



தொண்டமானாறு வளரிக்கலா நிலையம் நடாத்தும்  
நான்காம் தவணைப் பர்ட்செ - 2022

Conducted by Field Work Centre, Thondaimanaru.

4<sup>th</sup> Term Examination - 2022

Grade :- 13 (2022)

Combined Mathematics II - A

Three hours and ten minutes

Admission No

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**Instructions**

- This question paper consists of two parts; Part A (questions 1 - 10) and part B (questions 11 - 17).

**Part - A**

- Answer all questions. Answers should be written in the space provided on the questions paper. If additional space needed, you may use additional answer sheets.

**Part - B**

- Answer only 5 questions.
- After the allocated time hand over the paper to the supervisor with both parts attached together.
- Only part B of the paper is allowed to be taken out of the examination hall.

Combined mathematicsI		
Part	Question	Marks
A	1	
	2	
	3	
	4	
	5	
	6	
	7	
	8	
	9	
	10	
B	11	
	12	
	13	
	14	
	15	
	16	
	17	
	Total	

Combined Maths I

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Combined MathsII

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Total

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Final Marks

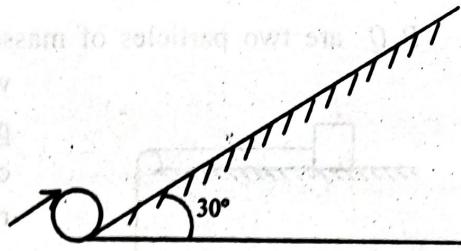
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### **Part - A**

- 1) Two spheres A and B with equal radii of mass  $2m$  and  $3m$  respectively are placed at an interval on the horizontal table and given the velocities  $3u$ ,  $2u$  respectively in the direction AB along the line joining the centers. Find the velocities of A, B shortly after the collision of A with B and show that the kinetic energy lost in the collision as  $\frac{9mu^2}{16}$  where the coefficient of restitution between the two spheres is  $\frac{1}{4}$ .

- 2) Show that the equation of path of a particle in the vertical plane, thrown from a point O in the horizontal ground making an angle  $\tan^{-1}\left(\frac{3}{4}\right)$  with the vertical component of the velocity  $3\sqrt{ag}$  is  $x^2 - 24ax + 32ay = 0$ , where OX and OY are horizontal and vertical axis respectively. Hence find the horizontal range b between the two points when the particle is in the depth  $\frac{a}{2}$  below the highest point.

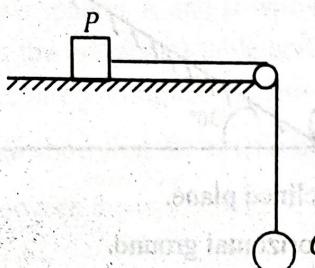
- 3) A particle of mass  $m$  is thrown with a velocity  $4\sqrt{ag}$  along the line of highest slope in the inclined plane of length  $4a$  which makes an angle  $30^\circ$  with horizontal. Using only the principle of conservation of energy.



- Find the velocity of particle at the highest point of the inclined plane.
- Find the maximum height the particle reaches from the horizontal ground.

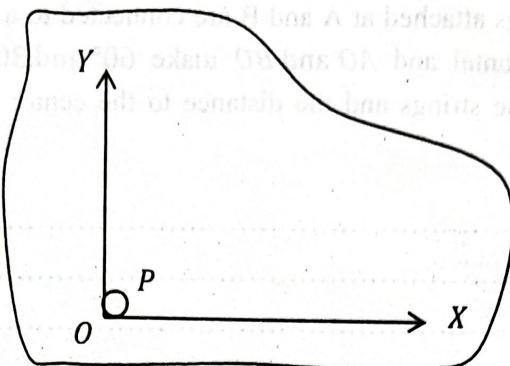
- 4) Find the power of the engine when the car of mass  $2700 \text{ kg}$  is travelling along an inclined plane with an inclination  $30^\circ$  to the horizontal, against resistance force of  $800 \text{ N}$  with a velocity  $16 \text{ ms}^{-1}$  when the car passes the point A the engine switches off. Find the distance it travels before comes to rest (take that the resistance force to the motion does not change)

- 5)  $P, Q$  are two particles of masses  $12m$ ,  $6m$  respectively.  $P$  is on a rough horizontal table which is attached to one end of a light inelastic string which passes over a smooth pulley fixed on the edge of the table and carries  $Q$  while the string is taut, the system is released from rest if the velocities of the particles in the continuous motion at the time  $\sqrt{\frac{8a}{g}}$  seconds is  $\sqrt{2ag}$ . Find the coefficient of friction between  $P$  and the table and find the tension of the string.
- .....  
 .....



