Assignment 1

Y.kavya

Download all python codes from

https://github.com/Y.kavya/Matrix−Theory/tree/main/Assignment1/Codes

and latex-tikz codes from

https://github.com/Y.kavya/Matrix−Theory/tree/main/Assignment1

1 Question No. 2.10

Construct $\triangle ABC$ where $AB = 4.5$, $BC = 5$ and CA=6

2 Explanation

Let us assume that:

$$\mathbf{A} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} c \\ 0 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} p \\ q \end{pmatrix} \tag{2.0.1}$$

Then

$$AB = \|\mathbf{B} - \mathbf{A}\|^2 = \|\mathbf{B}\|^2 = c^2 \quad \because \mathbf{A} = \mathbf{0} \tag{2.0.2}$$
$$BC = \|\mathbf{B} - \mathbf{C}\|^2 = a^2 \tag{2.0.3}$$
$$AC = \|\mathbf{C} - \mathbf{A}\|^2 = \|\mathbf{C}\|^2 = b^2 \tag{2.0.4}$$

From (2.0.3),

$$a^2 = \|\mathbf{B} - \mathbf{C}\|^2 = \|\mathbf{B} - \mathbf{C}\|^T \|\mathbf{B} - \mathbf{C}\| \tag{2.0.5}$$
$$= \mathbf{B}^T\mathbf{B} + \mathbf{C}^T\mathbf{C} - \mathbf{B}^T\mathbf{C} - \mathbf{C}^T\mathbf{B} \tag{2.0.6}$$
$$= \|\mathbf{B}\|^2 + \|\mathbf{C}\|^2 - 2\mathbf{B}^T\mathbf{C} \quad \left(\because \mathbf{B}^T\mathbf{C} = \mathbf{C}^T\mathbf{B}\right) \tag{2.0.7}$$
$$= b^2 + c^2 - 2bp \tag{2.0.8}$$

yielding

$$p = \frac{b^2 + c^2 - a^2}{2.b} \tag{2.0.9}$$
$$p = \frac{6^2 + (4.5)^2 - 5^2}{2.6} \tag{2.0.10}$$
$$p = \frac{36 + 20.25 - 25}{12} \tag{2.0.11}$$
$$p = 2.60416667 \tag{2.0.12}$$
$$\tag{2.0.13}$$

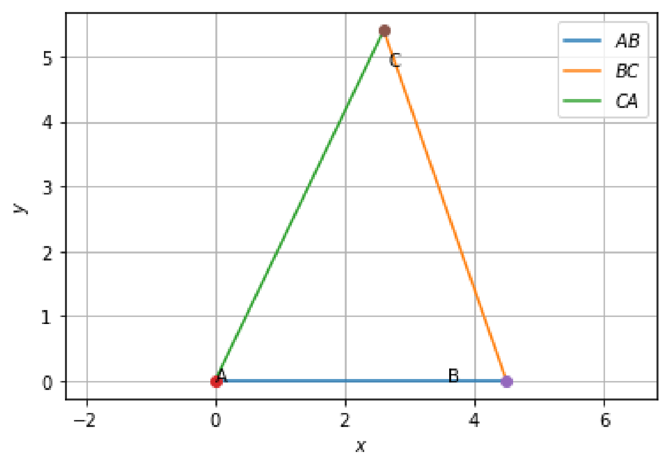
From (2.0.4),

$$\|\mathbf{C}\|^2 = b^2 = p^2 + q^2 \tag{2.0.14}$$
$$\implies q = \pm\sqrt{b^2 - p^2} \tag{2.0.15}$$
$$q = \pm\sqrt{6^2 - 2.60416667^2} \tag{2.0.16}$$
$$q = \pm\sqrt{29.218316} \tag{2.0.17}$$
$$q = 5.40539693 \tag{2.0.18}$$

Now, Vertices of given $\triangle ABC$ can be written as,

$$\mathbf{C} = \begin{pmatrix} p \\ q \end{pmatrix} = \begin{pmatrix} 2.60416667 \\ 5.40539693 \end{pmatrix}, \mathbf{A} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} c \\ 0 \end{pmatrix} = \begin{pmatrix} 5 \\ 0 \end{pmatrix} \tag{2.0.19}$$

Now, $\triangle ABC$ can be plotted using vertices AB ,BC and CA .
Plot of the $\triangle ABC$:



$\triangle ABC$