Al Assignment 1 - Coding

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Heuristics used:

- $h_a(n) = 0$
- Manhattan Distance: sum of x and y distances of each tile from its place in the goal state
- Euclidean Distance: square root of sum of squares of the x and y distances of each tile from goal tile
- Misplaced tiles: sum of number of tiles in the same place as in goal state

Input.txt has randomly generated 50 inputs with some unsolvable inputs, which are indicated by -1.

Output: The output is also present in output.txt.

- We see that, in most cases, misplaced tiles heuristic takes the longest time.
- Maximum nodes are explored in misplaced tiles heuristic.
- In few cases, euclidean gives outrageous running time.

A*										
+ Start A* +	N0 t		N1	t1	N2	2 1	12	N3	t3	+ +
[3, 1, 2, 4, 0, 5, 6, 7, 8										
[1, 2, 0, 4, 8, 3, 7, 6, 5]	5] 20 1.	03776334	20	0.06347	172 2	0.0	04733376	28	15.66652274	
[1, 3, 5, 7, 2, 6, 8, 0, 4	4] 28 2.	37207187	28	0.10577	174 2	28 0.0	05886474	30	19.23183269	
[1, 2, 3, 4, 6, 5, 7, 8, 0	0] -1	-1	-1	-1	-	-1	-1	-1	-1	
[0, 4, 1, 5, 3, 2, 7, 8, 6	6] 30 2.	12184450	30	0.11852	2891 3	30 0.	10726926	30	15.90167311	
[8, 6, 7, 2, 5, 4, 1, 3, 0	0] -1	-1	-1	-1	-	1	-1	-1	-1	
[1, 4, 3, 7, 0, 8, 6, 5, 2	2] 34 0.	73108209	34	0.03989	968 3	34 0.0	02030717	34	15.29814516	
[6, 0, 8, 4, 3, 5, 1, 2, 7	7] 34 4.	46976559	34	0.22015	713 3	34 0.3	30442352	34	17.70579238	
[2, 0, 8, 1, 3, 5, 4, 6, 7	7] 34 0.	13419359	34	0.00799	375 3	34 0.0	00486309	34	7.51391728	
[1, 0, 3, 2, 4, 5, 6, 7, 8	3] -1	-1	-1	-1	-	-1	-1	-1	-1	
[8, 7, 2, 1, 5, 0, 4, 6, 3	3] 34 4.	61804560	34	0.21142	2870 3	34 0.3	30260497	34	15.91888786	
[6, 3, 8, 5, 4, 1, 7, 2, 0	0] 39 2.	18695434	39	0.08940	288 3	39 0.0)5587300	39	15.86218707	
[4, 1, 2, 3, 0, 6, 5, 7, 8	3] 39 1.	33426040	39	0.08160	160 3	39 0.0	7370772	39	17.82897775	
[1, 2, 3, 4, 5, 6, 7, 8, 0	0] 39 2.4	47893124	39	0.13292	2724 3	39 0.	10812089	39	16.71167520	
[1, 3, 6, 5, 2, 8, 4, 0, 7	7] 39 4.	63422823	39	0.27009	163 3	39 0.3	30075601	39	16.87090056	
[1, 8, 5, 0, 2, 4, 3, 6, 7	7] 39 0.4	48900347	39	0.02588	3134 3	39 0.0	01774247	39	13.26048517	
[5, 3, 6, 4, 0, 7, 1, 8, 2	2] 39 4.	52698905	39	0.14842	2411 3	39 0.	15836724	39	16.56543868	
[1, 2, 3, 4, 5, 0, 7, 8, 6	6] 39 2.	09871019	39	0.10621	782 3	39 0.0	07325357	39	18.20022833	
[7, 0, 2, 8, 5, 3, 6, 4,	1] -1	-1	-1	-1	-	-1	-1	-1	-1	
[0, 1, 2, 4, 5, 3, 7, 8, 6	6] 39 2.	37415034	39	0.12739	910 3	39 0.	10897407	39	17.32334804	
[1, 2, 3, 4, 0, 5, 7, 8, 6	6] 39 1.	57134223	39	0.08418	3459 3	39 0.0	05467428	39	16.33954513	

