

HW # 2: Planar Kinematics

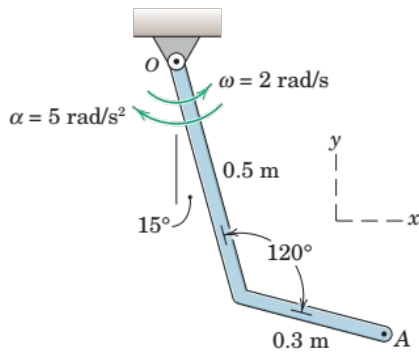


Figure 1

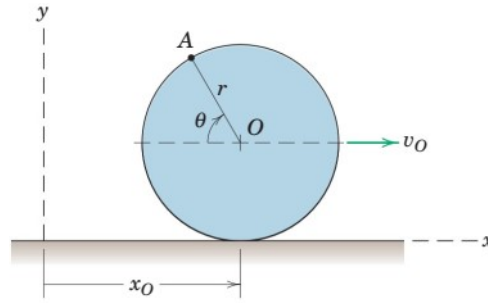


Figure 2

Q1: The bent flat bar rotates about a fixed axis through point O with the instantaneous angular properties indicated in the Figure 1. Determine the velocity and acceleration of point A.

Q2: The wheel of radius r rolls without slipping, and its center O has a constant velocity v_O to the right as shown in Figure 2. Determine expressions for the magnitudes of the velocity v and acceleration a of point A on the rim by differentiating its x - and y -coordinates.

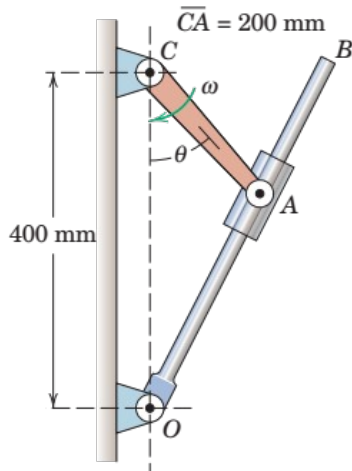


Figure 3

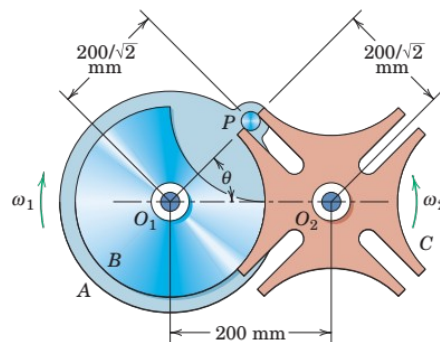


Figure 4

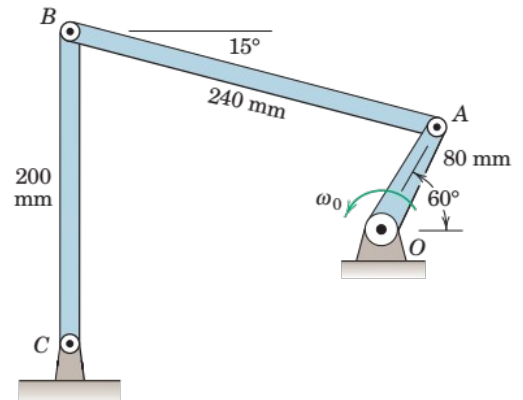


Figure 5

Q3: The rod OB slides through the collar pivoted to the rotating link at A as shown in Figure 3. If CA has an angular velocity $\omega = 3 \text{ rad/s}$ for an interval of motion, calculate the angular velocity of OB when $\theta = 45^\circ$.

Q4: Figure 4 shows the Geneva wheel mechanism used for producing intermittent rotation. Pin P in the integral unit of wheel A and locking plate B engages the radial slots in wheel C , thus turning wheel C one-fourth of a revolution for each revolution of the pin. At the engagement position shown, $\theta = 45^\circ$. For a constant clockwise angular velocity $\omega_1 = 2 \text{ rad/s}$ of wheel A , determine the corresponding counterclockwise angular velocity ω_2 of wheel C for $\theta = 20^\circ$. (Note that the motion during engagement is governed by the geometry of triangle O_1O_2P with changing θ .)

Q5. A four-bar linkage is shown in the Figure 5 (the ground “link” OC is considered the fourth bar). If the drive link OA has a counterclockwise angular velocity $\omega_0 = 10 \text{ rad/s}$, determine the angular velocities of links AB and BC .

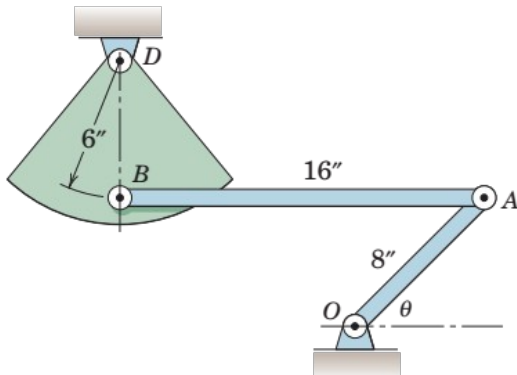


Figure 6

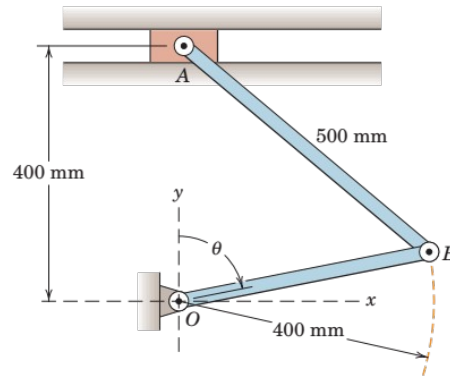


Figure 7

Q6. Link OA has a counterclockwise angular velocity $d\theta/dt = 4 \text{ rad/sec}$ during an interval of its motion. Use method of instantaneous centre of rotation to determine the angular velocity of link AB and of sector BD for $\theta = 45^\circ$ at which instant AB is horizontal and BD is vertical.

Q7. For the Figure 7, determine the angular acceleration of AB and the linear acceleration of A for the position $\theta = 90^\circ$ if $d\theta/dt = 4 \text{ rad/s}$ and $d^2\theta/dt^2 = 0$ at that position.

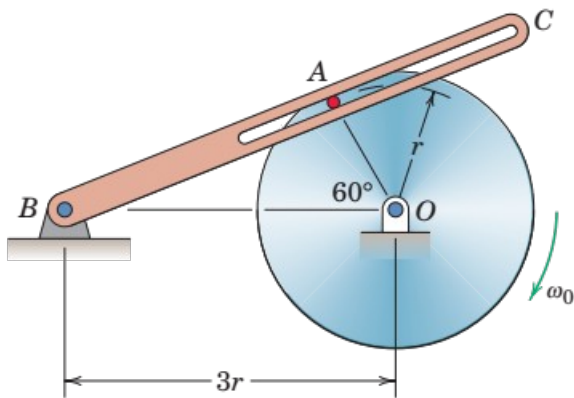


Figure 8

Q8. The disk rotates about a fixed axis through point O with a clockwise angular velocity $\omega_0 = 20 \text{ rad/s}$ and a counterclockwise angular acceleration $\alpha_0 = 5 \text{ rad/s}^2$ at the instant under consideration (see Figure 8). The value of r is 200 mm . Pin A is fixed to the disk but slides freely within the slotted member BC . Determine the velocity and acceleration of A relative to slotted member BC and the angular velocity and angular acceleration of BC .