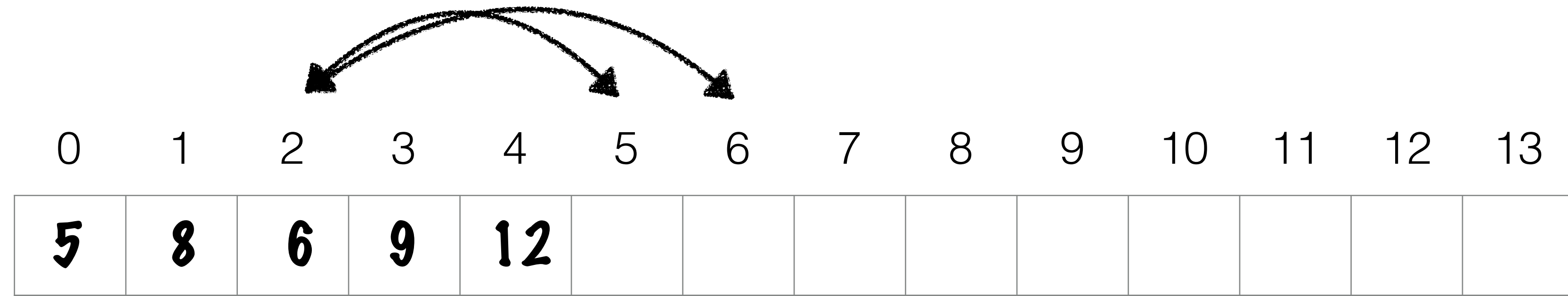
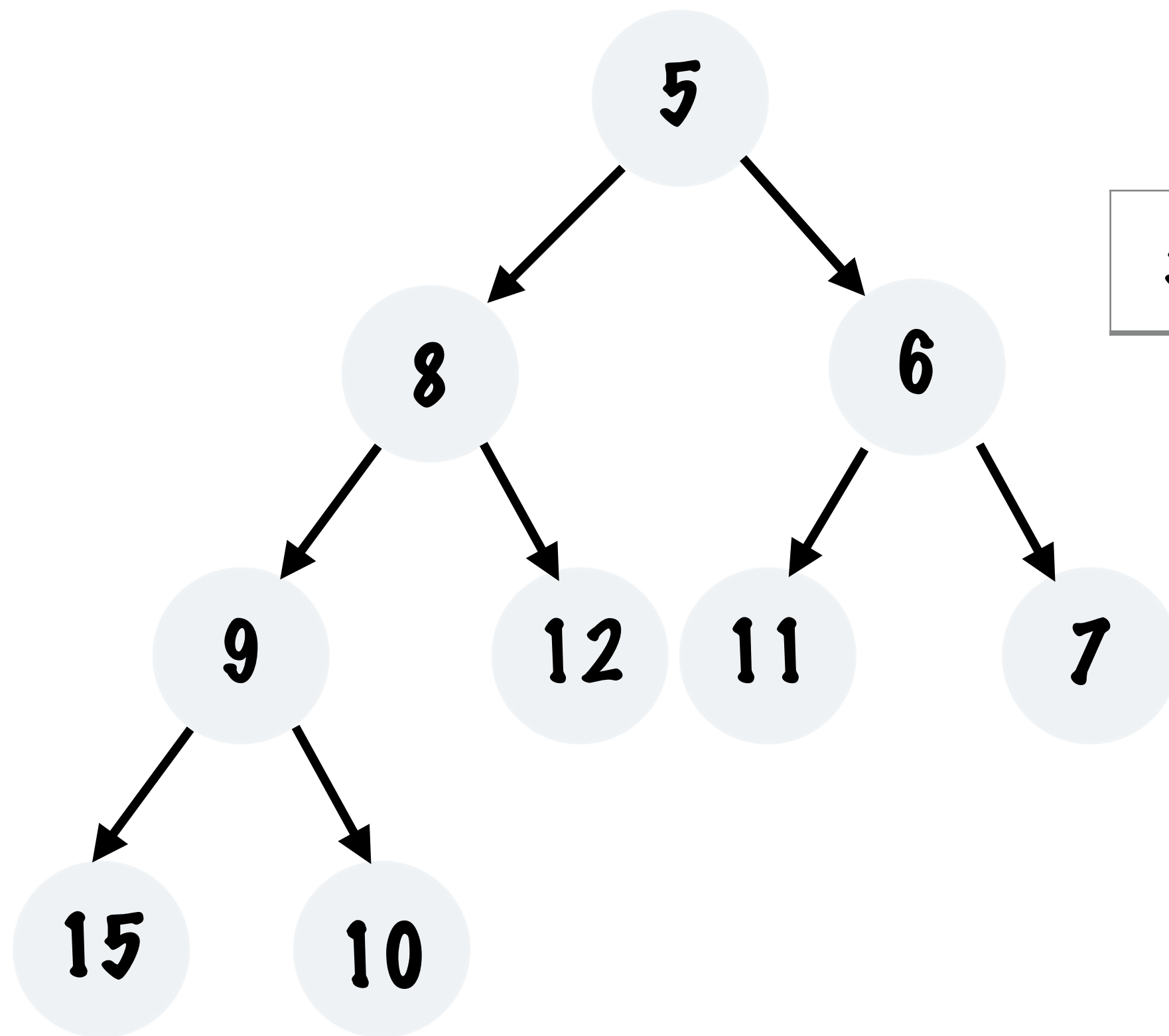
HAS A RIGHT CHILD AT INDEX:  $2i + 2$

