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Regional Office: H.No. 1-10-237, 2nd Floor, Room No. 202 R.K.'s Kancham's Blue Sapphire Ashok Nagar, Hyderabad-20. Ph: 9652351152, 9652661152

MAINS TEST SERIES-2018

• (JUNE-2018 to SEPT.-2018) •

IAS/IFoS MATHEMATICS

Under the guidance of K. VENKANNA

PAPER - I : LINEAR ALGEBRA, CALCULUS & 3D

TEST CODE: TEST-01: IAS(M)/10-JUNE-2018

Time: Three Hours

Maximum Marks: 250

INSTRUCTIONS

Each question is printed only in English.

Answer must be written in the medium specified in the admission Certificate issued to you, which must be stated clearly on the cover of the answer-book in the space provided for the purpose. No marks will be given for the answers written in a medium other than that specified in the Admission Certificate.

Candidates should attempt Question Nos. 1 and 5, which are compulsory, and any THREE of the remaining questions selecting at least ONE question from each Section.

The number of marks carried by each question is indicated at the end of the question.

Assume suitable data if considered necessary and indicate the same clearly.

Symbols/notations carry their usual meanings, unless otherwise indicated.

All questions carry equal marks.

Important Note: Whenever a question is being attempted, all its parts/ sub-parts must be attempted contiguously. This means that before moving on to the next question to be attempted, candidates must finish attempting all parts/ sub-parts of the previous question attempted. This is to be strictly followed.

Pages left blank in the answer-book are to be clearly struck out in ink. Any answers that follow pages left blank may not be given credit.



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SECTION – A

1. (a) (i) Let V be a vector space over K . Show that, if for $\alpha \in K$ and $x \in V$, $\alpha x = x$ then $\alpha = 1$ or $x = 0$.
(ii) Let V be a vector space over \mathbb{C} . Define another scalar multiplication $*$ on V : $\alpha * x = \operatorname{Re}(\alpha)x$, $\alpha \in \mathbb{C}, x \in V$, where $\operatorname{Re}(\alpha)$ is the real part of α . Is V a vector space with respect to original addition and scalar multiplication $*$? [10]
 1. (b) Suppose U and W are two-dimensional subspaces of \mathbb{R}^3 . Show that $U \cap W \neq \{0\}$. In particular, find the possible dimensions of $U \cap W$. [10]
 1. (c) Show that the height of the cylinder of maximum volume that can be inscribed in a sphere of radius a is $2a/\sqrt{3}$. [10]
 1. (d) Find the volume of the region in \mathbb{R}^3 bounded by the paraboloids with equations $z = 10 - x^2 - y^2$ and $z = x^2 + y^2 - 8$. [10]
 1. (e) Find the angle between the diagonals of a cube. [10]
- 2.(a)(i)** (a) Let $A = \begin{pmatrix} 2 & 2 \\ 1 & 3 \end{pmatrix}$. Is A diagonalizable? If yes, find P such that $P^{-1}AP$ is diagonal.
(b) If interchanging the eigenvectors of P , does P still diagonalize A ?
- 2.(a)(ii)** Show that no skew-symmetric matrix can be of rank 1. [12+8=20]
- 2. (b)** Prove that the function

$$f(x, y) = \sqrt{|xy|}$$

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OUR ACHIEVEMENTS IN IFoS (FROM 2008 TO 2017)

OUR RANKERS AMONG TOP 10 IN IFoS

PRATAP SINGH AIR-01 IFoS-2015	PRATEEK JAIN AIR-03 IFoS-2016	SIDDHARTHA GUPTA AIR-03 IFoS-2014	VARUN GUNTUPALLI AIR-04 IFoS-2014	TEWANG GYALTSON AIR-04 IFoS-2010	DESHAL DAN AIR-05 IFoS-2017
PARTH JAISWAL AIR-05 IFoS-2014	HIMANSHU GUPTA AIR-05 IFoS-2011	ASHISH REDDY MV AIR-06 IFoS-2015	ANUPAM SHUKLA AIR-07 IFoS-2012	HARSHVARDHAN AIR-10 IFoS-2017	

