

Question 1 - BIOS14 (HT2021)

Read and explore data

#Question 1

```
rm(list=ls())

library(ppcor)

## Loading required package: MASS

library(lmodel2)
library(lmtest)

## Warning: package 'lmtest' was built under R version 4.1.2

## Loading required package: zoo

##
## Attaching package: 'zoo'

## The following objects are masked from 'package:base':
##
##      as.Date, as.Date.numeric

library(car)

## Loading required package: carData

#read data and explore
plankton<-read.csv('plankton.csv')
str(plankton)

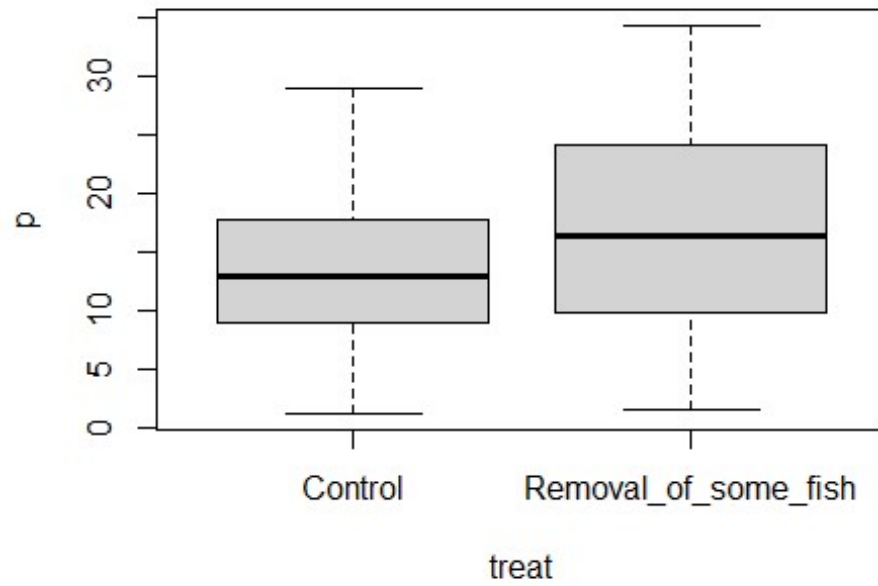
## 'data.frame':    40 obs. of  3 variables:
##  $ treat: chr  "Control" "Control" "Control" "Control" ...
##  $ p    : num  18.66 9.74 10.83 1.29 16.42 ...
##  $ plank: num  311.1 211.2 269.5 58.3 264.4 ...

plankton$treat <- factor(plankton$treat)
str(plankton)

## 'data.frame':    40 obs. of  3 variables:
##  $ treat: Factor w/ 2 levels "Control","Removal_of_some_fish": 1 1 1 1 1 1
##  $ p    : num  18.66 9.74 10.83 1.29 16.42 ...
##  $ plank: num  311.1 211.2 269.5 58.3 264.4 ...

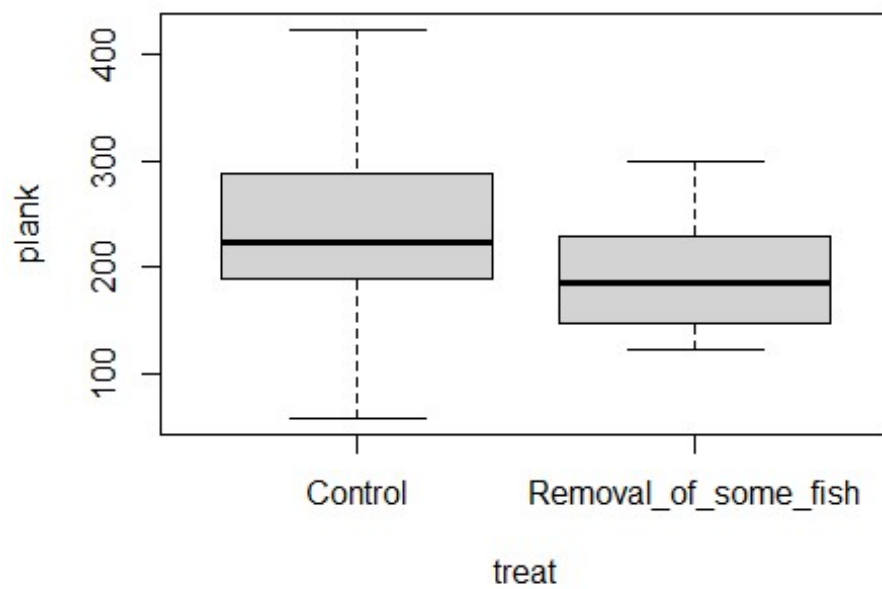
plot(p~treat, data=plankton, main='Phosphorus data')
```

Phosphorus data

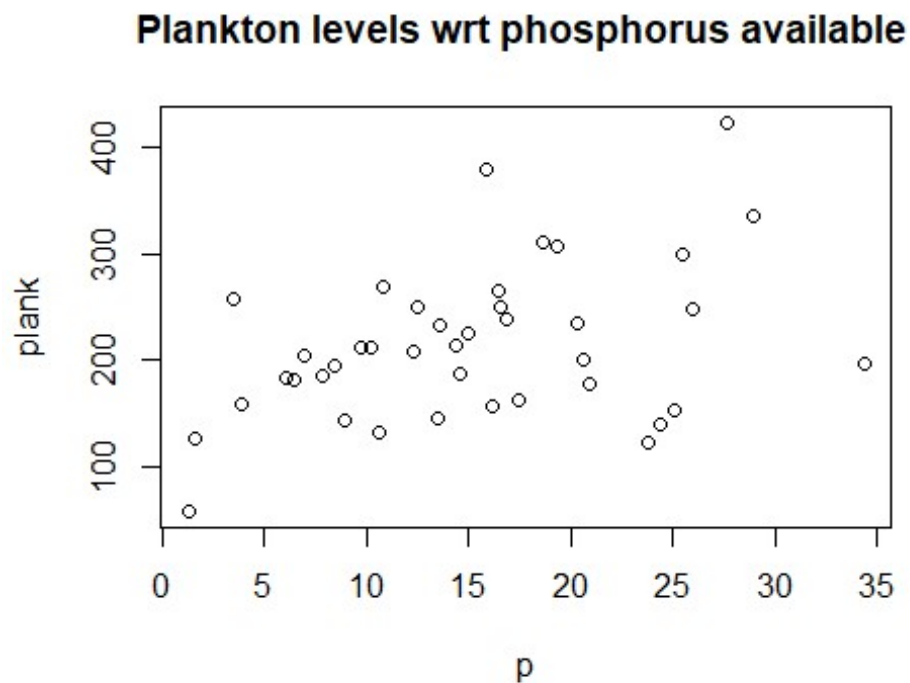


```
plot(plank~treat, data=plankton, main='Algal growth data')
```

Algal growth data



```
plot(plank~p, data=plankton, main='Plankton levels wrt phosphorus available')
```



#may be linear

Part (a)

Here, I have used **Partial correlation** to understand if the relationship between phosphorus concentration and plankton density vary with removal of fish from the pond

