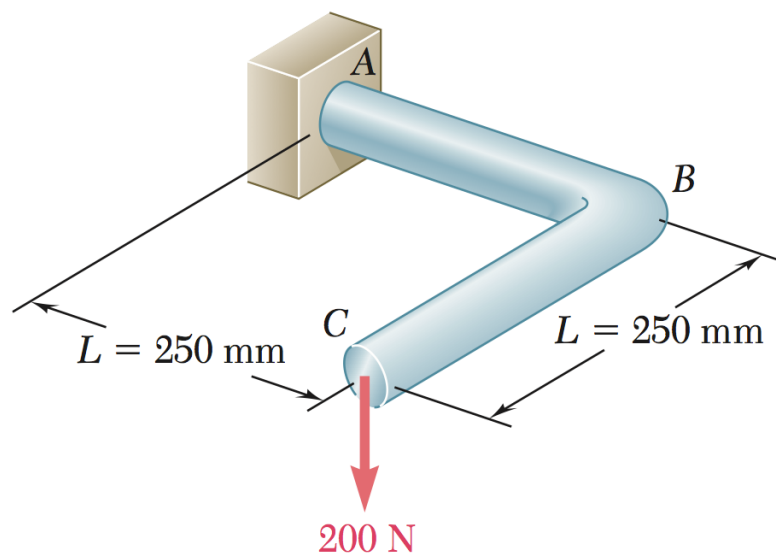
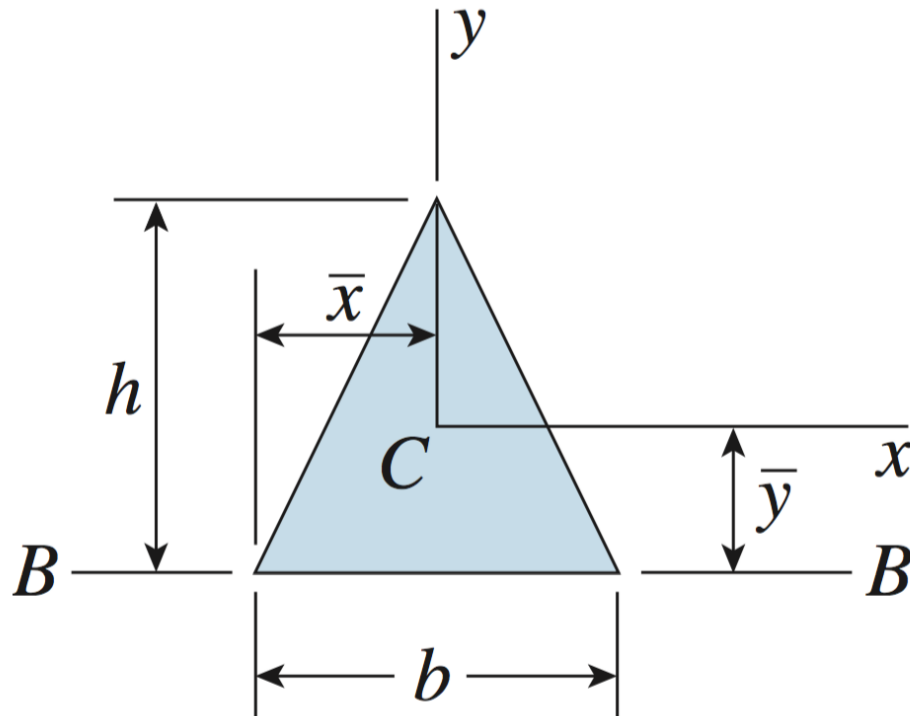


ME 202 Strength of Materials Spring 2023  
Tutorial 10 13 April 2023

1. Use CT2 (Castigliano Theorem 2) to find the displacement of the point C in the direction of the applied load  $P = 200\text{ N}$ .  $EI$  and  $GJ$  are respectively the flexural and torsional rigidities of the bent beam ABC.



2. A cantilever fixed at one end has an isosceles triangle cross-section shown below. Take  $b = 10\text{ mm}$ ,  $h = 20\text{ mm}$ . C is the centroid of the cross-section. Consider a new centroidal system  $x'-y'$  rotated through  $60^\circ$  anticlockwise about the  $z$ -axis with respect to the  $x-y$  system. The applied bending moments in the new system are  $M_{x'} = 10\text{ Nm}$ ,  $M_{y'} = 0\text{ Nm}$ . Find the equation of the neutral line in the new system.



3. Refer to the triangle ABC shown above which is the cross-section of a shaft of length  $L$  fixed at  $z = 0$  and free at  $z = L$ . An axial torque  $T$  is applied along the  $z$ -axis. Use the potential energy method to calculate the approximate angle of twist at the free end.  $G$  is the shear modulus of the shaft material.

4. A fin of an underwater vehicle is modeled as a solid prismatic shaft. The  $x$ - $y$  cross-section of this shaft (length  $L$ , shear modulus  $G$ ) is the quadrilateral region with vertices located at the points  $(0, a), (-b, 0), (0, -a), (b, 0)$  where  $0 < a \ll b \ll L$ . The shaft carries an axial torque along the length ( $z$  direction). Find the approximate torsional stiffness of this shaft using the soap film/membrane analogy.