P.V.S. REDDY AIR-22 IFoS-2017	PRakash GUPTA AIR-23 IFoS-2017	SUNNY K. SINGH AIR-24 IFoS-2017	SITANSHU PANDEY AIR-25 IFoS-2017	G. ROHITH AIR-30 IFoS-2017	SUNEEL SHEORAN AIR-36 IFoS-2017	VASU DUGAR AIR-40 IFoS-2017	SACHIN GUPTA AIR-45 IFoS-2017	ANKIT KUMAR AIR-51 IFoS-2017	ROSHAN CARR AIR-58 IFoS-2017	RAHUL KR. JADAV AIR-68 IFoS-2017	PRINCE KUMAR AIR-80 IFoS-2017
DHARMYKEER DAIRU AIR-93 IFoS-2017	NAVNEET ASRARWALI AIR-21 IFoS-2016	PAKWAJ VERMA AIR-22 IFoS-2016	AIR-23 IFoS-2016	AIR-30 IFoS-2016	AIR-31 IFoS-2016	AIR-29 IFoS-2016	AIR-32 IFoS-2016	AIR-36 IFoS-2016	AIR-48 IFoS-2016	AIR-57 IFoS-2016	AIR-58 IFoS-2016
SANGEETA MAHALA AIR-68 IFoS-2016	PUNEET SONKAR AIR-98 IFoS-2016	HIMANSHU P. AIR-108 IFoS-2016	SHUDHARTHA JAIN AIR-13 IFoS-2015	AKSHAY GODARA AIR-15 IFoS-2015	MANISHA RANA AIR-19 IFoS-2015	RAJEEV RANJAN AIR-29 IFoS-2015	VILAY SHANKAR P. AIR-30 IFoS-2015	MD. ADIL ASHRAF AIR-48 IFoS-2015	MAHATIM YADAV AIR-62 IFoS-2015	KUNAL DHADWAT AIR-67 IFoS-2015	RAVI KUMAR AIR-72 IFoS-2015
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NITISH KUMAR AIR-39 IFoS-2013	NAVIN P. SHARYA AIR-72 IFoS-2013	ABID QAYUM AIR-32 IFoS-2012	DILIP K. YADAV AIR-48 IFoS-2012	RAJESH KUMAR AIR-72 IFoS-2012	TIRUMALA RAYKRISHNA AIR-11 IFoS-2011	JAI YADAV AIR-36 IFoS-2010	VILAYA BATRE AIR-80 IFoS-2010	SHAMBHU KUMAR AIR-23 IFoS-2009	SUSHEEL KUMAR UP-PCS 2011		

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OUR TOPPER'S MARKS LIST (IAS/IFoS)

- For your final selection, optional subject marks are crucial.
- Choose Optional Subject Based on Your Graduation Studies & Score Highest Marks.
- Now Mathematics has become one of the most Cherished Optional Paper among Science Graduates, especially Students with Mathematics background including B.Tech.
- In the new pattern of exam, the average marks of successful candidates in Maths is more than 274 out of 500.
- Mathematics (Opt.) has proven to be the Most Reliable and High Scoring Subject in IAS/IFoS.
- IMS has been successfully providing consistent results since its inception.

MARKS ARE BEFORE YOU AND YOU SHOULD ANALYZE YOURSELF

RANK	NAME	RANK IN IAS-2017	SUBJECT	Max. Marks.		Marks Obtained								
				ESSAY (PAPER-I)	GENERAL STUDIES-I (PAPER-II)	GENERAL STUDIES-II (PAPER-III)	GENERAL STUDIES-III (PAPER-IV)	GENERAL STUDIES-IV (PAPER-V)	OPTIONAL-I (MATHEMATICS) (PAPER-VI)	OPTIONAL-II (MATHEMATICS) (PAPER-VII)	WRITTEN TOTAL	PERSONALITY TEST	TOTAL FINAL	
ATUL PRAKASH		AIR-04	SUBJECT	250	139	250	105	250	106	250	126	250	98	368/500
SAGAR KUMAR		AIR-13	SUBJECT	250	151	250	119	250	121	250	143	250	99	299/500
SUNNY K SINGH		AIR-91	SUBJECT	250	146	250	113	250	117	250	150	250	97	268/500
MANISH KR. SHANDILYA		AIR-138	SUBJECT	250	150	250	98	250	93	250	128	250	98	334/500
ARCHIT CHANDAK		AIR-184	SUBJECT	250	129	250	95	250	115	250	118	250	102	307/500
			SUBJECT	ESSAY (PAPER-I)	GENERAL STUDIES-I (PAPER-II)	GENERAL STUDIES-II (PAPER-III)	GENERAL STUDIES-III (PAPER-IV)	GENERAL STUDIES-IV (PAPER-V)	OPTIONAL-I (MATHEMATICS) (PAPER-VI)	OPTIONAL-II (MATHEMATICS) (PAPER-VII)	WRITTEN TOTAL	PERSONALITY TEST	TOTAL FINAL	
ANUBHAV SINGH		AIR-08	SUBJECT	250	155	250	92	250	107	250	129	250	81	375/500
PRATEEK JAIN		AIR-86	SUBJECT	250	137	250	117	250	125	250	127	250	101	285/500
RAHUL SINDHE		AIR-95	SUBJECT	250	150	250	94	250	101	250	133	250	94	290/500
RAM PRAKASH		AIR-162	SUBJECT	250	135	250	99	250	101	250	125	250	99	331/500
HARSHA VARDAN		AIR-213	SUBJECT	250	139	250	103	250	115	250	119	250	98	304/500

is not differentiable at the point $(0, 0)$, but that f_x and f_y both exist at the origin and have the value 0. Hence deduce that these two partial derivatives are continuous except at the origin. [15]

