



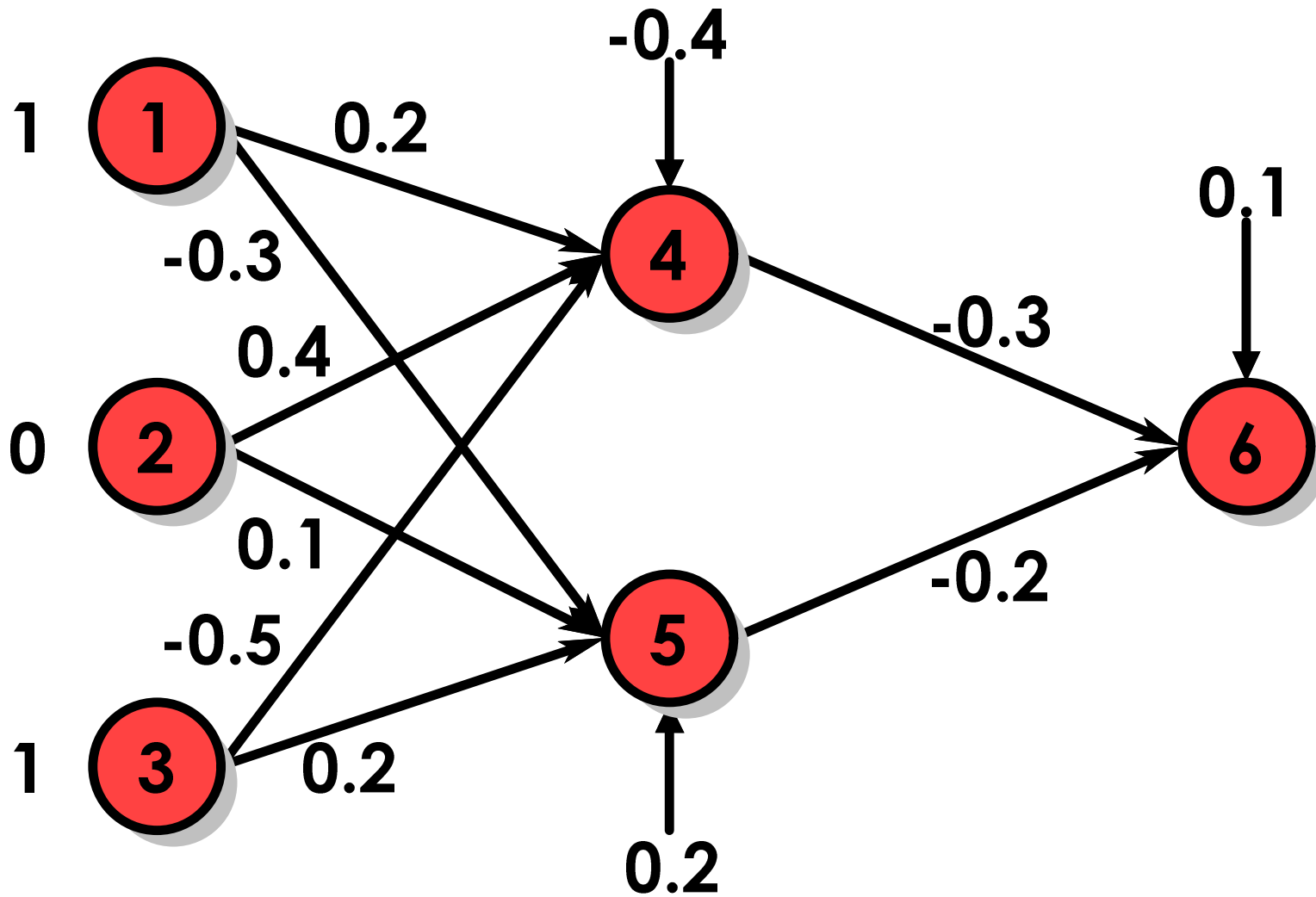
PEUVI  
FACULTAD DE CIENCIAS

UNIVERSIDAD NACIONAL AUTÓNOMA DE MÉXICO  
FACULTAD DE CIENCIAS  
DIPLOMADO EN MINERÍA DE DATOS

**Módulo 6.** *Minería de Datos*

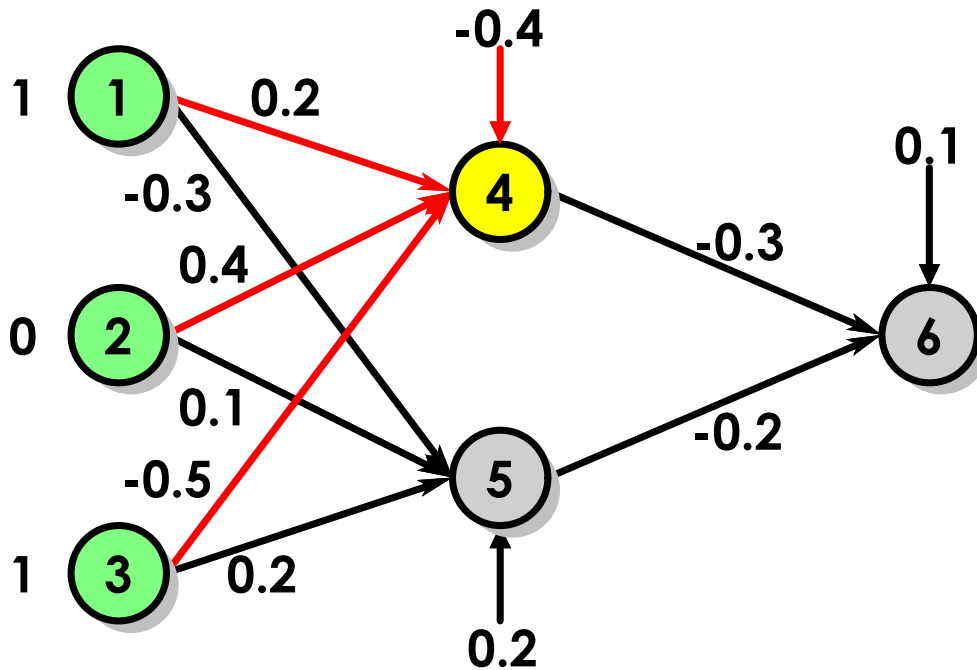
# Redes neuronales

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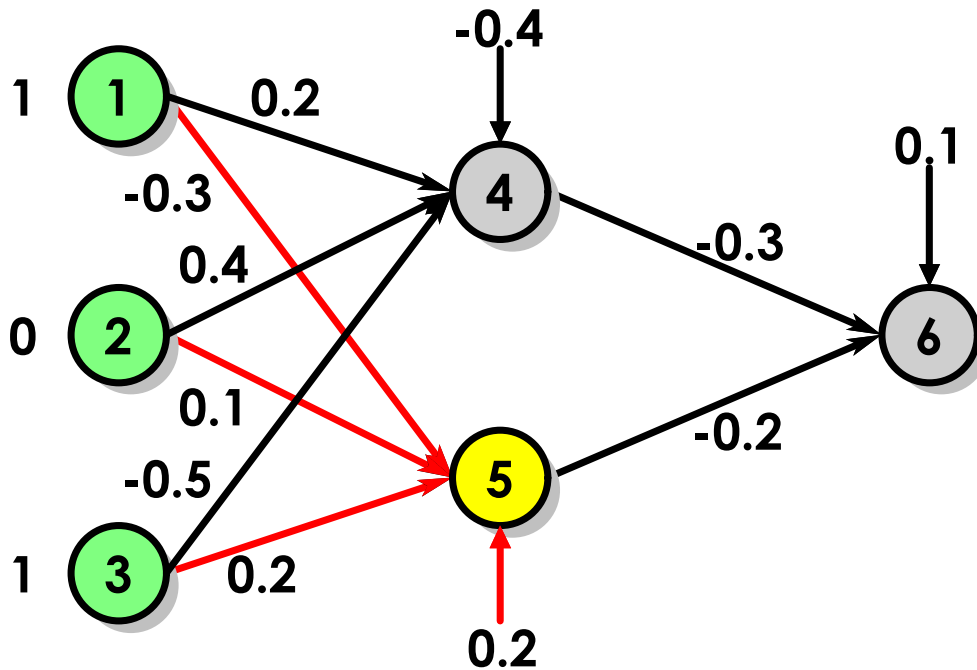
## ...Ejemplo



$$I_j = \sum_i w_{ij} O_i + \theta_j$$