# THE BINARY HEAP IMPLEMENTATION

GET LEFT CHILD

GET RIGHT CHILD

GET PARENT



NODE AT INDEX:  $i$

HAS A LEFT CHILD AT INDEX:  $2i + 1$

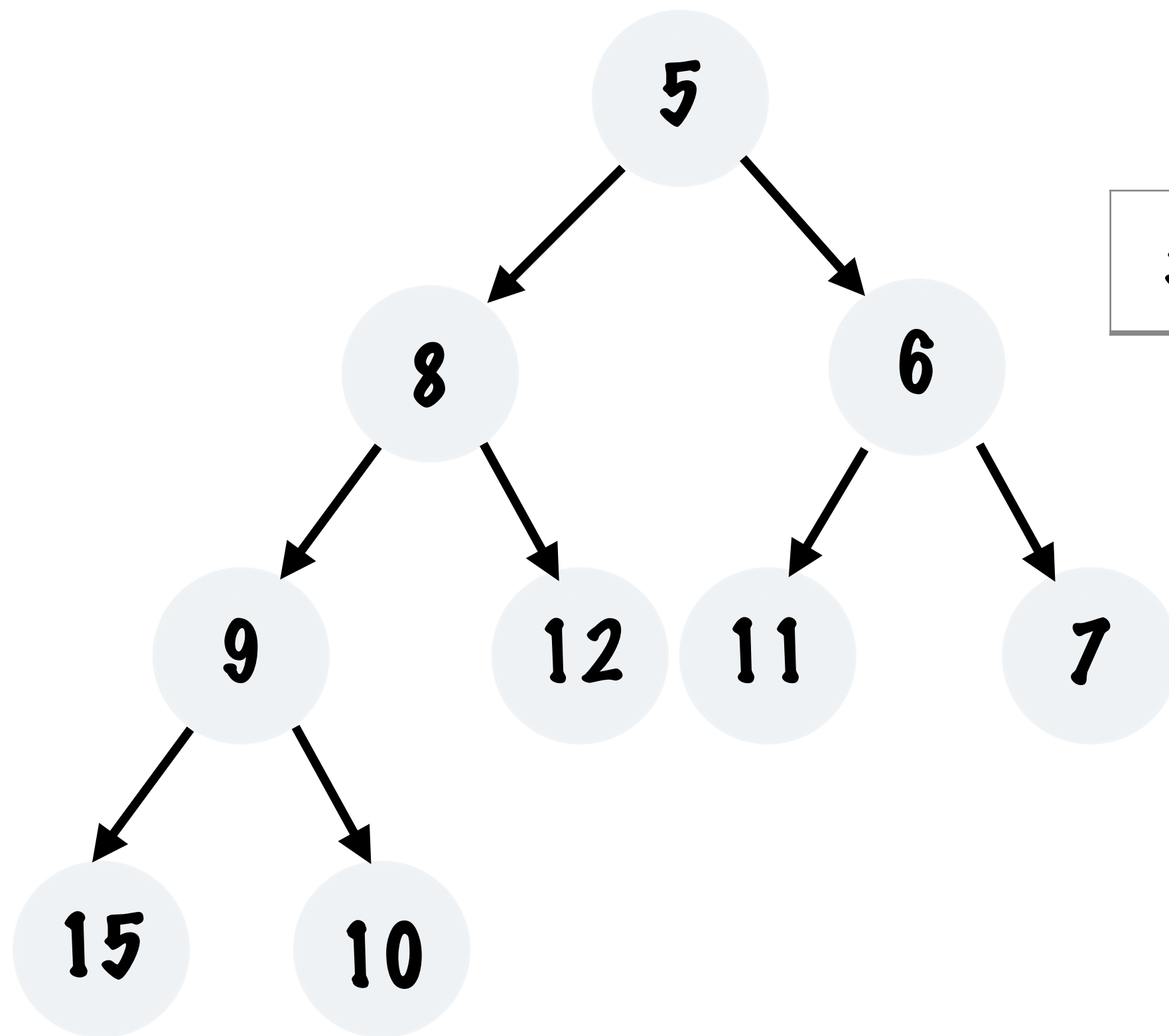