- (c) A cone has as base the circle $x^2 + y^2 + 2ax + 2by = 0$, $z = 0$ and passes through the fixed point $(0, 0, c)$. If the section of the cone by zx -plane is a rectangular hyperbola, prove that the vertex lies on a fixed circle. [15]
- (a) In C^3 , let $\alpha_1 = (1, 0, -i)$, $\alpha_2 = (1+i, 1-i, 1)$, $\alpha_3 = (i, i, i)$. Prove that these vectors form a basis for C^3 . What are the coordinates of the vector (a, b, c) in this basis? [08]
- (b) Let $U = \text{span}(u_1, u_2, u_3)$ and $W = \text{span}(v_1, v_2)$ be subspaces of \mathbf{R}^4 where $u_1 = (1, 2, -1, 3)$, $u_2 = (2, 4, 1, -2)$, $u_3 = (3, 6, 3, -7)$, $v_1 = (1, 2, -4, 11)$, $v_2 = (2, 4, -5, 14)$. Show that $U = W$. [07]
- (c) The ellipsoid with equation $x^2 + 2y^2 + z^2 = 4$ is heated so that its temperature at (x, y, z) is given by $T(x, y, z) = 70 + 10(x - z)$. find the hottest and coldest points on the ellipsoid. [15]
- (d) (i) A variable plane, which remains at a constant distance p from the origin, cuts the coordinate axes at A, B, and C. Show that the locus of the centroid of ΔABC is $x^2 + y^2 + z^2 = 9p^2$.
(ii) Find the S. D. between lines

$$\frac{x-3}{3} = \frac{y-8}{-1} = \frac{z-3}{1} \quad \text{and} \quad \frac{x+3}{-3} = \frac{y+7}{2} = \frac{z-6}{4}$$

Find also its equations and the points in which it meets the given lines. [8+12 = 20]

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4. (a) Let V be a subspace of \mathbb{R}^5 generated by

$$v_1 = \begin{bmatrix} 1 \\ 3 \\ -2 \\ 2 \\ 3 \end{bmatrix}, v_2 = \begin{bmatrix} 2 \\ 7 \\ -5 \\ 6 \\ 5 \end{bmatrix}, v_3 = \begin{bmatrix} 3 \\ 6 \\ -3 \\ 0 \\ 13 \end{bmatrix}$$

and let W be a subspace generated by

$$w_1 = \begin{bmatrix} 1 \\ 3 \\ 0 \\ 2 \\ 1 \end{bmatrix}, w_2 = \begin{bmatrix} 5 \\ 16 \\ -3 \\ 12 \\ 6 \end{bmatrix}, w_3 = \begin{bmatrix} 3 \\ 8 \\ 3 \\ 4 \\ 2 \end{bmatrix}$$

find a basis for $V + W$ and for $V \cap W$.

[15]

4. (b) Evaluate $\lim_{x \rightarrow 0} \left(\frac{1}{x^2} - \frac{1}{\sin^2 x} \right)$

[10]

4. (c) Evaluate $\int_0^{\pi/2} \frac{\sin^2 x}{\sin x + \cos x} dx$

[10]

4. (d) Prove that the enveloping cylinder of the ellipsoid $(x^2/a^2) + (y^2/b^2) + (z^2/c^2) = 1$ whose generators are parallel to the line

$$\frac{x}{0} = \frac{y}{\pm\sqrt{(a^2 - b^2)}} = \frac{z}{c}$$

meet the plane $z = 0$ in circles.

[15]

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2. Don't read Maths book / notes like GS. It is a recipe for disaster. Rather always study with pen, paper and calculator.
3. While solving examples don't jump to see solution first. Try giving your best shot and after making sure that you are not able to solve it using your present knowledge then only look at the answer. This will ensure that better retention.
4. Generally we make lots of silly mistakes while solving a question. It is best to catch these errors early and not repeat them in exam hall. The best strategy for this is to maintain a notebook of errors that you

Anyone who has done B.Tech / M.Tech / B.Sc / M.Sc and has an interest in Maths.

