

Data Structures & Algorithms

* Array.

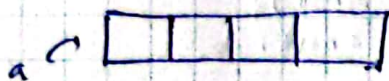
basic structure \rightarrow variable.

arrays \rightarrow control a number of values

Student marks

```
int a = 250
int b = 65
int c = 35
int d = 71
int e = 21
```

} 5 variables



Contiguous

int a[]

① Index system

$a[\text{index}] \times \text{base address}$

$+ [\text{index}] \times [\text{size of data type}]$

② Pointer system

$a^* + [\text{size of data type}]$

contiguous = one after the other

* Multidimensional Array

array of arrays (array inside array).

int a[3][5]

↑ ↑
row column

Arrays.

Pros

- Fast access any element in a constant time.
- Homogeneous \rightarrow only one data type can hold.
- Contiguous = one after the other.

Cons

- dynamic resizability issue
- for array, can't remove value and add value in 2nd, 3rd array and shift mem on 2nd - looping

Exercise: How to find size of array

$$\frac{\text{size of } (a)}{\text{size of } (0 \text{ index})} = \text{size}$$

Exercise or solution to this in multi-dimensional array.

There are two ways to store data in memory by chipset

- row major order - eg: intel
- column major order

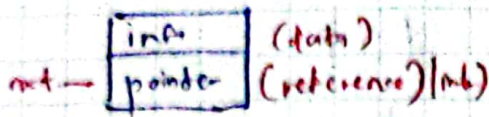
Linked List (in C-struct)

Why

- arrays dynamic resizability problem
- solution dynamic list

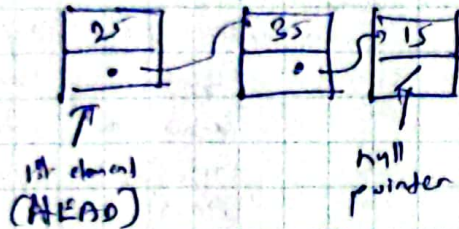
There are two ways that linked list works.

① Node Structure



```
struct {
    int a;
    int * ptr;
} (next)
```

Eg: A[25, 35, 15] A[25, 35, 15]



Head - reference to 1st block
 Head.info = 25
 Head.next.info = 35
 Head.next.next.info = 15

* Singly Lh, (SLL)

- One link between nodes
- $\square \rightarrow \square \rightarrow \square$
- HEAD → first element of the list
- TAIL → last element of the list

* Insert Operations

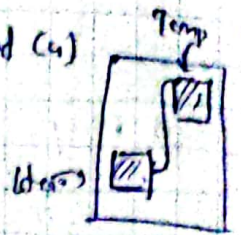
- putting new elements to a SLL
- Where are we going to put?

- Before HEAD
- After TAIL
- In the middle
- How do add to an empty list

a Data type matches?

How do add to an empty list

- 1) Head = Tail = ϕ
- 2) create a node element (a)
- 3) Head = Tail = a

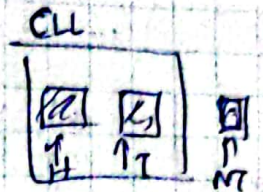


• Add to Head

Temp.next = Head;
 Head = Temp;

• Add to Tail

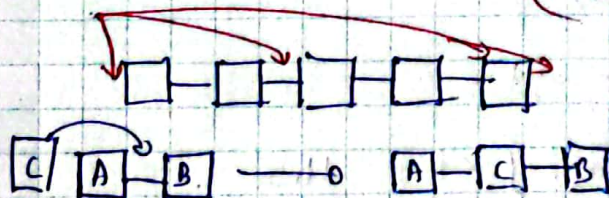
New Tail
 NewTail.next = Tail;
 Tail.next = newtail;
 newtail = tail;



Head = Tail = null
 if (Head == null) {
 tail.head = next node;
 }

ADD.

(Insert Point)



①

temp1 = A
 temp2 = B

temp1.next = C
 C.next = temp2

②

A.next = C
 C.next = B

Why?



when we do according to 2nd way, there A.next will work - when we doing that we remove A.next = B's reference. So C.next = B will not work because already we lost the list that's why!

(Finding Point)

Strategy (Manual indexing)

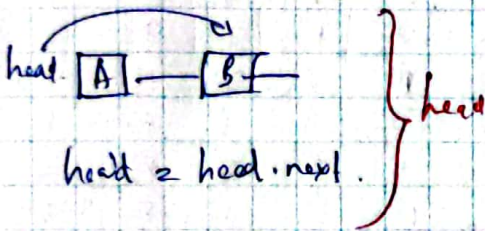
temp = head.
while (temp != null; counter = 2) {
temp = temp.next;
counter++;
}

Strategy Searching for an element

Delete

- ① Delete from head
- ② Delete from Tail
- ③ Delete from anywhere

① Delete from head/tail.