$$O_j = \frac{1}{1 + e^{-I_j}}$$

Unidad	Entrada ( $I_j$ )	Salida ( $O_j$ )
4	$0.2(1) + 0.4(0) - 0.5(1) - 0.4 = -0.7$	$\frac{1}{1 + e^{0.7}} = 0.332$



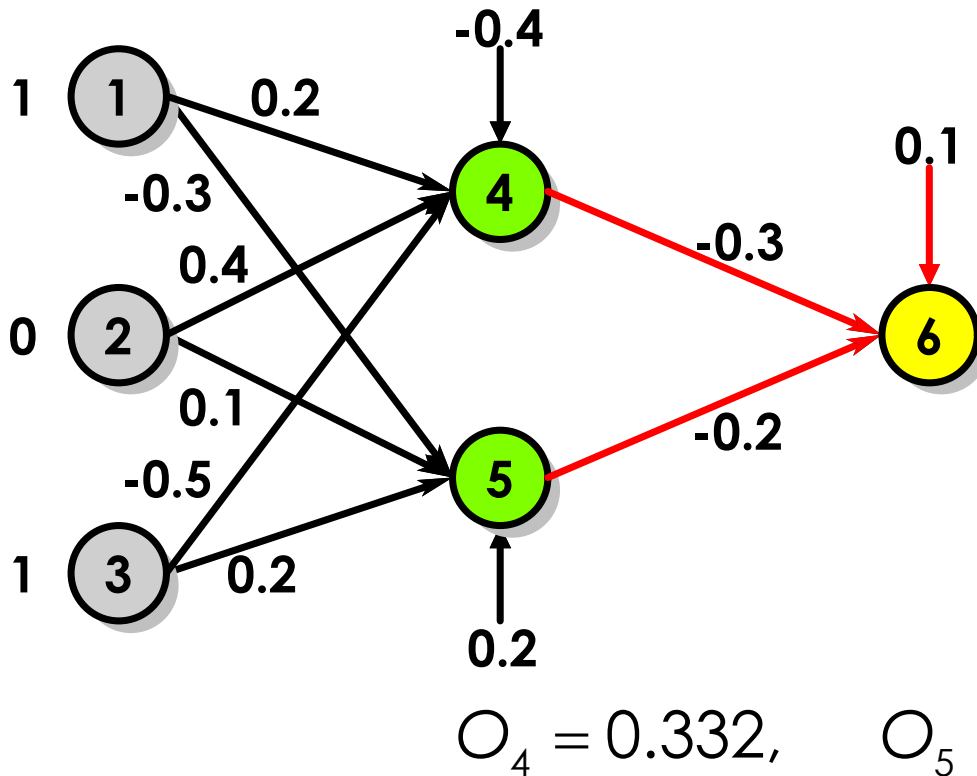
$$I_j = \sum_i w_{ij} O_i + \theta_j$$

$$O_j = \frac{1}{1 + e^{-I_j}}$$

Unidad	Entrada ( $I_j$ )	Salida ( $O_j$ )
5	$-0.3(1) + 0.1(0) + 0.2(1) + 0.2 = -0.1$	$\frac{1}{1 + e^{-0.1}} = 0.525$