#Partial correlation

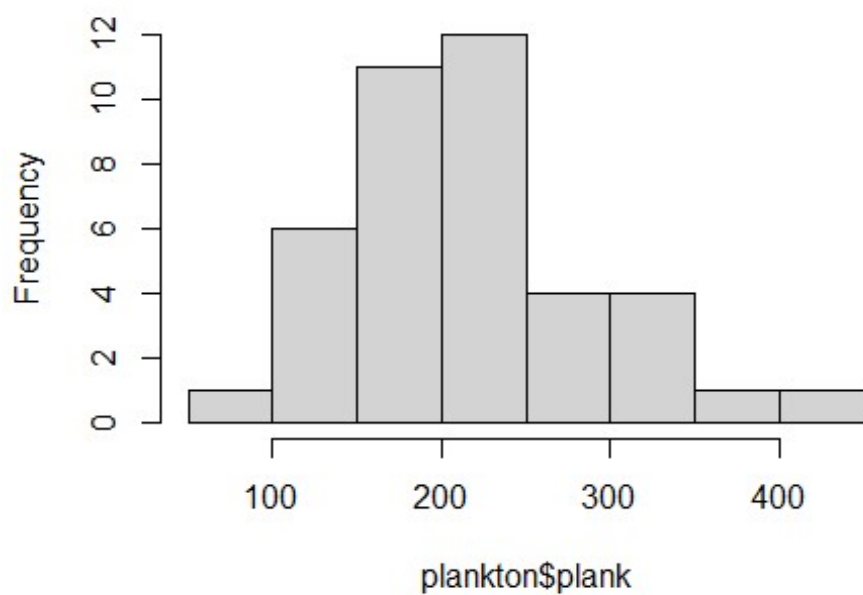
#plankton - dependent variable

#p level - predictor variable

#check assumptions

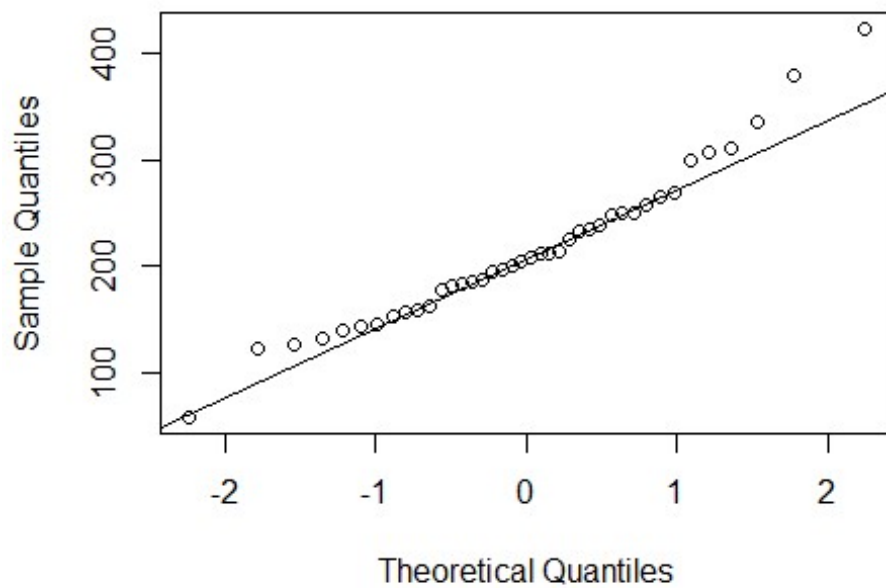
```
hist(plankton$plank)
```

Histogram of plankton\$plank



```
qqnorm(plankton$plank)  
qqline(plankton$plank)
```

Normal Q-Q Plot

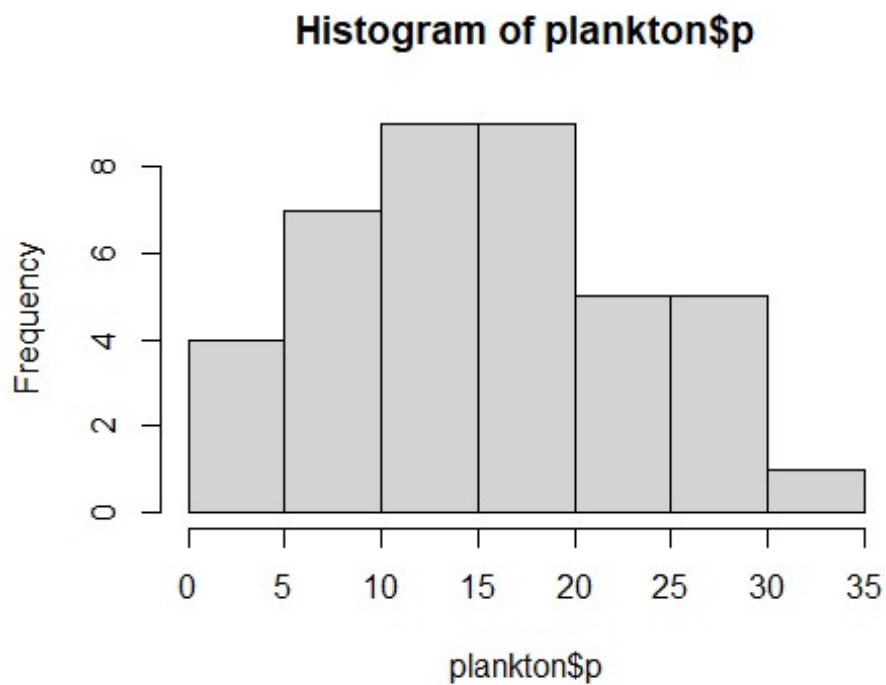


```
shapiro.test(plankton$plank)

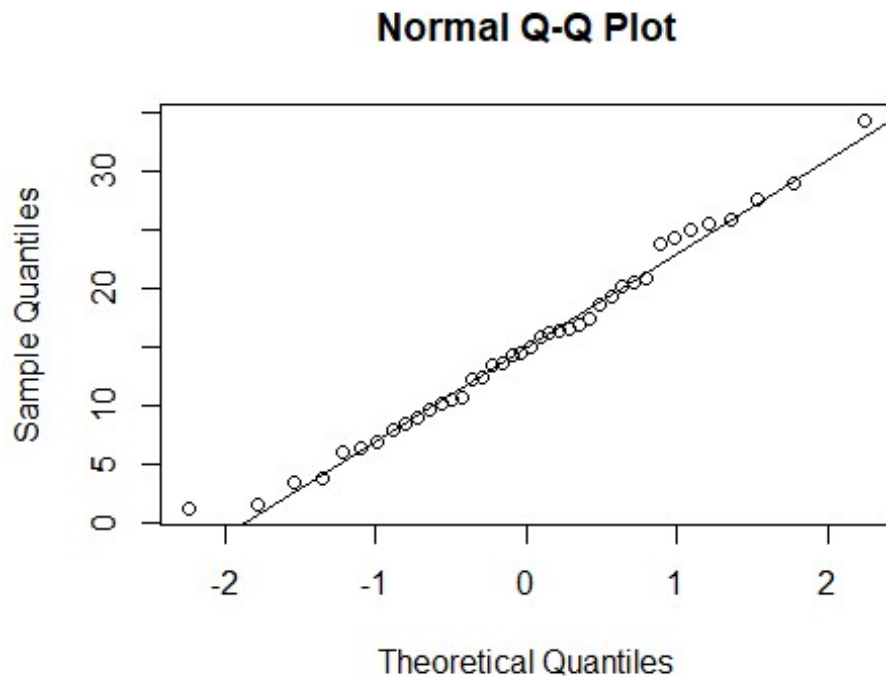
##
##  Shapiro-Wilk normality test
##
## data:  plankton$plank
## W = 0.96273, p-value = 0.2075

#not significant - normal distribution

hist(plankton$p)
```



```
qqnorm(plankton$p)
qqline(plankton$p)
```



```
shapiro.test(plankton$p)
```

```
##
##  Shapiro-Wilk normality test
##
## data:  plankton$p
## W = 0.98362, p-value = 0.8198
```

#not significant - normal distribution

#linear relationship and homoscedasticity
#scatterplot shows sort of linear relationship, but no deviations or data grouping at any point - both assumptions fulfilled

```
pcor.test(plankton$plank, plankton$p, as.numeric(plankton$treat),
method='pearson')
```

```
## estimate      p.value statistic  n gp Method
## 1 0.499641 0.001201947  3.508524 40  1 pearson
```

#significant p-value, correlation value is not zero, and zero does not lie within CI, so significant relationship between the presence of plankton in the lakes and the levels of phosphorus, independent of treatment (fish removal)

It is already understood from the partial correlation that fish removal does not significantly affect the relationship between plankton density and phosphorus concentration. So, we

could use a linear model including only plankton density and phosphorus concentration to analyze the linear relationship.

