

No. 1 INSTITUTE FOR IAS/IFoS EXAMINATIONS



OUR ACHIEVEMENTS IN IAS (FROM 2008 TO 2019)



HEAD OFFICE: 25/8, Old Rajender Nagar, Delhi-60. BRANCH OFFICE: 105-106, Top Floor, Mukherjee Tower Mukherjee Nagar, Delhi-9

Ph.: 011-45629987, 9999197625 www.ims4maths.com e-Mail: ims4maths@gmail.com

Regional Office: H.No. 1-10-237, 2nd Floor, Room No. 202 R.K.'s Kancham's Blue Sapphire Ashok Nagar, Hyderabad-20. Ph.: 9652351152, 9652661152

MAINS TEST SERIES-2020

(OCT. to JAN..-2020-21)

IAS/IFoS

MATHEMATICS

Under the guidance of **K. Venkanna**

DATE : 22-NOV.-2020

FULL SYLLABUS (PAPER-I)

Common Test (Test-13 for Batch-I) & (Test-5 for Batch-II)

Time: 3 Hours

Maximum Marks: 250

INSTRUCTIONS

Each question is printed only in English.

Answer must be written in the medium specified in the admission Certificate issued to you, which must be stated clearly on the cover of the answer-book in the space provided for the purpose. No marks will be given for the answers written in a medium other than that specified in the Admission Certificate.

Candidates should attempt Question Nos. 1 and 5, which are compulsory, and any **THREE** of the remaining questions selecting at least **ONE** question from each Section.

The number of marks carried by each question is indicated at the end of the question.

Assume suitable data if considered necessary and indicate the same clearly.

Symbols/notations carry their usual meanings, unless otherwise indicated.

All questions carry equal marks.

Important Note: Whenever a question is being attempted, all its parts/ sub-parts must be attempted contiguously. This means that before moving on to the next question to be attempted, candidates must finish attempting all parts/ sub-parts of the previous question attempted. This is to be strictly followed.

Pages left blank in the answer-book are to be clearly struck out in ink. Any answers that follow pages left blank may not be given credit.



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SECTION - A

1. (a) Let W_1 and W_2 be subspaces of a vector space V such that the set-theoretic union of W_1 and W_2 is also a subspace. Prove that one of the spaces W_i is contained in the other. **[10]**

1. (b) Let $T : M_{22} \rightarrow M_{22}$ be defined by $T(A) = A^T$. Give M_{22} the standard basis

$$S = \left\{ \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 1 \\ 0 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 0 \\ 1 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix} \right\} = \{e_1, e_2, e_3, e_4\}$$

and find the matrix for T with respect to S . **[10]**





















1. (c) If $u = At^{-1/2}e^{-x^2/4a^2t}$, Prove that $\frac{\partial u}{\partial t} = a^2 \frac{\partial^2 u}{\partial x^2}$. **[10]**

1. (d) Find the altitude and the semi-vertical angle of a cone of least volume which can be circumscribed to a sphere of radius a . **[10]**

1. (e) Prove that the circles $x^2 + y^2 + z^2 - 2x + 3y + 4z - 5 = 0$, $5y + 6z + 1 = 0$ and $x^2 + y^2 + z^2 - 3x - 4y + 5z - 6 = 0$, $x + 2y - 7z = 0$ lies on the same sphere and find its equation. Also find the value of a for which $x + y + z = a\sqrt{3}$ touches the sphere. **[10]**

2. (a) (i) Let V be the space of 2×2 matrices over F . Find a basis $\{A_1, A_2, A_3, A_4\}$ for V such that $A_i^2 = A_i$ for each i .
(ii) Let V be a vector space over a subfield F of the complex numbers. Suppose α , β , and γ are linearly independent vectors in V . Prove that $(\alpha + \beta)$, $(\beta + \gamma)$, and $(\gamma + \alpha)$ are linearly independent. **[10+10=20]**

No.1 INSTITUTE FOR IAS/IFoS EXAMINATIONS**OUR ACHIEVEMENTS IN IFoS (FROM 2008 TO 2019)****OUR RANKERS AMONG TOP 10 IN IFoS**

 AIR-01 IFoS-2019	 AIR-01 IFoS-2015	 AIR-03 IFoS-2016	 AIR-04 IFoS-2014	 AIR-04 IFoS-2014	 AIR-04 IFoS-2010	 AIR-05 IFoS-2019
 AIR-05 IFoS-2017	 AIR-05 IFoS-2014	 AIR-05 IFoS-2011	 AIR-06 IFoS-2015	 AIR-07 IFoS-2012	 AIR-09 IFoS-2018	 AIR-10 IFoS-2017
 AIR-13 IFoS-2016	 AIR-16 IFoS-2016	 AIR-20 IFoS-2019	 AIR-24 IFoS-2019	 AIR-30 IFoS-2019	 AIR-38 IFoS-2019	 AIR-83 IFoS-2019
 AIR-35 IFoS-2017	 AIR-36 IFoS-2017	 AIR-40 IFoS-2017	 AIR-45 IFoS-2017	 AIR-51 IFoS-2017	 AIR-58 IFoS-2017	 AIR-68 IFoS-2017
 AIR-31 IFoS-2016	 AIR-32 IFoS-2016	 AIR-35 IFoS-2016	 AIR-36 IFoS-2016	 AIR-48 IFoS-2016	 AIR-57 IFoS-2016	 AIR-58 IFoS-2016
 AIR-29 IFoS-2016	 AIR-30 IFoS-2016	 AIR-48 IFoS-2016	 AIR-62 IFoS-2016	 AIR-72 IFoS-2016	 AIR-78 IFoS-2016	 AIR-87 IFoS-2016
 AIR-48 IFoS-2014	 AIR-57 IFoS-2014	 AIR-16 IFoS-2012	 AIR-29 IFoS-2013	 AIR-39 IFoS-2015	 AIR-32 IFoS-2013	 AIR-48 IFoS-2012

