

Inertial frames.

$$\bar{v} = \frac{d}{dt}(\underline{r}) = \frac{dr}{dt} \underline{e}_1 + r \frac{de_1}{dt}$$

$$\frac{de_1}{dt} = \dot{\theta} \underline{e}_2$$

$$\frac{de_2}{dt} = -\dot{\theta} \underline{e}_1$$

0 when
coord system
does not acce.
↓

Radial tangential Inertial frame

$$\underline{v} = \dot{r} \underline{e}_r + r \dot{\theta} \underline{e}_\theta$$

$$\begin{aligned} \underline{a} = \frac{d\underline{v}}{dt} &= \ddot{r} \underline{e}_r + \dot{r} \cdot \frac{de_r}{dt} + \dot{r} \dot{\theta} \underline{e}_\theta \\ &\quad + r \ddot{\theta} \underline{e}_\theta + r \dot{\theta} \frac{de_\theta}{dt} - \dot{\theta} \underline{e}_r \end{aligned}$$

$$\Rightarrow [\ddot{r} - (\dot{r}^2)] \underline{e}_r + (2\dot{r}\dot{\theta} + r\ddot{\theta}) \underline{e}_\theta$$

Circular Motion.

$$v = r\omega \underline{e}_\theta$$

$$\underline{a} = -r(\dot{\theta})^2 \underline{e}_r + \dot{r}\dot{\theta} \underline{e}_\theta$$

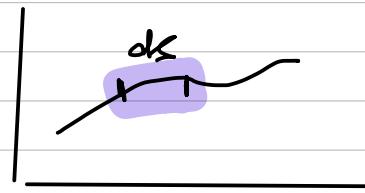
$$= -r\omega^2 \underline{e}_r + \dot{r} \cdot \alpha \underline{e}_\theta$$

tangential Component

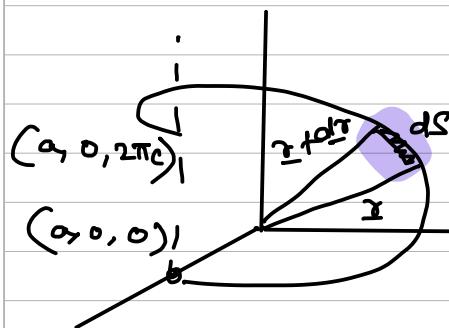
Tangential Normal force

Position vector expressed in terms of the arc length.

$$\gamma = \gamma(s(t))$$



Example:
helix



$$(ds)^2 = dr^2 + d\theta^2$$

$$= dx^2 + dy^2 + dz^2$$

$$= (-a \sin(\theta) dt)^2 + (a \cos(\theta) dt)^2 + (ct)^2$$

$$+ (ct)^2$$

$$ds = \sqrt{(a^2 + c^2)} dt$$

$$\int_0^s ds = \sqrt{a^2 + c^2} t$$

$$x_1 = a \cos\left(\frac{s}{\sqrt{a^2 + c^2}}\right)$$

$$x_2 = a \sin\left(\frac{s}{\sqrt{a^2 + c^2}}\right)$$

$$x_3 = \frac{c s}{\sqrt{a^2 + c^2}}$$

→ Scalar

why $d\vec{r} \perp \vec{s}$

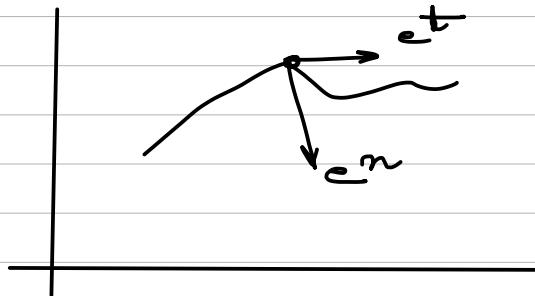
$$\underline{v} = \frac{d\vec{r}}{dt} = \left(\frac{d\vec{r}}{ds} \right) \cdot \left(\frac{ds}{dt} \right)$$

$$\left(\frac{d\vec{r}}{ds} \right) = \lim_{\Delta s \rightarrow 0} \left| \frac{\Delta \vec{r}}{\Delta s} \right| = 1$$

$\frac{d\vec{r}}{ds} \rightarrow$ unit tangent vector

$$e^t \sim = \frac{dr}{ds}$$

$$\underline{n} \quad \underline{da}$$



$$e^t \cdot e^t = 1$$

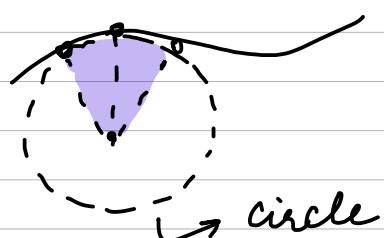
exists if
 $r = C^\infty$ of S .

$$\frac{de^t}{ds} \cdot e^t + e^t \cdot \frac{de^t}{ds} = 0$$

$$e^t \cdot \frac{de^t}{ds} = 0$$

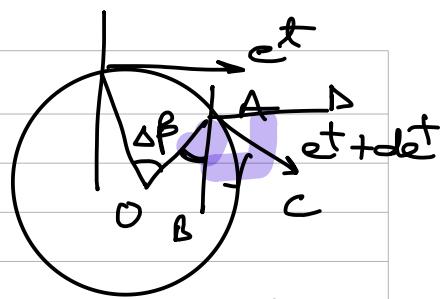
$$\boxed{\frac{de^t}{ds} = K \cdot \bar{n}}$$

Curvature of curve



given three points,
my circle would be
unique.