Here, I have however chosen to use **ANCOVA** to further support the results from the partial correlation analysis

```
#ancova to test with multiple predictors - continuous and categorical at the same time
```

```
#full model
```

```
fit.fullplank <- lm(plank~p*treat, data=plankton)
AIC(fit.fullplank)
```

```
## [1] 432.5379
```

```
#model with only main effects (w/o phosphorus and treatment aka fish removal interaction effect) - interaction effect not necessary as it is not relevant - fish removal and phosphorus availability interaction is not what we want to study here
```

```
fit.plank <- lm(plank~treat+p, data=plankton)
AIC(fit.plank)
```

```
## [1] 446.7461
```

```
#model with lower AIC - full model - further analysis
```

```
#ancova assumptions
```

```
#assumption 1: independent observations
```

```
dwtest(fit.fullplank)
```

```
##
```

```
## Durbin-Watson test
```

```
##
```

```
## data: fit.fullplank
```

```
## DW = 2.2295, p-value = 0.7214
```

```
## alternative hypothesis: true autocorrelation is greater than 0
```

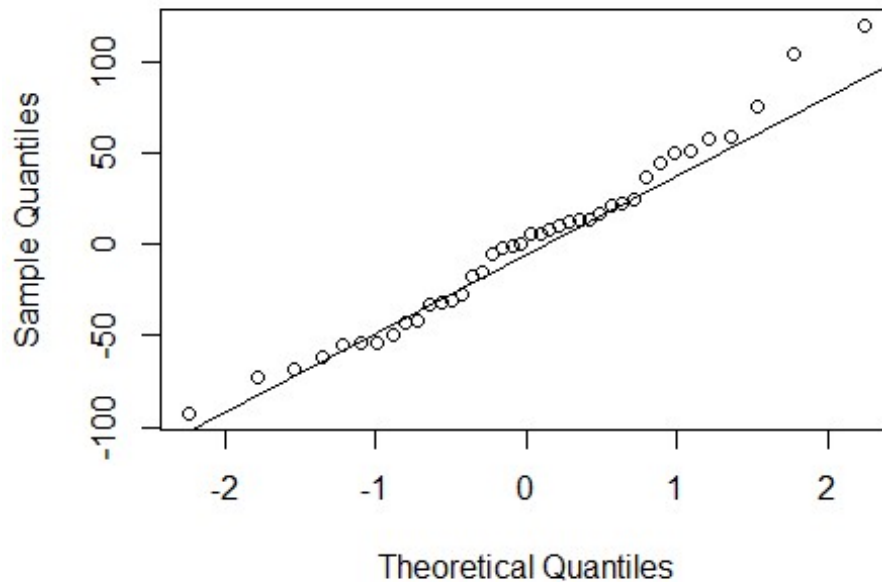
```
#not significant - assumption true
```

```
#assumption 2 and 3: normality of residuals and homoscedasticity of variances
```

```
qqnorm(resid(fit.fullplank))
```

```
qqline(resid(fit.fullplank))
```

Normal Q-Q Plot



```
shapiro.test(resid(fit.fullplank))
```

```
##
```

```
##  Shapiro-Wilk normality test
```

```
##
```

```
## data:  resid(fit.fullplank)
```

```
## W = 0.9799, p-value = 0.6859
```

```
#not significant - normality of residues true
```

```
leveneTest(plank~treat, data=plankton)
```

```
## Levene's Test for Homogeneity of Variance (center = median)
```

```
##      Df F value Pr(>F)
```

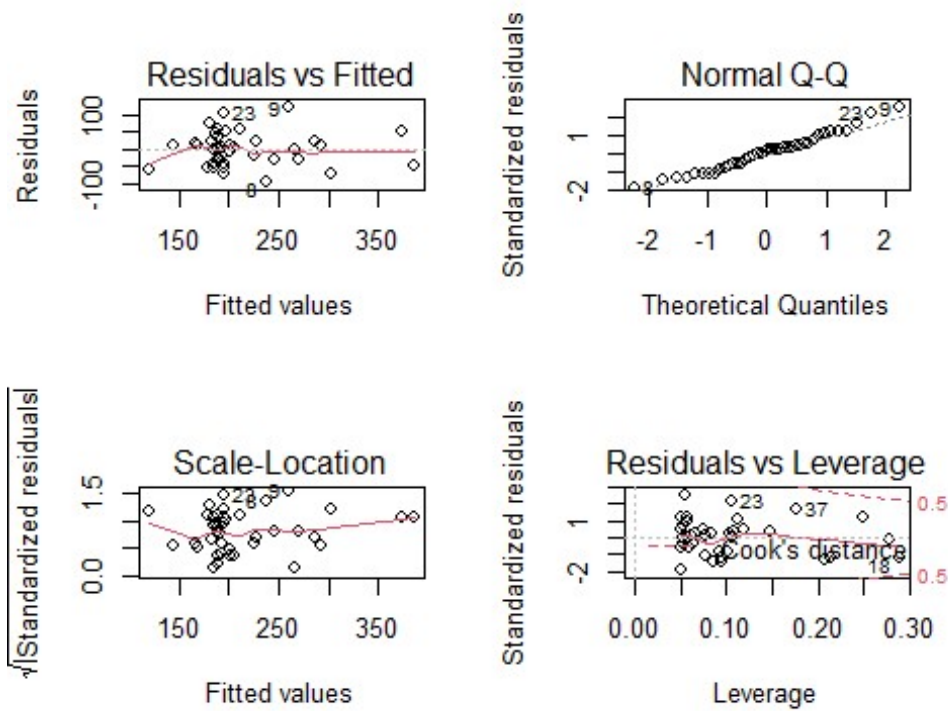
```
## group 1  2.4535 0.1256
```

```
##      38
```

```
#not significant - homoscedasticity proved
```

```
par(mfrow=c(2,2))
```