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IAS/IFoS MATHEMATICS

(Optional)

by K. Venkanna

OUR SUCCESSFUL STUDENTS IN CSE 2018 with HIGHEST MARKS



KANISHAK KATARIA
AIR-01
MARKS
361/500



K. VARUN REDDY
AIR-07
MARKS
324/500



TANMAY V. SHARMA
AIR-10
MARKS
336/500



G.S.S. PRAVEENCHAND
AIR-64
MARKS
342/500



MANISHA RANA
AIR-67
MARKS
326/500



DALIP KUMAR
AIR-73
MARKS
327/500



KHUSHBOO GUPTA
AIR-80
MARKS
326/500



JAY SHIVANI
AIR-81
MARKS
336/500



AANCHAL SRIVASTAVA
AIR-110
MARKS
309/500



HIMANSHU PRAJAPATI
AIR-124
MARKS
328/500



SUNEEL SHEORAN
AIR-192
MARKS
325/500



AKASH SINGH
AIR-193
MARKS
336/500



SACHIN BANSAL
AIR-348
MARKS
316/500



KATTA RAVI TEJA
AIR-349
MARKS
322/500



RAJAT BHARDWAJ
AIR-366
MARKS
302/500



C. VISHNU CHARAN
AIR-406
MARKS
312/500



PANKAJ KUMAWAT
AIR-443
MARKS
334/500



SANJAY SAHU
AIR-526
MARKS
305/500



AMIT KUMAWAT
AIR-600
MARKS
320/500

And Many More...

2. (b) Show that the function $f : \mathbb{R}^2 \rightarrow \mathbb{R}$ defined by setting

$$f(x, y) = \begin{cases} x \sin\left(\frac{1}{x}\right) + y \sin\left(\frac{1}{y}\right), & \text{when } xy \neq 0 \\ x \sin\frac{1}{x} & , \text{ when } x \neq 0, y = 0 \\ y \sin\frac{1}{y} & , \text{ when } x = 0, y \neq 0 \\ 0 & , \text{ when } x = y = 0 \end{cases}$$

is continuous but not differentiable at $(0, 0)$. [14]

2. (c) (i) The plane $x - 2y + 3z = 0$ is rotated through a right angle about its line of intersection with the plane $2x + 3y - 4z - 5 = 0$, find the equation of the plane in its new position.

(ii) Find the S. D. between lines

$$\frac{x-3}{3} = \frac{y-8}{-1} = \frac{z-3}{1} \text{ and } \frac{x+3}{-3} = \frac{y+7}{2} = \frac{z-6}{4}$$

Find also its equations and the points in which it meets the given lines. [6+10=16]

3. (a) We consider the 5×5 matrix

$$A = \begin{bmatrix} 1 & 2 & 0 & 3 & 0 \\ 1 & 2 & -1 & -1 & 0 \\ 0 & 0 & 1 & 4 & 0 \\ 2 & 4 & 1 & 10 & 1 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

and the following problems concerning A

- (a) Find an invertible matrix P such that PA is a row-reduced echelon matrix R.
(b) Find a basis for the row space W of A.
(c) Say which vectors $(b_1, b_2, b_3, b_4, b_5)$ are in W.

(3)

- (d) Find the coordinate matrix of each vector (b_1, b_2, b_3, b_4, b_5) in W in the ordered basis chosen in (b).
- (e) Write each vector (b_1, b_2, b_3, b_4, b_5) in W as a linear combination of the rows of A .
- (f) Give an explicit description of the vector space V of all 5×1 column matrices X such that $AX = 0$. [16]

3. (b) (i) Test for convergence the integrals

$$\int_0^{\infty} \frac{x \tan^{-1} x}{(1+x^4)^{1/3}} dx$$

- (ii) Let $E = \{ (x, y) \in \mathbf{R}^2 / 0 < x < y \}$. Then evaluate

$$\iint_E ye^{-(x+y)} dx dy \quad [18]$$

3. (c) If the feet of the three normals from P to the ellipsoid $x^2/a^2 + y^2/b^2 + z^2/c^2 = 1$ lie on the plane $x/a + y/b + z/c = 1$ prove that the feet of the other three lie on the plane $x/a + y/b + z/c + 1 = 0$ and P lies on the line $a(b^2 - c^2)x = b(c^2 - a^2)y = c(a^2 - b^2)z$. [16]

4. (a) (i) Let V be the (real) vector space of all polynomial functions from \mathbf{R} into \mathbf{R} of degree 2 or less, i.e., the space of all functions f of the form $f(x) = c_0 + c_1x + c_2x^2$.

Let t be a fixed real number and define

$$g_1(x) = 1, \quad g_2(x) = x + t, \quad g_3(x) = (x + t)^2.$$

Prove that $B = \{g_1, g_2, g_3\}$ is a basis for V . If

$$f(x) = c_0 + c_1x + c_2x^2$$

what are the coordinates of f in this ordered basis B ?

- (ii) Let $T : p_1 \rightarrow p_2$ be defined by $T(a + bx) = ax + (b/2)x^2$. Give p_1 and p_2 the standard bases $S = \{1, x\}$ and $\tau = \{1, x, x^2\}$, respectively. Find the matrix of T with respect to these bases. Do the same for $L : p_2 \rightarrow p_1$ defined by $L(a + bx + cx^2) = b + 2cx$.

[10+10=20]

(16)

Anyone who has done B.Tech / M.Tech / B.Sc / M.Sc and has an interest in Maths.

