

For the shear face, we can write,

~ ~= VQ; where, dm= v= Vertical shear force in the section.

Q= SOJA I = location where we want to find shear

1/2 = extreme fibre :. a = 1st moment of area about neutral axis from the location of interest to the extreme end.

Note that me assume prismothe but arbitrary cross-section. Instead of an arbitrary cross-section, let us now consider a rectangular crass-section.



of the sectongular cross-section

2= VB; for a cortain location, V, I, b me constant

$$Q = \begin{cases} y dA = \begin{cases} y b dy = b \left( \frac{y^2}{4} - y^2 \right) \end{cases}$$

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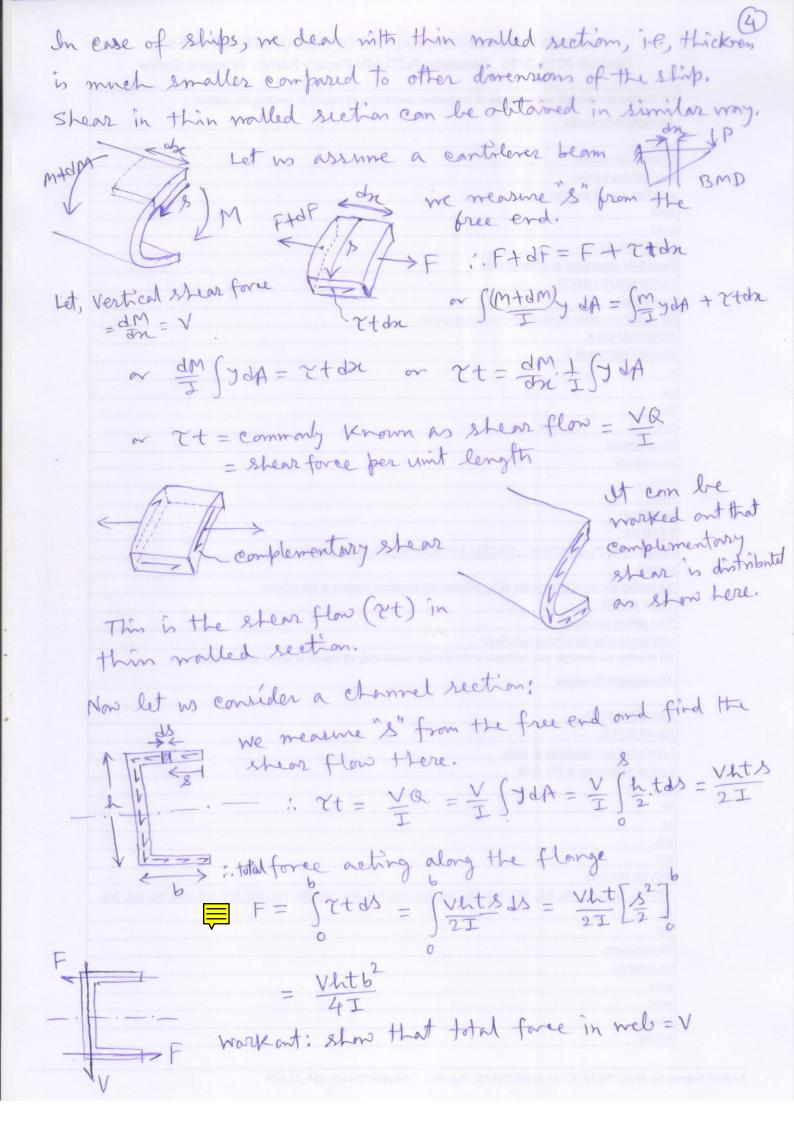
!.  $T = \frac{V}{Ib} \cdot \frac{b}{2} \left( \frac{h^2}{4} - y^2 \right) \rightarrow parabelie variation$ 

Then  $= \mathcal{T}(My=0) = \frac{V(h^2)}{2I(4)}$ Wing  $I = \frac{bh^2}{12}$ ,  $\mathcal{T}_{mon} = \frac{3}{2bh} = 1.5 \mathcal{T}_{avj}$ 

Note: V = Shear force (vertical) in the section to be found 3 from the stear force diagrams. V = Zaij = average stear stren. Example: An I- beam is made out of three rectangular wooden planks by driving nails. It will support a point load as shown Find the required spacing of the noils. Given, allewable normal stress in bending = 7 N/mm, extress in bending = 7 N/mm, allowable shear in rails = 3 KN 2m. First find the SFD of the problem and also 3 P (Nm) 3 P 4 P SFD all in mm N.A. will pass through the middle of the seether. So, the centroidal MOI = 25×200 +2×200×25 + (200×25)×112°52]×2 = 143°75×10 mm Given that allowable normal stress in bending = 7 N/mm

x1000 (since moment mas in Nm)

i. My = 0 ~ 3 P x 10 T  $\frac{M}{I}y = \sigma \sim \frac{3}{8}P \times 125 = 7 \text{ N/mm}^2$   $\frac{143.75 \times 10^6}{143.75 \times 10^6} = 7 \text{ N/mm}^2$ Due to bending, there will be longitudinal shear forces This force has to be carried by the rails. It "s" be the required spacing): 768 = 3000 N. ~ S= 3000; here, 6=25 mm  $\sim S = \frac{3000.1.6}{25.\sqrt{Q}} = \frac{3000 \times 143.75 \times 10}{(\frac{3}{4} \times \frac{35.6 \times 10}{21466}) \times (200 \times 25 \times 112.5)} = 47.62 \text{ mm}$ i. Drive rails @ 45 mm. Note Hat vertical stear force is taken 00 3 P.