Usually commit and their mitigation measures. For example, I commit a lot of mistakes when doing Integration by parts and usually the error involves missing negative (-) sign etc. Therefore whenever I come across such type of question I try to devote extra 1 minute to re-check all my steps.

Maths.stackexchange.com is the best online resource for preparation. You can create an account and get your maths questions answered within minutes.

Why did I score only 262?

Among all the students in the final list who had Maths as an optional, I have scored the least. My paper - 1 was a complete disaster and I only scored 92 marks in it. In fact I could only attempt 160 marks paper and had to leave 90 marks paper completely.

The reasons for the above situation in Paper - 1 are as follows:

1. **Lack of written practice:** In many topics (especially statics and dynamics) I used to just look at a question and its solution without solving it first. As a result I forgot the exact method in the exam hall!
2. **Left many topics:** I prepared only 25% 3-D, 80% Calculus and 25% Statics & Dynamics and had to pay a heavy price in the exam.

On the other hand my preparation for paper - 2 was excellent and therefore I scored an amazing 170 marks in it

BHAVESH MISHRA
AIR-58 in CSE-2014

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make it to the final list. This year one of my batch mate in IMS **Nitish K (Rank 8)** has got a mind boggling 346 marks.

Certainty: If you have attempted your paper well then you are sure that you will get good marks. For example this year just by attempting 400 marks paper you could get a decent 260+ marks. Even if you don't get good marks in first attempt but you can be sure that you will increase your marks in subsequent attempt(s).

Fun: Mathematics is a delightful subject and therefore doing maths takes you away from somewhat boring humanities.

Good Impression: The fact that you have taken Maths makes a good impression on interview board members

(it happened in my case !). They are very pleased to see that you have opted for a tough optional.

Easy paper: The difficulty level of paper is quite moderate and almost all questions are directly picked from the IMS Test Series / Standard Textbooks.

WHO SHOULD TAKE IT?

Myths around science subjects.

Coaching institutions have mastered the art of brainwashing students and creating an atmosphere of gloom and doom around science subjects. There are lots of myths circulating among students. Let's bust these myths.

- Maths optional is only for students from IITs: Definitely not.** Anyone willing to put in hard work can easily score very high marks. The best example being **Nitish K (Rank 8) who is not from any IIT.**
- There is heavy scaling:** Let the data speak for itself. I attempted 240 marks in Paper 2 and got 170 marks. Now would you call it a scaling?
- It plays no role in GS:** Yes it's true that science optional subjects don't overlap with GS but it's equally true that GS has never been a rank decider in UPSC IAS.
- There are 3 major things that decides your rank:** Essay, Optional and Interview. Even if one puts in 5 years of efforts in GS the advantage in terms of marks would be around 30 marks or so but 1 year of dedicated effort in maths would give you 50+ marks advantage straightforwardly.

Do's and Don'ts:

- Practice, Practice and Practice. The key to success in maths is filling up as many notebooks as you can, during the preparation stage. The more you sweat during preparation the less you will bleed in the battlefield!

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SECTION - B

5. (a) Let $a = \begin{bmatrix} 0 \\ 1 \\ -1 \end{bmatrix}$, $b = \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix}$, $c = \begin{bmatrix} -1 \\ 1 \\ 0 \end{bmatrix}$ and $d = \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}$ be vectors in \mathbb{R}^3 .

Let $W_1 = \langle a, b \rangle$, $W_2 = \langle b, c \rangle$ and $W_3 = \langle c, d \rangle$. Show that $W_2 = W_3$, $W_1 \cap W_2 = \langle b \rangle$. Also identify the subspace $W_1 + W_2$. Is $W_1 \cup W_2$ a subspace of \mathbb{R}^3 ? [10]

5. (b) What condition must be placed on a, b, and c so that the following system in unknowns x, y and z has a solution ?

$$\begin{aligned} x + 2y - 3z &= a \\ 2x + 6y - 11z &= b \\ x - 2y + 7z &= c \end{aligned}$$

[10]

5. (c) Test the convergence of the integral $\int_1^2 \frac{dx}{\sqrt{x^4 - 1}}$. [10]

5. (d) Show that $\frac{a}{y-z} + \frac{b}{z-x} + \frac{c}{x-y} = 0$ represents a pair of planes. Find angle between them also. [10]

5. (e) Find the equation of the sphere for which the circle $x^2 + y^2 + z^2 + 7y - 2z + 2 = 0$, $2x + 3y + 4z = 8$ is a great circle. [10]

6. (a) Let $\alpha_1 = (1, 1, -2, 1)$, $\alpha_2 = (3, 0, 4, -1)$, $\alpha_3 = (-1, 2, 5, 2)$. Let $\alpha = (4, -5, 9, -7)$, $\beta = (3, 1, -4, 4)$, $\gamma = (-1, 1, 0, 1)$.