Usually commit and their mitigation measures. For example, I commit a lot of mistakes when doing Integration by parts and usually the error involves missing negative (-) sign etc. Therefore whenever I come across such type of question I try to devote extra 1 minute to re-check all my steps.

Maths.stackexchange.com is the best online resource for preparation. You can create an account and get your maths questions answered within minutes.

Why did I score only 262?

Among all the students in the final list who had Maths as an optional, I have scored the least. My paper - 1 was a complete disaster and I only scored 92 marks in it. In fact I could only attempt 160 marks paper and had to leave 90 marks paper completely.

The reasons for the above situation in Paper - 1 are as follows:

1. **Lack of written practice:** In many topics (especially statics and dynamics) I used to just look at a question and its solution without solving it first. As a result I forgot the exact method in the exam hall!
2. **Left many topics:** I prepared only 25% 3-D, 80% Calculus and 25% Statics & Dynamics and had to pay a heavy price in the exam.

On the other hand my preparation for paper - 2 was excellent and therefore I scored an amazing 170 marks in it

BHAVESH MISHRA

AIR-58 in CSE-2014

Easy paper: The difficulty level of paper is quite moderate and almost all questions are directly picked from the IMS Test Series / Standard Textbooks.

WHO SHOULD TAKE IT?

Myths around science subjects.

Coaching institutions have mastered the art of brainwashing students and creating an atmosphere of gloom and doom around science subjects. There are lots of myths circulating among students. Let's bust these myths.

1. **Maths optional is only for students from IITs: Definitely not.** Anyone willing to put in hard work can easily score very high marks. The best example being **Nitish K (Rank 8) who is not from any IIT.**
2. **There is heavy scaling:** Let the data speak for itself. I attempted 240 marks in Paper 2 and got 170 marks. Now would you call it a scaling?
3. **It plays no role in GS:** Yes it's true that science optional subjects don't overlap with GS but it's equally true that GS has never been a rank decider in UPSC IAS.
4. **There are 3 major things that decides your rank:** Essay, Optional and Interview. Even if one puts in 5 years of efforts in GS the advantage in terms of marks would be around 30 marks or so but 1 year of dedicated effort in maths would give you 50+ marks advantage straightaway.

Do's and Don'ts:

1. Practice, Practice and Practice. The key to success in maths is filling up as many notebooks as you can, during the preparation stage. The more you sweat during preparation the less you will bleed in the battlefield!
2. Don't read Maths book / notes like GS. It is a recipe for disaster. Rather always study with pen, paper and calculator.
3. While solving examples don't jump to see solution first. Try giving your best shot and after making sure that you are not able to solve it using your present knowledge then only look at the answer. This will ensure that better retention.
4. Generally we make lots of silly mistakes while solving a question. It is best to catch these errors early and not repeat them in exam hall. The best strategy for this is to maintain a notebook of errors that you

4. (b) The ellipsoid with equation $x^2 + 2y^2 + z^2 = 4$ is heated so that its temperature at (x, y, z) is given by $T(x, y, z) = 70 + 10(x + z)$. find the hottest and coldest points on the ellipsoid. **[15]**
4. (c) Find the locus of the points from which three mutually perpendicular tangents can be drawn to the paraboid $(x^2/a^2) - (y^2/b^2) = 2z$ **[15]**

SECTION - B

5. (a) (i) Solve $dy/dx = (x + y - 2)/(y - x - 4)$
(ii) Solve $(2xy^4 e^y + 2xy^3 + y) dx + (x^2y^4 e^y - x^2y^2 - 3x) dy = 0$. **[10]**
5. (b) (i) Find $L\{F(t)\}$, where

$$F(t) = \begin{cases} \cos\left(t - \frac{2}{3}\pi\right), & t > \frac{2\pi}{3} \\ 0, & t < \frac{2\pi}{3} \end{cases}$$
 (ii) Find $L^{-1}\left\{\frac{(p+1)e^{-\pi p}}{p^2 + p + 1}\right\}$ **[10]**
5. (c) A heavy uniform cube balances on the highest point of a sphere whose radius is r . If the sphere is rough enough to prevent sliding and if the side of the cube be $\pi r/2$, show that the cube can rock through a right angle without falling. **[10]**
5. (d) A point moves in a straight line so that its distance s from a fixed point at any time t is proportional to t^n . If v be the velocity and f the acceleration at any time t , show that $v^2 = nfs/(n - 1)$. **[10]**

(5)

5. (e) (i) Prove that $F = (y^2 \cos x + z^3) \mathbf{i} + (2y \sin x - 4) \mathbf{j} + (3xz^2 + 2) \mathbf{k}$ is a conservative force field.
 (ii) Find the scalar potential for F .
 (iii) Find the work done in moving an object in this field from $(0, 1, -1)$ to $(\pi/2, -1, 2)$. **[10]**
6. (a) (i) Find the orthogonal trajectories of the family of curves $r = a(1 + \cos \theta)$, where a is the parameter.
 (ii) Solve : $p^3 - 4xyp + 8y^2 = 0$
 (iii) Find the values of λ for which all solutions of $x^2 (d^2y/dx^2) - 3x (dy/dx) - \lambda y = 0$ tend to zero $x \rightarrow \infty$. **[20]**
6. (b) A uniform chain of length l hangs between two points A and B which are at a horizontal distance a from one another, with B at a vertical distance b above A. Prove that the parameter of the catenary is given by

$$2c \sinh(a/2c) = \sqrt{l^2 - b^2}.$$

Prove also that, if the tensions at A and B are T_1 and T_2 respectively,

$$T_1 + T_2 = W \sqrt{1 + \frac{4c^2}{l^2 - b^2}} \text{ and } T_2 - T_1 = Wb/l,$$

where W is the weight of the chain. **[15]**

6. (c) (i) Given the space curve $x = t, y = t^2, z = \frac{2}{3}t^3$, find (i) the curvature κ , (ii) the torsion τ .
 (ii) Evaluate by Green's theorem in plane $\int_C (e^{-x} \sin y dx + e^{-x} \cos y dy)$, where C is the rectangle with vertices $(0, 0), (\pi, 0), \left(\pi, \frac{1}{2}\pi\right), \left(0, \frac{1}{2}\pi\right)$. **[15]**

7. (a) Apply the method of variation of parameters to solve the equation

(14)

Irrespective of whether you are very happy or deeply unsatisfied about paper 1, try to forget about it and stay calm for paper 2.