## ...Ejemplo: salidas

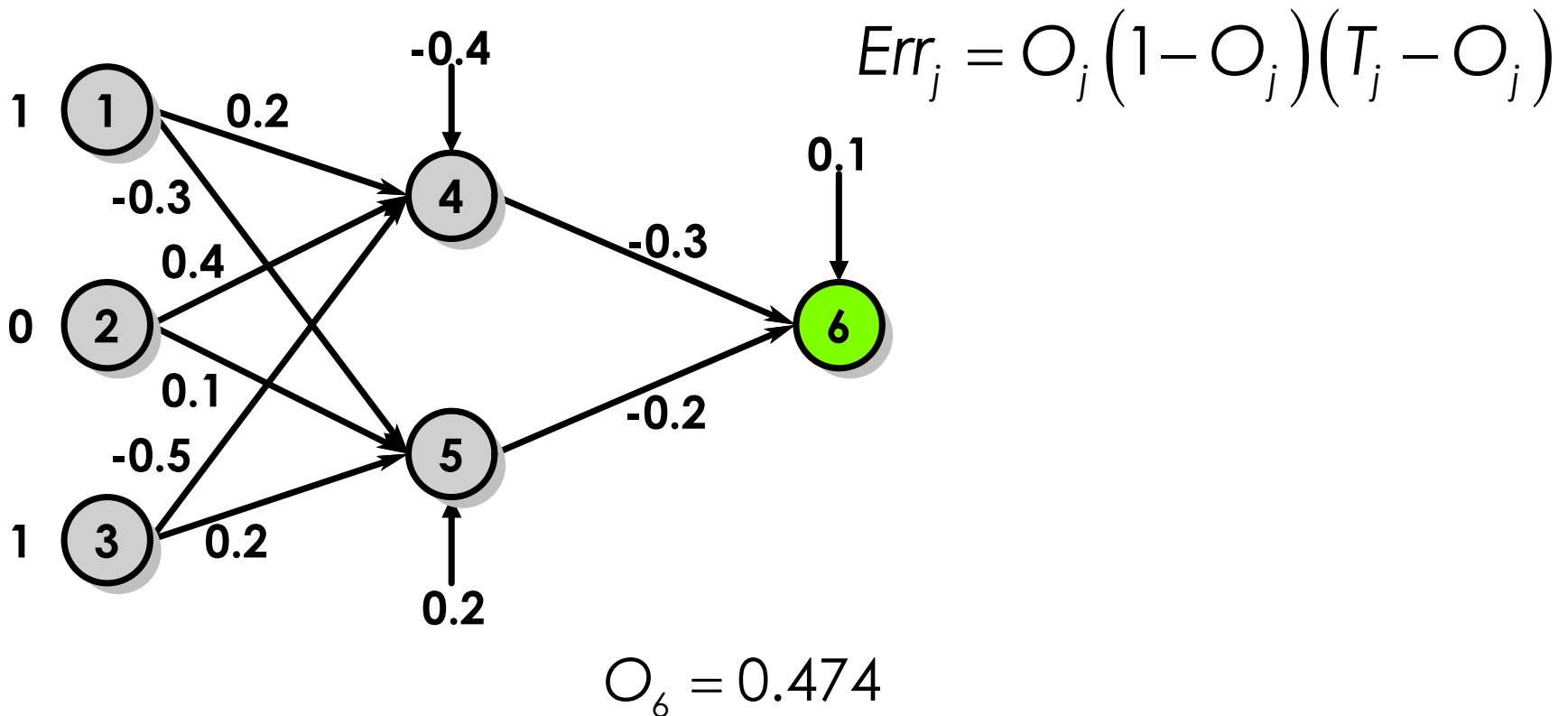


$$I_j = \sum_i w_{ij} O_i + \theta_j$$

$$O_j = \frac{1}{1 + e^{-I_j}}$$

Unidad	Entrada ( $I_j$ )	Salida ( $O_j$ )
6	$-0.3(0.332) - 0.2(0.525) + 0.1 = -0.105$	$\frac{1}{1 + e^{0.105}} = 0.474$