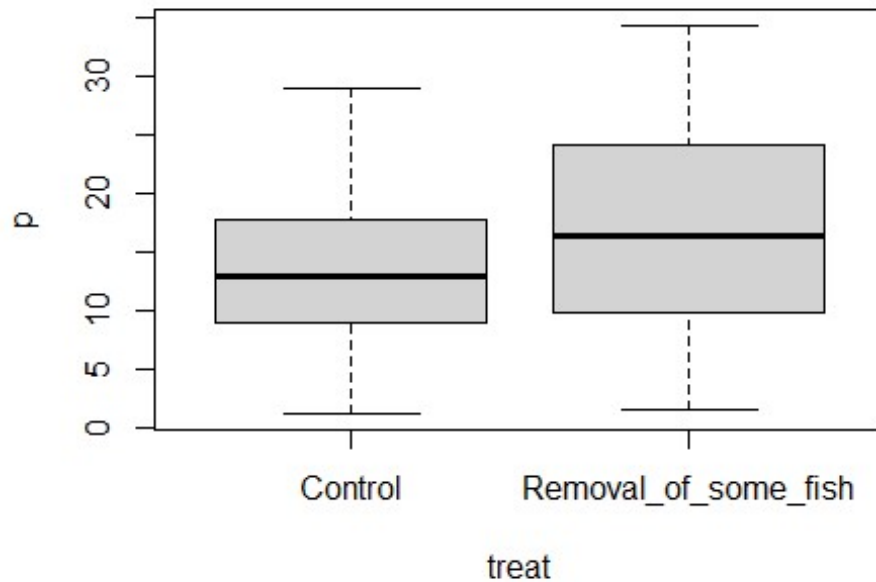
```
plot(fit.fullplank)
```

```
par(mfrow=c(1,1))
```

```
#assumption 4: linear relationship between covariate and dependent variable  
#can see from scatterplot above - true
```

```
#assumption 5: covariate independent from categorical predictor  
plot(p~treat, data=plankton)
```



```
#has an effect
#verify w/ anova
anova(lm(p~treat, data=plankton))

## Analysis of Variance Table
##
## Response: p
##          Df Sum Sq Mean Sq F value Pr(>F)
## treat      1   89.43   89.426   1.4439 0.2369
## Residuals 38 2353.53   61.935

#MS and SS values not equal to zero - has an effect

#get results
anova(fit.fullplank)

## Analysis of Variance Table
##
## Response: plank
##          Df Sum Sq Mean Sq F value    Pr(>F)
## p          1  32049   32049   12.732 0.0010402 **
## treat      1  37232   37232   14.790 0.0004716 ***
## p:treat    1  45276   45276   17.986 0.0001483 ***
## Residuals 36  90622    2517
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
summary(fit.fullplank)

##
## Call:
## lm(formula = plank ~ p * treat, data = plankton)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -92.571 -35.042   3.438  23.236 120.015
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    108.029     24.659   4.381 9.78e-05 ***
## p              9.580       1.604   5.974 7.52e-07 ***
## treatRemoval_of_some_fish  70.758     35.265   2.006 0.052367 .
## p:treatRemoval_of_some_fish  -8.899       2.098  -4.241 0.000148 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 50.17 on 36 degrees of freedom
## Multiple R-squared:  0.5583, Adjusted R-squared:  0.5215
## F-statistic: 15.17 on 3 and 36 DF, p-value: 1.524e-06
```

Part (b)

```
#illustrate results
plot(plank~p, data=plankton, type='n', main='Data illustration:\n Variation of
plankton density wrt to\n phosphorus levels in lakes', xlab='Phosphorus
concentration', ylab='Plankton density')

points(plankton$p[plankton$treat=='Control'],
plankton$plank[plankton$treat=='Control'], col='lightseagreen')

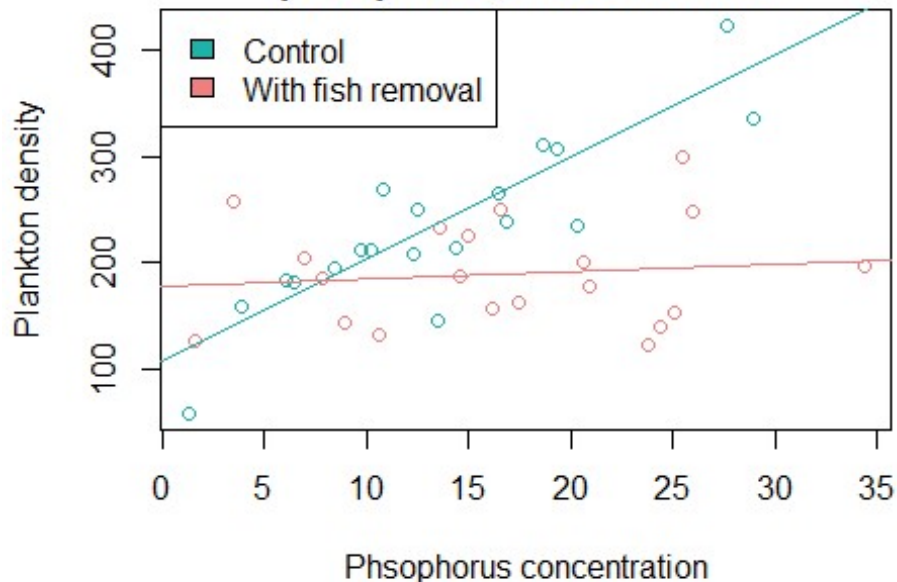
points(plankton$p[plankton$treat=='Removal_of_some_fish'],
plankton$plank[plankton$treat=='Removal_of_some_fish'], col='lightcoral')

#add predicted lines

abline(fit.fullplank$coefficients[1:2], col='lightseagreen')
abline(fit.fullplank$coefficients[1]+fit.fullplank$coefficients[3],
fit.fullplank$coefficients[2]+fit.fullplank$coefficients[4],
col='lightcoral')

legend('topleft', fill=c('lightseagreen', 'lightcoral'), legend=c('Control',
'With fish removal'))
```

**Data illustration:
Variation of plankton density wrt to
phosphorus levels in lakes**



This method of graphical illustration of scatter plot and line is helpful to show actual points and the model fitting together.

The graph shows that the second factor, or fish removal is not significant in the effect of plankton density over phosphorus concentration - the intersection of the two lines in the manner as seen on the graph indicates that the difference in plankton density seen due to the treatment averages over different values or levels of phosphorus treatment

This further supports our findings from partial correlation analysis that fish removal is not a significant effect here.

Part (c)

Linear equations:

(a) For control data

$$\text{plank} = 108.029 + 9.580p$$

(b) For data with fish removal

$$\text{plank} = 178.787 + 0.681p$$

Conclusions: A linear relationship between phosphorus concentration and plankton density exists, and there is a significant relationship between phosphorus concentration and treatment. The latter relationship does not however affect the increase in plankton density with increase in phosphorus concentration.

Model parameters can be pulled up using the `summary()` function that displays coefficients under the table column 'estimate'. The intercept value gives the intercept of the control and the `p` estimate value gives the slope of the control data, i.e, how phosphorus concentration influences plankton density in control lakes. The next estimate value provides the difference between the intercept for the control data and the data with fish removal. The final estimate gives a measure of how phosphorus concentration influences plankton density in the presence of fish removal.

The 95% confidence intervals of a model over a given data set can be found using the `predict()` function that utilizes the model to predict plank values for a given set of `p` values, and then calculate the 95% CI.

For normally distributed data, the 95% CI can be roughly defined as mean \pm 2*standard error. This can be calculated from the output of `summary()`, which provides the standard error values for the different groups.

#create dataset for confidence interval

```
new.x <- rep(seq(min(plankton$p), max(plankton$p), len=100), 2)
new.s <- rep(c('Control', 'Removal_of_some_fish'), each=100)

pred.data <- predict(fit.fullplank, new=data.frame(p=new.x, treat=new.s),
interval='conf', level=0.95)
pred.data
```

##		fit	lwr	upr
## 1		120.3930	74.08126	166.7047
## 2		123.5935	78.22498	168.9621
## 3		126.7941	82.36215	171.2260
## 4		129.9946	86.49235	173.4969
## 5		133.1952	90.61513	175.7752
## 6		136.3957	94.72998	178.0615
## 7		139.5963	98.83639	180.3562
## 8		142.7968	102.93376	182.6599
## 9		145.9974	107.02149	184.9733
## 10		149.1979	111.09888	187.2970
## 11		152.3985	115.16523	189.6317
## 12		155.5990	119.21973	191.9783
## 13		158.7996	123.26152	194.3376
## 14		162.0001	127.28970	196.7105
## 15		165.2007	131.30326	199.0981
## 16		168.4012	135.30112	201.5013
## 17		171.6018	139.28213	203.9214
## 18		174.8023	143.24502	206.3596
## 19		178.0029	147.18846	208.8172
## 20		181.2034	151.11101	211.2958
## 21		184.4039	155.01112	213.7968
## 22		187.6045	158.88716	216.3218
## 23		190.8050	162.73738	218.8727
## 24		194.0056	166.55997	221.4512