INTERVIEW

In the interview, you can expect some questions related to mathematics optional. Generally you won't be asked to solve a problem because that ability has been tested in mains. They would like to see whether you have a genuine curiosity regarding mathematics outside what is mentioned in syllabus. In both my UPSC interviews, I was asked about Ramanujan's work. There were questions on Vedic Mathematics, National Mathematics Day, important Indian Mathematical Institutions, Field medalist Manjula Bhargava etc. Hence while preparing for interview, try to be aware about these non-theoretical aspects of maths as well.

I hope above tips provide some clarity regarding maths optional to UPSC aspirants.

All the best!

Bhavesh Mishra (AIR-58)

in IAS-2014 Examination

CLASSROOM STUDENT

Why Maths?

Simply because it is the best performing optional subject in UPSC/IAS.

Extremely high scoring: If you get your maths optional right then you will make it to the final list. This year one of my batch mate in IMS Nitish K (Rank 8) has got a mind boggling 346 marks.

Certainty: If you have attempted your paper well then you are sure that you will get good marks. For example this year just by attempting 400 marks paper you could get a decent 260+ marks. Even if you don't get good marks in first attempt but you can be sure that you will increase your marks in subsequent attempt(s).

Fun: Mathematics is a delightful subject and therefore doing maths takes you away from somewhat boring humanities.

Good Impression: The fact that you have taken Maths makes a good impression on interview board members

(it happened in my case!). They are very pleased to see that you have opted for a tough optional.

PRACTICE

Just knowing theory is not enough. It needs to be accompanied by consistent problem solving practice. It is best to solve questions that have already been asked in mains. If some problem seems very non-intuitive, it would help if the trick to solve such problem is written in your notebook.

TEST SERIES

Test series is very important for this optional. I had joined IMS test series which helped me in identifying my weak areas. In both CSE and IFoS mains, there were many questions similar to those covered in IMS test series. With enough practice, a candidate can achieve the ability to complete the maths paper in 3 hours. It is important to assess your performance after each test. Necessary steps should be taken to rectify common mistakes that you are committing in the test series. You should be alert not to repeat the same mistakes again & again. As your performance improves with every test, the actual mains paper will seem just like any other test & you will be able to comfortably complete it. Presentation of your answer matters a lot. Your aim should be to make examiner's life as easy as possible so that he/she will award you maximum marks. Only the final answer doesn't matter. Writing proper steps is also important to show the logical flow with which you arrived at the solution. Specifically mention whichever theorem or property you are using in a particular step. Wherever possible, draw neat diagrams with proper labelling. Such small things will collectively fetch you the extra marks that you are expecting from this optional. The habit of writing such detailed answers will not develop overnight and hence you have to consciously work through the test series in this direction.

DURING MAINS

The mains exam schedule does not provide much gap between General Studies & Maths papers. You will generally have 1 day in between. Your notebook containing important formulae & theorems will be very useful at such times. You will be able to go through this summary of each chapter and it will provide much needed confidence before the actual paper. During the main exam, I would advise completing the compulsory questions 1 & 5 first. Then you can choose 3 out of remaining 6 questions. Easier questions like those from topics like linear programming, numerical analysis, linear algebra etc. should be the priority. Even if you don't know the complete answer to any question, write as many steps as you can since partial marks also matter. Once you finish paper 1, don't start immediately analyzing your performance.

$$(x + 2)y_2 - (2x + 5)y_1 + 2y = (x + 1) e^x. \quad [16]$$

7. (b) A particle is projected with velocity V from the cusp of a smooth inverted cycloid down the arc, show that the time of reaching the vertex is

$$2\sqrt{(a/g)} \tan^{-1} \left[\left(\sqrt{4ag} \right) / V \right]. \quad [16]$$

7. (c) (I) Find the angle of intersection at $(4, -3, 2)$ of spheres $x^2 + y^2 + z^2 = 29$ and $x^2 + y^2 + z^2 + 4x - 6y - 8z - 47 = 0$.

(II) (i) Prove that $r^n \mathbf{r}$ is an irrotational vector for any value of n but is solenoidal only if $n + 3 = 0$.

(ii) If $\mathbf{u} = (1/r) \mathbf{r}$, show that $\nabla \times \mathbf{u} = 0$.