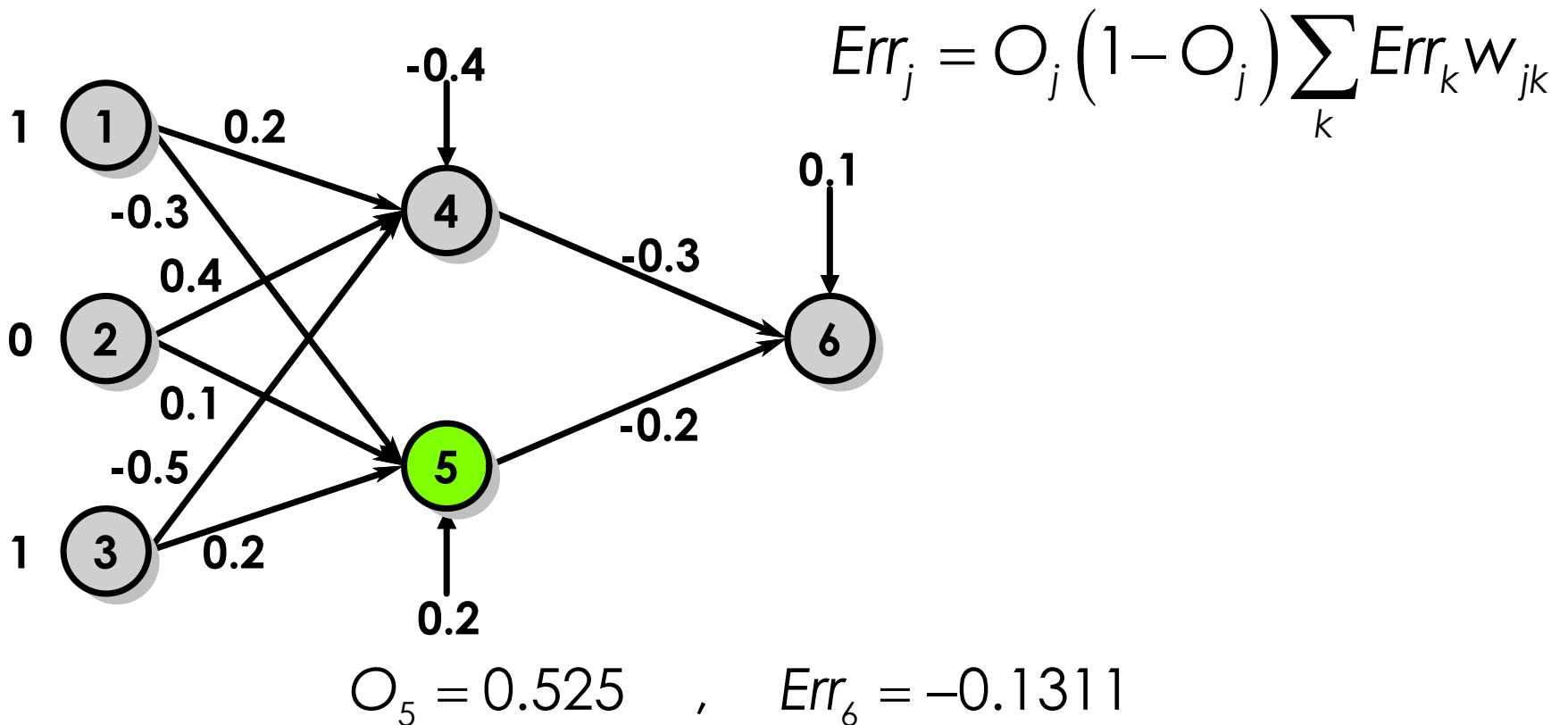
# Ejemplo: retropropagación



Unidad	$Err_6$
6	$(0.474)(1 - 0.474)(1 - 0.474) = -0.1311$

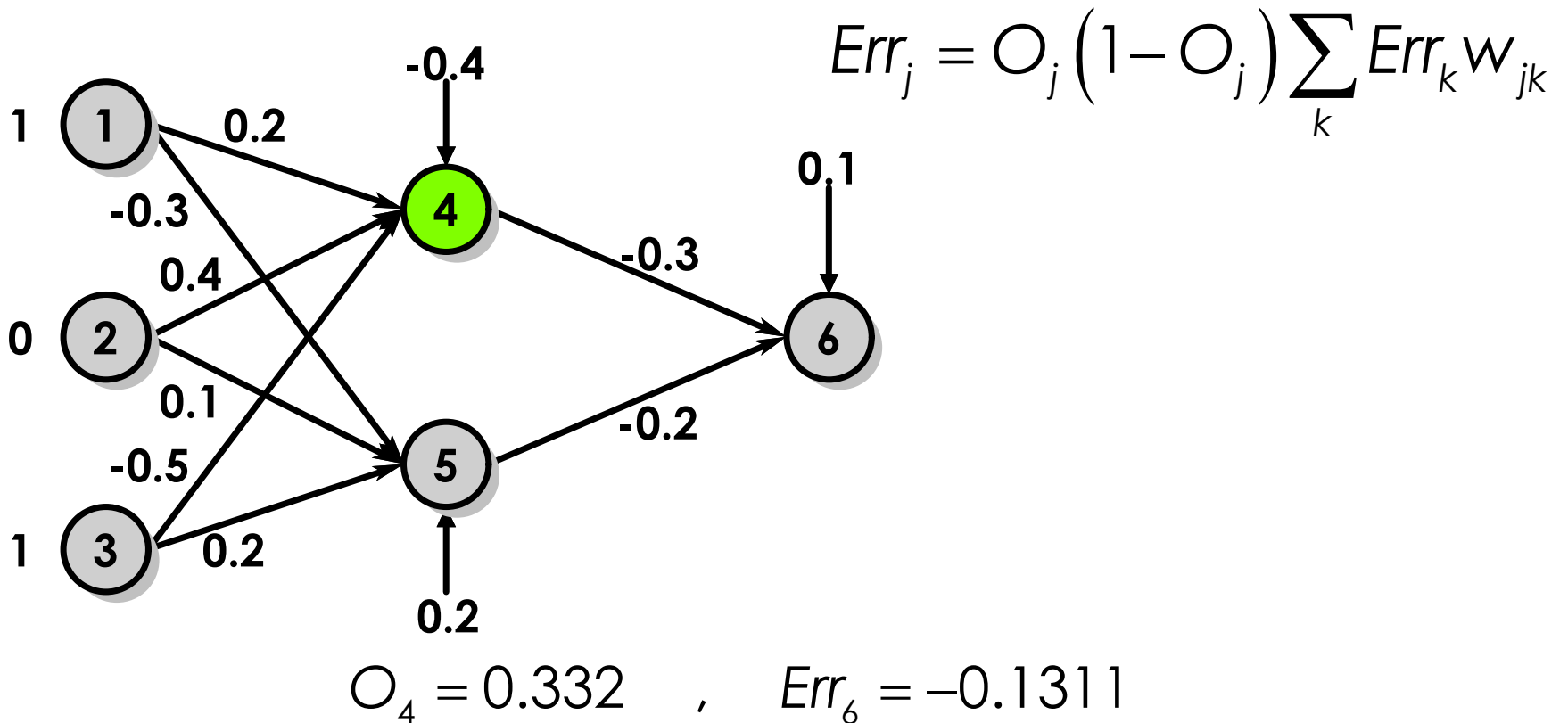


## ...Ejemplo: retropropagación



Unidad	$Err_5$
5	$(0.525)(1 - 0.525)(0.1311)(-0.2) = -0.0065$

# ...Ejemplo: retropropagación

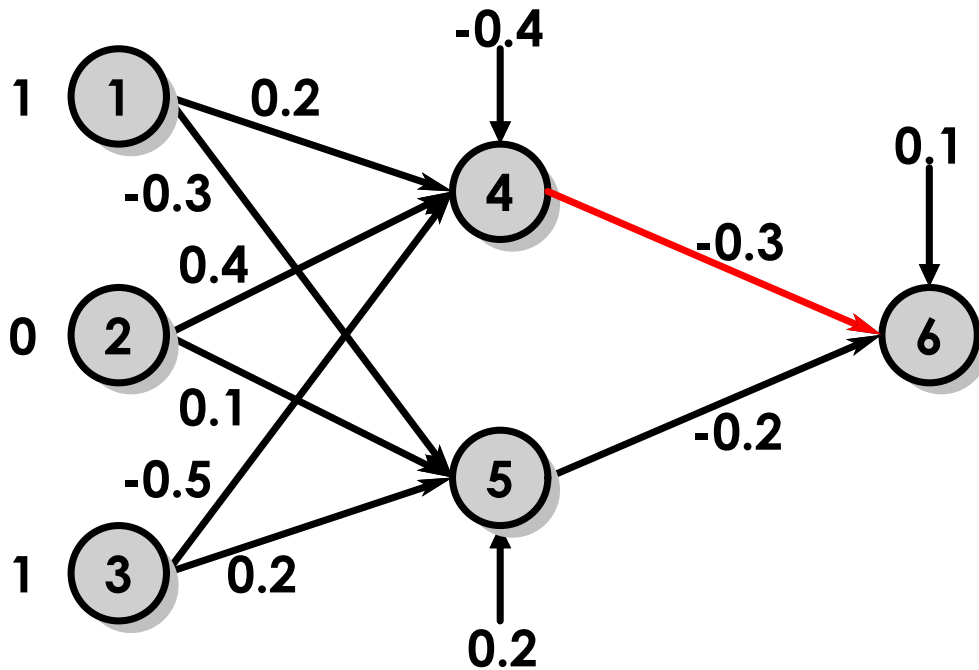


Unidad	$Err_4$
4	$(0.332)(1 - 0.332)(0.1311)(-0.3) = -0.0087$





# Ejemplo: Actualizar pesos



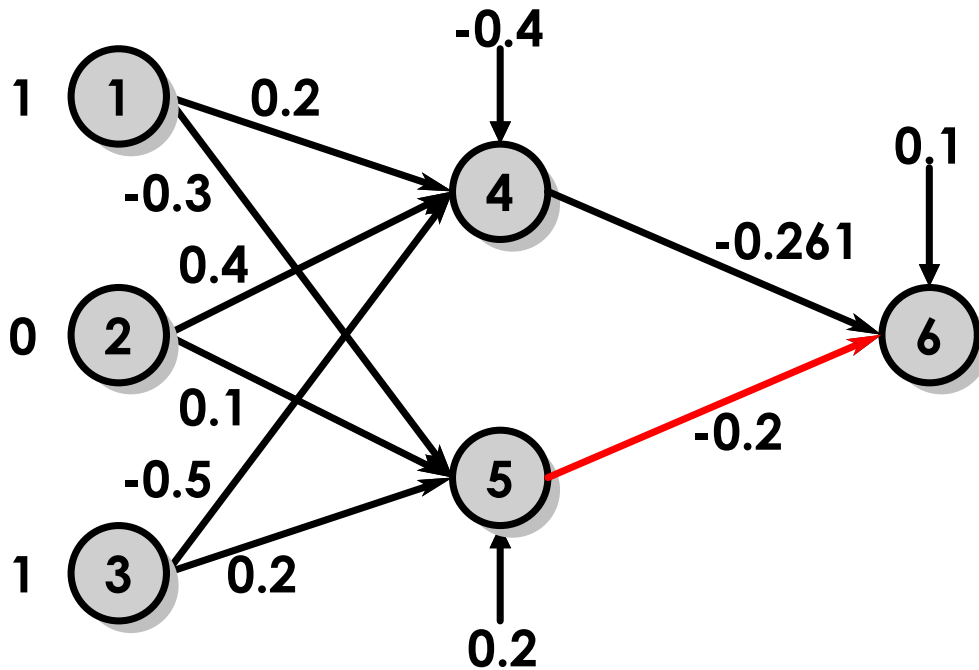
$$\Delta w_{ij} = (\ell) Err_j O_i$$

$$w_{ij} = w_{ij} + \Delta w_{ij}$$

$$O_4 = 0.332 \quad , \quad Err_6 = -0.1311 \quad , \quad \ell = 0.9$$