##	25	197.2061	170.35298	224.0593
##	26	200.4067	174.11443	226.6989
##	27	203.6072	177.84226	229.3722
##	28	206.8078	181.53435	232.0812
##	29	210.0083	185.18859	234.8281
##	30	213.2089	188.80287	237.6149
##	31	216.4094	192.37511	240.4437
##	32	219.6100	195.90335	243.3166
##	33	222.8105	199.38574	246.2353
##	34	226.0111	202.82060	249.2015
##	35	229.2116	206.20648	252.2167
##	36	232.4122	209.54220	255.2821
##	37	235.6127	212.82686	258.3986
##	38	238.8133	216.05989	261.5666
##	39	242.0138	219.24107	264.7865
##	40	245.2144	222.37053	268.0582
##	41	248.4149	225.44876	271.3810
##	42	251.6155	228.47657	274.7543
##	43	254.8160	231.45507	278.1769
##	44	258.0165	234.38565	281.6474
##	45	261.2171	237.26995	285.1642
##	46	264.4176	240.10975	288.7255
##	47	267.6182	242.90701	292.3294
##	48	270.8187	245.66379	295.9737
##	49	274.0193	248.38217	299.6564
##	50	277.2198	251.06428	303.3754
##	51	280.4204	253.71224	307.1285
##	52	283.6209	256.32811	310.9137
##	53	286.8215	258.91392	314.7290
##	54	290.0220	261.47161	318.5724
##	55	293.2226	264.00303	322.4421
##	56	296.4231	266.50995	326.3363
##	57	299.6237	268.99403	330.2533
##	58	302.8242	271.45683	334.1916
##	59	306.0248	273.89982	338.1497
##	60	309.2253	276.32438	342.1262
##	61	312.4259	278.73176	346.1200
##	62	315.6264	281.12317	350.1296
##	63	318.8270	283.49969	354.1542
##	64	322.0275	285.86234	358.1927
##	65	325.2281	288.21207	362.2440
##	66	328.4286	290.54974	366.3075
##	67	331.6291	292.87617	370.3821
##	68	334.8297	295.19209	374.4673
##	69	338.0302	297.49819	378.5623
##	70	341.2308	299.79511	382.6665
##	71	344.4313	302.08344	386.7792
##	72	347.6319	304.36371	390.9001
##	73	350.8324	306.63644	395.0284
##	74	354.0330	308.90209	399.1639

## 75	357.2335	311.16109	403.3060
## 76	360.4341	313.41383	407.4543
## 77	363.6346	315.66070	411.6085
## 78	366.8352	317.90203	415.7683
## 79	370.0357	320.13814	419.9333
## 80	373.2363	322.36933	424.1032
## 81	376.4368	324.59587	428.2778
## 82	379.6374	326.81803	432.4567
## 83	382.8379	329.03604	436.6398
## 84	386.0385	331.25013	440.8268
## 85	389.2390	333.46049	445.0175
## 86	392.4396	335.66734	449.2118
## 87	395.6401	337.87084	453.4094
## 88	398.8406	340.07118	457.6101
## 89	402.0412	342.26850	461.8139
## 90	405.2417	344.46296	466.0205
## 91	408.4423	346.65469	470.2299
## 92	411.6428	348.84384	474.4418
## 93	414.8434	351.03052	478.6563
## 94	418.0439	353.21484	482.8730
## 95	421.2445	355.39692	487.0920
## 96	424.4450	357.57687	491.3132
## 97	427.6456	359.75476	495.5364
## 98	430.8461	361.93071	499.7616
## 99	434.0467	364.10478	503.9886
## 100	437.2472	366.27707	508.2174
## 101	179.6667	131.68168	227.6516
## 102	179.8944	132.71464	227.0741
## 103	180.1221	133.74344	226.5007
## 104	180.3498	134.76789	225.9317
## 105	180.5775	135.78774	225.3672
## 106	180.8052	136.80274	224.8077
## 107	181.0329	137.81263	224.2532
## 108	181.2606	138.81713	223.7041
## 109	181.4883	139.81594	223.1607
## 110	181.7160	140.80873	222.6233
## 111	181.9438	141.79517	222.0923
## 112	182.1715	142.77487	221.5680
## 113	182.3992	143.74746	221.0509
## 114	182.6269	144.71251	220.5413
## 115	182.8546	145.66956	220.0396
## 116	183.0823	146.61816	219.5464
## 117	183.3100	147.55777	219.0622
## 118	183.5377	148.48786	218.5876
## 119	183.7654	149.40783	218.1230
## 120	183.9931	150.31707	217.6692
## 121	184.2208	151.21492	217.2268
## 122	184.4486	152.10065	216.7965
## 123	184.6763	152.97352	216.3790
## 124	184.9040	153.83274	215.9752

125 185.1317 154.67743 215.5859
126 185.3594 155.50672 215.2121
127 185.5871 156.31964 214.8546
128 185.8148 157.11520 214.5144
129 186.0425 157.89235 214.1927
130 186.2702 158.64998 213.8905
131 186.4979 159.38695 213.6089
132 186.7257 160.10208 213.3492
133 186.9534 160.79415 213.1126
134 187.1811 161.46190 212.9002
135 187.4088 162.10407 212.7135
136 187.6365 162.71938 212.5536
137 187.8642 163.30657 212.4218
138 188.0919 163.86436 212.3195
139 188.3196 164.39156 212.2477
140 188.5473 164.88700 212.2077
141 188.7750 165.34959 212.2005
142 189.0028 165.77834 212.2272
143 189.2305 166.17235 212.2886
144 189.4582 166.53087 212.3855
145 189.6859 166.85330 212.5185
146 189.9136 167.13918 212.6880
147 190.1413 167.38823 212.8944
148 190.3690 167.60035 213.1377
149 190.5967 167.77561 213.4178
150 190.8244 167.91427 213.7346
151 191.0521 168.01675 214.0875
152 191.2798 168.08364 214.4761
153 191.5076 168.11567 214.8994
154 191.7353 168.11371 215.3568
155 191.9630 168.07874 215.8472
156 192.1907 168.01183 216.3695
157 192.4184 167.91414 216.9227
158 192.6461 167.78688 217.5053
159 192.8738 167.63128 218.1164
160 193.1015 167.44863 218.7544
161 193.3292 167.24020 219.4183
162 193.5569 167.00726 220.1066
163 193.7847 166.75106 220.8183
164 194.0124 166.47283 221.5519
165 194.2401 166.17376 222.3064
166 194.4678 165.85500 223.0806
167 194.6955 165.51766 223.8733
168 194.9232 165.16279 224.6836
169 195.1509 164.79141 225.5104
170 195.3786 164.40447 226.3528
171 195.6063 164.00288 227.2098
172 195.8340 163.58750 228.0806
173 196.0618 163.15914 228.9644
174 196.2895 162.71855 229.8604


```
## 175 196.5172 162.26646 230.7679
## 176 196.7449 161.80354 231.6862
## 177 196.9726 161.33040 232.6148
## 178 197.2003 160.84766 233.5529
## 179 197.4280 160.35585 234.5002
## 180 197.6557 159.85550 235.4559
## 181 197.8834 159.34708 236.4198
## 182 198.1111 158.83106 237.3912
## 183 198.3388 158.30786 238.3698
## 184 198.5666 157.77787 239.3552
## 185 198.7943 157.24146 240.3471
## 186 199.0220 156.69899 241.3450
## 187 199.2497 156.15078 242.3486
## 188 199.4774 155.59712 243.3577
## 189 199.7051 155.03832 244.3719
## 190 199.9328 154.47463 245.3910
## 191 200.1605 153.90630 246.4148
## 192 200.3882 153.33358 247.4429
## 193 200.6159 152.75667 248.4752
## 194 200.8437 152.17580 249.5115
## 195 201.0714 151.59115 250.5516
## 196 201.2991 151.00291 251.5952
## 197 201.5268 150.41124 252.6423
## 198 201.7545 149.81632 253.6927
## 199 201.9822 149.21829 254.7461
## 200 202.2099 148.61729 255.8025
```

```
pred.data <- data.frame(pred.data, p=new.x, treat=new.s)
pred.data
```

