# Wisconsin Breast Cancer Data Analysis

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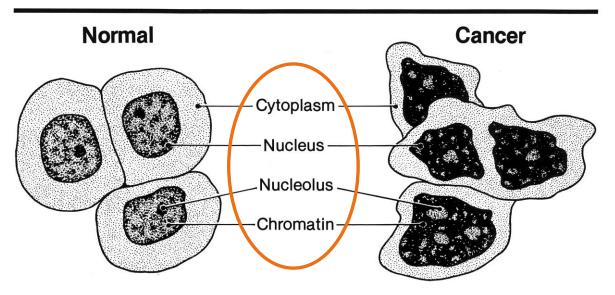
## Background Information

#### About the Dataset

- The University of Wisconsin Hospitals in 1992
- Collected 699 observations consisting of 11 attributes
- The features are computed from a digitized image

#### About the Dataset

#### Normal and Cancer Cells Structure



- Large cytoplasm
- Single nucleus
- Single nucleolus
- Fine chromatin

- Small cytoplasm
- Multiple nuclei
- Multiple and large nucleoli
- Coarse chromatin

# Attri	Attribute		Domain				
<ol> <li>Sample</li> </ol>	e code number	id numb	er				
2. Clump	Thickness	1 - 10					
<ol><li>Unifo</li></ol>	rmity of Cell Size	1 - 10					
4. Unifo	rmity of Cell Shape	1 - 10					
<ol><li>Margi</li></ol>	nal Adhesion	1 - 10					
<ol><li>Singl</li></ol>	e Epithelial Cell Size	1 - 10					
7. Bare	Nuclei	1 - 10					
8. Bland	Chromatin	1 - 10					
9. Norma	l Nucleoli	1 - 10					
10. Mitos	es	1 - 10					
11. Class	:	(2 for	benign,	4 :	for	malignant)	

<Source> https://archive.ics.uci.edu/ml/datasets/breast+cancer+wisconsin+(diagnostic)

#### About the Dataset

- Except class, all other attributes are numeric type
- Class attribute indicates Benign or Malignant
  - Benign: A tumor which can usually be removed without serious complications and will not be fatal to the patient.
  - Malignant: Cancerous cells have ability to spread to other sites in the body.



## An Exploratory Data Analysis

#### Step (1) Prepares the Dataset

#### **Packages**

```
library(tidyverse) # includes tibbles, ggplot2, dplyr, and more.
library(caret) # analyzes variable importance
library(MLmetrics)

## Warning: package 'MLmetrics' was built under R version 4.1.2

library(MASS)
library(ROCR)
```

Load this data set and store it as CancerData, using the following code:

```
CancerData<-read_csv("http://archive.ics.uci.edu/ml/machine-learning-databases/breast-cancer-wisconsin/breast-cancer-wiscons
in.data", col_names=FALSE, na="?")</pre>
```

```
## Rows: 699 Columns: 11

## -- Column specification -----
## Delimiter: ","
## dbl (11): X1, X2, X3, X4, X5, X6, X7, X8, X9, X10, X11
```

563649,8,8,8,1,2,2,6,10,1,4
601265,10,4,4,6,2,10,2,3,1,4
606140,1,1,1,1,2,2,2,2,1,1,2
606722,5,5,7,8,6,10,7,4,1,4
616240,5,3,4,3,4,5,4,7,1,2
61634,5,4,3,1,2,2,2,3,1,2

