

stage game G

Linear Cournot oligopoly

$$A_i = (0, \infty)$$

$$q_i \in A_i \quad \text{memoryless} \quad p(Q) \leftarrow \sum_{j \in N} q_j$$

$$u_i(q) = q_i [\max \{1 - Q, 0\} - c]$$

infinitely repeated $G^{\infty, \delta}$

$$u_i(s) = \sum_{t=0}^T \delta^t u_i(s_t) \mid h \text{ is induced by } s$$

per-period profit when each firm produces q

stage utility from BR-ing to everyone else producing q

$$\pi(q) = q [\max \{1 - nq, 0\} - c]$$

$$g(q) = \max_{q'} q' [\max \{1 - (n-1)q - q', 0\} - c]$$

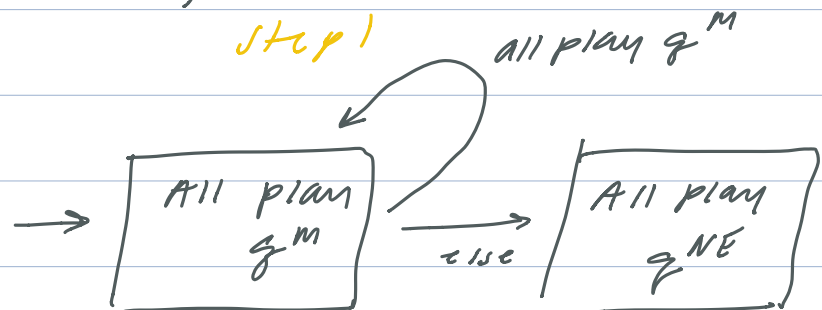
$$= \max \left\{ \frac{(1 - (n-1)q - c)^2}{4}, 0 \right\}$$

Grim Trigger to Nash

$s \rightarrow$

h_1, h_1, h_2, h_3

$1 - \delta + Q$



$$Q^m = \frac{1-c}{2}$$

$$q^m = \frac{1-c}{2n}$$

$$q^{NE} = \frac{1-c}{n+1}$$

STEP 2

Average
discounted value
 V

$$= (1-\delta) \underbrace{PV^m}_1 = f(q^m)$$

$$f(q^m) + \delta f(q^m) + \delta^2 f(q^m) + \dots$$

$$V^{NE} = f(q^{NE}) = g(q^{NE})$$

In each state, check deviation (one shot deviation)

↳ to check for subgame-perfect equilibria