

Q1. standard form:

$$\max Z = 5x_1 + 3x_2 + 0s_1 + 0s_2$$

$$\text{s.t. } 3x_1 + 5x_2 + s_1 = 15$$

$$5x_1 + 2x_2 + s_2 = 10$$

$$x_1, x_2, s_1, s_2 \geq 0$$

step 2:- starting simplex table.

	C_j	5	3	0	0		
C_B	BV	x_1	x_2	s_1	s_2	sol ⁿ	Ratio
0	s_1	3	5	1	0	15	5
0	s_2	5	2	0	1	10 \rightarrow	2 \rightarrow
	$C_j - Z_j$	5	3	0	0		

step 3:- calculate $c_j - z_j$ values, since all $c_j - z_j$ values are +ve \therefore the solⁿ is not optimal.

step 4:- Find incoming and outgoing vector

Since $x_1 = 5$ in $c_j - z_j$ is the largest +ve value, so it is incoming vector. and because in the Ratio column $S_2 = 2$ is the least value which is +ve, so it is outgoing vector.

step 5:- making iteration table 1.

	C_j	5	3	0	0		
C_B	B_V	x_1	x_2	S_1	S_2	Sol ⁿ	Ratio
0	S_1	0	19/5	1	-3/5	9	45/19
5	x_1	1	2/5	0	1/5	2	5
	Z_j	5	2	0	1		
	$C_j - Z_j$	0	1	0	-1		

for calculating R_1 values or (x_1 values) we will simply divide the whole row by the key element (5). and to obtain the new values of R_1 or S_1 we have a formula:-

$$N.V = O.V = \left(\frac{\text{corresponding key column value} \times \text{corresponding key row value}}{\text{key element}} \right)$$

Step 6 Since $x_2 = 1$ is the maximum (+)ve value in $C_j - Z_j$ row, so it is incoming variable and S_1 is the least (+)ve value in Ratio column so, S_1 is outgoing variable.

Step 7 making simplex table 2.

	C_j	5	3	0	0		
C_B	B_V	x_1	x_2	S_1	S_2	Sol^n	Ratio
3	x_2	0	1	$5/19$	$-3/19$	$45/19$	
5	x_1	1	0	$-2/19$	$5/19$	$20/19$	
	Z_j	5	3	$5/19$	$16/19$	$235/19$	
	$C_j - Z_j$	0	0	$-5/19$	$-16/19$		

all $C_j - Z_j \leq 0$, so above Sol^n is the optimal Sol^n .

Optimal Sol^n is $x_1 = \frac{20}{19}$, $x_2 = \frac{45}{19}$

and $Z_{max} = \frac{235}{19}$

Q2. Step 1:- standard form of primal:-

$$\min Z = 6x_1 + 4x_2$$

$$\text{s.t. } 2x_1 + x_2 \geq 1 \text{ and } 3x_1 + 4x_2 \geq 1.5$$

$$\text{where } x_1, x_2 \geq 0$$

Step 2:- dual of the primal is

$$\max W = y_1 + 1.5y_2$$

$$\text{s.t. } 2y_1 + 3y_2 \leq 6$$

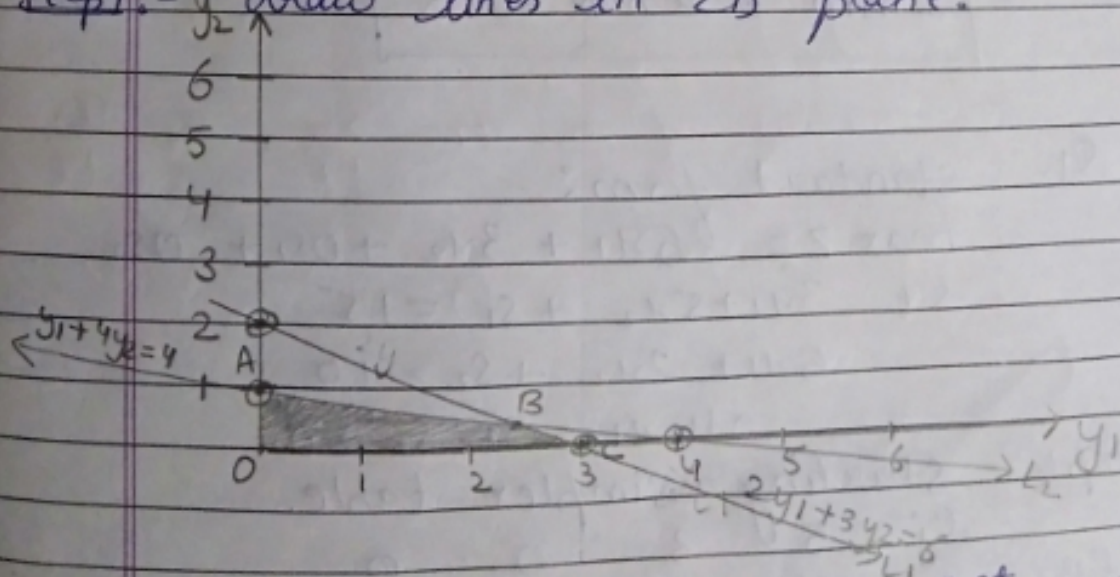
$$\text{and } y_1 + 4y_2 \leq 4, \quad y_1, y_2 \geq 0$$

Step 3:- Solving dual by graphical method.

Consider the constraints as equations.

$$2y_1 + 3y_2 = 6 \text{ and } y_1 + 4y_2 = 4$$

Step 4:- draw lines in 2D plane.



Step 5:- Solving L_1 and L_2 we get

$$y_1 = \frac{12}{5} \text{ and } y_2 = \frac{2}{5}, \text{ point B in } \left(\frac{12}{5}, \frac{2}{5}\right)$$

Step 6:- Shaded region is the permissible region for the values of y_1 & y_2 .

Step 7:- Calculating the values of w at the shaded region.

$$w_0 = 1(0) + 1.5(0) = 0$$

$$w_A = 1(0) + 1.5(1) = 1.5$$

$$w_B = 1\left(\frac{12}{5}\right) + 1.5\left(\frac{2}{5}\right) = \frac{12}{5} + \frac{3}{5} = 3$$

$$w_C = 1(3) + 1.5(0) = 3$$

$$w_{\max} = 3 \text{ at } \left(\frac{12}{5}, \frac{2}{5}\right) \text{ and } (3, 0)$$

∴ It have multiple solⁿ

$$\boxed{Z_{\min} = w_{\max} = 3}$$