- (i) which of the vectors α , β , γ are in the subspace of \mathbb{R}^4 spanned by the α_i ?
(ii) which of the vectors α , β , γ are in the subspace of \mathbb{C}^4 spanned by the α_i ?

- (iii) Does this suggest a theorem ? [15]

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6. (b) Let $T : \mathbf{R}^3 \rightarrow \mathbf{R}^2$ be the linear transformation defined by

$$T(x_1, x_2, x_3) = (x_1 + x_2, 2x_3 - x_1).$$

If $\beta = \{(1, 0, -1), (1, 1, 1), (1, 0, 0)\}$ and $\beta' = \{(1, 0), (0, 1)\}$ be ordered basis of \mathbf{R}^3 and \mathbf{R}^2 , respectively, then find the matrix of T relative to β, β' . Also find rank and nullity [10]

6. (c) (i) Show that the real field \mathbf{R} is a vector space of infinite dimension over the rational field \mathbf{Q} .
(ii) Let V be the vector space of ordered pairs of complex numbers over the real field \mathbf{R} . Show that V is of dimension 4. [12]

6. (d) If \mathbf{H} is any Hermitian matrix, then

$$\mathbf{A} = (\mathbf{H} + i\mathbf{I})^{-1} (\mathbf{H} - i\mathbf{I}) = (\mathbf{H} - i\mathbf{I}) (\mathbf{H} + i\mathbf{I})^{-1}$$

is unitary and every unitary matrix can be thus expressed provided, -1 , is not a characteristic root of \mathbf{A} . [13]

7. (a) By using the transformation $x + y = u, y = uv$, prove that $\int \{xy(1-x-y)\}^{1/2} dx dy$ taken over the area of the triangle bounded by lines $x = 0, y = 0, x + y = 1$ is $\frac{2\pi}{105}$. [12]

7. (b) A farmer wishes to build a rectangular bin, with a top, to hold a volume of 1000 cubic meters. Find the dimensions of the bin that will minimize the amount of material needed in its construction. [15]

7. (c) If $u = \tan^{-1} \frac{x^3 + y^3}{x - y}, x \neq y$ show that

$$x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2} = (1 - 4\sin^2 u) \sin 2u. \quad [10]$$

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you are expecting from this optional. The habit of writing such detailed answers will not develop overnight and hence you have to consciously work through the test series in this direction.

DURING MAINS

The mains exam schedule does not provide much gap between General Studies & Maths papers. You will generally have 1 day in between. Your notebook containing important formulae & theorems will be very useful at such times. You will be able to go through this summary of each chapter and it will provide much needed confidence before the actual paper. During the main exam, I would advise completing the compulsory questions 1 & 5 first. Then you can choose 3 out of remaining 6 questions. Easier questions like those from topics like linear programming, numerical analysis, linear algebra etc. should be the priority. Even if you don't know the complete answer to any question, write as many steps as you can since partial marks also matter. Once you finish paper 1, don't start immediately analyzing your performance. Irrespective of whether you are very happy or deeply unsatisfied about paper 1, try to forget about it and stay calm for paper 2.

INTERVIEW

In the interview, you can expect some questions related to mathematics optional. Generally you won't be asked to solve a problem because that ability has been tested in mains. They would like to see whether you have a genuine curiosity regarding mathematics outside what is mentioned in syllabus. In both my UPSC interviews, I was asked about Ramanujan's work. There were questions on Vedic Mathematics, National Mathematics Day, important Indian Mathematical Institutions, Field medalist Manjula Bhargava etc. Hence while preparing for interview, try to be aware about these non-theoretical aspects of maths as well.

*I hope above tips provide some clarity regarding maths optional to UPSC aspirants.
All the best!*

BHAVESH MISHRA (AIR-58)

**in IAS-2014 Examination
CLASSROOM STUDENT**

Why Maths?

Simply because it is the best performing optional subject in UPSC/IAS.