$$\frac{\underline{det}}{ds} = \lim_{\Delta s \rightarrow 0} \frac{\underline{det}}{\Delta s}$$



$$\angle OAB + \angle BAC = \pi/2$$

$$\angle BAC + \angle CAD = \pi/2$$

$$|\Delta e^t| = |\dot{e}^t| |\tan \beta| \quad \text{small angle}$$

$$|\Delta e^t| = |\tan \beta| \approx \Delta \beta$$

$$|\Delta \bar{e}^t| = \Delta \beta$$

$$\frac{\Delta \beta}{\Delta s} = \frac{1}{r}$$

$$\frac{\underline{det}}{ds} = k \bar{e}_n$$

$$k = \frac{1}{r}$$

$$\bar{r} = \bar{r}(s(t))$$

$$\bar{v} = \frac{dr}{dt} = \frac{d\bar{r}}{ds} \cdot \frac{ds}{dt}$$

$$\bar{v} = \dot{s} \cdot \underline{e}^t$$

$$a = \frac{d\bar{v}}{dt}, \quad a = \frac{d\dot{s}}{dt} \cdot \underline{e}^t + \dot{s} \frac{d\underline{e}^t}{dt}$$

$$a = \ddot{s} \underline{e}^t + \dot{s} \left[\frac{d\underline{e}^t}{ds} \cdot \frac{ds}{dt} \right]$$

$$\bar{a} = \ddot{s} \bar{e}^t + \frac{(\dot{s})^2 \bar{e}^n}{r}$$

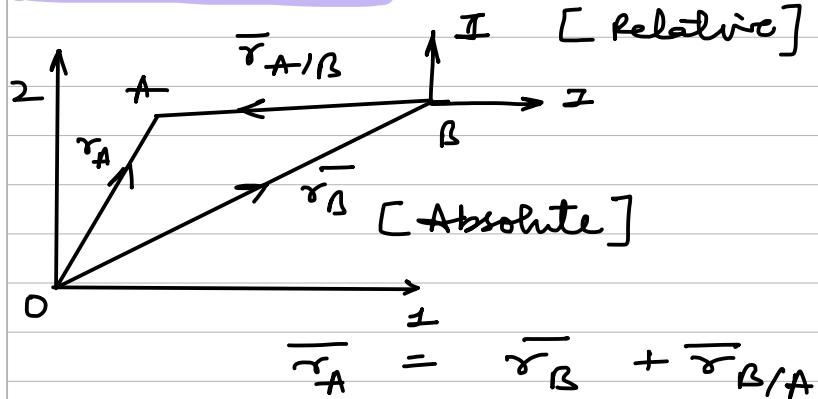
Make a map.

ef-en is the Serret-Ferret frame

Rigid body :

o collection of particles : distance b/w any 2 is unchanged .

Relative Motion



$$\bar{r}_A = \bar{r}_B + \bar{r}_{B/A}$$

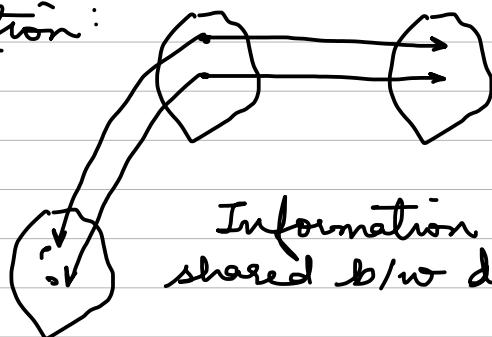
$$\bar{v}_A = \bar{v}_B + \bar{v}_{B/A}$$

$$\bar{\alpha}_A = \bar{\alpha}_B + \bar{\alpha}_{B/A}$$

If B is stationary, or non accelerating
then, inertial frame:

Rigid Body Motion:

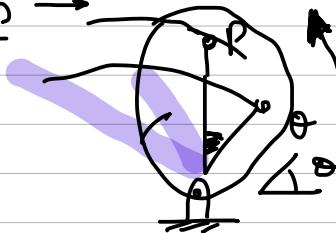
a) Translation:



Information can be shared b/w diff points'

what's the diff. b/w this and curvilinear motion.

Rotation →

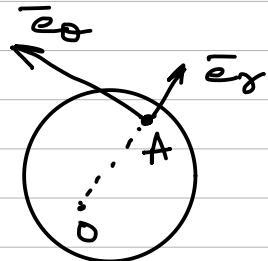


All radial points taking a circular path.

↪ b/w two points always remain the same.

$$\omega = \frac{d\theta}{dt}, \alpha = \frac{d\omega}{dt}$$

$$v_p = r \dot{\theta} e_\theta$$



$$\bar{e}_3 = \bar{e}_1 \times \bar{e}_2 \\ = \bar{e}_y \times \bar{e}_x$$

$$v = r \dot{\theta} [\bar{e}_3 \times \bar{e}_x]$$

$$= \bar{\omega} \times \bar{r}$$

Angular velocity vector.

\bar{c}^∞ is any general rotation axis.

$$\bar{v} = \frac{d\bar{r}}{dt} \Rightarrow \frac{d}{dt} (\gamma \bar{e}_x)$$

$$\begin{aligned} \bar{v} &= r \frac{d\bar{e}_x}{dt} \\ &= \bar{\omega} \times \bar{r} \\ &= \bar{\omega} \times \gamma \bar{e}_x \end{aligned}$$

$$\frac{d\bar{r}}{dt} = \bar{\omega} \times \bar{e}_y \quad \text{→ we derived it.}$$

Rate of change of a vector = cross product of its angular velocity vector and the vector itself.

$$\text{Acceleration: } a = \frac{d\bar{v}}{dt}$$

$$= \frac{d}{dt} (\bar{\omega} \times \bar{r})$$

$$= \frac{d\bar{\omega}}{dt} \times \bar{r} + \frac{d\bar{r}}{dt} \times \bar{\omega}$$

$$= \frac{d}{dt} (\dot{\theta} \cdot \bar{e}_3) = \frac{d\dot{\theta}}{dt} \bar{e}_3 = \alpha \bar{e}_3$$

$$\tilde{a} = \tilde{\omega} \times \tilde{r} + \bar{\omega} \times (\bar{\omega} \times \bar{r})$$

$$\tilde{\omega} = r\bar{\omega} \quad \bar{\omega} = \dot{\theta} \bar{e}_3, \quad \alpha = \alpha \bar{e}_3$$