#### glimpse(CancerData) ## Rows: 699 ## Columns: 11 <dbl> 1000025, 1002945, 1015425, 1016277, 1017023, 1017122, 1018099, 101~ ## \$ X2 <dbl> 5, 5, 3, 6, 4, 8, 1, 2, 2, 4, 1, 2, 5, 1, 8, 7, 4, 4, 10, 6, 7, 10~ ## \$ X3 <dbl> 1, 4, 1, 8, 1, 10, 1, 1, 1, 2, 1, 1, 3, 1, 7, 4, 1, 1, 7, 1, 3, 5,~ <dbl> 1, 4, 1, 8, 1, 10, 1, 2, 1, 1, 1, 1, 3, 1, 5, 6, 1, 1, 7, 1, 2, 5,~ ## \$ X5 <dbl> 1, 5, 1, 1, 3, 8, 1, 1, 1, 1, 1, 1, 3, 1, 10, 4, 1, 1, 6, 1, 10, 3 <dbl> 1, 10, 2, 4, 1, 10, 10, 1, 1, 1, 1, 1, 3, 3, 9, 1, 1, 1, 10, 1, 10~ <dbl> 3, 3, 3, 3, 3, 9, 3, 3, 1, 2, 3, 2, 4, 3, 5, 4, 2, 3, 4, 3, 5, 7, ~ <dbl> 1, 2, 1, 7, 1, 7, 1, 1, 1, 1, 1, 1, 4, 1, 5, 3, 1, 1, 1, 1, 4, 10,~ ## \$ X10 <dbl> 1, 1, 1, 1, 1, 1, 1, 1, 5, 1, 1, 1, 1, 1, 1, 1, 1, 1, 2, 1, 4, 1, ~ ## \$ X11 <dbl> 2, 2, 2, 2, 2, 4, 2, 2, 2, 2, 2, 4, 2, 4, 2, 4, 2, 4, 4, 2, 2, 4, 4, 4, ~ names(CancerData) <- c('id', 'thickness', 'unif\_cell\_size','unif\_cell\_shape','marginal\_adhesion','cell\_size','bare\_nucle i','band\_cromatin','normal\_nucleoli','mitoses','class' CancerData <- CancerData %>% dplyr::select(-id) #Remove ID column summary(CancerData) #Check out if there are any NA data thickness unif\_cell\_size unif\_cell\_shape marginal\_adhesion : 1.000 Min. : 1.000 Min. : 1.000 Min. : 1.000 1st Qu.: 1.000 1st Qu.: 1.000 1st Qu.: 1.000 ## 1st Qu.: 2.000 Median : 1.000 Median : 1.000 Median : 1.000 ## Median : 4.000 Mean : 3.207 Mean : 2.807 : 4.418 Mean : 3.134 Qu.: 6.000 3rd Qu.: 5.000 3rd Qu.: 5.000 3rd Qu.: 4.000 :10.000 Max. :10.000 Max. :10.000 Max. :10.000 cell size bare nuclei band cromatin normal nucleoli : 1.000 Min. : 1.000 Min. : 1.000 Min. : 1.000 Qu.: 2.000 1st Qu.: 1.000 1st Qu.: 2.000 1st Qu.: 1.000 Median : 1.000 Median : 3.000 Median : 1.000 ## Median : 2.000 Mean : 3.545 Mean : 3.438 Mean : 2.867 : 3.216 Qu.: 4.000 3rd Qu.: 6.000 3rd Qu.: 5.000 3rd Ou Max. :10.000 Max. :10.000 :10.000 Max. :10.000 NA's :16 mitoses class Min. :2.00 ## 1st Qu.: 1.000 1st Qu.:2.00 Median :2.00 : 1.589 Mean :2.69 Qu.: 1.000 3rd Qu.:4.00 :10.000 Max. :4.00

#### **L** Columns

Original data has no column names

#### 2 Class

- Benign: 2
- Malignant: 4

#### 3 Bare nuclei

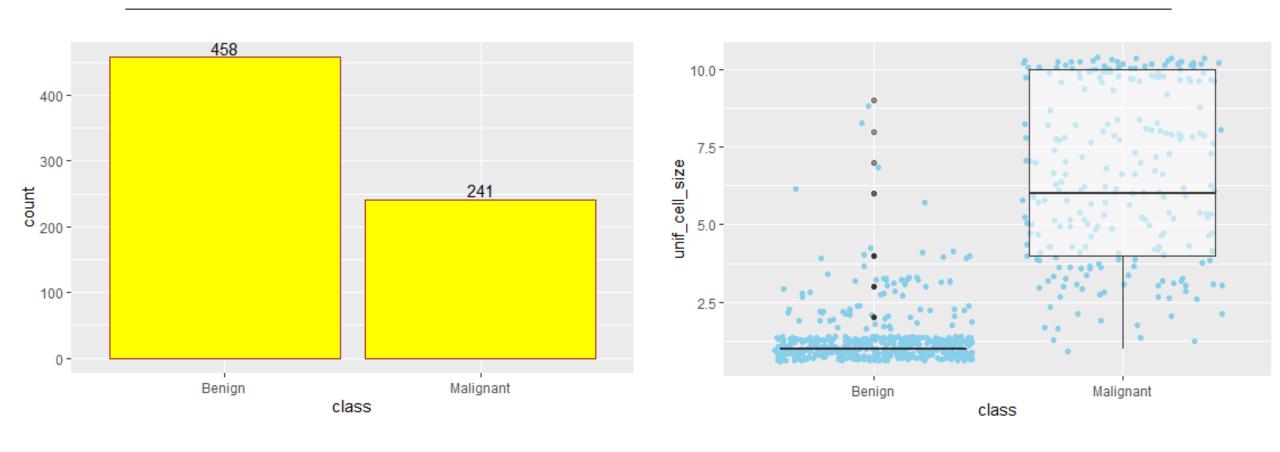
 16 missing values in the column (NA's 16)

