$\begin{aligned}
y_1 &= 1.0 \\
y_2 &= y_1 + Af(t_1, y_1) \\
&= 1.1 + 0.1 * (t_1 + y_1) \\
&= 1.1 + 0.1 * (0.1 + 1.1) \\
&= 1.1 + 0.1 * (0.1 + 1.1) \\
&= 1.22
\end{aligned}$ 

itn	1 42
10.1	1-1
0.2	1.22
0.3	1-362
0.4	1-5202
0.5	1.72102
0.6	1.943122
0.7	2.1943122
0.8	2-487178
0.9	2-815895
1-0	3.187485

Ex Do the serve postblam with h= 0.2, 0.3, 0:05.

```
Ger Solve the IVP U=-2kut, U10)=1 woing the wind
  point mother, with h=0.2 over the interval [0,1]. Use
  the Taylor series method of sectional order to compute
   4(0.2).
    Mid poul-wathrol
                                   f = -2hy2
           4j+1=4j-1 +2hfj
              Uj+ = uj- - 4h xj uj h=0.2
              4j+1=4j+-0.8 2j 4j 2
    (1 = U(24) = U(0+h) = U(0) + hullo) + h 2 ullo)
          410)=1, 410)=f(0,40)=0
                u = f(n,u)
                 u' = -2xu^2
 2600
                 " = -242 - Ase U
  4=.2
              (11(0) = -242 - 4x 40
  12= 4
  13 = . 6
                     =-2 - . $.0. ho
  My = . 8
   15 = 1.0
                ull(0) = -2
       U1 = .96 from (1)
j=1, 40=1, 41=-96 h=0.2
      u_2 = u_0 - .8 \times .2 \times (.96)^2
= 1 - .8 × .2 × (.96)<sup>2</sup>
              = .05244
```

$$j=2$$
 $u(.6) = u_3 = u_1 - .8. \chi_2 u_2$ 
 $= 0.96 - 0.8 \times 0.4 \times (.05244)$ 
 $= .7274139$ 

Y4= y(14) = y(.4) = 3.5109205

@ Apply Taylor's series method of order p to the possible no 17n- y(xn) 1 5 (b+1) xn exn 5d Taylork Deries materal of order p Jn+= Jn+ Ryn+ 1/21 yn + - + ep (b) y'=y, y''=y'=y, y''=yJnn = [1+ h+ h + - + h] Jn = [1+h+ b] + - + = ] Jn-1  $= \left[1 + h + \frac{h^{2}}{2!} + - + \frac{h}{p!} \right] y_{n+1}$   $cr' = \left[1 + h + \frac{h^{2}}{2!} + - + \frac{h}{p!} \right] y_{0}$ or  $y_n = [1 + h + \frac{1}{h} + - + \frac{h}{h!}]^n y_0$ MAD y = y, y(0)=1 dy = dr lny = 2 pluc y=cex for y(0)=1=)(=1 so y'= y wthy(0)=1 has exact solution 7 = ex

20 
$$y(x_n) = e^{2x_n} = e^{nh} = (e^{nh})^n$$

$$e^{h} = 1 + h + \frac{h^2}{2!} + - + \frac{h^2}{p!} + \frac{e^{h+1}}{(p+1)!} e^{hh} + \frac{h^2}{p!} e^{hh}$$

Then

$$y(x_n) - y_n = \left[ 1 + h + \frac{h^2}{2!} + - + \frac{h^2}{p!} + \frac{h^2}{(p+1)!} e^{hh} - \left[ 1 + h + \frac{h^2}{2!} + + \frac{h^2}{p!} \right]^n \right]$$

Take  $T = 1 + h + \frac{h^2}{2!} + - + \frac{h^2}{p!}$ 

Are we use Powerial and poweron

$$(2 + \pi)^h = x^h + n_n \cdot x^h = h + n_{n+1} \cdot x^h$$

 $| J(2m) - J_n | \leq 2m \frac{e^{\frac{1}{p}}}{(p+1)!} e^{2m} \cdot e^{2m} \cdot e^{2m} = \frac{(0+)^{\frac{1}{p}}}{e^{(1-9)^{\frac{1}{p}}}} \leq 1$   $| J(2m) - J_n | \leq 2m \frac{e^{\frac{1}{p}}}{(p+1)!} e^{2m}$