- 6) A particle  $P$  of mass  $m$  is attached to a light inelastic string of length  $5a$ .  $P$  is kept on a smooth horizontal table and the string is passed through a smooth hole on the table and carries a particle of mass  $m$ . Keeping the string taut the particle  $P$  moves with an angular velocity  $\omega$ . On the table while the particle  $Q$  moves with an angular velocity  $2\omega$ . Show that length of string below the table is and if  $\omega = \sqrt{\frac{g}{2a}}$ , Find the angle the string below the table makes with the vertical
- .....  
 .....

- 7)



$OX$ ,  $OY$  are two axes perpendicular to each other a smooth plane,  $\underline{i}$  and  $\underline{j}$  are corresponding vectors along the  $X$  and  $Y$  axes respectively. When the particle of mass  $m$  is placed at  $O$  and given forces of  $4\underline{i} - 5\underline{j}$  and  $x\underline{i} + y\underline{j}$  Newton, their resultant is found in the direction of  $\underline{i} - 2\underline{j}$ .

- i) Find the angle between the resultant and  $j$ .

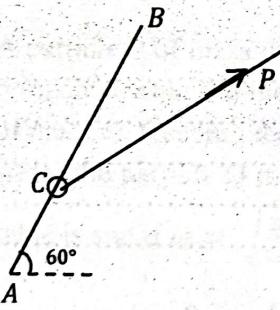
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- ii) Show that  $2x + y + 3 = 0$ .

8) The position vectors of points A, B and C are  $\underline{a}$ ,  $\underline{b}$  and  $\underline{c}$  respectively.  $\alpha$ ,  $\beta$  and  $\gamma$  are non zero constants. If  $\alpha\underline{a} + \beta\underline{b} + \gamma\underline{c} = \underline{0}$  and  $\alpha + \beta + \gamma = 0$  then show that A, B and C are collinear.

- 9) Weights  $2W$  and  $W$  are attached ends A, B of a rod of weight  $2W$  and length  $4a$  respectively and the ends of two light long strings attached at A and B are connected to a point O above. At equilibrium the parts AB is horizontal and  $AO$  and  $BO$  make  $60^\circ$  and  $30^\circ$  with horizontal respectively. Find the tension of the strings and the distance to the centre of gravity of rod from A.

10)



In a light rod fixed in an inclination  $60^\circ$  to the horizontal a ring of weight  $W$  is attached and is kept at limiting equilibrium by a force  $P$  given to the ring with an angle  $60^\circ$  to the upper vertical. If the coefficient of friction between the ring and the rod is  $\frac{\sqrt{3}}{2}$ . Find the force  $P$  and the normal reaction given to the ring by the rod.



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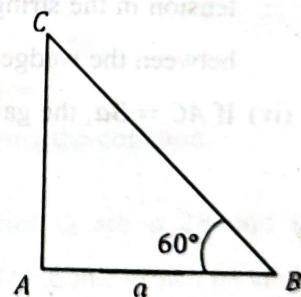
Grade :- 13 (2022)

Combined mathematics II - B

11) (a) A particle P is thrown vertically upwards with velocity V under gravity such that it reaches the maximum height  $\frac{25u^2}{2g}$  when the velocity of P is  $\frac{4V}{5}$  Upwards, another particle Q is thrown towards P with a velocity  $2u$  at a height  $h$  ( $h > \frac{9u^2}{2g}$ ) from the ground. If the velocity of Q when P, Q collide is  $5u$

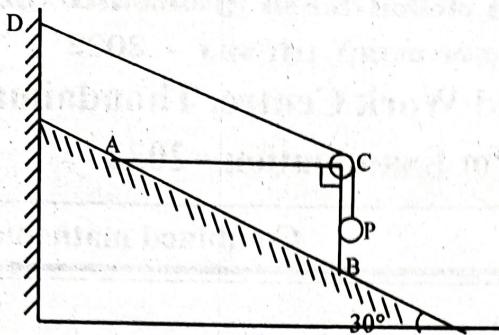
- (i) Show that  $V = 5u$
- (ii) Draw the velocity time graph for P and Q in the same diagram from the time when P is thrown till the collision.
- (iii) From the graph find the speed of P at the same time of collision (P and Q).
- (iv) Find the height of the particle P from the land when the velocity of the particle P is  $\frac{4V}{5}$ .
- (v) Find time taken for Q to collide with P from the moment it was thrown.
- (vi) Find the height of h.