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| [1, 2, 3, 0, 4, 5, 7, 8, 6] | 39 | 1.00657876 | 39 | 0.05037304 | 39 | 0.02740254 | 39 | 14.55579487 |
| [4, 3, 1, 0, 7, 2, 8, 5, 6] | 39 | 0.83403688 | 39 | 0.04529862 | 39 | 0.02584738 | 39 | 18.45131307 |
| [1, 6, 4, 0, 3, 5, 8, 2, 7] | 39 | 2.25840040 | 39 | 0.10769305 | 39 | 0.06390009 | 39 | 18.35260730 |
| [3, 4, 6, 2, 0, 8, 1, 7, 5] | 39 | 4.01919763 | 39 | 0.19885041 | 39 | 0.22096891 | 39 | 17.53456524 |
| [1, 2, 3, 0, 4, 8, 7, 6, 5] | 39 | 3.54303254 | 39 | 0.27940637 | 39 | 0.29558696 | 39 | 17.27101138 |
| [0, 4, 3, 2, 1, 6, 7, 5, 8] | 39 | 4.08657905 | 39 | 0.20440755 | 39 | 0.19110454 | 39 | 17.99183410 |
| [8, 1, 2, 0, 4, 3, 7, 6, 5] | -1 | -1
                                           |-1 |
                                                     -1
                                                              |-1 | -1
                                                                                 |-1|
| [1, 0, 2, 4, 6, 3, 7, 5, 8] | 39 | 0.36497568 | 39 | 0.02270967 | 39 | 0.01631466 | 39 | 11.96063456 |
| [6, 5, 3, 4, 1, 7, 0, 2, 8] | 39 | 5.01016218 | 39 | 0.29016297 | 39 | 0.41178320 | 39 | 20.87122613 |
| [6, 4, 7, 8, 5, 0, 3, 2, 1] | 39 | 4.44913346 | 39 | 0.18190959 | 39 | 0.24999777 | 39 | 16.41448763 |
| [5, 2, 1, 4, 8, 3, 7, 6, 0] | 39 | 4.90478548 | 39 | 0.39928514 | 39 | 0.57297959 | 39 | 16.69117055 |
| [4, 8, 7, 5, 3, 1, 0, 6, 2] | 39 | 3.96656049 | 39 | 0.16674004 | 39 | 0.14072912 | 39 | 18.14270238 |
| [8, 3, 5, 6, 4, 2, 1, 0, 7] | 39 | 3.10344402 | 39 | 0.15007538 | 39 | 0.14118152 | 39 | 16.87319222 |
| [7, 4, 3, 2, 8, 6, 0, 5, 1] | 39 | 3.69375211 | 39 | 0.09539716 | 39 | 0.06510507 | 39 | 16.54776787 |
| [8, 6, 7, 2, 0, 4, 3, 5, 1] | 39 | 4.93745823 | 39 | 0.22290780 | 39 | 0.40764254 | 39 | 14.24332675 |
| [0, 4, 3, 2, 1, 6, 7, 5, 8] | 39 | 4.09322756 | 39 | 0.29620662 | 39 | 0.18409950 | 39 | 18.97432475 |
[1, 2, 3, 4, 5, 0, 7, 8, 6] 39 1.96527501 39 0.10016849 39 0.07475672 39 16.24122037
| [1, 2, 3, 4, 0, 5, 7, 8, 6] | 39 | 1.58071910 | 39 | 0.07319126 | 39 | 0.05001318 | 39 | 16.16284472 |
| [8, 6, 7, 2, 5, 4, 1, 3, 0] | -1 | -1
                                                     -1
                                            |-1 |
                                                               |-1 | -1
                                                                                  |-1|
| [1, 2, 0, 4, 8, 3, 7, 6, 5] | 39 | 1.14398351 | 39 | 0.06371826 | 39 | 0.04972849 | 39 | 15.88866231 |
| [1, 0, 2, 4, 6, 3, 7, 5, 8] | 39 | 0.32820838 | 39 | 0.02033010 | 39 | 0.01650575 | 39 | 11.73351975 |
| [1, 2, 3, 4, 6, 5, 7, 8, 0] | -1 | -1
                                            |-1|
                                                     -1
                                                              |-1 | -1
                                                                                  |-1|
[0, 1, 2, 4, 5, 3, 7, 8, 6] 39 2.17892338 39 0.11925577 39 0.10758060 39 15.70272747
| [1, 2, 3, 4, 5, 6, 7, 8, 0] | 39 | 2.59542697 | 39 | 0.12648465 | 39 | 0.10154870 | 39 | 17.83437242 |
                                                              |-1 |
                                           |-1 |
| [7, 0, 2, 8, 5, 3, 6, 4, 1] | -1 | -1
                                                     -1
                                                                      -1
                                                                                 |-1|
                                                                                           -1
                                                              |-1 |
| [8, 1, 2, 0, 4, 3, 7, 6, 5] | -1 | -1
                                           |-1 |
                                                     -1
                                                                      -1
                                                                                 |-1|
                                                                                           -1
| [1, 2, 3, 0, 4, 8, 7, 6, 5] | 39 | 3.41588316 | 39 | 0.19684434 | 39 | 0.20537008 | 39 | 15.72081487 |
[1, 2, 3, 0, 4, 5, 7, 8, 6] 39 0.94715350 39 0.04507575 39 0.02909580 39 13.79254703
| [1, 0, 3, 2, 4, 5, 6, 7, 8] | -1 | -1
                                           |-1 |
                                                              |-1 | -1
                                                                                 |-1|
                                                     -1
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IDA*