##	fit	lwr	upr	p	treat
## 1	120.3930	74.08126	166.7047	1.290529	Control
## 2	123.5935	78.22498	168.9621	1.624604	Control
## 3	126.7941	82.36215	171.2260	1.958679	Control
## 4	129.9946	86.49235	173.4969	2.292753	Control
## 5	133.1952	90.61513	175.7752	2.626828	Control
## 6	136.3957	94.72998	178.0615	2.960903	Control
## 7	139.5963	98.83639	180.3562	3.294977	Control
## 8	142.7968	102.93376	182.6599	3.629052	Control
## 9	145.9974	107.02149	184.9733	3.963127	Control
## 10	149.1979	111.09888	187.2970	4.297201	Control
## 11	152.3985	115.16523	189.6317	4.631276	Control
## 12	155.5990	119.21973	191.9783	4.965351	Control
## 13	158.7996	123.26152	194.3376	5.299425	Control
## 14	162.0001	127.28970	196.7105	5.633500	Control
## 15	165.2007	131.30326	199.0981	5.967575	Control
## 16	168.4012	135.30112	201.5013	6.301649	Control
## 17	171.6018	139.28213	203.9214	6.635724	Control
## 18	174.8023	143.24502	206.3596	6.969799	Control
## 19	178.0029	147.18846	208.8172	7.303873	Control

## 20	181.2034	151.11101	211.2958	7.637948	Control
## 21	184.4039	155.01112	213.7968	7.972023	Control
## 22	187.6045	158.88716	216.3218	8.306097	Control
## 23	190.8050	162.73738	218.8727	8.640172	Control
## 24	194.0056	166.55997	221.4512	8.974247	Control
## 25	197.2061	170.35298	224.0593	9.308321	Control
## 26	200.4067	174.11443	226.6989	9.642396	Control
## 27	203.6072	177.84226	229.3722	9.976471	Control
## 28	206.8078	181.53435	232.0812	10.310545	Control
## 29	210.0083	185.18859	234.8281	10.644620	Control
## 30	213.2089	188.80287	237.6149	10.978695	Control
## 31	216.4094	192.37511	240.4437	11.312770	Control
## 32	219.6100	195.90335	243.3166	11.646844	Control
## 33	222.8105	199.38574	246.2353	11.980919	Control
## 34	226.0111	202.82060	249.2015	12.314994	Control
## 35	229.2116	206.20648	252.2167	12.649068	Control
## 36	232.4122	209.54220	255.2821	12.983143	Control
## 37	235.6127	212.82686	258.3986	13.317218	Control
## 38	238.8133	216.05989	261.5666	13.651292	Control
## 39	242.0138	219.24107	264.7865	13.985367	Control
## 40	245.2144	222.37053	268.0582	14.319442	Control
## 41	248.4149	225.44876	271.3810	14.653516	Control
## 42	251.6155	228.47657	274.7543	14.987591	Control
## 43	254.8160	231.45507	278.1769	15.321666	Control
## 44	258.0165	234.38565	281.6474	15.655740	Control
## 45	261.2171	237.26995	285.1642	15.989815	Control
## 46	264.4176	240.10975	288.7255	16.323890	Control
## 47	267.6182	242.90701	292.3294	16.657964	Control
## 48	270.8187	245.66379	295.9737	16.992039	Control
## 49	274.0193	248.38217	299.6564	17.326114	Control
## 50	277.2198	251.06428	303.3754	17.660188	Control
## 51	280.4204	253.71224	307.1285	17.994263	Control
## 52	283.6209	256.32811	310.9137	18.328338	Control
## 53	286.8215	258.91392	314.7290	18.662412	Control
## 54	290.0220	261.47161	318.5724	18.996487	Control
## 55	293.2226	264.00303	322.4421	19.330562	Control
## 56	296.4231	266.50995	326.3363	19.664636	Control
## 57	299.6237	268.99403	330.2533	19.998711	Control
## 58	302.8242	271.45683	334.1916	20.332786	Control
## 59	306.0248	273.89982	338.1497	20.666860	Control
## 60	309.2253	276.32438	342.1262	21.000935	Control
## 61	312.4259	278.73176	346.1200	21.335010	Control
## 62	315.6264	281.12317	350.1296	21.669084	Control
## 63	318.8270	283.49969	354.1542	22.003159	Control
## 64	322.0275	285.86234	358.1927	22.337234	Control
## 65	325.2281	288.21207	362.2440	22.671308	Control
## 66	328.4286	290.54974	366.3075	23.005383	Control
## 67	331.6291	292.87617	370.3821	23.339458	Control
## 68	334.8297	295.19209	374.4673	23.673533	Control
## 69	338.0302	297.49819	378.5623	24.007607	Control

## 70	341.2308	299.79511	382.6665	24.341682	Control
## 71	344.4313	302.08344	386.7792	24.675757	Control
## 72	347.6319	304.36371	390.9001	25.009831	Control
## 73	350.8324	306.63644	395.0284	25.343906	Control
## 74	354.0330	308.90209	399.1639	25.677981	Control
## 75	357.2335	311.16109	403.3060	26.012055	Control
## 76	360.4341	313.41383	407.4543	26.346130	Control
## 77	363.6346	315.66070	411.6085	26.680205	Control
## 78	366.8352	317.90203	415.7683	27.014279	Control
## 79	370.0357	320.13814	419.9333	27.348354	Control
## 80	373.2363	322.36933	424.1032	27.682429	Control
## 81	376.4368	324.59587	428.2778	28.016503	Control
## 82	379.6374	326.81803	432.4567	28.350578	Control
## 83	382.8379	329.03604	436.6398	28.684653	Control
## 84	386.0385	331.25013	440.8268	29.018727	Control
## 85	389.2390	333.46049	445.0175	29.352802	Control
## 86	392.4396	335.66734	449.2118	29.686877	Control
## 87	395.6401	337.87084	453.4094	30.020951	Control
## 88	398.8406	340.07118	457.6101	30.355026	Control
## 89	402.0412	342.26850	461.8139	30.689101	Control
## 90	405.2417	344.46296	466.0205	31.023175	Control
## 91	408.4423	346.65469	470.2299	31.357250	Control
## 92	411.6428	348.84384	474.4418	31.691325	Control
## 93	414.8434	351.03052	478.6563	32.025399	Control
## 94	418.0439	353.21484	482.8730	32.359474	Control
## 95	421.2445	355.39692	487.0920	32.693549	Control
## 96	424.4450	357.57687	491.3132	33.027623	Control
## 97	427.6456	359.75476	495.5364	33.361698	Control
## 98	430.8461	361.93071	499.7616	33.695773	Control
## 99	434.0467	364.10478	503.9886	34.029847	Control
## 100	437.2472	366.27707	508.2174	34.363922	Control
## 101	179.6667	131.68168	227.6516	1.290529	Removal_of_some_fish
## 102	179.8944	132.71464	227.0741	1.624604	Removal_of_some_fish
## 103	180.1221	133.74344	226.5007	1.958679	Removal_of_some_fish
## 104	180.3498	134.76789	225.9317	2.292753	Removal_of_some_fish
## 105	180.5775	135.78774	225.3672	2.626828	Removal_of_some_fish
## 106	180.8052	136.80274	224.8077	2.960903	Removal_of_some_fish
## 107	181.0329	137.81263	224.2532	3.294977	Removal_of_some_fish
## 108	181.2606	138.81713	223.7041	3.629052	Removal_of_some_fish
## 109	181.4883	139.81594	223.1607	3.963127	Removal_of_some_fish
## 110	181.7160	140.80873	222.6233	4.297201	Removal_of_some_fish
## 111	181.9438	141.79517	222.0923	4.631276	Removal_of_some_fish
## 112	182.1715	142.77487	221.5680	4.965351	Removal_of_some_fish
## 113	182.3992	143.74746	221.0509	5.299425	Removal_of_some_fish
## 114	182.6269	144.71251	220.5413	5.633500	Removal_of_some_fish
## 115	182.8546	145.66956	220.0396	5.967575	Removal_of_some_fish
## 116	183.0823	146.61816	219.5464	6.301649	Removal_of_some_fish
## 117	183.3100	147.55777	219.0622	6.635724	Removal_of_some_fish
## 118	183.5377	148.48786	218.5876	6.969799	Removal_of_some_fish
## 119	183.7654	149.40783	218.1230	7.303873	Removal_of_some_fish