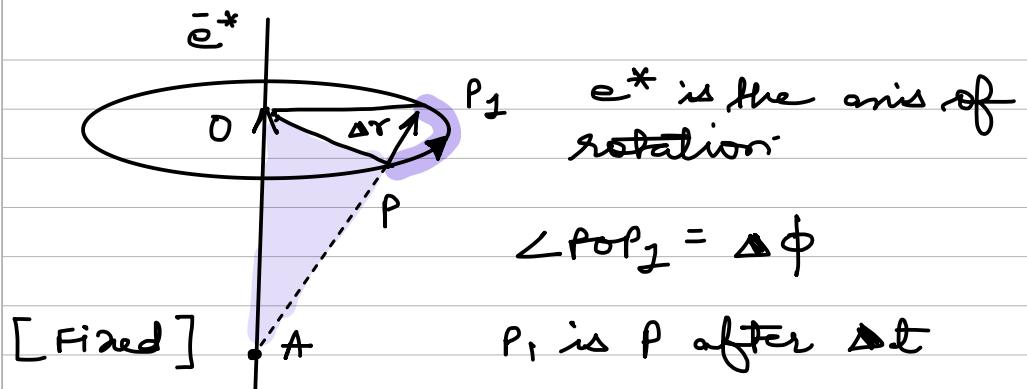
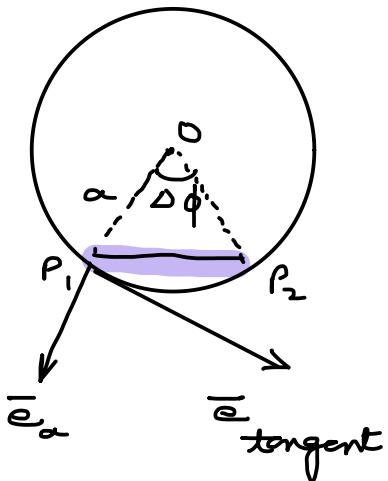
$$a = \alpha r \bar{e}_3 \times \bar{e}_r + (\dot{\theta}^2) r [\bar{e}_3 \times \bar{e}_3 \times \bar{e}_\theta]$$

$$= \alpha r \tilde{\bar{e}}_\theta + \dot{\theta}^2 r [\tilde{\bar{r}}]$$

$$a = \underbrace{r\alpha \tilde{\bar{e}}_\theta}_{\text{Tangential}} + \underbrace{\dot{\theta}^2 r \tilde{\bar{r}}}_{\text{Radial}}$$

Tangential Radial

Rotation about a fixed point



$$v_p = \lim_{\Delta t \rightarrow 0} \frac{\Delta r}{\Delta t} =$$

$$\Delta r = a \Delta \phi$$

Tangent to the circle at point P.

$$\tilde{\Delta r} = a \Delta \phi (\hat{e}^* \times \hat{e}_a)$$

Direction $\hat{e}_{\Delta r}$

$$= \hat{e}_r^* \times \hat{e}_a$$

$$v_p = \lim_{\Delta t \rightarrow 0} \frac{a \Delta \phi (\hat{e}^* \times \hat{e}_a)}{\Delta t}$$

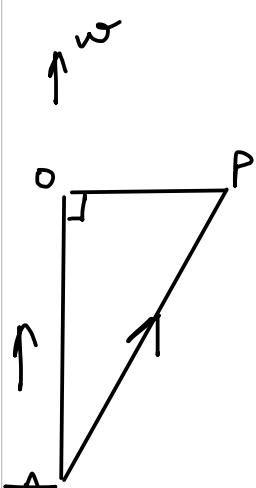
$$= \lim_{\Delta t \rightarrow 0} \frac{\Delta \phi}{\Delta t} [r_{p/o}]$$

$$= \omega \hat{e}^* \times \bar{r}_{p/o}$$

$$= \bar{\omega} \times \bar{r}_{p/o}$$

In ΔAOP ,

$$\tau_{p/A} = \tau_{o/A} + \tau_{p/o}$$



$$\bar{v}_p = \bar{\omega} \times [\bar{r}_{p/A} - \bar{r}_{0/A}]$$

$$\bar{v}_p = \bar{\omega} \times \bar{r}_{p/A} - \bar{\omega} \times \cancel{\bar{r}_{0/A}}$$

$$\bar{v}_p = \bar{\omega} \times \bar{r}_{p/A}$$

$$\frac{d}{dt}(\bar{r}_{p/A}) = \bar{\omega} \times \bar{r}_{p/A}$$

Acceleration:

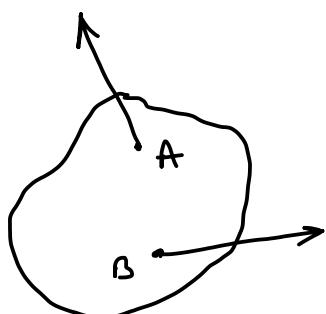
$$\bar{a} = \frac{d\bar{v}}{dt}, \bar{a} = \frac{d}{dt}(\bar{\omega} \times \bar{r}_{p/A})$$

$$= \frac{d\bar{\omega}}{dt} \times \bar{r}_{p/A}$$

$$+ \bar{\omega} \times \frac{d\bar{r}_{p/A}}{dt}$$

$$\Rightarrow \bar{a} = \bar{\omega} \times \bar{r}_{p/A} + \bar{\omega} \times \bar{v}$$

$$\bar{a} = \bar{\omega} \times \bar{r}_{p/A} + \bar{\omega} \times \bar{v}$$



For a plane case, $\omega = \omega \hat{e}_z$

w.r.t point B, since distance between points A and B does not change, the rel. motion A/B is rotational.

$$\bar{v}_{A/B} = \bar{\omega} \times \bar{r}_{A/B}$$

$$\bar{v}_A = \bar{v}_B + \bar{\omega} \times \bar{r}_{A/B}$$

$\bar{\omega}$ is Independent of frame?

$$\vec{v}_{A/B} = \vec{\omega} \times \vec{r}_{A/B}$$

Planar case \rightarrow 2 Components and thus
2 equations

diff. w.r.t time,

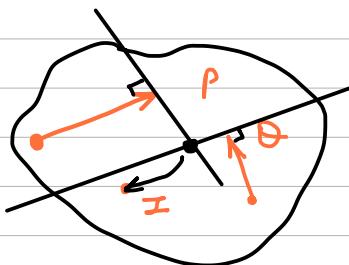
$$\vec{a}_A = \vec{a}_B + \frac{d}{dt} (\vec{\omega} \times \vec{r}_{A/B})$$

$$\vec{a}_A = \vec{a}_B + \alpha \times \vec{r}_{A/B} + \vec{\omega} \times \vec{v}_{A/B}$$

$$\vec{v}_A = \vec{v}_B + \vec{\omega} \times \vec{r}_{A/B}$$

If at a given instance, $\vec{J}_B = 0$, then
it becomes the int. point of rotation
 \downarrow
Centre

This is called inst. axis of rotation.



