

A group generator \mathcal{GG} is an efficient randomized algorithm that on input λ , outputs the description of a cyclic group \mathcal{G} of prime order p along with a generator g for \mathcal{G} .

A pseudorandom family of functions $\{G(K, \cdot)\}_{K \in \{0,1\}^*}$ such that for each K of length λ , function $G(K, \cdot)$ takes λ -bit long inputs and outputs strings of length λ .

A pseudorandom family of functions $\{F(K, \cdot)\}_{K \in \{0,1\}^*}$ such that for each K of length λ , function $F(K, \cdot)$ takes λ -bit long inputs and outputs elements of \mathbb{Z}_p , for p prime of length $\Theta(\lambda)$.

A CPA secure private-key encryption scheme (Enc, Dec) .

Algorithm 1 $Setup(\lambda; \perp) \rightarrow (SK; EDB)$

Data Owner

1. Randomly select $(g, \mathcal{G}) \leftarrow \mathcal{GG}(\lambda)$
 2. Randomly select three master keys $K_1, K_2, K_3 \xleftarrow{\$} \{0, 1\}^\lambda$
 3. Initialize $XSet, USet, ASet \leftarrow \Phi$
 4. $SK \leftarrow (K_1, K_2, K_3)$
 5. $EDB \leftarrow (XSet, USet, ASet)$
 6. Send EDB to the Server
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Algorithm 2 $Add(SK, DOC; EDB) \rightarrow (\perp; EDB')$

Data Owner

1. Parse $SK = (K_1, K_2, K_3)$
2. Initialize $TmpSet \leftarrow \Phi$
3. For every document $d \in DOC$
4. Set $K_d \leftarrow F(K_1, d)$, $\tilde{K}_d \leftarrow F(K_2, d)$, $K_d^{enc} \leftarrow G(K_3, d)$
5. For every keyword $w \in KW(d)$
6. Set $X_{w,d} \leftarrow g^{F(\tilde{K}_d, d) \cdot F(K_d, w)}$
7. Set $Y_{w,d} \leftarrow Enc(K_d^{enc}, d)$

8. Update $\text{TmpSet} \leftarrow \text{TmpSet} \cup \{(X_{w,d}, Y_{w,d})\}$
9. Randomly permute the tuple-entries of TmpSet
10. Send TmpSet to the Server

Server

1. Parse $\text{EDB} = (\text{XSet}, \text{USet}, \text{ASet})$
 2. Update $\text{XSet}' \leftarrow \text{XSet} \cup \text{TmpSet}$
 3. $\text{EDB}' \leftarrow (\text{XSet}', \text{USet}, \text{ASet})$
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Algorithm 3 $\text{Enroll}(\lambda; u) \rightarrow (\perp; \text{UK}, \text{UST})$

Data Owner

1. Randomly select two user's keys $K_u, \tilde{K}_u \xleftarrow{\$} \{0, 1\}^\lambda$
 2. Initialize $\text{UsrAuth}, \text{DocKey} \leftarrow \Phi$
 3. $\text{UK} \leftarrow (K_u, \tilde{K}_u)$
 4. $\text{UST} \leftarrow (\text{UsrAuth}, \text{DocKey})$
 5. Send UK, UST to the Data User
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Algorithm 4 $\text{OnlineAuth}(\text{SK}, \text{DOC}; \text{UK}, \text{UST}; \text{EDB}) \rightarrow (\perp; \text{UST}', \text{EDB}')$

Data Owner

1. Parse $\text{SK} = (K_1, K_2, K_3)$, $\text{UK} = (K_u, \tilde{K}_u)$
2. Initialize $\text{TmpArr} \leftarrow \Phi$, $\text{TmpKey} \leftarrow \Phi$
3. For every document Data Owner authorize Data User to access $d \in \text{DOC}$
4. Set $K_d \leftarrow F(K_1, d)$, $\tilde{K}_d \leftarrow F(K_2, d)$, $K_d^{\text{enc}} \leftarrow G(K_3, d)$
5. Set $\text{uid}_{u,d} \leftarrow F(\tilde{K}_u, d)$
6. Set $U_{u,d} \leftarrow F(\tilde{K}_d, d) \cdot (F(K_u, d))^{-1}$
7. Set $\text{TmpArr}[\text{uid}_{u,d}] \leftarrow U_{u,d}$
8. Update $\text{TmpKey} \leftarrow \text{TmpKey} \cup \{(d, K_d, K_d^{\text{enc}})\}$
9. Send TmpKey to the Data User
10. Send TmpArr to the Server

Data User

1. Parse $UST = (UsrAuth, DocKey)$
2. Update $DocKey' \leftarrow DocKey \cup TmpKey$
3. $UST' \leftarrow (UsrAuth, DocKey')$

Server

1. Parse $EDB = (XSet, USet, ASet)$
 2. Update $USet' \leftarrow USet \cup TmpArr$
 3. $EDB' \leftarrow (XSet, USet', ASet)$
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Algorithm 5