① Counting method. ②

temp = tail check.
if (temp.next == null) {
temp = tail;
}

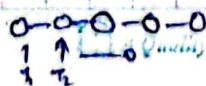
③ Delete from anywhere



A.next = B.next.

if (temp.next != null) {
temp = temp.next;
}

* 2 pointer method
set t1 and the
temp t2.next.next



Doubly Linked List

What is a data structure?

A data structure is

Q1 Searching for a specific value in an array?
locating to array by it's indexes.
Ex: int arr[3] = {50, 60, 70};
printf("%d", arr[0]);

Q2 Testing for uniqueness and deleting duplicates in an array?
to check if that got first value of the array and check if there any duplicates in that array. If there any duplicate then that array index equals to zero for deleting the value. (2 for loop)

Q3 Finding the min/max in an array?

to store data of the first index of the array in a variable. Then compare that variable with other indexes, where that is minimum or maximum. If that is minimum then it is the min function that stored to the above variable.

int arr[3] = {50, 60, 70};
int min = arr[0];
int max = arr[0];

```

for (int i = 0; i < 3; i++) {
    if (min > arr[i])
        min = arr[i];
}
  
```

```

for (int i = 0; i < 3; i++) {
    if (max < arr[i])
        max = arr[i];
}
  
```

Q4 Counting how many times a specific value appear in an array.
to get the value from the user that need to check. Then compare that value with first array index whether it is equal

or not.

if this equal then counter will increase.

Q) Set Intersection/Union between array 1 and another sorted array 2?

Q) Counting how many values in an array is inside range.
to define array, assign first value of the first index into variable.
Then compare it with the given range. If it is in the range then count will increase.

```
int arr[5] = {43, 45, 23, 32, 56};
int a = arr[0];
int count = 0;
for (int i = 0; i < 5; i++) {
    if ((range) < a < (range2))
        count = count + 1;
    arr[0] = arr[i];
}
```

Sorting

Sorting Algorithms

What is sorting?

Sorting refers to the operation or technique of arranging and rearranging sets of data in some specific order.

O X D P → E D P X
 4 1 3 2 → 1 3 4 2

Different types of sorting algorithms:

- ↳ Bubble Sort
- ↳ Insertion Sort
- ↳ Selection Sort
- ↳ Merge Sort
- ↳ Quick Sort

1) Bubble Sort

↳ which continuously switches nearby components if they are in the wrong order.

Large data sets should not be used with this approach due to its high average and worst case time complexity.

Q) 8 3 7 9 2 1

3 8 7 9 2 1

3 7 8 9 2 1

3 7 8 9 2 1

3 7 8 2 9 1

3 7 8 2 1 9

3 7 8 2 1 9

3 7 2 8 1 9

3 7 2 1 8 9

3 7 2 1 8 9

3 2 7 1 8 9

3 2 7 1 8 9

3 2 1 7 8 9

3 2 1 7 8 9

2 3 1 7 8 9

2 1 3 7 8 9

2 1 3 7 8 9

2 1 3 7 8 9

2 1 3 7 8 9

1 2 3 7 8 9

1 2 3 7 8 9

1 2 3 7 8 9

1 2 3 7 8 9

1 2 3 7 8 9

1 2 3 7 8 9

int arr[5] = {8, 3, 7, 9, 2, 1};

```
int temp;
int i = 0;
int j = 0;
int a = arr[0];
for (int i = 0; i < 6; i++) {
    for (int j = 0; j < 6; j++) {
        if (arr[j] > arr[j+1]) {
            temp = arr[j];
            arr[j] = arr[j+1];
            arr[j+1] = temp;
        }
    }
}
```


int a = 5;
int b = 6;
int temp;

int a = temp; temp = a;
a = b;
b = temp;

for i <= 0 to list.Length - 1
for j <= 0 to list.Length - 1 - i
if list[j] > list[j+1]
Swap(list[j], list[j+1])

enhancing algorithm

Q. 3. 4. 1. 5. 6

for i <= 5 to list.Length - 1
for j <= 5 to list.Length - 1 - i

3 4 1 5 6
3 4 1 5 6
3 1 4 5 6
2 1 4 5 6
1 3 4 5 6
1 3 4 5 6
1 3 4 5 6

* Stable / Unstable Algorithms

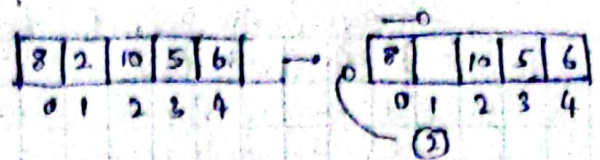
Stable Algorithms

Let two items with equal keys appear in the output data set in the same order as they do in the input data set, a sorting algorithm is described as stable.

