1

ASSIGNMENT-1

Y.kavya

Download all python codes from

https://github.com/kavya/ASSIGNMENT-1/tree/main/ASSIGNMENT%201/CODES

and latex-tikz codes from

https://github.com/kavya/ASSIGNMENT-1/tree/main/ASSIGNMENT%201

1 QUESTION NO-2.10

Construct $\triangle ABC$ where AB=4.5,BC=5 and CA=6

2 SOLUTION

Let the vertices of $\triangle ABC$ be

$$\mathbf{A} = \begin{pmatrix} p \\ q \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} a \\ 0 \end{pmatrix} \tag{2.0.1}$$

Then

$$\|\mathbf{A} - \mathbf{B}\|^2 = \|\mathbf{A}\|^2 = c^2 = (4.5)^2 = 20.25$$
 (2.0.2)

$$\|\mathbf{C} - \mathbf{B}\|^2 = \|\mathbf{C}\|^2 = a^2 = 5^2 = 25$$
 (2.0.3)

$$\|\mathbf{A} - \mathbf{C}\|^2 = b^2 = 6^2 = 36$$
 (2.0.4)

From(2.0.4)

$$b^{2} = \|\mathbf{A} - \mathbf{C}\|^{2} = \|\mathbf{A} - \mathbf{C}\|^{T} \|\mathbf{A} - \mathbf{C}\|$$

$$= \mathbf{A}^{T} \mathbf{A} + \mathbf{C}^{T} \mathbf{C} - \mathbf{A}^{T} \mathbf{C} - \mathbf{C}^{T} \mathbf{A}$$

$$= \|\mathbf{A}\|^{2} + \|\mathbf{C}\|^{2} - 2\mathbf{A}^{T} \mathbf{C}$$

$$b^{2} = a^{2} + c^{2} - 2ab$$

$$p = (a^{2} + c^{2} - b^{2})/2a$$

$$p = (5^{2} + (4.5)^{2} - 6^{2})/2(5)$$

$$p = 0$$

From(2.0.2)

$$\|\mathbf{A}\|^2 = c^2 = p^2 + q^2$$
 (2.0.5)

$$(4.5)^2 = 0 + q^2 (2.0.6)$$

$$q^2 = 20.25 \tag{2.0.7}$$

$$q = 4.5$$
 (2.0.8)

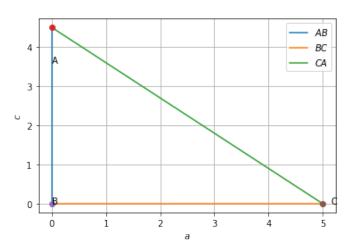
(2.0.9)

Now, Vertices of given $\triangle ABC$ can be written as,

$$\mathbf{A} = \begin{pmatrix} p \\ q \end{pmatrix} = \begin{pmatrix} 0 \\ 4.5 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} a \\ 0 \end{pmatrix} = \begin{pmatrix} 5 \\ 0 \end{pmatrix} \quad (2.0.10)$$

Now, $\triangle ABC$ can be plotted using vertices AB, BC and CA.

Plot of the Right angle $\triangle ABC$:



Right Angle $\triangle ABC$