Extremely high scoring: If you get your maths optional right then you will

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didn't have to spend time scanning reference books for relevant material. Venkanna Sir's classroom coaching helped me in completing the syllabus in a disciplined manner. Initially I would underline important theorems, formulae, results mentioned in the notes. Then i used to compile them in a notebook and this was useful for revision. So eventually i had a notebook with just the crux of the matter. I would advise all candidates with maths optional to prepare such a summary for all topics. Due to large syllabus, there is a natural tendency to skip a few chapters. But for the sake of compulsory questions, it is necessary to know at least basics of each chapter. The physics related chapters of statics, dynamics, mechanics are generally left untouched while preparing maths optional. Regarding these chapters, my preparation was such that i would be able to solve the compulsory 10 mark questions. They are quite manageable once you know the basic theory and there is no point in unnecessarily losing marks. The real analysis/calculus & modern algebra chapters are time consuming but candidates can't afford to skip them.

PRACTICE

Just knowing theory is not enough. It needs to be accompanied by consistent problem solving practice. It is best to solve questions that have already been asked in mains. If some problem seems very non-intuitive, it would help if the trick to solve such problem is written in your notebook.

TEST SERIES

Test series is very important for this optional. I had joined IMS test series which helped me in identifying my weak areas. In both CSE and IIT-JEE mains, there were many questions similar to those covered in IMS test series. With enough practice, a candidate can achieve the ability to complete the maths paper in 3 hours. It is important to assess your performance after each test. Necessary steps should be taken to rectify common mistakes that you are committing in the test series. You should be alert not to repeat the same mistakes again & again. As your performance improves with every test, the actual mains paper will seem just like any other test & you will be able to comfortably complete it. Presentation of your answer matters a lot. Your aim should be to make examiner's life as easy as possible so that he/she will award you maximum marks. Only the final answer doesn't matter. Writing proper steps is also important to show the logical flow with which you arrived at the solution. Specifically mention whichever theorem or property you are using in a particular step. Wherever possible, draw neat diagrams with proper labelling. Such small things will collectively fetch you the extra marks that

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$$7. \text{ (d) If } f(x,y) = \begin{cases} \frac{xy}{x^2 + y^2}, & (x,y) \neq (0,0) \\ 0, & (x,y) = (0,0) \end{cases}$$

show that both the partial derivatives exist at (0, 0) but the function is not continuous there at. [13]

8. (a) If the feet of the three normals from P to the ellipsoid $x^2/a^2 + y^2/b^2 + z^2/c^2 = 1$ lie on the plane $x/a + y/b + z/c = 1$ prove that the feet of the other three lie on the plane $x/a + y/b + z/c + 1 = 0$ and P lies on the line $a(b^2 - c^2)x = b(c^2 - a^2)y = c(a^2 - b^2)z$. [15]
8. (b) If A and A' are the extremities of the major axis of the principal elliptic section and any generator meets two generators of the same system through A and A' in P and P' respectively, then prove that $AP \cdot A'P' = b^2 + c^2$ [15]
8. (c) Prove that $z(ax + by + cz) + \alpha x + \beta y = 0$ represents paraboloid and the equations to the axis are $ax + by + 2cz = 0, (a^2 + b^2)z + \alpha\alpha + b\beta = 0$. [20]

PREPARATION STRATEGY

for IAS/IFoS

MATHEMATICS

(Optional)

by Successful Candidate

DIPESH MALHOTRA

AIR-30 in IFoS-2016

CLASSROOM STUDENT

Hello Everyone I am Dipesh Malhotra. I have done my B.Tech in Civil Engineering from IIT Roorkee. I have given Civil Services Exam and Forest Service Exam, 2016. I have got AIR 30 in Indian Forest Service Exam and waiting for my final result of CSE, 2016. I have taken coaching through classroom programme of IMS under the guidance of K. Venkanna Sir.

Why Mathematics? Mathematics optional has few myths attached to it:-

- It suits people from IITs only.
- It has a very vast syllabus.
- There is a huge scaling against it.
- It affects your G.S. preparation.

So, let me first breakdown these myths to help you make a informed decision regarding optional. Results of last years show that many people from non-IIT institutes are able to get very good marks in Maths. Most prominent among them is Rank-08 Nitish K. Maths optional requires temperance, hardwork and concentration in terms of preparation and not extra-ordinary intelligence. That's why clearing IIT-JEE and CSE is a very different game altogether. So, its more of a psychological thing rather than a meaningful idea.