(iii) if $\mathbf{u} = (1/r) \mathbf{r}$ find $\text{grad}(\text{div } \mathbf{u})$. [18]

8. (a) By using Laplace transform method solve the initial value problem $(D^3 - 2D^2 + 5D) y = 0$ if $y(0) = 0, y'(0) = 1, y(\pi/8) = 1$. [15]

8. (b) A particle describes the curve $r^n = a^n \cos n\theta$ under a force to the pole. Find the law of force. [17]

8. (c) If $\mathbf{F} = (y^2 + z^2 - x^2) \mathbf{i} + (z^2 + x^2 - y^2) \mathbf{j} + (x^2 + y^2 - z^2) \mathbf{k}$, evaluate $\iint \text{curl } \mathbf{F} \cdot \mathbf{n} dS$ taken over the portion of the surface $x^2 + y^2 + z^2 - 2ax + az = 0$ above the plane $z = 0$, and verify Stoke's theorem. [18]

OUR TOPPER'S MARKS LIST (IAS)

- For your final selection, optional subject marks are crucial.
- Choose Optional Subject based on Your Graduation Studies & Score Highest Marks.
- Now Mathematics has become one of the most Cherished Optional Paper among Science Graduates, especially Students with Mathematics background including B.Tech.
- In the new pattern of exam, the average marks of successful candidates in Maths is more than 300 out of 500.
- Mathematics (Opt.) has proven to be the Most Reliable and High Scoring Subject in IAS/IFoS.
- IMS has been successfully providing consistent results since its inception.

MARKS ARE BEFORE YOU AND YOU SHOULD ANALYZE YOURSELF

SUBJECT		Max. Marks	Marks Obtained
ESSAY (PAPER-I)		250	133
GENERAL STUDIES-I (PAPER-II)		250	098
GENERAL STUDIES-II (PAPER-III)		250	117
GENERAL STUDIES-III (PAPER-IV)		250	117
GENERAL STUDIES-IV (PAPER-V)		250	116
OPTIONAL-I (MATHEMATICS) (PAPER-VI)		170/250	361/500
OPTIONAL-II (MATHEMATICS) (PAPER-VII)		170/250	
WRITTEN TOTAL		1750	942
PERSONALITY TEST		275	179
TOTAL FINAL		2025	1121

KANISHAK KATARMA			
AIR-01			
IAS-2018			

SUBJECT		Max. Marks	Marks Obtained
ESSAY (PAPER-I)		250	138
GENERAL STUDIES-I (PAPER-II)		250	091
GENERAL STUDIES-II (PAPER-III)		250	111
GENERAL STUDIES-III (PAPER-IV)		250	097
GENERAL STUDIES-IV (PAPER-V)		250	104
OPTIONAL-I (MATHEMATICS) (PAPER-VI)		168/250	336/500
OPTIONAL-II (MATHEMATICS) (PAPER-VII)		168/250	
WRITTEN TOTAL		1750	877
PERSONALITY TEST		275	187
TOTAL FINAL		2025	1064

TANMAY V. SHARMA			
AIR-10			
IAS-2018			

SUBJECT		Max. Marks	Marks Obtained
ESSAY (PAPER-I)		250	130
GENERAL STUDIES-I (PAPER-II)		250	105
GENERAL STUDIES-II (PAPER-III)		250	099
GENERAL STUDIES-III (PAPER-IV)		250	112
GENERAL STUDIES-IV (PAPER-V)		250	100
OPTIONAL-I (MATHEMATICS) (PAPER-VI)		155/250	326/500
OPTIONAL-II (MATHEMATICS) (PAPER-VII)		171/250	
WRITTEN TOTAL		1750	872
PERSONALITY TEST		275	157
TOTAL FINAL		2025	1029

MANISHA RANA			
AIR-67			
IAS-2018			

SUBJECT		Max. Marks	Marks Obtained
ESSAY (PAPER-I)		250	141
GENERAL STUDIES-I (PAPER-II)		250	088
GENERAL STUDIES-II (PAPER-III)		250	103
GENERAL STUDIES-III (PAPER-IV)		250	093
GENERAL STUDIES-IV (PAPER-V)		250	103
OPTIONAL-I (MATHEMATICS) (PAPER-VI)		175/250	326/500
OPTIONAL-II (MATHEMATICS) (PAPER-VII)		151/250	
WRITTEN TOTAL		1750	854
PERSONALITY TEST		275	171
TOTAL FINAL		2025	1025

KHUSHBOO GUPTA			
AIR-80			
IAS-2018			

SUBJECT		Max. Marks	Marks Obtained
ESSAY (PAPER-I)		250	125
GENERAL STUDIES-I (PAPER-II)		250	090
GENERAL STUDIES-II (PAPER-III)		250	107
GENERAL STUDIES-III (PAPER-IV)		250	106
GENERAL STUDIES-IV (PAPER-V)		250	109
OPTIONAL-I (MATHEMATICS) (PAPER-VI)		152/250	309/500
OPTIONAL-II (MATHEMATICS) (PAPER-VII)		157/250	
WRITTEN TOTAL		1750	846
PERSONALITY TEST		275	171
TOTAL FINAL		2025	1017

ANACHAL SRIVASTAVA			
AIR-110			
IAS-2018			

SUBJECT		Max. Marks	Marks Obtained
ESSAY (PAPER-I)		250	113
GENERAL STUDIES-I (PAPER-II)		250	097
GENERAL STUDIES-II (PAPER-III)		250	113
GENERAL STUDIES-III (PAPER-IV)		250	117
GENERAL STUDIES-IV (PAPER-V)		250	121
OPTIONAL-I (MATHEMATICS) (PAPER-VI)		178/250	324/500
OPTIONAL-II (MATHEMATICS) (PAPER-VII)		146/250	
WRITTEN TOTAL		1750	885
PERSONALITY TEST		275	182
TOTAL FINAL		2025	1067

K. VARUN REDDY			
AIR-07			
IAS-2018			

SUBJECT		Max. Marks	Marks Obtained
ESSAY (PAPER-I)		250	119
GENERAL STUDIES-I (PAPER-II)		250	098
GENERAL STUDIES-II (PAPER-III)		250	107
GENERAL STUDIES-III (PAPER-IV)		250	106
GENERAL STUDIES-IV (PAPER-V)		250	101
OPTIONAL-I (MATHEMATICS) (PAPER-VI)		175/250	342/500
OPTIONAL-II (MATHEMATICS) (PAPER-VII)		167/250	
WRITTEN TOTAL		1750	873
PERSONALITY TEST		275	157
TOTAL FINAL		2025	1030