.. We see that the vertical bending is coursing not only the vertical force (total) in web = V, but a comple that tries to twist the section = Fh. (I eff.
This is equivalent to apply "

the vertical force V at a distance" e" from the meb, such that  $\therefore Ve = Fh = \frac{Vhtb^2}{4I} \therefore e = \frac{b^2h^2t}{4I}$ The point on the Longontal oxis at a distance "e"

is called shear centre(s). Since the honizontal asin is an axis of symmetry, 's' will lie on it. Note that b, h, t, I all are sectional properties.

Hence shear centre is also a property of the section. Two important facts about shear centre - O If force / vertical force is applied along stear centre, there will be only beneling and ro torsian. (1) Under a tristing moment, a rection trists about its shear centre.

Try to understand there two points. Hint: for a consider FBD of the whole section carridoring reaction also. for fristing/ rotation takes place about that point where moment = 0,

As you can see in above that me start from a free end since we know that shear stress at the pree end must be equals to zero (0).

But, for example in case of a ship which is rectangular type closed section, there is no free end. Such sections are taken A 2 as indeterminate problem. Typically there will be a vertical axis of symmetry. - [. - . ] - Let us consider the distribution of normal

4 B 3 stress due to bending.

We split the section along restread line AB:

ED You can inderstand that the resultant largitudinal force in A 14B and A'23B' are zero, hence there is no action along AC a A'D for relative movement.

Hence shear stren at A,A', B, B' must be zero. Note that it is passible only when AB is an axis of symmetry. So, now the shear strin can by taking one half of the section and this is similar to a channel section. A Sty Shear flow along AB:

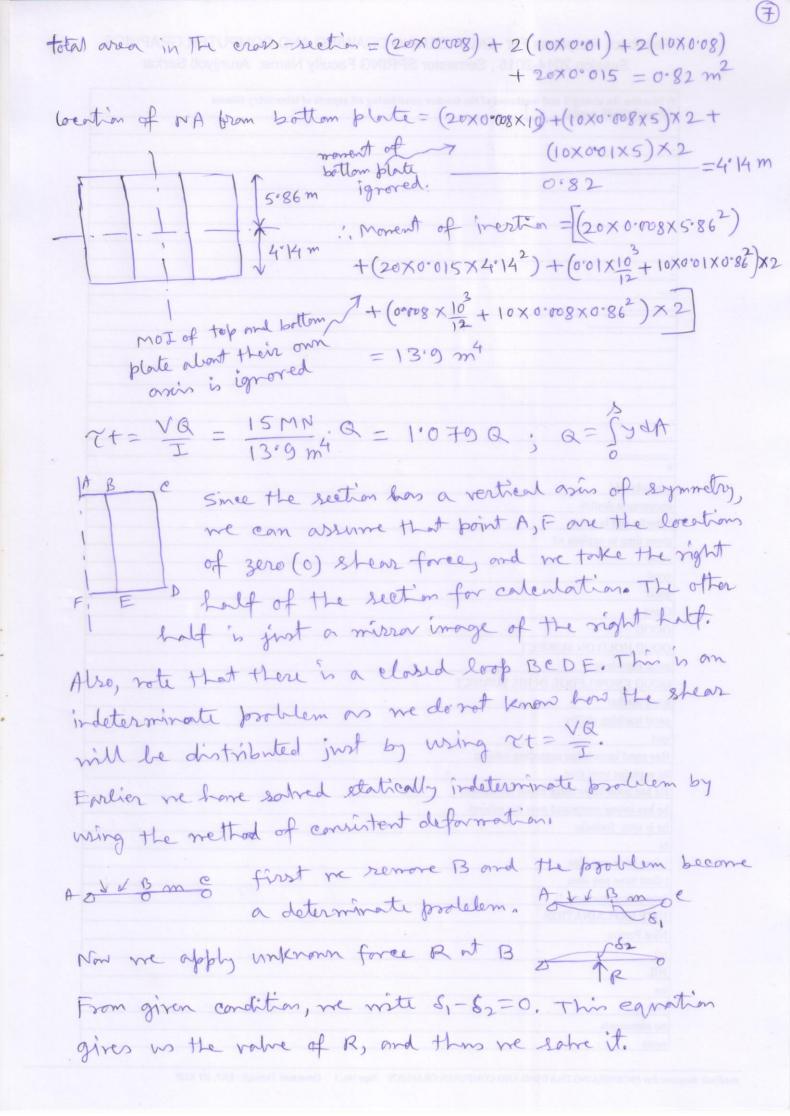
No Sty Shear flow along AB:

The Sty Shitteds = Vhitteds

The Congrethickness livearly along AB.

