

Q. Give a formula to predict the running time of a program for a problem of size N , when doubling experiments have shown that the doubling factor is 2^b and the running time for problems of size N_0 is T .

A. Given,

$f(N_0) = T$, where $f(N)$ is running time of algorithm with input size N

Also, given that

$$f(2N) = 2^b \cdot f(N/2)$$

$$\text{Therefore, } f(2N_0) = 2^b \cdot T$$

$$\text{or, } f(2^a \cdot N_0) = 2^{ab} \cdot T$$

$$\text{Now, let } N = 2^a \cdot N_0$$

$$\Rightarrow N/N_0 = 2^a$$

$$\Rightarrow f(N) = T \cdot (N/N_0)^b$$