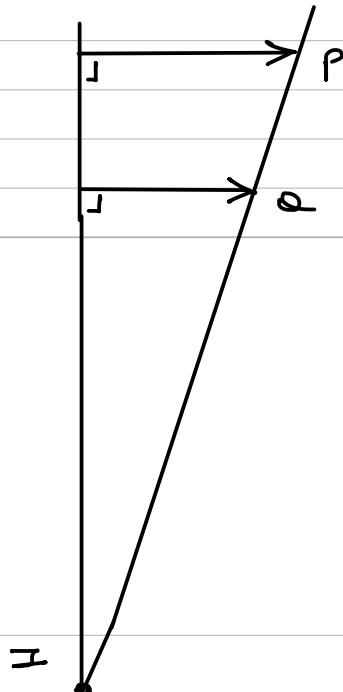
$I \rightarrow$ Inst. Center

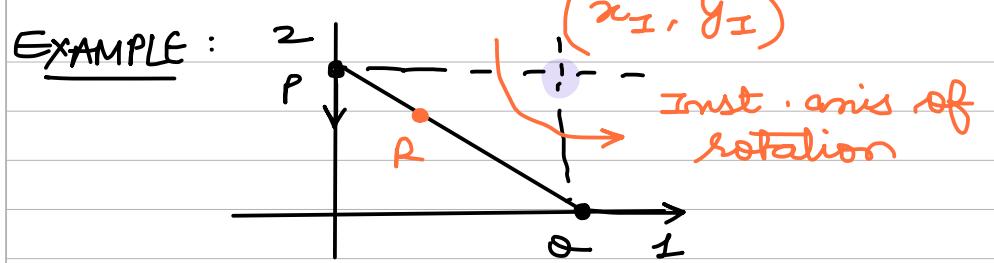
$$\vec{v}_P = \vec{y}_I + \vec{\omega} \times \vec{r}_{P/I}$$

$$\vec{v}_Q = \vec{y}_I + \vec{\omega} \times \vec{r}_{Q/I}$$

Int. of lines $\perp r$ to radii.

Special case: If the velocity vectors
are \parallel to each other.





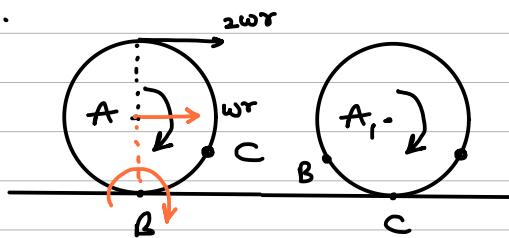
$$\left(\frac{x_I}{L}\right)^2 + \left(\frac{y_I}{L}\right)^2 = 1$$

$$\vec{v}_P = \vec{r}_{I'}^0 + \vec{\omega} \times \vec{r}_{P/I}$$

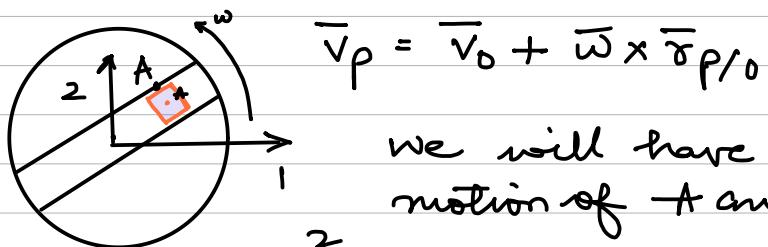
$$\vec{v}_P = \vec{\omega} \times \vec{r}_{P/I}$$

$$|v_P| = \omega |r_{P/I}|$$

Disk:



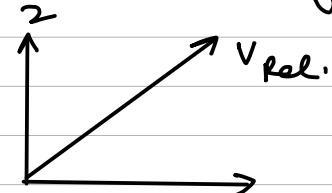
Turntable with slot.



$$\vec{v}_P = \vec{v}_0 + \vec{\omega} \times \vec{r}_{P/0}$$

we will have rel.
motion of A and B

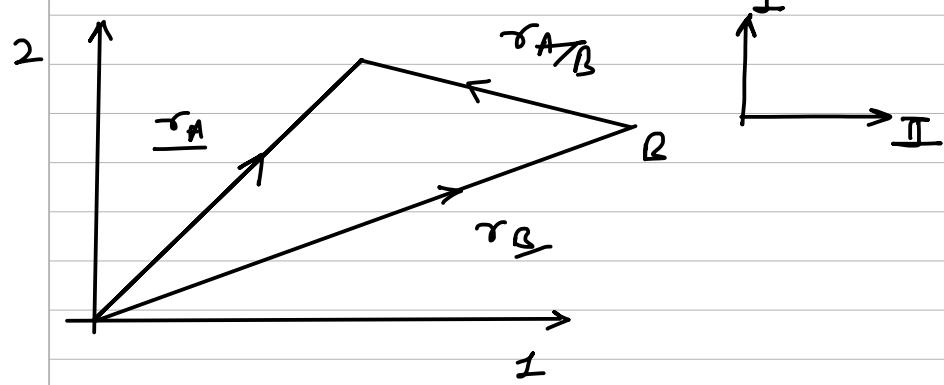
$$v_A = v_P + v_{\text{rel.}}$$



$$\vec{v}_A = \vec{v}_0 + \vec{\omega} \times \vec{r}_{P/0} + \vec{v}_{\text{rel.}}$$

WEEK 3

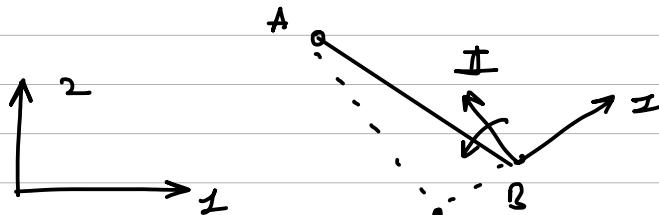
Rotating frame of ref.



$$\bar{r}_A = \bar{r}_B + \bar{r}_{A/B}$$

$$\bar{v}_A = \bar{v}_B + \bar{v}_{A/B}$$

$$\bar{a}_A = \bar{a}_B + \bar{a}_{A/B}$$



Inertial frame

Rotating frame

$$\bar{AB} = \alpha_I \bar{e}_I + \alpha_{II} \bar{e}_{II}$$

$$\bar{r}_A = \bar{r}_B + \alpha_I \bar{e}_I + \alpha_{II} \bar{e}_{II}$$

$$\bar{v}_A = \bar{v}_B + \dot{\alpha}_I \bar{e}_I + \alpha_I \dot{\bar{e}}_I + \dot{\alpha}_{II} \bar{e}_{II}$$