##	120	183.9931	150.31707	217.6692	7.637948	Removal_of_some_fish
##	121	184.2208	151.21492	217.2268	7.972023	Removal_of_some_fish
##	122	184.4486	152.10065	216.7965	8.306097	Removal_of_some_fish
##	123	184.6763	152.97352	216.3790	8.640172	Removal_of_some_fish
##	124	184.9040	153.83274	215.9752	8.974247	Removal_of_some_fish
##	125	185.1317	154.67743	215.5859	9.308321	Removal_of_some_fish
##	126	185.3594	155.50672	215.2121	9.642396	Removal_of_some_fish
##	127	185.5871	156.31964	214.8546	9.976471	Removal_of_some_fish
##	128	185.8148	157.11520	214.5144	10.310545	Removal_of_some_fish
##	129	186.0425	157.89235	214.1927	10.644620	Removal_of_some_fish
##	130	186.2702	158.64998	213.8905	10.978695	Removal_of_some_fish
##	131	186.4979	159.38695	213.6089	11.312770	Removal_of_some_fish
##	132	186.7257	160.10208	213.3492	11.646844	Removal_of_some_fish
##	133	186.9534	160.79415	213.1126	11.980919	Removal_of_some_fish
##	134	187.1811	161.46190	212.9002	12.314994	Removal_of_some_fish
##	135	187.4088	162.10407	212.7135	12.649068	Removal_of_some_fish
##	136	187.6365	162.71938	212.5536	12.983143	Removal_of_some_fish
##	137	187.8642	163.30657	212.4218	13.317218	Removal_of_some_fish
##	138	188.0919	163.86436	212.3195	13.651292	Removal_of_some_fish
##	139	188.3196	164.39156	212.2477	13.985367	Removal_of_some_fish
##	140	188.5473	164.88700	212.2077	14.319442	Removal_of_some_fish
##	141	188.7750	165.34959	212.2005	14.653516	Removal_of_some_fish
##	142	189.0028	165.77834	212.2272	14.987591	Removal_of_some_fish
##	143	189.2305	166.17235	212.2886	15.321666	Removal_of_some_fish
##	144	189.4582	166.53087	212.3855	15.655740	Removal_of_some_fish
##	145	189.6859	166.85330	212.5185	15.989815	Removal_of_some_fish
##	146	189.9136	167.13918	212.6880	16.323890	Removal_of_some_fish
##	147	190.1413	167.38823	212.8944	16.657964	Removal_of_some_fish
##	148	190.3690	167.60035	213.1377	16.992039	Removal_of_some_fish
##	149	190.5967	167.77561	213.4178	17.326114	Removal_of_some_fish
##	150	190.8244	167.91427	213.7346	17.660188	Removal_of_some_fish
##	151	191.0521	168.01675	214.0875	17.994263	Removal_of_some_fish
##	152	191.2798	168.08364	214.4761	18.328338	Removal_of_some_fish
##	153	191.5076	168.11567	214.8994	18.662412	Removal_of_some_fish
##	154	191.7353	168.11371	215.3568	18.996487	Removal_of_some_fish
##	155	191.9630	168.07874	215.8472	19.330562	Removal_of_some_fish
##	156	192.1907	168.01183	216.3695	19.664636	Removal_of_some_fish
##	157	192.4184	167.91414	216.9227	19.998711	Removal_of_some_fish
##	158	192.6461	167.78688	217.5053	20.332786	Removal_of_some_fish
##	159	192.8738	167.63128	218.1164	20.666860	Removal_of_some_fish
##	160	193.1015	167.44863	218.7544	21.000935	Removal_of_some_fish
##	161	193.3292	167.24020	219.4183	21.335010	Removal_of_some_fish
##	162	193.5569	167.00726	220.1066	21.669084	Removal_of_some_fish
##	163	193.7847	166.75106	220.8183	22.003159	Removal_of_some_fish
##	164	194.0124	166.47283	221.5519	22.337234	Removal_of_some_fish
##	165	194.2401	166.17376	222.3064	22.671308	Removal_of_some_fish
##	166	194.4678	165.85500	223.0806	23.005383	Removal_of_some_fish
##	167	194.6955	165.51766	223.8733	23.339458	Removal_of_some_fish
##	168	194.9232	165.16279	224.6836	23.673533	Removal_of_some_fish
##	169	195.1509	164.79141	225.5104	24.007607	Removal_of_some_fish