Peso	Nuevo valor
$w_{46}$	$-0.3 + (0.9)(0.1311)(0.332) = -0.261$

# ...Ejemplo: Actualizar pesos



$$\Delta w_{ij} = (\ell) Err_j O_i$$

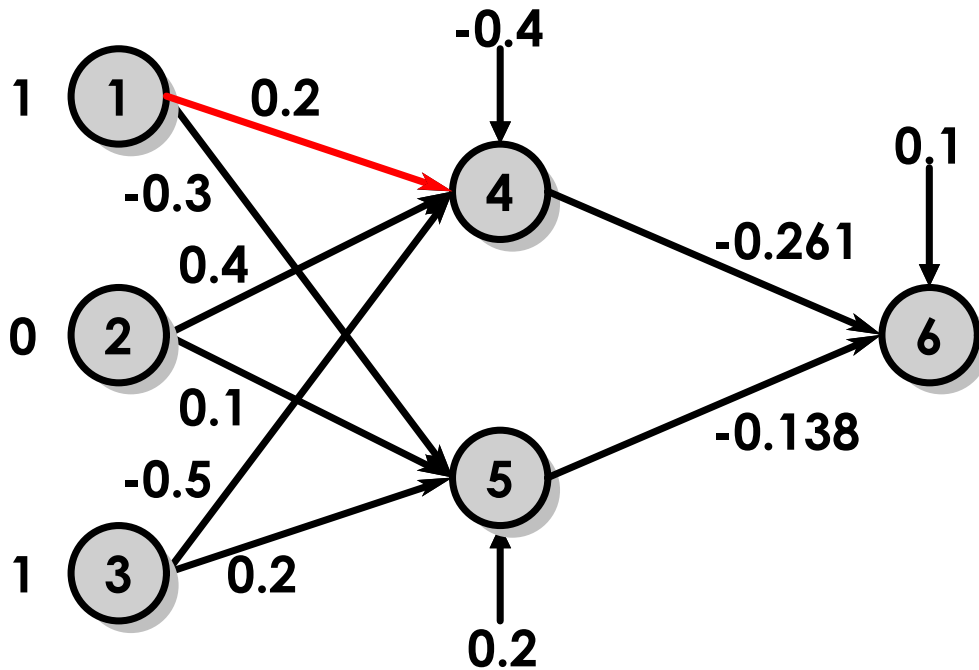
$$w_{ij} = w_{ij} + \Delta w_{ij}$$

$$O_5 = 0.525 \quad , \quad Err_6 = -0.1311 \quad , \quad \ell = 0.9$$

Peso	Nuevo valor
$w_{56}$	$-0.2 + (0.9)(0.1311)(0.525) = -0.138$



## ...Ejemplo: Actualizar pesos



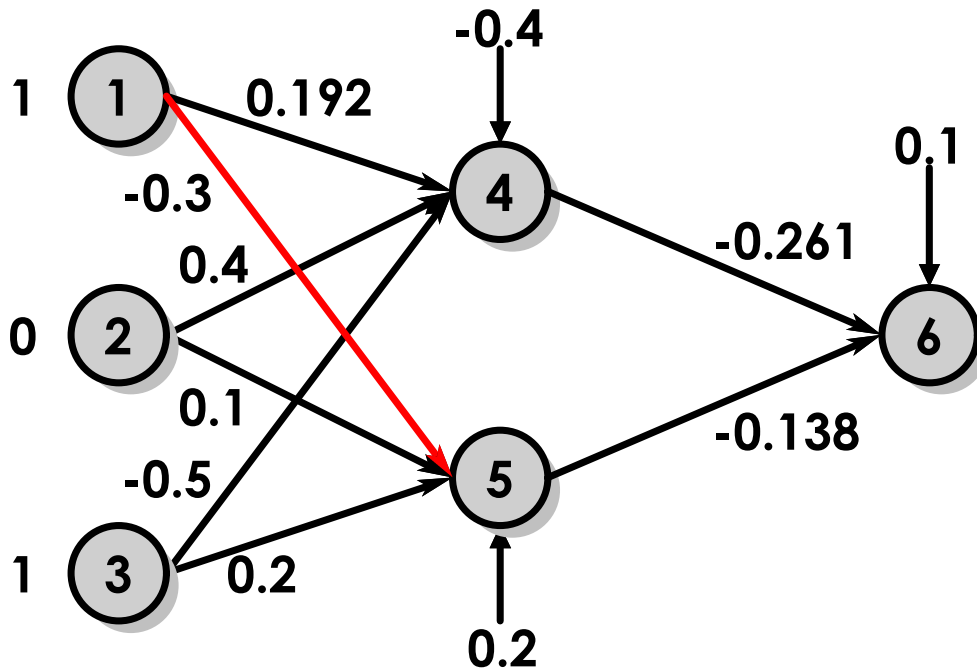
$$\Delta w_{ij} = (\ell) Err_j O_i$$

$$w_{ij} = w_{ij} + \Delta w_{ij}$$

$$O_1 = 1, \quad Err_4 = -0.0087, \quad \ell = 0.9$$

Peso	Nuevo valor
$w_{14}$	$-0.2 + (0.9)(-0.0087)(1) = 0.192$