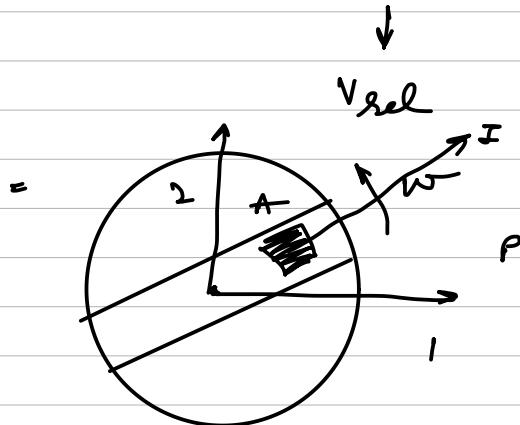
$$+ \alpha_I \bar{e}_{II}$$

$$\frac{\partial}{\partial} \bar{e}_I = \omega \times \bar{e}_I$$

$$\bar{e}_{II} = \omega \times \bar{e}_{II}$$

$$= \bar{v}_B + \dot{\alpha}_I \bar{e}_I + \alpha_I \bar{\omega} \times \bar{e}_I + \ddot{\alpha}_I \bar{e}_I \\ + \alpha_I \bar{\omega} \times \bar{e}_I$$

$$= \bar{v}_B + (\dot{\alpha}_I e_I + \dot{\alpha}_I e_{II}) + \bar{\omega} \times \bar{r}_{A/B}$$



Diff. the velocity

$$\bar{\alpha}_A = \bar{\alpha}_B + \dot{\bar{\omega}} \times \bar{r}_{A/B}$$

$$+ \bar{\omega} \times \frac{d}{dt}(\bar{r}_{A/B}) + \frac{d}{dt}(\bar{v}_{rel})$$

$$\bar{r}_{A/B} = \alpha_I e_I + \alpha_{II} e_{II}$$

$$\frac{d}{dt}(\bar{v}_{rel}) = \frac{d}{dt}(\dot{\alpha}_I e_I + \dot{\alpha}_{II} e_{II})$$

$$= \ddot{\alpha}_I e_I + \alpha_{II} \ddot{\alpha}_{II}$$

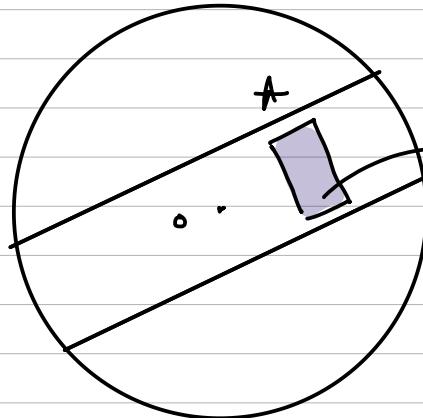
$$- \dot{\alpha}_I \dot{e}_I + \dot{\alpha}_{II} \dot{e}_{II}$$

=

$$\bar{\alpha}_A = \bar{\alpha}_B + \bar{\omega} \times \bar{r}_{A/B} + \bar{\omega} \times (\bar{\omega} \times \bar{r}_{A/B} + \bar{v}_{rel})$$

$$+ \ddot{\alpha}_I \bar{e}_I + \ddot{\alpha}_{II} \bar{e}_{II} + \bar{\omega} \times \bar{v}_{rel}$$

$$= \bar{a}_B + \bar{\alpha} \times \bar{\tau}_{A/B} + \bar{\omega} \times (\bar{\omega} \times \bar{\tau}_{A/B}) \\ + 2\bar{\omega} \times \bar{v}_{rel} + \bar{a}_{rel}$$



* coincides with point P at the given instant of time -

$$\bar{a}_P = \bar{a}_o + \bar{\omega} \times (\bar{\omega} \times \bar{\tau}_{P/o}) + \bar{\alpha} \times \bar{\tau}_{P/o}$$

$$\bar{a}_{A/P} = 2 \underbrace{\bar{\omega} \times \bar{v}_{rel}}_{\text{Coriolis}} + \bar{a}_{rel}$$

diff of global rel. acc - relativ
accn in Rot. frame

$$a_A = a_B + a_{A/B}$$



$$\bar{\omega} \times (\bar{\omega} \times \bar{\tau}_{A/B}) + \bar{\alpha} \times \bar{\tau}_{A/B} + \bar{a}_{rel} \\ + 2(\bar{\omega} \times \bar{v}_{rel})$$

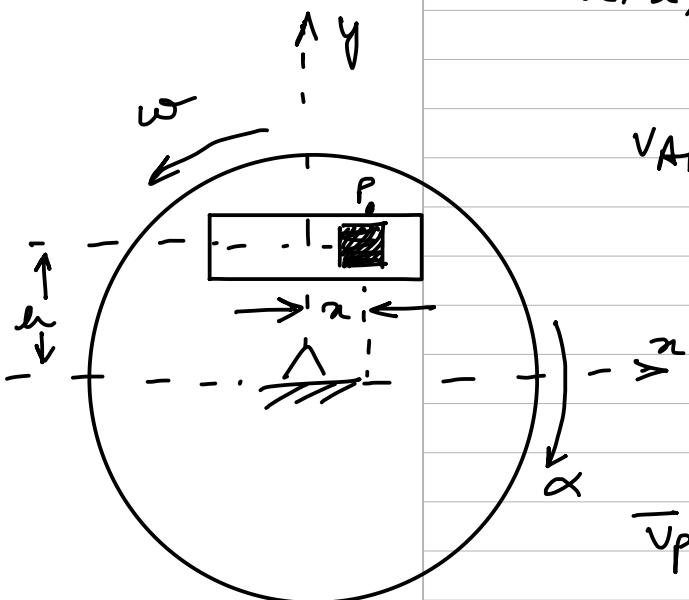
$-G_{400}$

$$a_{A/B} = a_B + \frac{16}{3} \times \left(\frac{16}{3} \times 500 \right) + \alpha \times 500 + 0$$

$$a_B = 6.4 \hat{i}$$

Example:

$$h, \alpha, \omega, \alpha, \frac{dx}{dt}, \frac{d^2x}{dt^2}$$



Absolute and α_{abs}

at $t_1 \rightarrow$ coincides with P .
[Assumption]

$$\bar{r}_{A0} = \bar{r}_A = \bar{r}_P \\ (\bar{x}\bar{e}_1 + h\bar{e}_2)$$

$$\bar{v}_P = \bar{v}_0 + \bar{\omega} \times \bar{r}_{P/0}$$

$$= \omega \bar{e}_3 \times [\bar{x}\bar{e}_1 + h\bar{e}_2]$$

$$= \omega \bar{x}\bar{e}_2 - wh\bar{e}_1$$

$$\bar{v}_A = \bar{v}_P + \bar{v}_{A/P}$$

$$\bar{v}_{abs} = \bar{v}_A - wh\bar{e}_1 + \underbrace{\frac{dh}{dt}\bar{e}_1}_{V_{rel}}$$

$$\bar{a}_P \Rightarrow \bar{a}_0 + \bar{a}_{P/0}$$

$$\Rightarrow \bar{a}_{P/0} = \bar{\omega} \times (\bar{\omega} \times \bar{r}_{P/0}) + \alpha \times \bar{r}_{P/0}$$

$$\bar{a}_P = \alpha [-\bar{x}\bar{e}_2 + h\bar{e}_1] - \omega^2 [\bar{x}\bar{e}_1 + h\bar{e}_2]$$

$$a_A = a_P + a_{P/A}$$

$$\rightarrow \alpha_{\text{app}} = \alpha_{\text{rel}} + 2\bar{\omega} \times \bar{V}_{\text{rel}}$$

