

SARDAR VALLABHBHAI PATEL INSTITUTE OF TECHNOLOGY  
VASAD

B. E. Third Semester (2017-18)

Subject: Advanced Engineering Mathematics (2130002)

**Tutorial: 2**

**1** Solve  $(xy \sin xy + \cos xy)ydx + (xy \sin xy - \cos xy)xdy = 0$

**2** Solve  $(3x^2y^4 + 2xy)dx + (2x^3y^3 - x^2)dy = 0$

**3** Solve  $\frac{dy}{dx} + \frac{4x}{x^2+1}y = \frac{1}{(x^2+1)^3}$

**4** Solve  $(x + 2y^3)\frac{dy}{dx} = y$

**5** Solve  $(1 + x^2)\frac{dy}{dx} + y = \tan^{-1} x$

**6** Solve  $\frac{dy}{dx} + x \sin 2y = x^3 \cos^2 y$

**7** Solve  $\frac{dz}{dx} + \frac{z}{x} \log z = \frac{z}{x} (\log z)^2$

**8** Solve the following Initial Value Problem

(i)  $\frac{dy}{dx} = \frac{y}{x} - \cos^2 \frac{y}{x}$ , given that  $y=0$ , when  $x=1$

(ii)  $\frac{2x}{y^3} + \frac{y^2 - 3x^2}{y^4} \cdot \frac{dy}{dx} = 0$ , given that  $y=1$ , when  $x=2$

(iii)  $\frac{dy}{dx} + \frac{y}{x} = x^2$ , given that  $y=1$ , when  $x=1$

**9** Find the orthogonal trajectories of the family  $ay^2 = x^3$

**10** Find the orthogonal trajectory of  $y^2 = 4a(x+a)$

**11** Find the orthogonal trajectories of  $r = 2a \cos \theta$

**12** Find the orthogonal trajectory of the family of cardioids  $r = a(1 + \cos \theta)$ ,  
where  $a$  is a parameter.