Sorting Algorithms

- 1) Bubble Sort
- 2) Insertion Sort
- 3) Selection Sort

① Insertion Sort



Status : [8, 2, 10, 5, 6]
[0, 1, 2, 3, 4]

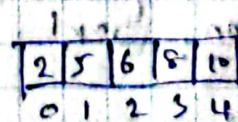
Step 1: Take the first value of the first index and compare it with (temp variable). Take the value of the first index and compare it with value of the zeroth index value.

Step 2: If it is greater than the value, then move the value of the first index to first index.

Step 3: Then insert the value of the temp variable into the zeroth index.

Step 4: Then take the value of the second index, compare it with sorted items, according to closest. In this example with first index if it is greater than the value simply move and then insert the temp value to previous index.

Step 5: Likewise do this until getting a sorted list.



Algorithm

To sort an array of size N in ascending order:

↳ Iterate from arr[1] to arr[N-1] over the array.

- Compare the current element (key) to its predecessor.
- If the key element is smaller than its predecessor compare it to the elements before.
- Move the greater elements one position up to make space for the swapped element.

Pseudo Code

```

mark the first element as sorted.
for each unsorted element X {
    'extract' the element X
    for (j is last sorted index down to 0) {
        if (current element j > X) {
            move sorted element to the
            right by 1.
        }
    }
    breaks the loop and insert X here
}

```

→ When to use Insertion Sort?

- Used when number of elements is small.
- Can be useful when input array is almost sorted.
- When only few elements are misplaced in complete big array.

② Selection Sort

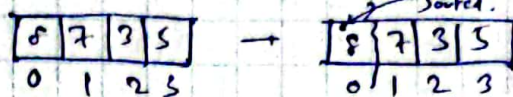
This sort an array by repeatedly finding the minimum item (when talking about ascending order) from the unsorted part and putting it in front.

The algorithm have two sub-arrays in a given array.

- The sub-array which already sorted.

• The remaining sub-array was unsorted.

- Define two arrays.
- One array that hold the unsorted array.
- Define the ~~first~~ index value as sorted.
- Then compare with ~~first one~~ if it is ~~large~~ ~~then~~ minimum value of the unsorted array if it is ~~higher~~ ~~than~~ smaller than the sorted one. push it to the front.
- do this again until sorted the array.



Algorithm

- Initialize minimum value (minindex) to location 0.
- Traverse the array to find the minimum element in the array.
- While traversing if any element smaller than minindex is found then swap both the index values.
- Swap elements.
- Then, increment minindex to point to the next element.
- Repeat until the array is sorted.

Pseudo Code

$N \geq \text{Length of the array } Arr$
for $i \leftarrow 0$ to $(N-1)$:

$min_index \leftarrow i$

 for $j \leftarrow i+1$ to $(N-1)$:

 if $Arr[min_index] > Arr[j]$:

$min_index \leftarrow j$

 Swap ($Arr[i]$, $Arr[min_index]$)

Q. When to use Selection Sort?

- On short arrays, it works really well.
- It's useful for determining whether everything has already been sorted.
- When memory utilization should be considered, this is due to the fact that selection sort uses less temporary storage space since, in contrast to other sorting algorithms, it moves the element by only switching items at the very end.

Recursion

Academic Game

Algorithm

```

Ask and wait
Ask and wait
Ask and wait
Reach first in line Tell person behind it's 0.
Tell person it is a 1
Tell person it is x + 1
    
```

What is Recursion?

Recursion is the process of defining a problem (or the solution to a problem) in terms of a simpler version of itself.

Two main components of a recursive algorithm

1. Base Case

The point where you stop applying the recursive case.

2. The Recursive Case
The set of instructions that will be used over and over.

Pseudo Code

Definition: A recursive function is a function that calls itself.

```

numberOfPeopleInFront(person) {
  If (there is no one in front)
    return 0
    
```

Else

```

  let the person in front of you (P)
  return 1 + numberOfPeopleInFront(P)
    
```

Fibonacci → 1, 1, 2, 3, 5, 8, 13, 21.