Not the absolute
v

$$\alpha_{\text{rel}} = \left(\frac{d^2 \mathbf{x}}{dt^2} \right) \bar{\mathbf{e}}_1$$

$$\text{Coriolis} = 2\bar{\omega} \times \bar{V}_{\text{rel}} = 2\omega \frac{d\mathbf{r}}{dt} \bar{\mathbf{e}}_2$$

$$\begin{aligned} \alpha_{\text{f}} &= \alpha \left[-\mathbf{n} \mathbf{e}_2 + \mathbf{h} \mathbf{e}_1 \right] - \omega^2 \left[\mathbf{x} \mathbf{e}_1 + \mathbf{h} \mathbf{e}_2 \right] \\ &\quad + \frac{d^2 \mathbf{x}}{dt^2} \bar{\mathbf{e}}_1 \end{aligned}$$

INTRO TO MECHANICS

Machine → Combination of mechanisms to provide power from source to load.

Result → 1 DOF



Prismatic → 1 DOF
Trans



→ much motion?

Higher pair → Point contacts

Lower pair → Surface contacts.

Robotics → open chain -

Mechanism : links joined by joints or kinematic pairs

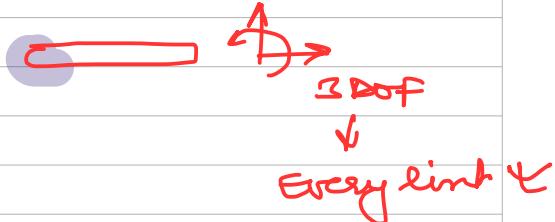
Joint →
lower
higher [point / line]

Linkage mechanism:

DOF → Min. no. of inputs to completely specify location of all links

Fritzsch / Grubbe Criteria:

Planar Case:



Each link → 3 DOF

Total → $3n$ DOF

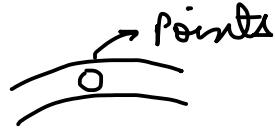
1 link is grounded, $\text{DOF} = F = 3(n-1)$

High → Point Contact

Fixed link -

If all remaining links are isolated

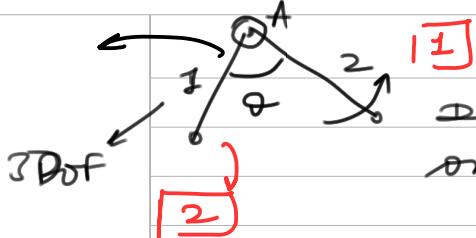
Lower → Surface Contact



Mech → Translating Motion

Mech → Transmitting power

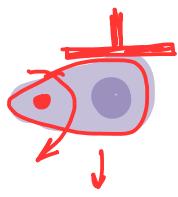
grounded Link



$$3[2-1] - 2 \cdot 1 = 0$$

Dof → :

Due to the joint, we require only 2 to be known



quick rises and falls as well

Each turning pair reduces the Dof by

$$[3-1] = 2$$

If j are turning joints →

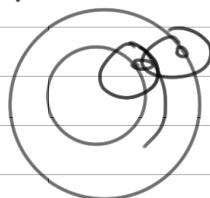
$$\text{Dof} = 3[n-1] - 2j$$

If we have "h" higher pair reduction

$$h[3-2]$$

$$-2j.$$

$$-1$$



Dof, modified :

$$F = 3[n-1] - 2j - h$$

Kutzbach:

If $F = 1$, constrained mechanism

$$1 = 3[n-1] - 2j - h$$

grubler Criteria:

with one grounded Link'

All these of 2D Closed loops.

Definitions :

Link : Body common to 2 or more joints

Kutzbach → derive the Dof of a kinematic chain.

$$\text{Dof} = 3[L-1] - 2J - H$$

[Planar Mech]

↓
No. of links

↓
Joints

→ Higher pairs

CLOSED LOOP

Link \rightarrow 3 DOF

\downarrow
Redundant
 \downarrow

2 Eff.

\rightarrow Lower pair

\downarrow

Removes 1 DOF.

\rightarrow Higher pair

\downarrow

- 2 DOF

can't have arbitrary no. of joints.

$$n = ! F$$

\downarrow
odd even
even odd

$$3[2] \cdot 2[3] - 1$$

"

$$6(n-1) - \begin{cases} (6-1) j_1 \\ (6-2) j_2 \\ (6-3) j_3 \\ (6-4) j_4 \\ (6-5) j_5 \end{cases}$$

$$F = 6[n-1] - 5j_1 - 4j_2 - 3j_3 - 2j_4 - j_5$$

where j_k denotes joint with k DOFs

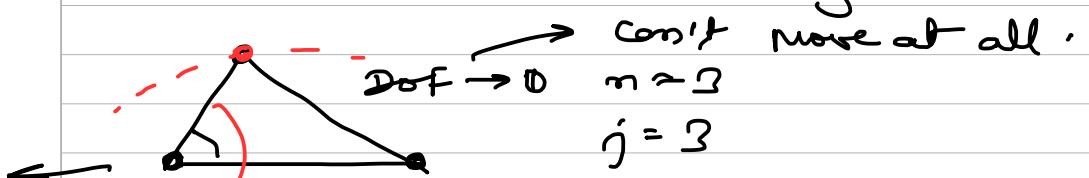
Planar Linkage, with lower pair

\downarrow
Number synthesis -

$$\begin{aligned} F &= 3[n-1] - 2j \\ j &= \frac{\{J(n-1) - F\}}{2} \xrightarrow{\text{Restricted}} \\ F &\Rightarrow [2 - 3(n-1)] \% 2 = 0 \end{aligned}$$

odd - odd $\rightarrow n \rightarrow$ Even.
Even - Even $\rightarrow n \rightarrow$ odd

For a closed loop \rightarrow Min. no. of links = 3.