HAS A RIGHT CHILD AT INDEX:  $2i + 2$

# THE BINARY HEAP IMPLEMENTATION

GET LEFT CHILD

GET RIGHT CHILD

GET PARENT



0	1	2	3	4	5	6	7	8	9	10	11	12	13
5	8	6	9	12									

NODE AT INDEX:  $i$

HAS A LEFT CHILD AT INDEX:  $2i + 1$

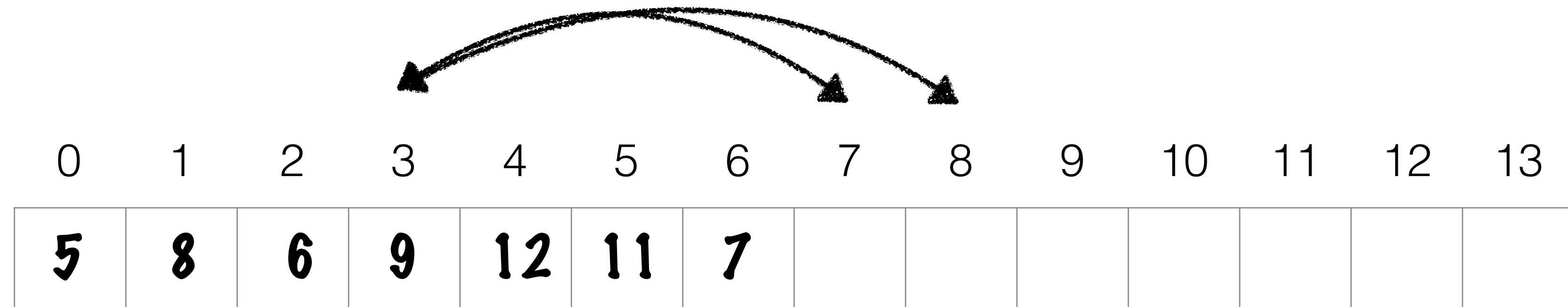
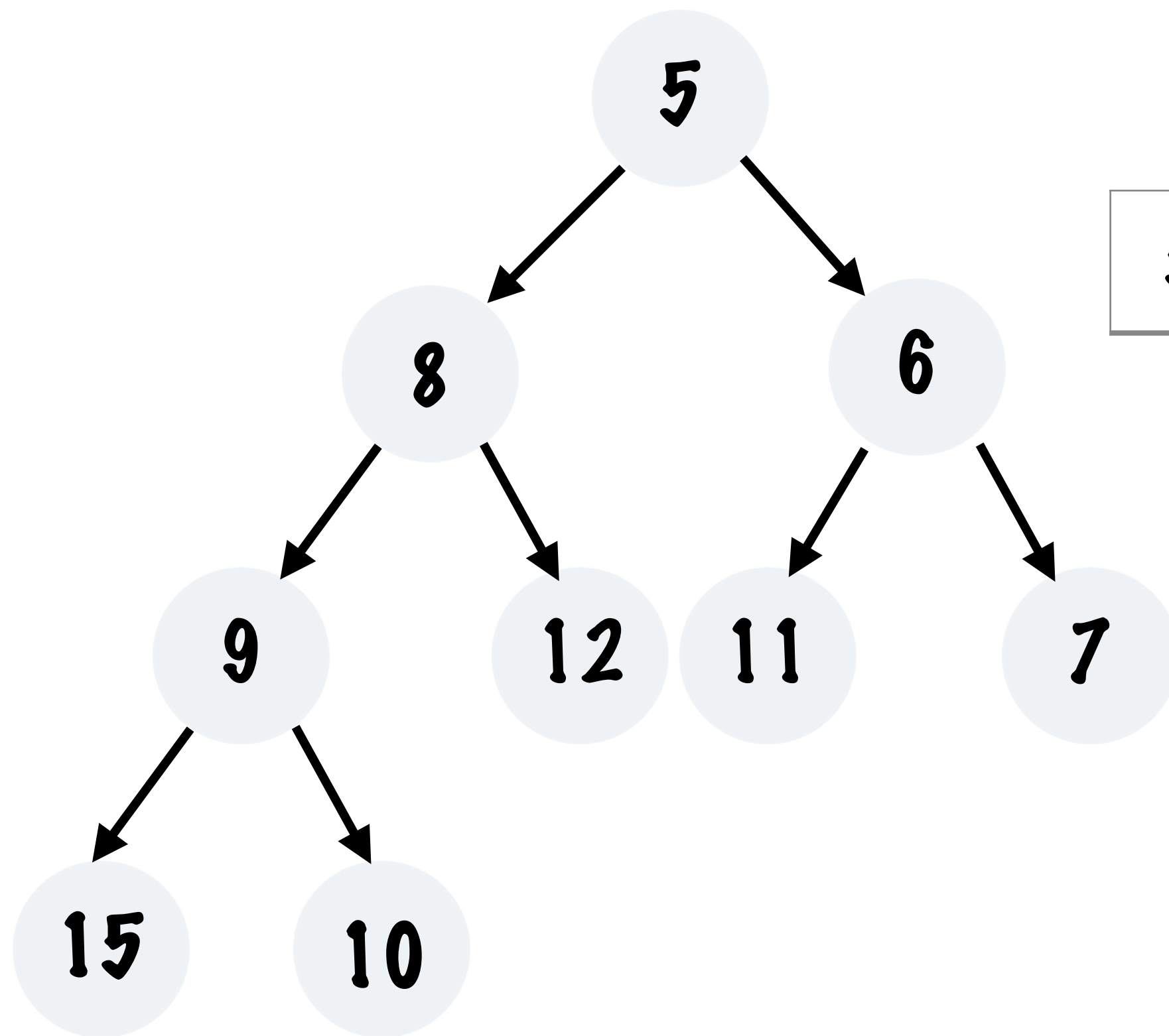
HAS A RIGHT CHILD AT INDEX:  $2i + 2$