G.S.S. PRAVEENCHAND			
AIR-64			
IAS-2018			

SUBJECT		Max. Marks	Marks Obtained
ESSAY (PAPER-I)		250	117
GENERAL STUDIES-I (PAPER-II)		250	084
GENERAL STUDIES-II (PAPER-III)		250	115
GENERAL STUDIES-III (PAPER-IV)		250	109
GENERAL STUDIES-IV (PAPER-V)		250	097
OPTIONAL-I (MATHEMATICS) (PAPER-VI)		171/250	327/500
OPTIONAL-II (MATHEMATICS) (PAPER-VII)		156/250	
WRITTEN TOTAL		1750	849
PERSONALITY TEST		275	179
TOTAL FINAL		2025	1028

DALIP KUMAR			
AIR-73			
IAS-2018			

SUBJECT		Max. Marks	Marks Obtained
ESSAY (PAPER-I)		250	117
GENERAL STUDIES-I (PAPER-II)		250	096
GENERAL STUDIES-II (PAPER-III)		250	104
GENERAL STUDIES-III (PAPER-IV)		250	098
GENERAL STUDIES-IV (PAPER-V)		250	103
OPTIONAL-I (MATHEMATICS) (PAPER-VI)		164/250	336/500
OPTIONAL-II (MATHEMATICS) (PAPER-VII)		172/250	
WRITTEN TOTAL		1750	854
PERSONALITY TEST		275	171
TOTAL FINAL		2025	1025

JAY SHIVANI			
AIR-81			
IAS-2018			

SUBJECT		Max. Marks	Marks Obtained
ESSAY (PAPER-I)		250	113
GENERAL STUDIES-I (PAPER-II)		250	075
GENERAL STUDIES-II (PAPER-III)		250	104
GENERAL STUDIES-III (PAPER-IV)		250	099
GENERAL STUDIES-IV (PAPER-V)		250	094
OPTIONAL-I (MATHEMATICS) (PAPER-VI)		168/250	328/500
OPTIONAL-II (MATHEMATICS) (PAPER-VII)		160/250	
WRITTEN TOTAL		1750	813
PERSONALITY TEST		275	201
TOTAL FINAL		2025	1014

HIMANSHU PRAJAPATI			
AIR-124			
IAS-2018			

am awaiting the Mains result. This article is a humble attempt to share my experience of maths optional preparation for CSE/IFoS exam. I would be glad if it helps any UPSC aspirant who is undecided about choosing the optional or those who are already preparing with mathematics as their optional.

WHY MATHEMATICS

It is very important for a UPSC aspirant to have genuine interest in mathematics if he/she wants to choose this optional. Maths used to be my favourite subject in school and in IITB also I had pursued additional courses in mathematics out of interest. Since the syllabus is large & requires considerable practice, it is necessary to have a genuine interest. Apart from my inherent inclination, this optional offers certain advantages which made it an obvious choice. In this optional, the marks you get are almost proportional to your efforts. With proper hard work, a candidate can comfortably attempt all the questions in exam and expect to score around 50% marks even after heavy scaling which can offer the necessary edge in this intense competition. Such candidate generally would not find any question surprising in mains. This kind of certainty is not present in humanities optionals.

THE SYLLABUS

The prescribed syllabus for maths is quite large which makes it necessary to stick to limited sources. I relied on notes provided by Venkanna Sir at IMS for covering the syllabus. Since these notes were very comprehensive, I didn't have to spend time scanning reference books for relevant material. Venkanna Sir's classroom coaching helped me in completing the syllabus in a disciplined manner. Initially I would underline important theorems, formulae, results mentioned in the notes. Then I used to compile them in a notebook and this was useful for revision. So eventually I had a notebook with just the crux of the matter. I would advise all candidates with maths optional to prepare such a summary for all topics. Due to large syllabus, there is a natural tendency to skip a few chapters. But for the sake of compulsory questions, it is necessary to know at least basics of each chapter. The physics related chapters of statics, dynamics, mechanics are generally left untouched while preparing maths optional. Regarding these chapters, my preparation was such that I would be able to solve the compulsory 10 mark questions. They are quite manageable once you know the basic theory and there is no point in unnecessarily losing marks. The real analysis/calculus & modern algebra chapters are time consuming but candidates can't afford to skip them.

the best mode of judging your preparation. You can fairly evaluate your performance with your marks and then focus on the weak topics. Secondly, its a rehearsal of Mains Exam and thus helps you greatly in time management.

Mains exam is nearly a marathon for your hand and thus you get very much trained for facing them.

Test Series also provided me another pool of questions to practise. They also helped in developing the ability of answer writing which definitely can't be developed overnight. I attended Test Series of IMS and luckily many questions of Test Series appeared in both IFoS Exam and CSE. I would also request all the candidates to give the test series by coming to classroom if possible and stick to the timelines as it really helps in completion of syllabus.

I hope this writeup clears some of the doubts and gives clarity on maths optional to UPSC IAS aspirants. All the Best

If anyone wants to contact me, please drop me an email - parthjaiswal512@gmail.com. I will be more than happy to help you.

