

# DAA C-2 Assignment-1

Frequency of  $x$  in Sorted array using Divide and conquer algorithm.

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March 22, 2021

# Overview

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# Introduction

- Count number of occurrences (or frequency) of  $x$  in a given sorted array `arr[]` using divide and conquer algorithm.
- Divide and Conquer is an algorithm design paradigm in which we recursively break down a problem into two or more sub-problems of the same or related type, until these subproblems become simple enough to be solved directly.
- The solutions to the sub-problems are then combined to give a solution to the original problem.
- Binary search is a search algorithm that finds the position of a target value within a sorted array.
- Binary search compares the target value to the middle element of the array. If they are not equal, the half in which the target cannot lie is eliminated and the search continues on the remaining half, again taking the middle element to compare to the target value, and repeating this until the target value is found.

# Algorithm

## Algorithm Description

Since the array is sorted, all occurrences of  $x$  will be adjacent.

So, the steps used in this algorithm are :

- 1) Use Binary search to get index of the first occurrence of  $x$  in `arr[]`. Let the index of the first occurrence be  $i$ .
- 2) Use Binary search to get index of the last occurrence of  $x$  in `arr[]`. Let the index of the last occurrence be  $j$ .
- 3) Return  $(j - i + 1)$ ; //And This will be the frequency of  $x$ .

# Algorithm

## Algorithm Analysis

As the given array is already sorted so we will find the first occurrence of  $x$  in  $arr[]$  using the function `search()` by passing the array  $arr[]$  ,  $n$  i.e. size of array ,  $x$  and  $1$ .

If the returned value is  $-1$  that means the element is not present in array and we will stop our algorithm here and if it is not  $-1$  then we will find the last occurrence of  $x$  in array  $arr[]$  by using `search()` function again but this time we will pass  $0$  instead of  $1$  in `flg` value to get the last occurrence of  $x$ .

So, after getting the first and last occurrence of  $x$  in  $arr[]$  , the number of occurrence of  $x$  will be  $last - first + 1$ .

# Algorithm

## Pseudo Code

```
PSEUDO CODE for main() :  
int first = search(arr, n, x, 1);  
if (first != -1)  
int last = search(arr, n, x, 0);  
int count = last - first + 1;  
cout<<"Element " <<x<<" occurs " <<count<<" times.";  
else  
cout<<"Element not found in the array.";
```

# Algorithm

```
int low = 0;
int high = N - 1;
int result = -1;
while (low <= high) :
    int mid = (low + high)/2;
    if (x == arr[mid])
        result = mid;
        if (flg)
            high = mid - 1;
        else
            low = mid + 1;
    else if (x < arr[mid])
        high = mid - 1;
    else
        low = mid + 1;
```

# Algorithm

## Example

We have used random numbers generator for testing purpose. let Say after Random Generation our arr is

12 , 14 , 14 , 14 , 15 , 18 , 20 and x is 14.

So Output will be Element 14 Occurs 3 Times.

And if x is 13

Then Output will be : Element not found in array.



# TIME COMPLEXITY

While Finding the First and Last Occurrence of  $x$  if the complexity of the entire Algorithm is  $T(n)$  where  $n$  signifies number of elements, we are actually reducing the list to half i.e  $T(n/2)$  in every step of the loop along with some constant time ( $O(1)$  for reference) needed to find middle index and do comparisons.

Hence Time Complexity of Binary Search :

$$T(n) = T(n/2) + O(1)$$

Let say after  $k$  divisions, the size of search space becomes 1.

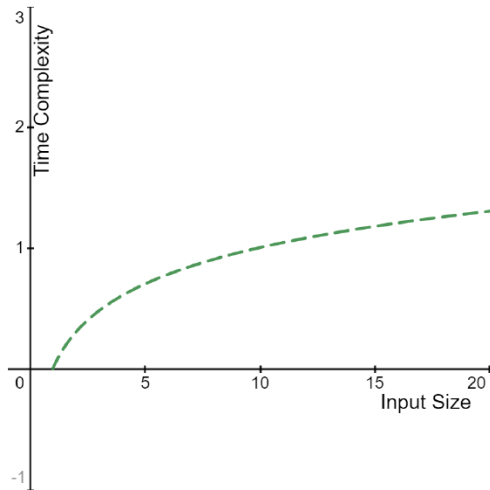
Therefore size of search space  $= n/2^k = 1$

Applying log function on both sides:

$$k = \log(n)$$

Hence the complexity of finding freq of  $x$  is  $\log(n)$

# Figure



# SPACE COMPLEXITY

Space required for searching is  $O(1)$  because we just use some variables which come under  $O(1)$  or constant space complexity.

Only Space required is for storing the array `arr[]` of size  $n$  which will be  $O(n)$ .

# References

- Introduction to Algorithms by TH Cormen, Charles E. Leiserson, Ronald L. Rivest, and Clifford Stein.
- Binary Search : <https://en.wikipedia.org/wiki/Binarysearchalgorithm>
- Divide and Conquer : <https://www.geeksforgeeks.org/divide-and-conquer/>

The End