

ASSIGNMENT 2

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Download all python codes from

<https://github.com/kavya309/ASSIGNMENT2/tree/main/CODES>

and latex-tikz codes from

<https://github.com/kavya309/ASSIGNMENT2/tree/main>

1 QUESTION No 2.11

Which of the following pairs of linear equations has a unique solution, no solution or infinitely many solutions ?

1)

$$\begin{aligned} (1 \quad -3)\mathbf{x} &= 3 \\ (3 \quad -9)\mathbf{x} &= 2 \end{aligned} \quad (1.0.1)$$

2)

$$\begin{aligned} (2 \quad 1)\mathbf{x} &= 5 \\ (3 \quad 2)\mathbf{x} &= 8 \end{aligned} \quad (1.0.2)$$

2 SOLUTION

1)

$$\begin{aligned} (1 \quad -3)\mathbf{x} &= 3 \\ (3 \quad -9)\mathbf{x} &= 2 \end{aligned} \quad (2.0.1)$$

The above equations can be expressed as the matrix equation

$$\begin{pmatrix} 1 & -3 \\ 3 & -9 \end{pmatrix} \mathbf{x} = \begin{pmatrix} 3 \\ 2 \end{pmatrix} \quad (2.0.2)$$

The augmented matrix for the above equation is row reduced as follows

$$\begin{pmatrix} 1 & -3 & 3 \\ 3 & -9 & 2 \end{pmatrix} \xrightarrow{R_2 \leftarrow R_2 - 3R_1} \begin{pmatrix} 1 & -3 & 3 \\ 0 & 0 & -7 \end{pmatrix} \quad (2.0.3)$$

\therefore Given lines (1.0.1) have no solutions so we can say they are parallel.

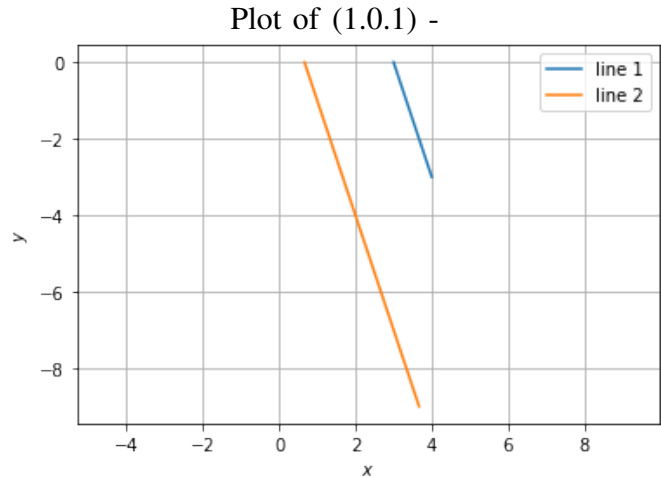


Fig. 2.1: PARALLEL LINES.

2)

$$\begin{aligned} (2 \quad 1)\mathbf{x} &= 5 \\ (3 \quad 2)\mathbf{x} &= 8 \end{aligned} \quad (2.0.4)$$

The above equations can be expressed as the matrix equation

$$\begin{pmatrix} 2 & 1 \\ 3 & 2 \end{pmatrix} \mathbf{x} = \begin{pmatrix} 5 \\ 8 \end{pmatrix} \quad (2.0.5)$$

The augmented matrix for the above equation is row reduced as follows

$$\begin{pmatrix} 2 & 1 & 5 \\ 3 & 2 & 8 \end{pmatrix} \xrightarrow{R_2 \leftarrow 2R_2 - 3R_1} \begin{pmatrix} 2 & 1 & 5 \\ 0 & 1 & 1 \end{pmatrix} \quad (2.0.6)$$

$$\begin{pmatrix} 2 & 1 & 5 \\ 0 & 1 & 1 \end{pmatrix} \xrightarrow{R_1 \leftarrow R_1 - R_2} \begin{pmatrix} 2 & 0 & 4 \\ 0 & 1 & 1 \end{pmatrix} \quad (2.0.7)$$

$$\begin{pmatrix} 2 & 0 & 4 \\ 0 & 1 & 1 \end{pmatrix} \xrightarrow{R_1 \leftarrow \frac{R_1}{2}} \begin{pmatrix} 1 & 0 & 2 \\ 0 & 1 & 1 \end{pmatrix} \quad (2.0.8)$$

$$\Rightarrow \mathbf{x} = \begin{pmatrix} 2 \\ 1 \end{pmatrix} \quad (2.0.9)$$

is a solution of (1.0.2)

\therefore (1.0.2) has a unique solution so we can say they are intersect.

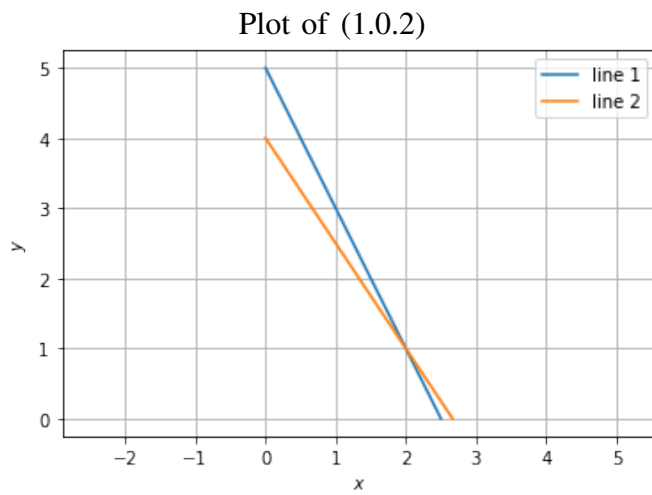


Fig. 2.2: INTERSECTING LINES.