## ...Ejemplo: Actualizar pesos



$$\Delta w_{ij} = (\ell) Err_j O_i$$

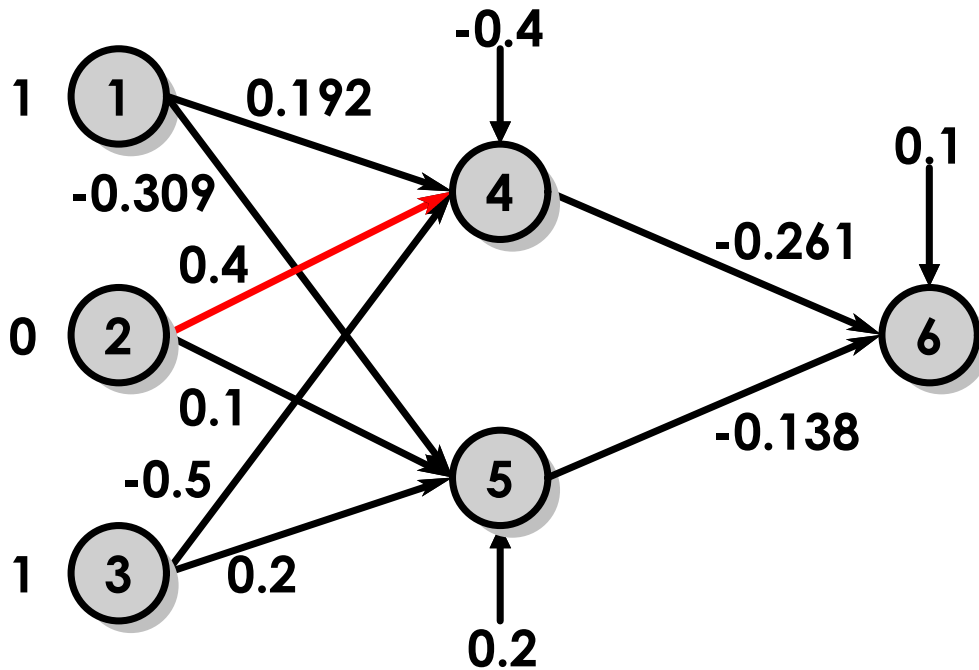
$$w_{ij} = w_{ij} + \Delta w_{ij}$$

$$O_1 = 1, \quad Err_5 = -0.0065, \quad \ell = 0.9$$

Peso	Nuevo valor
$w_{15}$	$-0.3 + (0.9)(-0.0065)(1) = -0.309$



## ...Ejemplo: Actualizar pesos



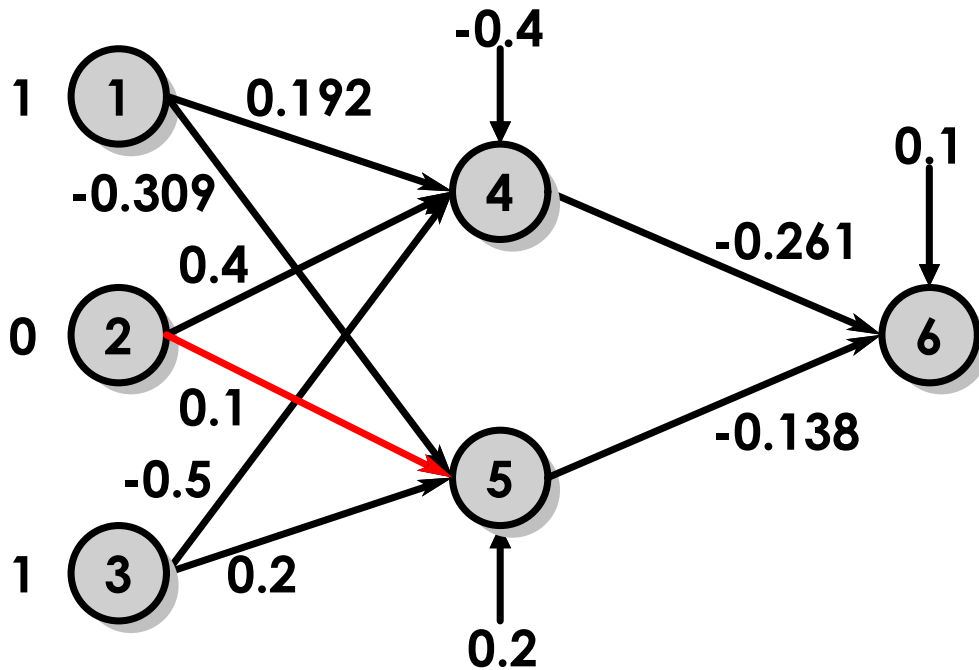
$$\Delta w_{ij} = (\ell) Err_j O_i$$

$$w_{ij} = w_{ij} + \Delta w_{ij}$$

$$O_2 = 0, \quad Err_4 = -0.0087, \quad \ell = 0.9$$

Peso	Nuevo valor
$w_{24}$	$0.4 + (0.9)(-0.0087)(0) = 0.4$

## ...Ejemplo: Actualizar pesos



$$\Delta w_{ij} = (\ell) Err_j O_i$$

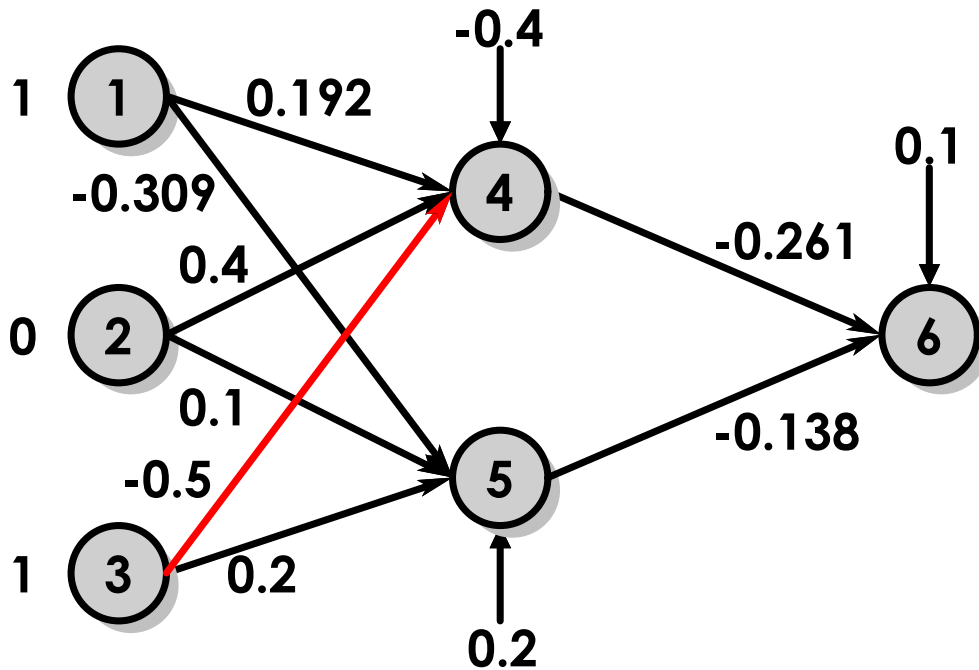