Comparing the level of syllabus with social sciences/ humanities syllabus gives a partial picture of the relative length. Every chapter may seem very lengthy in maths but that is the only limited part that one has to study for maths. On the other hand for humanities optional you have to study many other things not mentioned in syllabus creating two types of problem (a) Uncertainty and (b) Increased burden. So, in my opinion maths is one of the safe optional given the kind of result and uncertainty that

KUMBHEJKAR YOGESH VIJAY

(AIR-13 IFoS) & (AIR-143 IAS)

in IFoS-2014 & IAS-2014 Examinations

CLASSROOM STUDENT

MY BACKGROUND

I am Yogesh Kumbhejkar. I am an Electrical Engineer from IIT Bombay. I secured AIR 13 in Indian Forest Service Exam (IFoS) 2014 with Mathematics & Physics as the optional subjects. For Civil Service Exam (CSE) also, my optional is Mathematics. In IFoS exam, I scored 231/400 (118 + 113) in maths. In 2013 CSE Mains, my maths score was 250/500 (109 + 141). Hence mathematics has helped me in clearing mains in both CSE and IFoS. I was not selected in the final list of CSE 2013. In my second CSE attempt also I appeared for mains in 2014 with Maths as the optional subject. Now i am awaiting the Mains result. This article is a humble attempt to share my experience of maths optional preparation for CSE/IFoS exam. I would be glad if it helps any UPSC aspirant who is undecided about choosing the optional or those who are already preparing with mathematics as their optional.

WHY MATHEMATICS

It is very important for a UPSC aspirant to have genuine interest in mathematics if he/she wants to choose this optional. Maths used to be my favourite subject in school and in IITB also I had pursued additional courses in mathematics out of interest. Since the syllabus is large & requires considerable practice, it is necessary to have a genuine interest. Apart from my inherent inclination, this optional offers certain advantages which made it an obvious choice. In this optional, the marks you get are almost proportional to your efforts. With proper hard work, a candidate can comfortably attempt all the questions in exam and expect to score around 50% marks even after heavy scaling which can offer the necessary edge in this intense competition. Such candidate generally would not find any question surprising in mains. This kind of certainty is not present in humanities optionals.

THE SYLLABUS

The prescribed syllabus for maths is quite large which makes it necessary to stick to limited sources. I relied on notes provided by Venkanna Sir at IMS for covering the syllabus. Since these notes were very comprehensive, I

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Besides that, I solved the questions of previous year papers provided by sir, again multiple times. I restricted my preparation upto this point. But if any student faces difficulty in understanding any particular topic or finds notes insufficient for it or wants to practise more, he/she can use any reference book for any particular topic which can easily be found on internet or available in market.

But again a word of caution, try to limit your preparation to the concepts relevant to the syllabus and don't delve into unnecessary theorems or proofs otherwise its a slippery slope to a massive ocean. We tend to skip the proofs of various theorems provided in the syllabus while studying them as they are of not much use. Proofs of theorems are generally not asked in the exams. But still I used to go through each and every proof in a brief manner provided in the notes. The reason being it would give me a better insight of the topic and often helped in me developing solutions of questions.

Test Series:

No optional is complete without writing a test series and it holds true in Maths also. Test Series is as important in your preparation as your notes + books. Firstly, Test Series is the best mode of judging your preparation. You can fairly evaluate your performance with your marks and then focus on the weak topics. Secondly, its a rehearsal of Mains Exam and thus helps you greatly in time management.

Mains exam is nearly a marathon for your hand and thus you get very much trained for facing them. Test Series also provided me another pool of questions to practise. They also helped in developing the ability of answer writing which definitely can't be developed overnight. I attended Test Series of IMS and luckily many questions of Test Series appeared in both IFoS Exam and CSE. I would also request all the candidates to give the test series by coming to classroom if possible and stick to the timelines as it really helps in completion of syllabus.

I hope this writeup clears some of the doubts and gives clarity on maths optional to UPSC IAS aspirants. All the Best

If anyone wants to contact me, please drop me an email -
parthjaiswal512@gmail.com. I will be more than happy to help you.

Thank You

Parth Jaiswal

AIR-5 in IFoS-2014,
AIR-299 in CSE-2014

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surrounds other optionals.

Scaling is a scientific statistical tool used by UPSC to bring different optional on a same level playing field. However, when raw checking of answer sheets of different optional are done marks are awarded in an objective manner.

Therefore, marks in science optional especially mathematics would come out to be very high as around 90% of marks are awarded for right answer. Humanities answers always have subjectivity attached to them. Therefore, they get around 50-60% marks for correct attempt. Scaling causes 15-20% lowering of low marks that still makes maths to retain enviable position in marks tally.

There is a very big misconception in preparation circles that optional helps you in G.S. (General Studies) preparation. G.S. answers require a very different approach in terms of diversity and multi-dimensionality. Optional knowledge can be used as a foot-note and not as a main theme of a G.S. answer. Given, the changing nature of prelims and mains G.S. papers, knowledge of humanities optional is not going to help in future. So, in my opinion maths can give you better opportunity in terms of marks and certainty to clean the exam.