Thank You
Parth Jaiswal
AIR-5 in IFoS-2014,
AIR-299 in CSE-2014

KUMBHEJKAR YOGESH VIJAY (AIR-08 in IAS-2015)

(AIR-13 IFoS) & (AIR-143 IAS)
in IFoS-2014 & IAS-2014 Examinations
CLASSROOM STUDENT

MY BACKGROUND

I am Yogesh Kumbhejkar. I am an Electrical Engineer from IIT Bombay. I secured AIR 13 in Indian Forest Service Exam (IFoS) 2014 with Mathematics & Physics as the optional subjects. For Civil Service Exam (CSE) also, my optional is Mathematics. In IFoS exam, I scored 231/400 (118 + 113) in maths. In 2013 CSE Mains, my maths score was 250/500 (109 + 141). Hence mathematics has helped me in clearing mains in both CSE and IFoS. I was not selected in the final list of CSE 2013. In my second CSE attempt also I appeared for mains in 2014 with Maths as the optional subject. Now i

SUBJECT	Max. Marks	Marks Obtained
ESSAY (PAPER-I)	250	118
GENERAL STUDIES-I (PAPER-II)	250	087
GENERAL STUDIES-II (PAPER-III)	250	090
GENERAL STUDIES-III (PAPER-IV)	250	105
GENERAL STUDIES-IV (PAPER-V)	250	096
OPTIONAL-I (MATHEMATICS) (PAPER-VI)	173/250	
OPTIONAL-II (MATHEMATICS) (PAPER-VII)	152/250	
WRITTEN TOTAL	1750	821
PERSONALITY TEST	275	182
TOTAL FINAL	2025	1003

SUBJECT	Max. Marks	Marks Obtained
ESSAY (PAPER-I)	250	124
GENERAL STUDIES-I (PAPER-II)	250	091
GENERAL STUDIES-II (PAPER-III)	250	109
GENERAL STUDIES-III (PAPER-IV)	250	104
GENERAL STUDIES-IV (PAPER-V)	250	105
OPTIONAL-I (MATHEMATICS) (PAPER-VI)	167/250	
OPTIONAL-II (MATHEMATICS) (PAPER-VII)	149/250	
WRITTEN TOTAL	1750	849
PERSONALITY TEST	275	138
TOTAL FINAL	2025	987

SUBJECT	Max. Marks	Marks Obtained
ESSAY (PAPER-I)	250	135
GENERAL STUDIES-I (PAPER-II)	250	086
GENERAL STUDIES-II (PAPER-III)	250	093
GENERAL STUDIES-III (PAPER-IV)	250	096
GENERAL STUDIES-IV (PAPER-V)	250	085
OPTIONAL-I (MATHEMATICS) (PAPER-VI)	162/250	
OPTIONAL-II (MATHEMATICS) (PAPER-VII)	134/250	
WRITTEN TOTAL	1750	791
PERSONALITY TEST	275	195
TOTAL FINAL	2025	986

SUBJECT	Max. Marks	Marks Obtained
ESSAY (PAPER-I)	250	105
GENERAL STUDIES-I (PAPER-II)	250	093
GENERAL STUDIES-II (PAPER-III)	250	099
GENERAL STUDIES-III (PAPER-IV)	250	090
GENERAL STUDIES-IV (PAPER-V)	250	094
OPTIONAL-I (MATHEMATICS) (PAPER-VI)	153/250	
OPTIONAL-II (MATHEMATICS) (PAPER-VII)	159/250	
WRITTEN TOTAL	1750	793
PERSONALITY TEST	275	187
TOTAL FINAL	2025	980

SUBJECT	Max. Marks	Marks Obtained
ESSAY (PAPER-I)	250	111
GENERAL STUDIES-I (PAPER-II)	250	087
GENERAL STUDIES-II (PAPER-III)	250	105
GENERAL STUDIES-III (PAPER-IV)	250	106
GENERAL STUDIES-IV (PAPER-V)	250	101
OPTIONAL-I (MATHEMATICS) (PAPER-VI)	134/250	
OPTIONAL-II (MATHEMATICS) (PAPER-VII)	171/250	
WRITTEN TOTAL	1750	815
PERSONALITY TEST	275	138
TOTAL FINAL	2025	953

SUBJECT	Max. Marks	Marks Obtained
ESSAY (PAPER-I)	250	118
GENERAL STUDIES-I (PAPER-II)	250	079
GENERAL STUDIES-II (PAPER-III)	250	093
GENERAL STUDIES-III (PAPER-IV)	250	103
GENERAL STUDIES-IV (PAPER-V)	250	092
OPTIONAL-I (MATHEMATICS) (PAPER-VI)	155/250	
OPTIONAL-II (MATHEMATICS) (PAPER-VII)	165/250	
WRITTEN TOTAL	1750	805
PERSONALITY TEST	275	138
TOTAL FINAL	2025	943

SUBJECT	Max. Marks	Marks Obtained
ESSAY (PAPER-I)	250	114
GENERAL STUDIES-I (PAPER-II)	250	082
GENERAL STUDIES-II (PAPER-III)	250	099
GENERAL STUDIES-III (PAPER-IV)	250	095
GENERAL STUDIES-IV (PAPER-V)	250	101
OPTIONAL-I (MATHEMATICS) (PAPER-VI)	161/250	
OPTIONAL-II (MATHEMATICS) (PAPER-VII)	175/250	
WRITTEN TOTAL	1750	827
PERSONALITY TEST	275	176
TOTAL FINAL	2025	1003

SUBJECT	Max. Marks	Marks Obtained
ESSAY (PAPER-I)	250	069
GENERAL STUDIES-I (PAPER-II)	250	101
GENERAL STUDIES-II (PAPER-III)	250	110
GENERAL STUDIES-III (PAPER-IV)	250	105
GENERAL STUDIES-IV (PAPER-V)	250	101
OPTIONAL-I (MATHEMATICS) (PAPER-VI)	173/250	
OPTIONAL-II (MATHEMATICS) (PAPER-VII)	149/250	
WRITTEN TOTAL	1750	808
PERSONALITY TEST	275	179
TOTAL FINAL	2025	987