Length can't change! $F = 3(3-1) - 2 \times 3$

Structure

$$\underline{\underline{F = 0}}$$

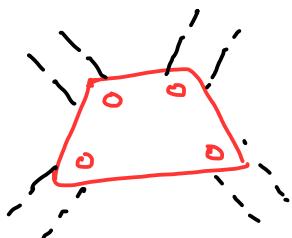
all trusses are triangular

Triangular mechanisms cannot move \rightarrow length of sides can't change

Diagonals
length can
change

$$3[3] - 2[7] \Rightarrow 1$$

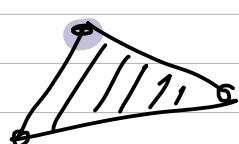
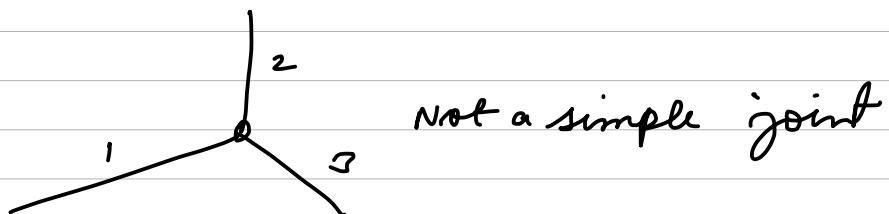
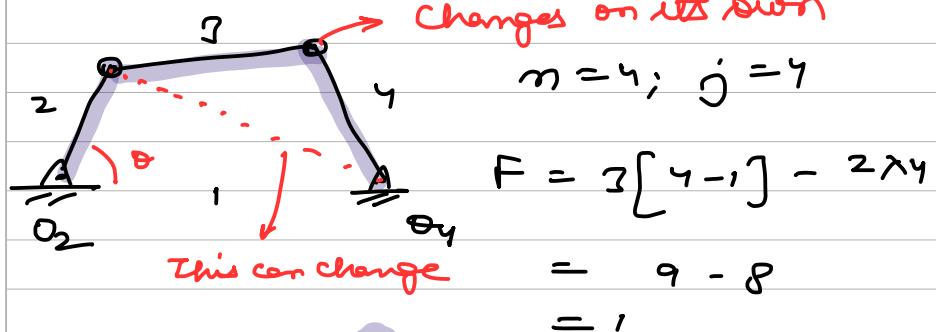
All joints are
simple



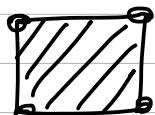
$n_k \rightarrow$ how many
more

Links

for mechanism, no. of links should be $\geq j$



Ternary



Quaternary

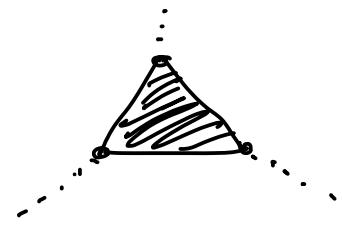
$n_2 \rightarrow$ binary. $n_3 \rightarrow$ ternary

$$n = 0 + n_2 + \dots + n_k$$

joints $\rightarrow j$, each is a simple
link.

No. of elements $\rightarrow 2^j$

$$2n_2 \dots$$



$$n = n_2 + n_3 + \dots + n_k \rightarrow \text{No. of links}$$

\downarrow joints can be made



$$[27] = 2n_2 + 3n_3$$

Total no. of

elements

$$2j^o = 2n_2 + 3n_3 \dots \text{knk}$$

Kutzbach criteria

$$F = 3[n_2 + n_3 \dots]$$

Kutzbach criterion

If $F = 1$ [Constrained mechanism]

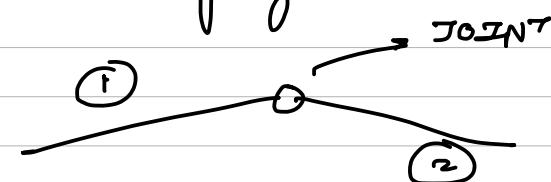
$$3n - 2j - h = 1$$

Grubbe crit.

n_1, n_2, \dots, n_k be binary, tertiary, etc.

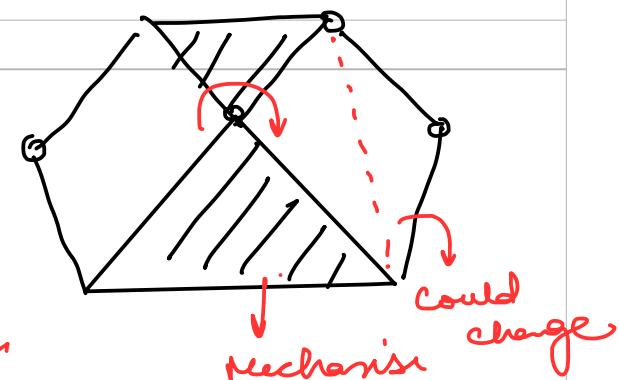
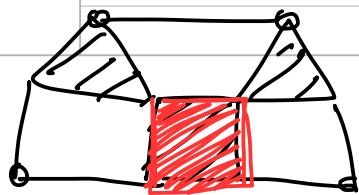
$$n = n_2 + n_3 + \dots + n_k$$

$j \rightarrow$ no. of joints



Total no. of elements

Given n no. of links, we want to find the max. no. of hinges, link.



$N \rightarrow$ no. of links \rightarrow Max. hinges, link

$n \rightarrow$ even

$$n = 8, \text{DOF} = 1, j = 10$$

$$1 = 3[n-1] - 2j$$

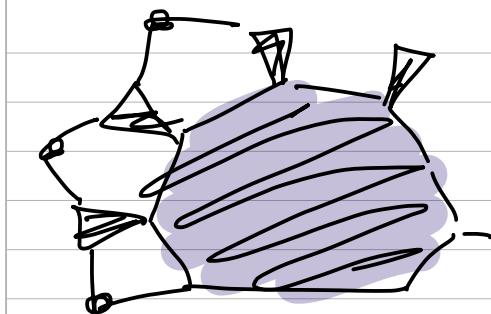
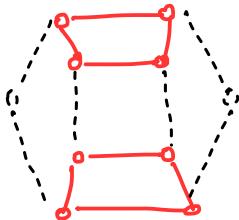
$$\boxed{3n-2j = 4}$$

$$\boxed{n = n_2 + n_3 \dots n_k}$$

$$2j = 2n_2 + 3n_3 \dots n_k$$

$$\boxed{j=10, n=8}$$

Konse.



