

SARDAR VALLABHBHAI PATEL INSTITUTE OF TECHNOLOGY  
VASAD

B. E. Third Semester (2017-18)

Subject: Advanced Engineering Mathematics (2130002)

**Tutorial: 1**

**1** Determine Order and Degree of the following Differential Equations.

(i)  $\left(\frac{dy}{dx}\right)^2 = 5\sqrt{y} - 3x$

(ii)  $3\left(\frac{d^2y}{dx^2}\right)^3 - 5\frac{dy}{dx} = 0$

(iii)  $3\left(\frac{d^2y}{dx^2}\right)^3 - 5\sqrt{\frac{dy}{dx}} = 0$

(iv)  $\left(\frac{d^2y}{dx^2}\right)^3 - \frac{5}{\left(\frac{d^2y}{dx^2}\right)} = 0$

**2** Obtain the differential equation for  $y = ae^{2x} + be^{-2x}$ .

**3** Form the differential equation of all circles of radius a.

**4** Verify that  $y = e^{-x}(a \cos x + b \sin x)$  is a solution of  $y'' + 2y' + 2y = 0$  where a & b are Constants.

**5** Verify that  $(x-2)^2 + y^2 = 4$  is a solution of  $\frac{dy}{dx} = \frac{y^2 - x^2}{2xy}$

**6** Solve  $xy \frac{dy}{dx} = 1 + x + y + xy$

**7** Solve  $(e^{2y} + 1) \cos x dx + 2e^y \sin x dy = 0$

**8** Solve  $\frac{dy}{dx} = 1 + x \tan(y - x)$

**9** Solve  $\frac{dy}{dx} = e^{2x-3y} + 4x^2 e^{-3y}$

**10** Solve  $\frac{dy}{dx} = (4x + y + 1)^2$

**11** Solve  $\frac{(x-2y)}{(3x+y)} \frac{dy}{dx} = 3x^2 - 5xy - 2y^2$

**12** Solve  $(x^2 - y^2)dx = 2xydy$

**13** Solve  $\frac{dy}{dx} = \frac{y}{x} + x \sin \frac{y}{x}$

**14** Solve  $(y^2 e^{xy^2} + 4x^3)dx + (2xye^{xy^2} - 3y^2)dy = 0$

**15** Solve  $\frac{dy}{dx} + \frac{y \cos x + \sin y + y}{\sin x + x \cos y + x} = 0$