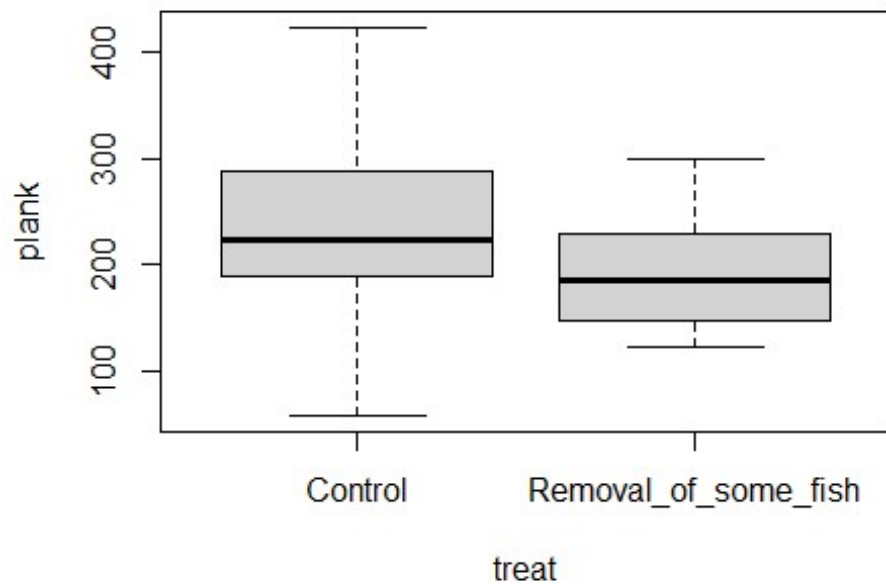
```
## 170 195.3786 164.40447 226.3528 24.341682 Removal_of_some_fish
## 171 195.6063 164.00288 227.2098 24.675757 Removal_of_some_fish
## 172 195.8340 163.58750 228.0806 25.009831 Removal_of_some_fish
## 173 196.0618 163.15914 228.9644 25.343906 Removal_of_some_fish
## 174 196.2895 162.71855 229.8604 25.677981 Removal_of_some_fish
## 175 196.5172 162.26646 230.7679 26.012055 Removal_of_some_fish
## 176 196.7449 161.80354 231.6862 26.346130 Removal_of_some_fish
## 177 196.9726 161.33040 232.6148 26.680205 Removal_of_some_fish
## 178 197.2003 160.84766 233.5529 27.014279 Removal_of_some_fish
## 179 197.4280 160.35585 234.5002 27.348354 Removal_of_some_fish
## 180 197.6557 159.85550 235.4559 27.682429 Removal_of_some_fish
## 181 197.8834 159.34708 236.4198 28.016503 Removal_of_some_fish
## 182 198.1111 158.83106 237.3912 28.350578 Removal_of_some_fish
## 183 198.3388 158.30786 238.3698 28.684653 Removal_of_some_fish
## 184 198.5666 157.77787 239.3552 29.018727 Removal_of_some_fish
## 185 198.7943 157.24146 240.3471 29.352802 Removal_of_some_fish
## 186 199.0220 156.69899 241.3450 29.686877 Removal_of_some_fish
## 187 199.2497 156.15078 242.3486 30.020951 Removal_of_some_fish
## 188 199.4774 155.59712 243.3577 30.355026 Removal_of_some_fish
## 189 199.7051 155.03832 244.3719 30.689101 Removal_of_some_fish
## 190 199.9328 154.47463 245.3910 31.023175 Removal_of_some_fish
## 191 200.1605 153.90630 246.4148 31.357250 Removal_of_some_fish
## 192 200.3882 153.33358 247.4429 31.691325 Removal_of_some_fish
## 193 200.6159 152.75667 248.4752 32.025399 Removal_of_some_fish
## 194 200.8437 152.17580 249.5115 32.359474 Removal_of_some_fish
## 195 201.0714 151.59115 250.5516 32.693549 Removal_of_some_fish
## 196 201.2991 151.00291 251.5952 33.027623 Removal_of_some_fish
## 197 201.5268 150.41124 252.6423 33.361698 Removal_of_some_fish
## 198 201.7545 149.81632 253.6927 33.695773 Removal_of_some_fish
## 199 201.9822 149.21829 254.7461 34.029847 Removal_of_some_fish
## 200 202.2099 148.61729 255.8025 34.363922 Removal_of_some_fish
```

Part (d)

To study the effect of fish removal on plankton density excluding the effect of phosphorus levels, we use **two-sample t-test** here.

```
#effect of fish removal on plankton density - two-sample t-test
```

```
plot(plank~treat, data=plankton)
```



#t-test assumptions

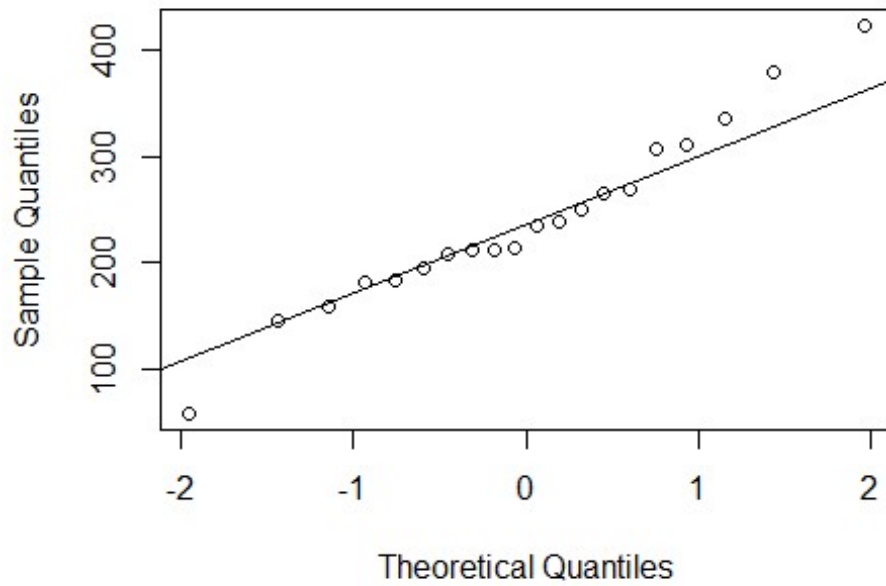
#assumption 1: independent observations

#assumed to be true

#assumption 2: continuous data and normally distributed within group

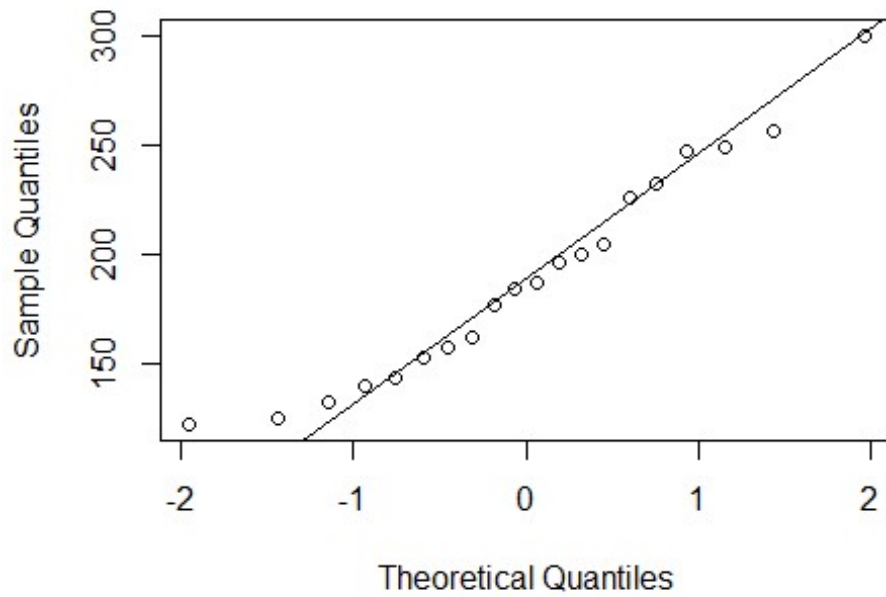
```
control <- subset(plankton, treat=='Control')
fish_rem <- subset(plankton, treat=='Removal_of_some_fish')
qqnorm(control$plank)
qqline(control$plank)
```

Normal Q-Q Plot



```
qqnorm(fish_rem$plank)  
qqline(fish_rem$plank)
```

Normal Q-Q Plot



```

shapiro.test(control$plank)

##
##  Shapiro-Wilk normality test
##
## data:  control$plank
## W = 0.97348, p-value = 0.8259

shapiro.test(fish_rem$plank)

##
##  Shapiro-Wilk normality test
##
## data:  fish_rem$plank
## W = 0.95396, p-value = 0.4313

#normally distributed

leveneTest(plank~treat, data=plankton)

## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group 1  2.4535 0.1256
##      38

#variances are not significantly different

t.test(plank~treat, data=plankton, var.equal=TRUE)

##
##  Two Sample t-test
##
## data:  plank by treat
## t = 2.2472, df = 38, p-value = 0.03051
## alternative hypothesis: true difference in means between group Control and
## group Removal_of_some_fish is not equal to 0
## 95 percent confidence interval:
##  4.864117 93.254297
## sample estimates:
##              mean in group Control mean in group Removal_of_some_fish
##              239.2182              190.1590

```

There is a statistically significant difference between plankton density observed in the control lakes and the treated lakes.

Thus, the effect of fish removal on plankton density seems significant when the phosphorus levels in the different lakes are not taken into consideration.