The Glange thickness (Streams) similarly, along DC, Tt varies linearly: Tt = Vhates Along BC, Tt = VQ Q = SydA = (btfh)+ S(h,-8,)tnds, this part is = btfh, + h, tw 8, - tn 8, for floringe = btfh, + h, tw 8, - tn 8, 2  $- 2t = \frac{V}{I} \left( bt_f h_1 + h_1 tw \delta_1 - tw \delta_1^2 \right)$ this Tt is masimum at s,= h, i.e., at the rentral axis. Note that Q = gydA -> is the 1st moment of over from free end (zero stear here) who the point of interest. Its Hence, moment of the flarge (constant) and web are added together. Take the following example: The cross-section of a ship is shown.

The cross-section of a ship is shown. symmetry.



So, in case of the closed loop, we can take similar approach. We assume that there is a slit/ent in the loop, so ~= 0 at 1 of ent/slit Then estimate the value of gap created by the applied londs. longitudinal of the displacement/gap when top view created total gap created by this = grds = g = ds = igf cds = igf eds Now we apply on unknown training moment in the section to close the gap. Tristing moment in a section causes shear stress/shear flow (2t). It can be shown that in an arbitrary section (thin malled), It due to tarque remains constant. (This is shown little later). is gap created by tristing moment = fifth = fifth is = CCt) f ds (: Ct = constant) Then me wse (of ra) = (ct) gds to get (ct) we to the thisting moment. = V fads ement for a torque, take force of is short and 2 must be same.

Common to both the force of the same.

Hence of the same. For equilibrium of there 2 elements, the force narked equilibrium of each elements. Thus I't remains constant along the section encountering a tristing moment T.

going back to the problem, Is2 at the top of the vertical plate. since, 7t = 1.079 Q; Q= SydA, Let m evaluate Q along the lines.

Q = \( \frac{5}{5} \) \( \frac{5}{3} \)

Q = \( \frac{5}{5} \) \( 86 \times \) \( \frac{3}{5} \)

Q 10 \( \frac{3}{5} \) Q1(8,=10) = 0.47m, ~(8,=10) = 0.507 MN/m Q2 = 0.47 + S(5.86-82) ×0.01×ds2 = 0.47 + 0.058682-0.00582 Q2(82=5.86)=0.6417, Q2(82=10)=0.556m3 .. Tt (82=5.86) = 0.692 MN/m, Tt (82=10) = 0.6 MN/m Q3 = 0.556 + S(-4.14) x0.015 db3 = 0.556-0.062183 Q3 (83=5) = 0.245, ~(83=5) = 0.264 MN/m.  $Q_4 = 0 + \int (5.86 - 84) \times 0.008 \times 354 = 0.047 84 - 0.004 84$  $Q_4(84=5.86)=0.138 \text{ m}, Q_4(84=10)=0.07 \text{ m}$ 7+(34=5.86) = 0.149 mN/m, 7+(84=10) = 0.075 mN/m Q5 = (0.07 + 0.245) + SE 4.14) x0.015 x ds = 0.315 - 0.0621 85 Q5(35=5) = 0.0045 -> this should be actually = 0. Due to

approximations made before, some small values appeared, me can ignore it.

Now since we have to use the expression Ing that = Tt gds Let us find & I do for the loop.

evaluation of 
$$\frac{V}{TG} \int_{T}^{6} ds$$

$$\frac{S_{1}^{4}}{S_{1}} = \int_{S}^{10} \frac{0.047}{0.047} \int_{S_{1}}^{8} ds = \left[ 5.875 \frac{S_{1}^{2}}{5} \right]_{S}^{10} = 220.31$$

$$\int_{T_{1}}^{82} ds_{1} = \int_{S}^{10} \frac{0.047}{0.0586} \int_{S_{2}}^{8} - 0.005 \frac{S_{2}^{2}}{0.015} ds_{2} = 596.3$$

$$\int_{T_{1}}^{83} ds_{3} = \int_{S_{1}}^{10} \frac{0.0556}{0.015} - 0.004 \frac{S_{2}^{2}}{0.08} ds_{2} = 133.58$$

$$\int_{T_{1}}^{84} ds_{3} = \int_{S_{1}}^{10} \frac{0.047}{0.004} \int_{S_{1}}^{8} ds_{3} = 133.58$$

$$\int_{S_{1}}^{84} ds_{3} = \int_{S_{1}}^{10} \frac{0.047}{0.004} \int_{S_{1}}^{8} ds_{4} = 127.1$$

$$\int_{S_{1}}^{8} ds_{1} = \left[ \frac{0.047}{0.008} + 596.3 + 133.58 - 127.1 \right] \int_{S_{1}}^{8} ds_{1} = 127.1$$

$$\int_{S_{1}}^{8} ds_{1} = \left[ \frac{1.07}{0.008} + 596.3 + 133.58 - 127.1 \right] \int_{S_{1}}^{8} ds_{1} = \frac{10}{0.008} \int_$$