WHAT SHOULD BE THE STRATEGY OF PREPARATION?

Mathematics require large amount of practice, clarity and revision. Given the limited nature of sources and syllabus this seems to be a easy task. But it is easier said than done. So, in order to bring clarity one needs to be very through with the concepts and fundamentals. For this I would recommend IMS classroom programme and notes prepared by venkanna Sir. It will make your preparation easy and focused as different topics are available at one place and in a more exam focused manner. Venkanna Sir in a very student friendly manner that makes you very comfortable in that environment and helps to clear doubts. After that you can go for certain basic books for practice and some specific set of problems. But those things are also guided well by Sir himself.

For practice purpose various tutorial sheets provided by institute are very helpful. At the same time it should be kept in mind all the concepts and problems from IMS should be practiced first hand and then go for books. Test series by IMS helps in revision and practice as all the books problems and previous year questions are prepared and covered well. So, few basic points are very important:-

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1. Continuous preparation from first.
2. Revision and practice of those notes.
3. Some specific and typical problems from books.
4. IMS Test series.
5. Formulae sheet notes to be used before exam and tests.

For preparation chronology I would recommend going for easy and scoring topics first like ordinary differential equations, partial differential equations, linear algebra, vectors, numerical analysis, complex analysis, LPP etc. Some topics like statics and dynamics as well as mechanics have to be prepared thoroughly given the changing nature of exam. For them go for all previous year questions and basic concepts.

Do not try to go into very deep physics as ultimate aim is to score well and not to become a physicist. At the end of preparation and near the exam, one faces problem of revision – So, I would recommend following points:–

1. Summary of chapters
2. Formulae sheets.
3. Test Series.

Reason I am stressing on test series are following:–

1. It helps to get into touch with all type of problems
2. Give an idea relating to format of presentation in exam.
3. Real-time and real-exam simulation to get an experience to handle stress.

Habit of writing well will not develop overnight. So, constant grilling before exam is required.

PARTH JAISWAL

(AIR-5 IFoS) & (AIR-299 IAS)

in IFoS-2014 & IAS-2014 Examinations

CLASSROOM STUDENT

MY BACKGROUND

Hello, My name is Parth Jaiswal. I come from Jaipur, Rajasthan. I completed my graduation in Computer Science discipline from IIT Delhi in 2013. Soon afterwards I started preparing for Civil services and Indian Forest Service, aiming for the attempt of year 2014.

Luckily I was able to clear both the examinations in my first attempt. I

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secured AIR-5 in IFoS-2014 and AIR-299 in CSE-2014. My optional subject was Mathematics. In case of Forest Service Examination, candidate is required to choose 2 Optionals, thus my second optional was Forestry with Mathematics as my first optional. I secured 250/400 (125+125) marks in IFoS Exam and 300/500 (147+153) marks in CSE in Maths. Thus I would give much credit for my success to my correct choice of optional as well as performance in it. I am writing this to share my experience with Maths as an optional subject and would feel happy if I am able to clear some of the doubts as well as apprehensions regarding it which many UPSC aspirants possess.

Why I Chose Mathematics?

I chose **Mathematics** because of my inherent interest in it from childhood. I have performed well in this in my throughout education and thus was confident enough to handle it well. Another reason for choosing it was, I wanted to have my optional from my background and thus Maths proved to be appropriate choice. Having a science background, I found it much easier to study than any other subject, many of which we have to study for GS prep. I would like to assert few points regarding it very clearly.

- This subject is vast in syllabus and takes more time to study than other optionals.
- It also requires consistent practise. But the positive part is - If you are thorough with the subject and have practised it well, you can comfortably attempt complete paper with correct answers and thus gives you a great opportunity to score well in your optional (inspite of the scaling often carried out in it) pushing you above the list.
- In this way, this optional gives a bit of security as well as certainty which again comes at a price i.e great amount of hard work. Also IFoS Exam prescribes certain optionals only and Mathematics is one of them. Not all optionals are available for this exam.
- So again it gives you the flexibility of giving IFoS Exam.

From where to study?

I attended classroom coaching of IMS, Rajinder Nagar. I restricted my preparation to the handouts provided by Venkanna Sir. Because of the voluminous syllabus, it is necessary to gauge the point where you have to stop. I found that the notes quite comprehensive and provided me a holistic coverage of the syllabus in a highly structured manner. I believe that those notes are sufficient from the theory point of view.

For practising questions which is of utmost importance, I solved all the questions given in the notes (whether solved or unsolved) multiple times in my registers.