$OfflineAuth(UK_A, UST_B, DOC; u_B, UST_B; EDB) \rightarrow (\perp; UST'_B; EDB')$

Data User A

1. Parse $UK_A = (K_{u_A}, \tilde{K}_{u_A})$, $UST_A = (UsrAuth_A, DocKey_A)$,
2. Initialize $TmpASet \leftarrow \Phi$, $TmpUsrAuth \leftarrow \Phi$, $TmpKey \leftarrow \Phi$
3. Set $aid \leftarrow F(\tilde{K}_{u_A}, u_B)$
4. Set $\alpha \leftarrow F(K_{u_A}, u_B)^{-1}$
5. Set $TmpASet \leftarrow \{(aid, \alpha)\}$
6. For every document Data User A authorize Data User B to access $d \in DOC$
7. Initialize $AList \leftarrow \Phi$
8. If $UsrAuth_A[d] = \perp$ then
9. Set $uid \leftarrow F(\tilde{K}_{u_A}, d)$
10. Set $offtok \leftarrow g^{F(K_{u_A}, d) \cdot F(K_{u_A}, u_B)}$
11. Set $AList \leftarrow \{aid\}$
12. Else if $(uid, offtok, AList) \leftarrow UsrAuth_A[d]$ then
13. Set $offtok \leftarrow offtok^{F(K_{u_A}, u_B)}$
14. Update $AList \leftarrow AList \cup \{aid\}$
15. Set $TmpUsrAuth[d] \leftarrow (uid, offtok, AList)$
16. Set $(d, K_d, K_d^{enc}) \leftarrow DocKey_A$
17. Update $TmpKey \leftarrow TmpKey \cup \{(d, K_d, K_d^{enc})\}$

18. Send TmpUsrAuth , TmpKey to the Data User B
19. Send TmpASet to the Server

Data User B

1. Parse $\text{UST}_B = (\text{UsrAuth}_B, \text{DocKey}_B)$
2. Update $\text{UsrAuth}'_B \leftarrow \text{UsrAuth}_B \cup \text{TmpUsrAuth}$
3. Update $\text{DocKey}'_B \leftarrow \text{DocKey}_B \cup \text{TmpKey}$
4. $\text{UST}'_B \leftarrow (\text{UsrAuth}'_B, \text{DocKey}'_B)$

Server

1. Parse $\text{EDB} = (\text{XSet}, \text{USet}, \text{ASet})$
 2. Update $\text{ASet}' \leftarrow \text{ASet} \cup \text{TmpASet}$
 3. $\text{EDB}' \leftarrow (\text{XSet}, \text{USet}, \text{ASet}')$
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Algorithm 6 $\text{Search}(w, \text{UK}, \text{UST}; \text{EDB}) \rightarrow (\text{Res}; \text{EDB}')$

Data User

1. Parse $\text{UK} = (K_u, \tilde{K}_u)$, $\text{UST} = (\text{UsrAuth}, \text{DocKey})$
2. Initialize $\text{Query} \leftarrow \Phi$
3. For every document key information $(d, K_d, K_d^{enc}) \in \text{DocKey}$
4. If $\text{UsrAuth}[d] = \perp$ then
5. Set $\text{uid}_{u,d} \leftarrow F(\tilde{K}_u, d)$
6. Set $\text{stk}_d \leftarrow g^{F(K_d, w) \cdot F(K_u, d)}$
7. Initialize $\text{AList} \leftarrow \Phi$
8. Else if $(\text{uid}, \text{offtok}, \text{AList}) \leftarrow \text{UsrAuth}[d]$ then
9. Set $\text{stk}_d \leftarrow \text{offtok}^{F(K_d, w)}$
10. Update $\text{Query} \leftarrow \text{Query} \cup \{(\text{uid}, \text{stk}_d, \text{AList})\}$
11. Randomly permute the tuple-entries of Query
12. Send Query to the Server

Server

1. Parse $EDB = (XSet, USet, ASet)$
2. Initialize $TmpRes \leftarrow \Phi$
3. For every query tuple $(uid, stk_d, AList) \in \text{Query}$
4. Set $x \leftarrow stk_d^{USet[uid]}$
5. If $AList \neq \Phi$ then
6. For every $aid \in AList$
7. Set $x \leftarrow x^{ASet[aid]}$
8. If $(x, Y) \in XSet$ then $TmpRes \leftarrow TmpRes \cup \{Y\}$
9. $EDB' \leftarrow EDB$
10. Send $TmpRes$ to the Data User

Data User: Final Output

1. Initialize $Res \leftarrow \Phi$
 2. For every encrypted document identifier result $y_d \in TmpRes$
 3. Recover $d \leftarrow Dec(K_d^{enc}, y_d)$
 4. Update $Res \leftarrow Res \cup \{d\}$
 5. **Output** Res
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