

## src\arithmetic\_coder.py

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1 from fractions import Fraction
2 from collections import defaultdict
3 from bitarray import bitarray
4 import struct
5
6 def build_freqs(symbols):
7     # symbols: iterable of ints (0..7)
8     freq = [0]*8
9     for s in symbols:
10         freq[s] += 1
11     # ensure nonzero for stable CDF (add 1 to any zero freq)
12     for i in range(8):
13         if freq[i] == 0:
14             freq[i] = 1
15     total = sum(freq)
16     # cumulative
17     cdf = [0]*(len(freq)+1)
18     c = 0
19     for i,f in enumerate(freq):
20         cdf[i] = c
21         c += f
22     cdf[len(freq)] = c
23     return freq, cdf, total
24
25 def arithmetic_encode(symbols):
26     # Build freq model from symbols
27     freq, cdf, total = build_freqs(symbols)
28     # arithmetic encode using Fractions
29     low = Fraction(0,1)
30     high = Fraction(1,1)
31     for s in symbols:
32         range_ = high - low
33         high = low + range_ * Fraction(cdf[s+1], total)
34         low = low + range_ * Fraction(cdf[s], total)
35     # choose a binary fraction inside [low, high)
36     # produce bits by repeatedly doubling low until it >= high
37     bits = bitarray()
38     x = low
39     # produce enough bits: until x < high and either enough precision produced
40     # Stop when low and high have different binary prefixes
41     max_bits = 1024 # safety cap
42     while True:
43         if x >= 1:
44             bits.append(1)
45             x -= 1
46         else:
47             bits.append(0)
48         # advance low/high by doubling
49         low = low * 2
50         high = high * 2
51         if low >= 1:
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52         low -= 1
53     if high >= 1:
54         high -= 1
55     if len(bits) > 0:
56         # rebuild fractions represented by current bit sequence as binary fraction
57         # value_v is the rational represented by bits
58         value_v = Fraction(0,1)
59         pow2 = Fraction(1,1)
60         for b in bits:
61             pow2 *= 2
62             if b:
63                 value_v += Fraction(1, pow2)
64         # if value_v >= low and value_v < high then we can stop
65         if (value_v >= low) and (value_v < high):
66             break
67     if len(bits) >= max_bits:
68         break
69     # pack header (frequencies) as 8 uint32 little-endian
70     header = b''.join(struct.pack('<I', f) for f in freq)
71     # pack bit length as uint32 big-endian
72     bitlen = len(bits)
73     header2 = struct.pack('>I', bitlen)
74     # pack bits to bytes
75     bitbytes = bits.tobytes()
76     return header + header2 + bitbytes
77
78 def arithmetic_decode(blob):
79     import struct
80     # read 8*4 bytes freq header
81     if len(blob) < 8*4 + 4:
82         raise ValueError("Invalid encoded blob")
83     header = blob[:8*4]
84     freq = []
85     for i in range(8):
86         (f,) = struct.unpack('<I', header[i*4:(i+1)*4])
87         freq.append(f)
88     rest = blob[8*4:]
89     (bitlen,) = struct.unpack('>I', rest[:4])
90     bitbytes = rest[4:]
91     bits = bytearray()
92     bits.frombytes(bitbytes)
93     # trim to bitlen
94     bits = bits[:bitlen]
95     # build cdf
96     total = sum(freq)
97     cdf = [0]*(len(freq)+1)
98     c = 0
99     for i,f in enumerate(freq):
100         cdf[i] = c
101         c += f
102     cdf[len(freq)] = c
103     # reconstruct encoded_value fraction from bits
104     encoded_value = Fraction(0,1)
105     pow2 = Fraction(1,1)

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106     for b in bits:
107         pow2 *= 2
108         if b:
109             encoded_value += Fraction(1, pow2)
110     # decoding loop (Algorithm 2)
111     low = Fraction(0,1)
112     high = Fraction(1,1)
113     symbols = []
114     max_symbols = 1000000
115     for _ in range(max_symbols):
116         range_ = high - low
117         # compute scaled value = (encoded_value - low) / range_
118         scaled = (encoded_value - low) / range_
119         # find symbol j s.t. CDF(j) <= scaled*total < CDF(j+1)
120         # scaled is Fraction in [0,1)
121         target = scaled * total
122         # find j
123         j = None
124         for idx in range(len(freq)):
125             if target >= cdf[idx] and target < cdf[idx+1]:
126                 j = idx
127                 break
128         if j is None:
129             break
130         symbols.append(j)
131         # update interval
132         high = low + range_ * Fraction(cdf[j+1], total)
133         low = low + range_ * Fraction(cdf[j], total)
134         # termination heuristic: if low==high break
135         if high - low <= 0:
136             break
137         # If the decoded symbols so far, when encoded, would give an interval that
contains encoded_value,
138         # we continue until bit precision exhausted. We cap by bitlen.
139         # Stop condition: if we've decoded more symbols than some bound and the next
refinement gives no change, break.
140         if len(symbols) > 0 and len(symbols) > (bitlen*2):
141             break
142     return symbols

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