$$w_{ij} = w_{ij} + \Delta w_{ij}$$

$$O_2 = 0, \quad Err_5 = -0.0065, \quad \ell = 0.9$$

Peso	Nuevo valor
$w_{25}$	$0.1 + (0.9)(-0.0065)(0) = 0.1$



## ...Ejemplo: Actualizar pesos



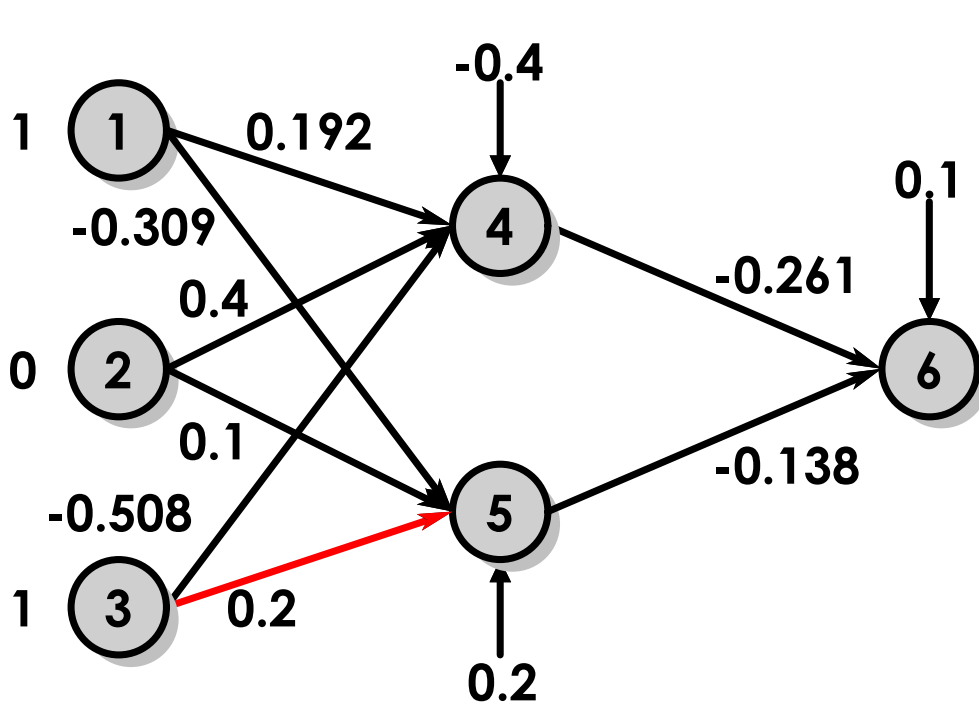
$$\Delta w_{ij} = (\ell) Err_j O_i$$

$$w_{ij} = w_{ij} + \Delta w_{ij}$$

$$O_3 = 1, \quad Err_4 = -0.0087, \quad \ell = 0.9$$

Peso	Nuevo valor
$w_{34}$	$-0.5 + (0.9)(-0.0087)(1) = -0.508$

## ...Ejemplo: Actualizar pesos



$$\Delta w_{ij} = (\ell) Err_j O_i$$

$$w_{ij} = w_{ij} + \Delta w_{ij}$$

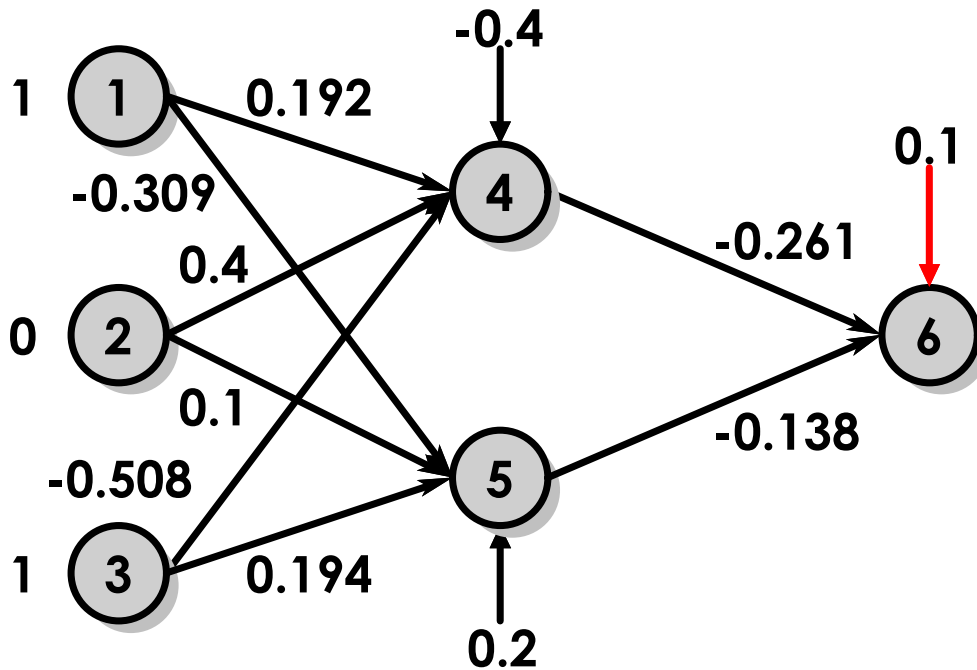
$$O_3 = 1, \quad Err_5 = -0.0065, \quad \ell = 0.9$$

