

SARDAR VALLABHBHAI PATEL INSTITUTE OF TECHNOLOGY  
VASAD

B. E. Third Semester (2017-18)

Subject: Advanced Engineering Mathematics (2130002)

**Tutorial: 8**

- 1** Classify the singularities for the differential equation

$$y'' + 3x^2y' + 2xy = 0, \text{ where } y'' = \frac{d^2y}{dx^2}, y' = \frac{dy}{dx}$$

- 2** Determine that  $x=1$  is a regular singular point of  $(1-x^2)y'' - 2xy' + n(n+1)y = 0$ ,  $n$  is a constant.

- 3** Classify the singularities for differential equation  $(x^2+1)y'' - xy' - y = 0$

- 4** Determine the singular points of the differential equation  $2x(x-2)^2y'' + 3xy' + (x-2)y = 0$  and classify them as regular or irregular.

- 5** Determine the singular points of the differential equation  $(x-3)y'' - 2x^2y' + 7(x-1)y = 0$  and classify them as regular or irregular.

- 6** Find Power series solution of  $\frac{d^2y}{dx^2} + xy = 0$

- 7** Solve the equation  $\frac{d^2y}{dx^2} + y = 0$  by the power series method.

- 8** Obtain the series solution of  $(1-x^2)y'' - 2xy' + 2y = 0$

- 9** Find the power series solution in power of  $x$  of  $y' + 2xy = 0$

- 10** Solve the Legendre's equation  $(1-x^2)y'' - 2xy' + n(n+1)y = 0$ , for  $n=0$