# THE BINARY HEAP IMPLEMENTATION

GET LEFT CHILD

GET RIGHT CHILD

GET PARENT



NODE AT INDEX:  $i$

HAS A LEFT CHILD AT INDEX:  $2i + 1$

HAS A RIGHT CHILD AT INDEX:  $2i + 2$

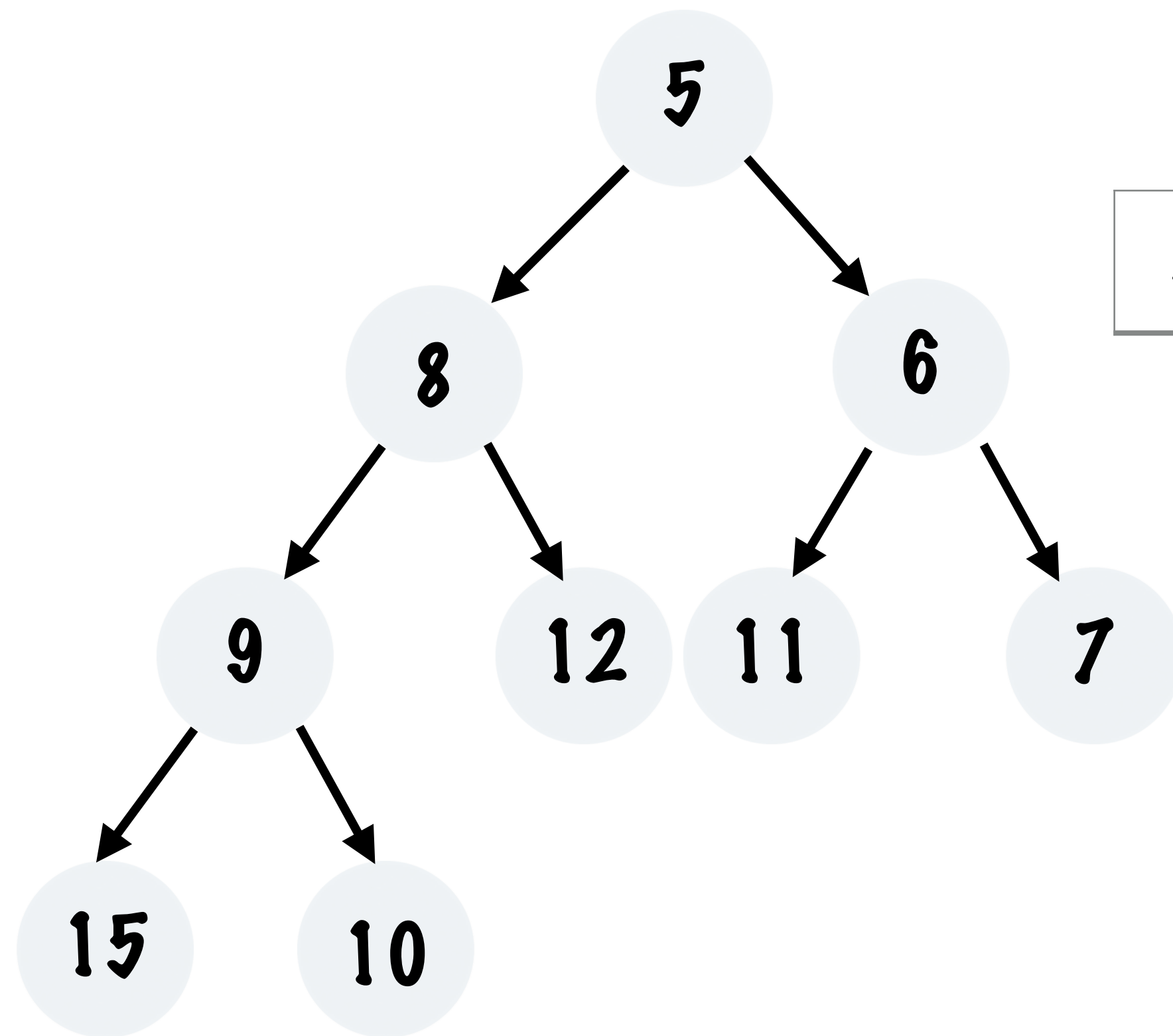


# THE BINARY HEAP IMPLEMENTATION

GET LEFT CHILD

GET RIGHT CHILD

GET PARENT



0	1	2	3	4	5	6	7	8	9	10	11	12	13
5	8	6	9	12	11	7	15	10					

NODE AT INDEX:  $i$

HAS A LEFT CHILD AT INDEX:  $2i + 1$

HAS A RIGHT CHILD AT INDEX:  $2i + 2$