Peso	Nuevo valor
$w_{35}$	$0.2 + (0.9)(-0.0065)(1) = 0.194$





# Ejemplo: Actualizar sesgos



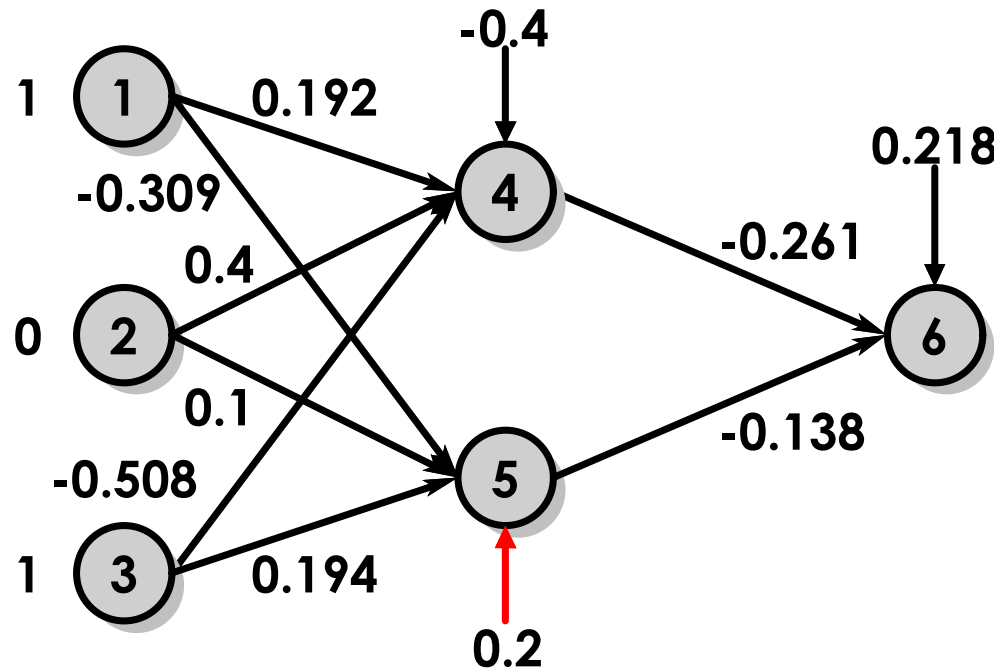
$$\Delta \theta_j = (\ell) Err_j$$

$$\theta_j = \theta_j + \Delta \theta_j$$

$$\theta_6 = 0.1 \quad , \quad Err_6 = 0.1311 \quad , \quad \ell = 0.9$$

Sesgo	Nuevo valor
$\theta_6$	$0.1 + (0.9)(0.1311) = 0.218$

# ...Ejemplo: Actualizar sesgos



$$\Delta \theta_j = (\ell) Err_j$$

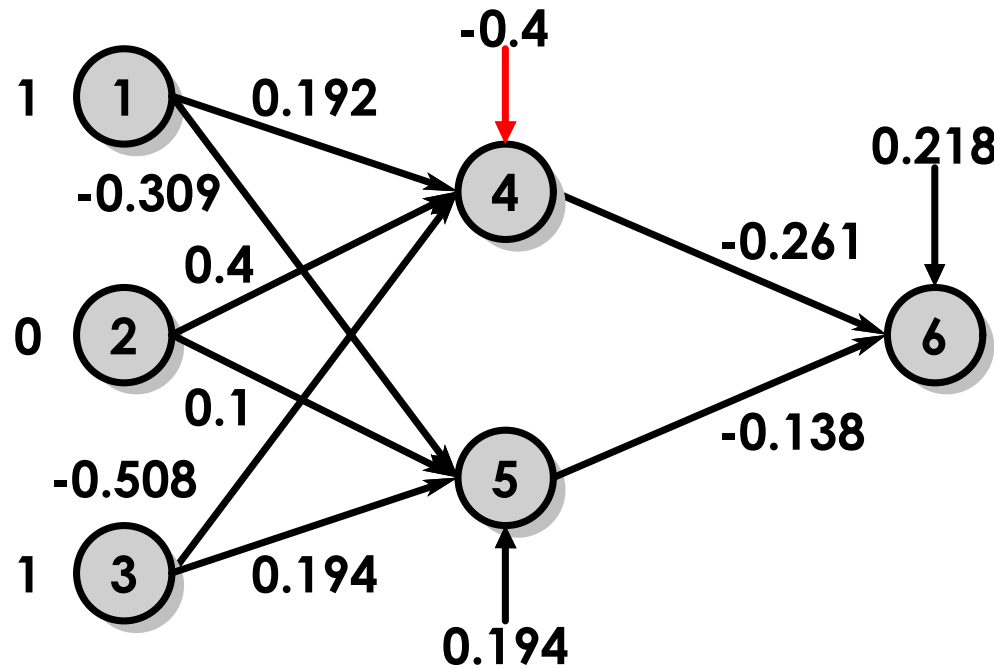
$$\theta_j = \theta_j + \Delta \theta_j$$

$$\theta_5 = 0.2 \quad , \quad Err_5 = -0.0065 \quad , \quad \ell = 0.9$$

Sesgo	Nuevo valor
$\theta_5$	$0.2 + (0.9)(-0.0065) = 0.194$



## ...Ejemplo: Actualizar sesgos

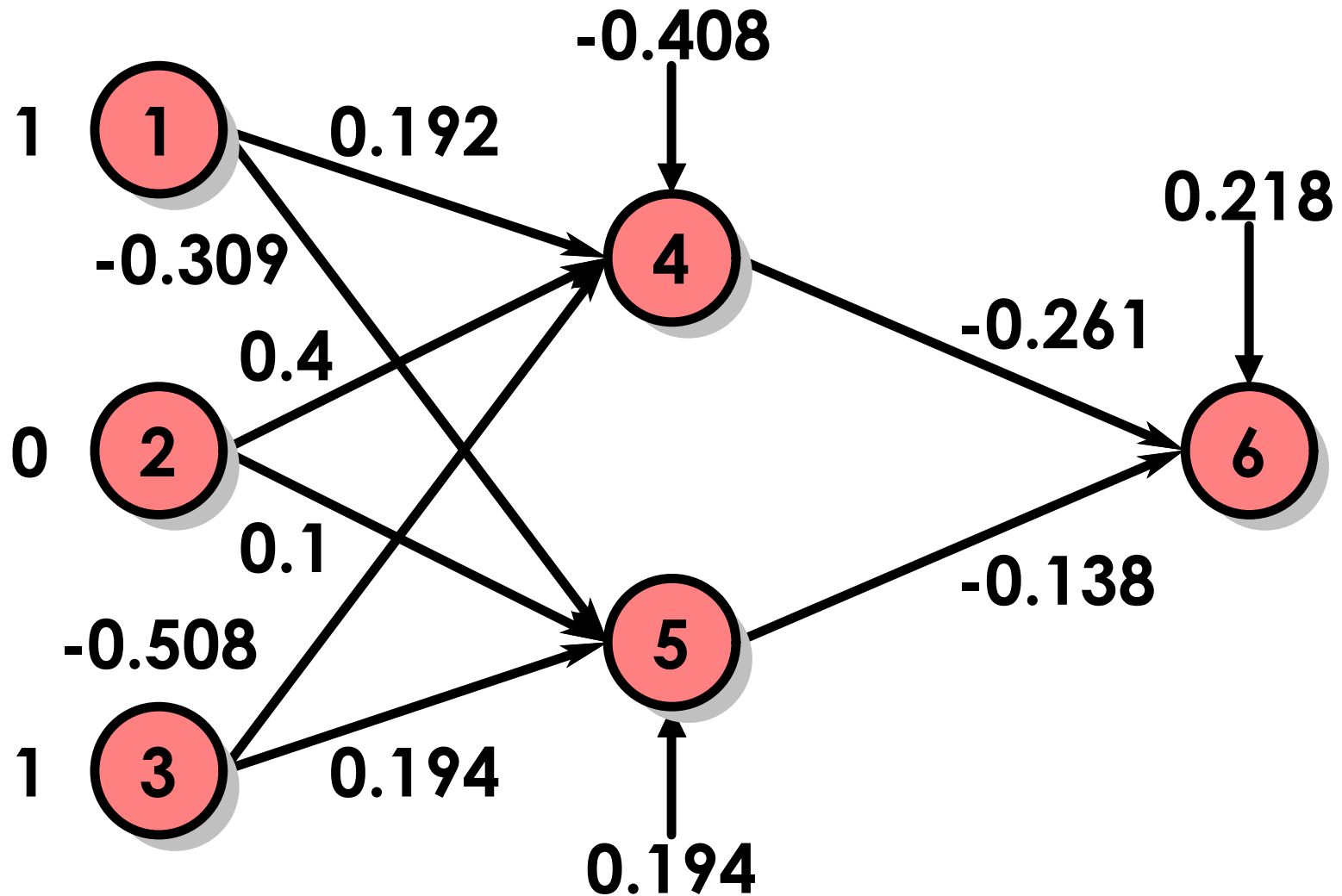


$$\Delta\theta_j = (\ell)Err_j$$

$$\theta_j = \theta_j + \Delta\theta_j$$

$$\theta_4 = -0.4 \quad , \quad Err_5 = -0.0087 \quad , \quad \ell = 0.9$$

Sesgo	Nuevo valor
$\theta_4$	$-0.4 + (0.9)(-0.0087) = -0.408$



*¡Gracias!*

