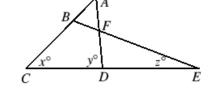
Question

Question ID: 878





8. In the figure shown, AB = AF and ABC, AFD, BFE and CDE are all straight lines. Which of the following expressions gives z in terms of x and y?



- A $\frac{y-x}{2}$ B $y-\frac{x}{2}$ C $\frac{y-x}{3}$ D $y-\frac{x}{3}$
- E y x

0878



©UKMT

Answer

8. In triangle ACD, $\angle CAD = (180 - x - y)^{\circ}$. As AB = AF, triangle ABF is isosceles hence $\angle ABF = \angle AFB = \frac{1}{2}(x + y)^{\circ}.$ Thus $\angle DFE = \angle AFB = \frac{1}{2}(x + y)^{\circ}$ (vertically opposite angles). Now in triangle DFE, $\angle FDE = (180 - y)^{\circ}$. Hence $z^{\circ} = 180^{\circ} - \angle DFE - \angle FDE = \frac{1}{2}(y - x)^{\circ}.$