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Start IDA*
                                       |N1| t1
                                                       | N2 | t2
                     | N0 |
                             t0
                                                                         | N3 |
             | [3, 1, 2, 4, 0, 5, 6, 7, 8] | 10 | 0.00022592 | 10 | 0.00021800 | 10 | 0.00025725 | 10 | 0.00117420 |
| [1, 2, 0, 4, 8, 3, 7, 6, 5] | 28 | 1.18621707 | 28 | 1.76509812 | 28 | 26.63045239 | 28 | 0.79611658 |
| [1, 3, 5, 7, 2, 6, 8, 0, 4] | 30 | 1.45959460 | 30 | 2.72914703 | 30 | 63.31747508 | 30 | 0.65905786 |
                                                       |-1 | -1
| [1, 2, 3, 4, 6, 5, 7, 8, 0]| -1 | -1
                                      |-1 |
                                                                        |-1|
                                               -1
                                                                                 -1
| [0, 4, 1, 5, 3, 2, 7, 8, 6] | 30 | 1.64454527 | 34 | 5.37690712 | 34 | 165.04616852 | 34 | 0.90202970 |
                                                       |-1 | -1
| [8, 6, 7, 2, 5, 4, 1, 3, 0] | -1 | -1
                                      |-1 |
                                               -1
                                                                         |-1|
| [1, 4, 3, 7, 0, 8, 6, 5, 2] | 34 | 1.01240193 | 34 | 1.43934710 | 34 | 6.61842412 | 34 | 0.89474859 |
| [6, 0, 8, 4, 3, 5, 1, 2, 7] | 34 | 2.94737913 | 34 | 1.73855718 | 34 | 29.04872442 | 34 | 2.63117403 |
[2, 0, 8, 1, 3, 5, 4, 6, 7] 34 0.21768334 34 0.08873737 34 0.31426391 34 0.13959156
| [1, 0, 3, 2, 4, 5, 6, 7, 8] | -1 | -1
                                       |-1|
                                                        |-1 | -1
                                               -1
                                                                         |-1|
[8, 7, 2, 1, 5, 0, 4, 6, 3] | 34 | 3.03257470 | 39 | 10.04505874 | 39 | 359.84012511 | 39 | 15.04397236
[6, 3, 8, 5, 4, 1, 7, 2, 0] 39 1.61184448 39 1.61504128 39 33.38959117 39 2.43032827
[4, 1, 2, 3, 0, 6, 5, 7, 8] 39 1.37640290 39 2.70666649 39 51.69246632 39 4.05774473
[1, 2, 3, 4, 5, 6, 7, 8, 0] 39 1.79246634 39 7.88604425 39 232.78805638 39 1.47507325
[1, 3, 6, 5, 2, 8, 4, 0, 7] 39 2.95919466 39 7.94529886 39 273.79163340 39 0.39802402
[1, 8, 5, 0, 2, 4, 3, 6, 7] | 39 | 0.53886985 | 39 | 0.32652876 | 39 | 3.02122611 | 39 | 0.09736517 |
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| [5, 3, 6, 4, 0, 7, 1, 8, 2] | 39 | 2.86084209 | 39 | 4.04018089 | 39 | 24.31634789 | 39 | 0.10116328 |
| [1, 2, 3, 4, 5, 0, 7, 8, 6] | 39 | 1.68076651 | 39 | 6.57481090 | 39 | 183.87465976 | 39 | 1.09762525 |
| [7, 0, 2, 8, 5, 3, 6, 4, 1] | -1 | -1
                                         |-1 | -1
                                                           |-1 | -1
                                                                              |-1|
[0, 1, 2, 4, 5, 3, 7, 8, 6] 3 1 1.91433713 3 1 10.88588089 3 1 2 2 9 6.08508099 3 1 1 2.29244722
[1, 2, 3, 4, 0, 5, 7, 8, 6] 39 1.36795751 39 4.85078917 39 124.41268015 39 7.14885411
[1, 2, 3, 0, 4, 5, 7, 8, 6] | 39 | 0.90215369 | 39 | 0.35455519 | 39 | 2.07355041 | 39 | 0.57225562 |
| [4, 3, 1, 0, 7, 2, 8, 5, 6] | 39 | 0.72276964 | 39 | 1.80561544 | 39 | 3.68258140 | 39 | 0.06184927 |
[1, 6, 4, 0, 3, 5, 8, 2, 7] 39 1.94948593 39 2.45946815 39 37.78323441 39 2.84720888
| [3, 4, 6, 2, 0, 8, 1, 7, 5] | 39 | 2.88921335 | 39 | 4.26877734 | 39 | 73.13384019 | 39 | 4.36466623 |
| [1, 2, 3, 0, 4, 8, 7, 6, 5] | 39 | 2.36596775 | 39 | 1.43187188 | 39 | 20.32376594 | 39 | 1.92799334 |
| [0, 4, 3, 2, 1, 6, 7, 5, 8] | 39 | 2.53414340 | 39 | 4.00869156 | 39 | 102.10481882 | 39 | 6.15688130 |