No. of links

$$= k + [k-1+1]$$

$$= 2k$$

hinge

$$\text{No. of elements} \rightarrow n \left[\frac{n}{2}, \frac{n+1}{2} \right]$$

given "n" links, we can have a link with max. $\frac{n}{2}$ [n = even]

$$\left[\frac{n+1}{2} \right] \quad n = \text{odd}$$

hinges .

$$\begin{aligned} j &= 7, \\ \frac{n}{2} &\rightarrow \frac{6}{2} \Rightarrow 3; \\ n &= 6 \end{aligned}$$

what's the use

$$F = 1; n = 6$$

$$1 = 3[n-1] - 2j$$

$$j = 7$$

$$\frac{n}{2} \rightarrow \frac{6}{2} \Rightarrow 3;$$

$$\begin{aligned} 2 &\rightarrow \text{Link } 1, 3 \\ 1 &\rightarrow 2, 6, 5 \\ 4 &\rightarrow 3, 6, 5 \\ 3 &\rightarrow 4, 2 \\ 6 &\rightarrow 1, 4 \\ 5 &\rightarrow 4, 1 \end{aligned}$$

→ Non-link capacity

$$n_2 + n_3 = 6$$

$$2n_2 + 3n_3 = 14$$

$$n_2 = 4; n_3 = 2$$



$$z = 3[6] - 2j$$

$$j = 8$$

$$\frac{n}{8} \Rightarrow n_4$$

$$16 = 2n_2 + 3n_3 + 4n_4$$

$$\underline{n_2 + n_3 + n_4 = 7}$$

Family of
solutions

$$n = 7 ; F = 2$$

$$F = 3(n-1) - 2j$$

$$j = 8$$

Links with max no. of rings

$$\Rightarrow \frac{7+1}{2} = 4 \rightarrow \text{Bim}\text{-}\text{Quat}\text{-}\text{Tern-}$$

$$n_2 + n_3 + n_4 = 7$$

$$2n_2 + 3n_3 + 4n_4 = 16$$

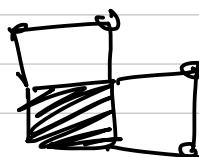
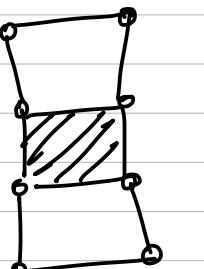
get a family of solution

$$n_3 + 2n_4 = 2$$

$$n_3 = 2, n_4 = 0$$

$$n_3 = 0, n_4 = 1$$

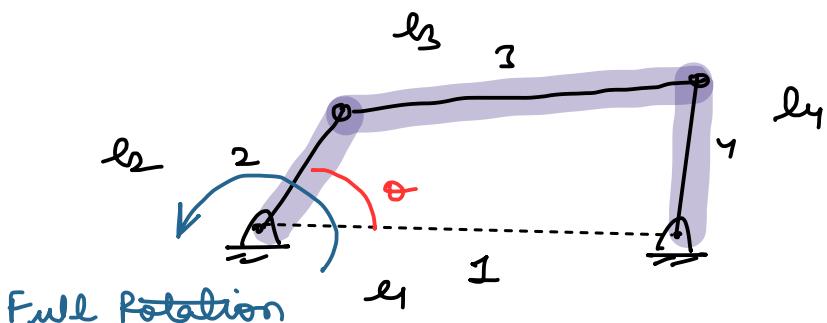
$$n_2 = 6$$



understood

MAINS!

4-BAR MECHANICS



GRASHOFF.

$\theta \rightarrow$ defines the whole state

$\Delta \rightarrow$ Rigid bar or frame.

$s + l <$

CRANK

↓
the one that
rotates
fully.

SIDE LINK
MECHANISM:

Double Rocker

Double
CRANK

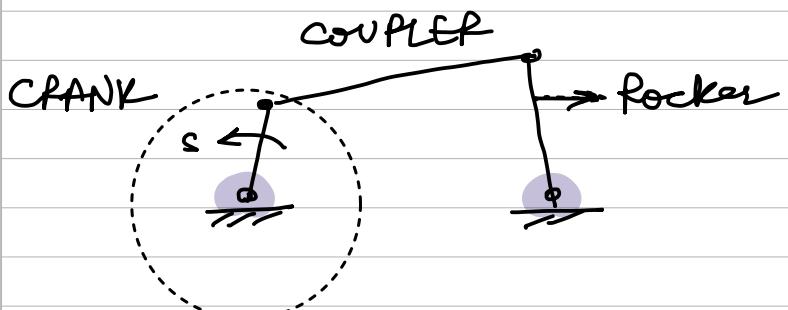
s, p, q, l

If $s + l < p + q$

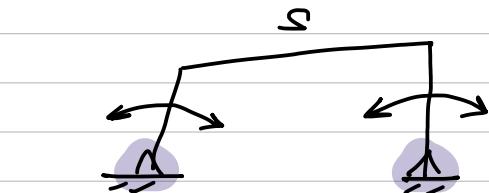
then one of the links will undergo full rotation.

If $l + s > p + q \rightarrow$ triple rocker mechanism.

Link adjacent to s is fixed, shortest will complete one rotation and will have a crank-rocker mechanism.



b) If link opposite to " s " is fixed we have double rocker mech.

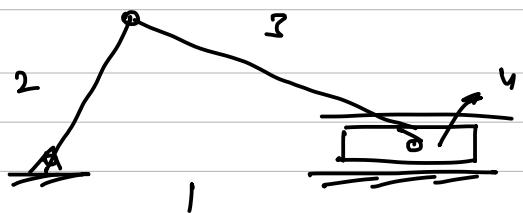


c) If s is fixed, we will have a double crank mechanism.



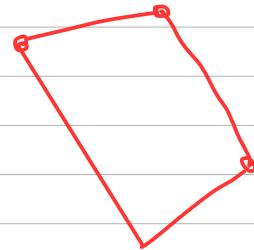
Inversion of mechanisms are obtained by changing fixed length

CUT-OFF \rightarrow satisfy homocentricity



$$F = 3[4 - 1] - 2 \times 4 = 1$$

Bump Jack :



First bicycle → Germany.

Karl Drais.

Watt's linkage → Suspension.

James Watt, engine wala.

Mechanism → Inversions.