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**Note :** The chapter 1 of Unit-I, chapter 1 of Unit-II and two chapters of Unit-III of this book are not in the syllabus of C.C.S. University, Meerut. The chapters 2 to 9 cover the syllabus of Unit I and the chapters 2 to 7 of Unit-II cover the syllabus of Unit II.