| [8, 1, 2, 0, 4, 3, 7, 6, 5]| -1 | -1
                                                           |-1 | -1
                                         |-1 |
                                                  -1
| [1, 0, 2, 4, 6, 3, 7, 5, 8] | 39 | 0.46668315 | 39 | 1.89515738 | 39 | 33.69497854 | 39 | 2.75250115 |
[6, 5, 3, 4, 1, 7, 0, 2, 8] 39 4.29567293 39 6.42287127 39 167.10238073 39 7.87676348
[6, 4, 7, 8, 5, 0, 3, 2, 1] 39 3.04172373 39 5.23823269 39 195.65455071 39 0.27365738
| [5, 2, 1, 4, 8, 3, 7, 6, 0] | 39 | 3.25987760 | 39 | 7.77450474 | 39 | 265.23596379 | 39 | 1.32458905 |
[4, 8, 7, 5, 3, 1, 0, 6, 2] 39 2.33121600 39 1.40017213 39 39.56823937 39 0.05670114
| [8, 3, 5, 6, 4, 2, 1, 0, 7] | 39 | 2.21527330 | 39 | 5.45081104 | 39 | 149.34345633 | 39 | 7.93359656 |
| [7, 4, 3, 2, 8, 6, 0, 5, 1] | 39 | 2.64620719 | 39 | 6.15746936 | 39 | 235.94325016 | 39 | 0.92651821 |
| [8, 6, 7, 2, 0, 4, 3, 5, 1] | 39 | 3.34223387 | 39 | 9.97582106 | 39 | 382.20616752 | 39 | 0.84931198 |
| [0, 4, 3, 2, 1, 6, 7, 5, 8] | 39 | 2.66662816 | 39 | 4.12810618 | 39 | 108.52898368 | 39 | 6.04419354 |
| [1, 2, 3, 4, 5, 0, 7, 8, 6] | 39 | 1.67587210 | 39 | 6.08372335 | 39 | 179.65024711 | 39 | 1.08590094 |
[1, 2, 3, 4, 0, 5, 7, 8, 6] 39 1.23066501 39 4.63301563 39 121.48032202 39 7.09913538
| [8, 6, 7, 2, 5, 4, 1, 3, 0] | -1 | -1
                                         |-1 |
                                                   -1
                                                           |-1 | -1
                                                                              |-1|
                                                                                       -1
| [1, 2, 0, 4, 8, 3, 7, 6, 5] | 39 | 1.13844423 | 39 | 1.75628105 | 39 | 25.69064542 | 39 | 0.62895389 |
| [1, 0, 2, 4, 6, 3, 7, 5, 8] | 39 | 0.55487725 | 39 | 1.90937736 | 39 | 33.48617017 | 39 | 2.77442414 |
| [1, 2, 3, 4, 6, 5, 7, 8, 0] | -1 | -1
                                         |-1 |
                                                   -1
                                                           |-1 | -1
                                                                              |-1|
[0, 1, 2, 4, 5, 3, 7, 8, 6] 3 1 1.85357404 3 1 10.21510852 3 1 3 1 3 3 1 3 3 5 3 6 6 4 7 6 4 3 9 1 4 5 3 5 9 2 6 4 4
| [1, 2, 3, 4, 5, 6, 7, 8, 0] | 39 | 1.73513545 | 39 | 7.97322167 | 39 | 226.76123054 | 39 | 1.36926909 |
| [7, 0, 2, 8, 5, 3, 6, 4, 1]| -1 | -1
                                         |-1 |
                                                  -1
                                                           |-1 | -1
                                                                             |-1|
                                                                                      -1
| [8, 1, 2, 0, 4, 3, 7, 6, 5] | -1 | -1
                                         |-1 |
                                                  -1
                                                           |-1 | -1
                                                                              |-1|
                                                                                       -1
[1, 2, 3, 0, 4, 8, 7, 6, 5] 39 2.19080933 39 1.38792584 39 19.77927678 39 1.91302866
[1, 2, 3, 0, 4, 5, 7, 8, 6] 3 | 0.81664424 3 | 0.34060505 3 | 1.93568368 3 | 3 | 0.46379428
| [1, 0, 3, 2, 4, 5, 6, 7, 8] | -1 | -1
                                         |-1 |
                                                           |-1 | -1
                                                                              |-1|
                                                                                       -1
                                                   -1
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