Fib(n) {

take first two numbers as 1 and 1
add two numbers when number count equal to 2.

recursive case

add two numbers with the previous number,
count = count + 1.

loop runs until count equal to 6
return the value

Base case

```

2 = 0;
x = 1;
y = 1;
new_number = x + y;
count = 2;
for (int i = count; i < 22; i++) {
  count++;
    
```


Jan-20 - 510

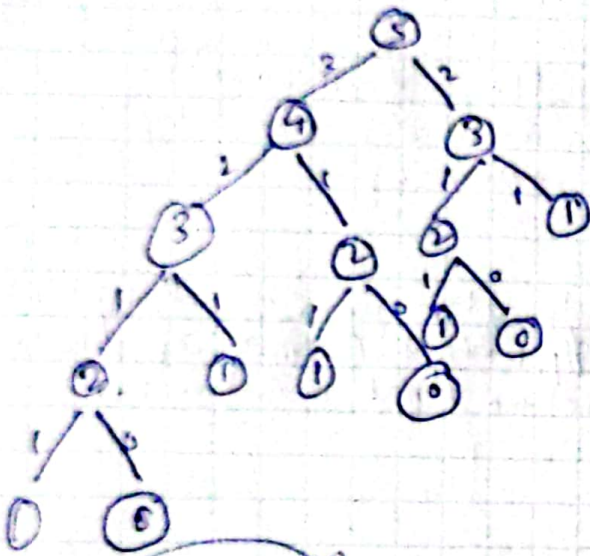
2: new number;
y: new number.

Algorithm

function: $fib(n)$;

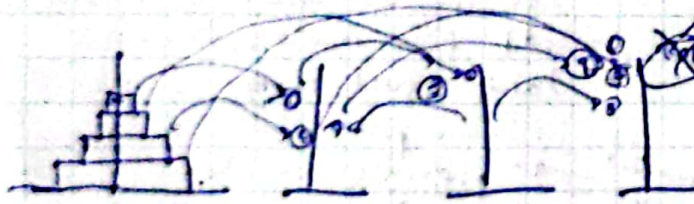
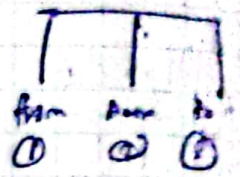
if ($n \leq 0$ or $n \leq 1$);
return 1

return $fib(n-1) + fib(n-2)$

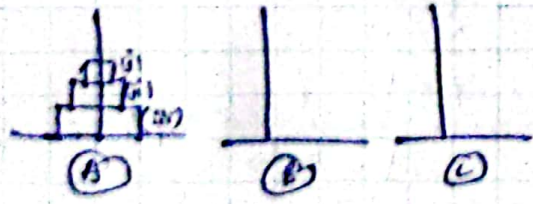


Step 1: 0 to B.
1 to C
2 to C
3 to B
4 to A
5 to B
0 to B

Step 2: 1 to B.
2 to C
3 to C
4 to B
5 to A
6 to B
7 to B
8 to C
9 to A
10 to C
11 to B.



Algorithm



function TowerOfHanoi (n, f-rod, t-rod, aux-rod)
if $n \geq 0$;
return.

TowerOfHanoi (n-1, f-rod, aux-rod, t-rod)
print ("Move disk", n, "from", f-rod, "to", t-rod)
TowerOfHanoi (n-1, aux-rod, t-rod, f-rod)

Sorting Methods

Internal Sorting Algorithms

When all data is placed in the main memory or internal memory then sorting is called internal sorting.

Ex: heap sort, bubble sort, selection sort, quick sort, shell sort, insertion sort.

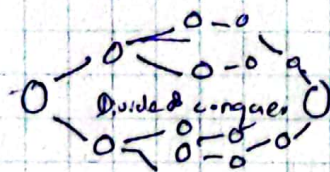
External Sorting Algorithms

When the data being sorted do not fit into the main memory of a computing device, (usually RAM) and instead they must reside in the slower external memory (usually the hard drive)

Ex: Merge Sort.

Merge Sort

basic concept.



algorithm depend on divide and conquer concept.

to divide the array into two equal parts until it becomes empty or one element left sort them separately and finally join them together

Merge Sort - Pseudo Code

merge-sort (int A[], int start, int end)

```

{
  if (start < end) {
    int mid = (start + end) / 2; // divides the array
    merge-sort(A, start, mid); // sort the 1st part
    merge-sort(A, mid+1, end); // sort the 2nd part of array
  }
}

```

// merge both parts by comparing elements of both parts.

merge (A, start, mid, end);

```

}
merge (int A[], int start, int mid, int end) {

```

// stores the starting position of both parts in temporary array.

int p = start, q = mid+1