SUBJECT	Max. Marks	Marks Obtained
ESSAY (PAPER-I)	250	122
GENERAL STUDIES-I (PAPER-II)	250	093
GENERAL STUDIES-II (PAPER-III)	250	108
GENERAL STUDIES-III (PAPER-IV)	250	113
GENERAL STUDIES-IV (PAPER-V)	250	107
OPTIONAL-I (MATHEMATICS) (PAPER-VI)	162/250	
OPTIONAL-II (MATHEMATICS) (PAPER-VII)	140/250	
WRITTEN TOTAL	1750	845
PERSONALITY TEST	275	140
TOTAL FINAL	2025	985

SUBJECT	Max. Marks	Marks Obtained
ESSAY (PAPER-I)	250	093
GENERAL STUDIES-I (PAPER-II)	250	084
GENERAL STUDIES-II (PAPER-III)	250	101
GENERAL STUDIES-III (PAPER-IV)	250	115
GENERAL STUDIES-IV (PAPER-V)	250	106
OPTIONAL-I (MATHEMATICS) (PAPER-VI)	176/250	
OPTIONAL-II (MATHEMATICS) (PAPER-VII)	158/250	
WRITTEN TOTAL	1750	833
PERSONALITY TEST	275	138
TOTAL FINAL	2025	971

SUBJECT	Max. Marks	Marks Obtained
ESSAY (PAPER-I)	250	102
GENERAL STUDIES-I (PAPER-II)	250	091
GENERAL STUDIES-II (PAPER-III)	250	104
GENERAL STUDIES-III (PAPER-IV)	250	085
GENERAL STUDIES-IV (PAPER-V)	250	120
OPTIONAL-I (MATHEMATICS) (PAPER-VI)	145/250	
OPTIONAL-II (MATHEMATICS) (PAPER-VII)	153/250	
WRITTEN TOTAL	1750	800
PERSONALITY TEST	275	143
TOTAL FINAL	2025	943

PREPARATION STRATEGY

for IAS/IFoS MATHEMATICS

(Optional)

by Successful Candidate

PARTH JAISWAL

(AIR-5 IFOS) & (AIR-299 IAS)

in IFoS-2014 & IAS-2014 Examinations

CLASSROOM STUDENT

MY BACKGROUND

Hello, My name is Parth Jaiswal. I come from Jaipur, Rajasthan. I completed my graduation in Computer Science discipline from IIT Delhi in 2013. Soon afterwards I started preparing for Civil services and Indian Forest Service, aiming for the attempt of year 2014.

Luckily I was able to clear both the examinations in my first attempt. I secured AIR-5 in IFoS-2014 and AIR-299 in CSE-2014. My optional subject was Mathematics. In case of Forest Service Examination, candidate is required to choose 2 Optionals, thus my second optional was Forestry with Mathematics as my first optional. I secured 250/400 (125+125) marks in IFoS Exam and 300/500 (147+153) marks in CSE in Maths. Thus I would give much credit for my success to my correct choice of optional as well as performance in it. I am writing this to share my experience with Maths as an optional subject and would feel happy if I am able to clear some of the doubts as well as apprehensions regarding it which many UPSC aspirants possess.

Why I Chose Mathematics?

I chose **Mathematics** because of my inherent interest in it from childhood. I have performed well in this in my throughout education and thus was confident enough to handle it well. Another reason for choosing it was, I wanted to have my optional from my background and thus Maths proved to be appropriate choice. Having a science background, I found it much easier to study than any other subject, many of which we have to study for GS prep.

I would like to assert few points regarding it very clearly.

- This subject is vast in syllabus and takes more time to study than other optionals.
- It also requires consistent practise. But the positive part is - If you are thorough with the subject and have practised it well, you can comfortably attempt complete paper with correct answers and thus gives you a great opportunity to score well in your optional (inspite of the scaling often carried out in it) pushing you above the list.
- In this way, this optional gives a bit of security as well as certainty which again comes at a price i.e great amount of hard work. Also IFoS Exam prescribes certain optionals only and Mathematics is one of them. Not all optionals are available for this exam.
- So again it gives you the flexibility of giving IFoS Exam.

From where to study?

I attended classroom coaching of IMS, Rajinder Nagar. I restricted my preparation to the handouts provided by Venkanna Sir. Because of the voluminous syllabus, it is necessary to gauge the point where you have to stop. I found that the notes quite comprehensive and provided me a holistic coverage of the syllabus in a highly structured manner. I believe that those notes are sufficient from the theory point of view.

For practising questions which is of utmost importance, I solved all the questions given in the notes (whether solved or unsolved) multiple times in my registers. Besides that, I solved the questions of previous year papers provided by sir, again multiple times. I restricted my preparation upto this point. But if any student faces difficulty in understanding any particular topic or finds notes insufficient for it or wants to practise more, he/she can use any reference book for any particular topic which can easily be found on internet or available in market.

But again a word of caution, try to limit your preparation to the concepts relevant to the syllabus and don't delve into unnecessary theorems or proofs otherwise its a slippery slope to a massive ocean. We tend to skip the proofs of various theorems provided in the syllabus while studying them as they are of not much use. Proofs of theorems are generally not asked in the exams. But still I used to go through each and every proof in a brief manner provided in the notes. The reason being it would give me a better insight of the topic and often helped in me developing solutions of questions.

Test Series:

No optional is complete without writing a test series and it holds true in Maths also. Test Series is as important in your preparation as your notes + books. Firstly, Test Series is