(b) A, B and C are three positions in a ground as shown in the figure P, Q and R are 3 racers in the positions A, B, C respectively. At the same time Q, R from the positions B, C respectively move in the direction AC with the uniform velocities. Mean while P with aim of catching up with Q first moves with the velocities  $2V$ . First he shakes hand with Q and immediately meet with the R moving with the same speed in a straight line.



- (i) Using the principle of relative velocity draw the velocity triangle.
- (ii) Using the velocity triangle find the time taken for P to meet Q.
- (iii) Find the distance between P and R when P and Q meets.
- (iv) Find the time taken for P to meet R.
- (v) Show that the time taken meet P and R is  $\frac{4a}{(\sqrt{13}-3)V}$

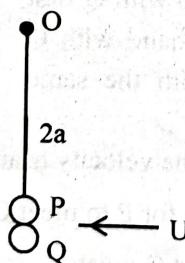
12)



The given figure shows vertical cross section through the centre of gravity of a smooth uniform wedge of mass  $4m$ . Where  $\hat{A}C\hat{B} = 90^\circ$ . This wedge as shown in the figure is placed on an smooth inclined plan inclined to the horizontal such that the face  $BC$  is vertical and the face  $AB$  touches the inclined plane a particle of mass  $m$  is attached to a light inelastic string and the string passes through a smooth pulley in  $C$  and the other end is attached to  $D$  such that  $DC$  is parallel to  $AB$  as shown in the figure. The system is initially held Such that the particle  $P$  is held close to  $B$  and face  $BC$  and is in the line of highest slope of the face and the system is released from the rest in the continuous motion, before  $P$  reaches  $C$ .

- Mark all the forces acting in the particle and wedge.
- Mark clearly the accelerations of the particle and the wedge.
- Gain enough equations to determine the accelerations of particle and the wedge, the tension in the string, the reaction given by the inclined plane to the wedge and the reaction between the wedge and the particle.
- If  $AC = 3a$ , the gain the equation to determine the time taken for  $P$  to reach  $C$ .

13)



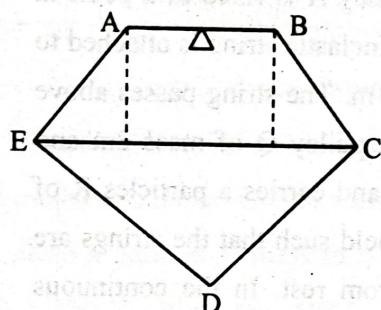
One end of a light inelastic string of length  $2a$  is attached to a point  $O$  which is at a height  $3a$  from ground and a particles of equal masses  $P$ ,  $Q$  are joined to the other end and the particles are given the velocity  $u$  horizontally.

- In the continuous motion when the string makes an angle  $\theta$  with downward vertical. Find the velocity of particles  $P$ ,  $Q$  and the tension in the string.
- If the particle  $P$  leaves smoothly from the particle  $Q$  when the string makes an angle  $\frac{\pi}{3}$  with the downward vertical then in the continuous motion. Find the velocity of  $P$  and the tension in the string when the particle  $P$  makes an angle  $\theta$  upward with the horizontal line passing through point  $O$ .

- (iii) Find the minimum velocity  $u_0$  of U for P to execute full circular motion.
- (iv) If the particles are initially given the velocity  $u_0$ , find the distance from the vertical line through O to the point where Q reaches the ground.
- 14) (a) As shown in the figure a light pulley A is fixed to a point in the ceiling and one end of a light inelastic string is attached to smooth uniform pulley P of mass m. The string passes above the pulley A and passes below a pulley Q of mass  $2m$  and again passes about the pulley P, and carries a particle R of mass  $4m$ . Initially the system is held such that the strings are taut and vertical and released from rest. In the continuous motion clearly mark the forces and acceleration of the particles, gain enough equations to determine the tension and accelerations of particles P, Q and R.
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- (b) Two smooth spheres A and B of equal radii of masses  $km$  and  $m$  ( $2 < k < 3$ ) are projected towards each other with the velocity  $2u$ ,  $4u$  along the line joining the centres on a smooth floor. After the collision the speed of particle A is halved and the direction is reversed.
- Find the velocity of B just after the collision in terms of  $k$ .
  - If  $k$  is given as  $k = \frac{7}{3}$ 
    - Show that the velocity of B is inverted after the collision.
    - Find the coefficient of restitution and the impulse during the collision.
- 15) (a) The position vectors of A, B, C respectively to the point O are  $\underline{a}$ ,  $2\underline{b}$  and  $(\underline{a} + \underline{b})$  respectively the midpoint of OC is M. AM and OB meet at D the line drawn parallel to MA through O meet the extended CA at N. Let  $OD = \lambda OB$ ,  $AN = \mu CA$  and  $AD = \gamma AM$ .
- Find the vectors  $\overrightarrow{CA}$  and  $\overrightarrow{AM}$  in terms of  $\gamma, \lambda, \mu, \underline{a}, \underline{b}$ .
  - Find the vector  $\overrightarrow{OD}$ ,  $\overrightarrow{AN}$  and  $\overrightarrow{AD}$  in terms of  $\gamma, \lambda, \mu, \underline{a}, \underline{b}$
  - Using appropriate vector additions find  $\lambda, \mu$ , and  $\gamma$ . Hence find the position vectors of D and N and find the ratio of the A divide the line CN.
- (b) In triangle ABC the midpoint of AC is D and  $AB = BD = DC = 2a$ . The forces of magnitude  $2P$ ,  $\sqrt{3}P$ ,  $P$ ,  $2P$  and  $P$  act along  $\overrightarrow{AB}$ ,  $\overrightarrow{BC}$ ,  $\overrightarrow{DB}$ ,  $\overrightarrow{DC}$ , and  $\overrightarrow{DA}$  respectively.
- Find the resultant in direction and magnitude of the system.
  - Show that the line of action of resultant is perpendicular to BD.

- (iii) Find the point whose the line of action the resultant intersect AB.
- (iv) Find the sense and magnitude of the couple that has to be added for the resultant to go through B.
- (v) When the resultant in goes through B, if an additional force of  $6P$  is added through  $\overrightarrow{BD}$ . Find the direction of new resultant.

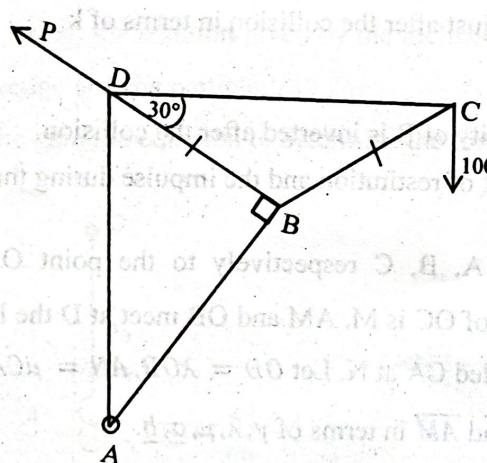
16) (a)



The uniform rods of weight  $W$  such that  $AB = AE = BC = 2a$ ,  $CD = DE = 4a$ . These are joined smoothly as shown in the figure and is kept in equilibrium by a wedge in the midpoint of AB and a light rod of length joined to the point C, E.

- (i) Find the reaction given by the wedge.
- (ii) Find the stress in the light rod EC and the reaction in the joint D.
- (iii) Find the horizontal and vertical components of the reaction in a point A in the rod AB.

(b)



The frame work made up of light rods is hinged at the joint A as shown in the figure. A force  $P$  act on D in the direction BD and a weight of 100 N is hanged at C So that DC is horizontal and AD is vertical.

- i) Find the direction of the reaction in the joint a using the bow notation draw the stress diagram and find the stress in each of the rods stating whether they are tension or thrust.
- ii) Find the value of  $P$ .

- 17) (a) A smooth hemisphere container of radius  $\sqrt{3}a$  is fixed such that its curved surface touches the ground and its edge is horizontal inside the container rod AB of weight W and length  $6a$  is placed such that the end A is inside the hemisphere and the end B is on the outside. The point C on the rod touches the horizontal edge of the hemisphere. The rod is in equilibrium. If the centre of gravity of the rod G is such that  $AG : GB = 1 : 2$
- Show that the inclination of the rod to the horizontal is  $\theta = \frac{\pi}{6}$ .
  - Find the reaction on A, C by the hemisphere.
  - If a particle of weight W is attached on the end B, show that the rod will never be in equilibrium.
- (b) A rod at length  $2a$  and weight W is in limiting equilibrium in such a way that its one end is on a rough inclined plane and the other end is on a vertical smooth wall BD it makes an angle  $\theta$  with vertical. let B is above A, If the coefficient of friction between the rod and the inclined plane is  $\lambda$ .
- Show that  $\tan \theta = 2 \tan(\lambda - \alpha)$
  - Find the reaction given by the wall to the rod.
  - Find the frictional force and reaction given by the inclined plane in the rod.