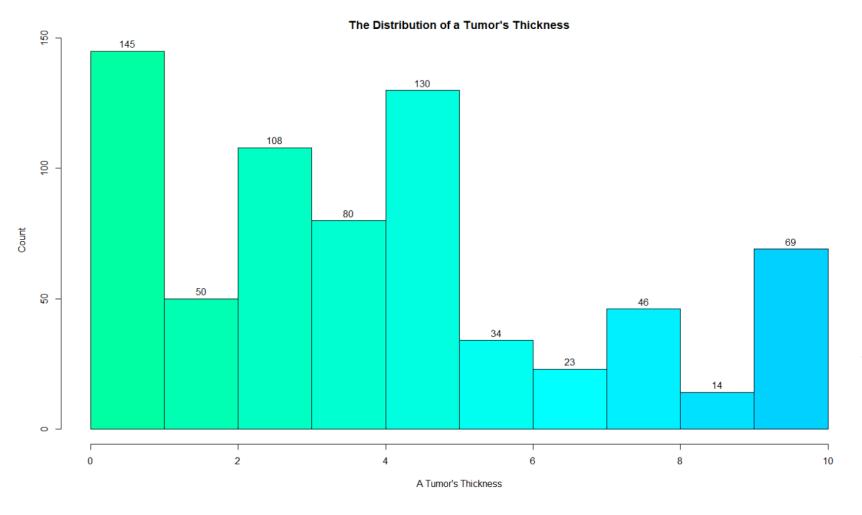
```
# remove missing values from bare_nuclei
CancerData$bare_nuclei[is.na(CancerData$bare_nuclei)] <- median(CancerData$bare_nuclei, na.rm = TRUE)</pre>
```

It changes from value 2 to Benign and from value 4 to Malignant.

```
CancerData$class <- factor(ifelse(CancerData$class==2,"Benign","Malignant"))</pre>
                                          glimpse(CancerData)
#confirm the result of changes
summary(CancerData)
                                          ## Rows: 699
                                          ## Columns: 10
      thickness
                    unif_cell_size
                                          ## $ thickness
                                                                 <dbl> 5, 5, 3, 6, 4, 8, 1, 2, 2, 4, 1, 2, 5, 1, 8, 7, 4, 4~
                    Min. : 1.000
        : 1.000
                                     Mi:
                                                                <dbl> 1, 4, 1, 8, 1, 10, 1, 1, 1, 2, 1, 1, 3, 1, 7, 4, 1, ~
                                          ## $ unif cell size
   1st Ou.: 2.000
                    1st Ou.: 1.000
                                                                <dbl> 1, 4, 1, 8, 1, 10, 1, 2, 1, 1, 1, 1, 3, 1, 5, 6, 1, ~
                                          ## $ unif cell shape
   Median : 4.000
                    Median : 1.000
                                          ## $ marginal adhesion <dbl> 1, 5, 1, 1, 3, 8, 1, 1, 1, 1, 1, 1, 3, 1, 10, 4, 1, ~
         : 4.418
                    Mean : 3.134
                                          ## $ cell size
                                                                <dbl> 2, 7, 2, 3, 2, 7, 2, 2, 2, 2, 1, 2, 2, 2, 7, 6, 2, 2~
   3rd Qu.: 6.000
                    3rd Qu.: 5.000
                                          ## $ bare nuclei
                                                                <dbl> 1, 10, 2, 4, 1, 10, 10, 1, 1, 1, 1, 1, 3, 3, 9, 1, 1~
                                    Max
          :10.000
                    Max. :10.000
                                                                <dbl> 3, 3, 3, 3, 3, 9, 3, 3, 1, 2, 3, 2, 4, 3, 5, 4, 2, 3~
                                          ## $ band chromatin
     cell_size
                     bare nuclei
                                          ## $ normal nucleoli
                                                                <dbl> 1, 2, 1, 7, 1, 7, 1, 1, 1, 1, 1, 1, 4, 1, 5, 3, 1, 1~
                                    Mir
         : 1.000
                    Min. : 1.000
                                                                <dbl> 1, 1, 1, 1, 1, 1, 1, 1, 5, 1, 1, 1, 1, 1, 4, 1, 1, 1~
                                          ## $ mitoses
   1st Qu.: 2.000
                    1st Qu.: 1.000
                                     15
                                                                <fct> Benign, Benign, Benign, Benign, Benign, Malignant, B~
                                          ## $ class
   Median : 2.000
                    Median : 1.000
                                     Mee
        : 3.216
                    Mean : 3.486
   3rd Qu.: 4.000
                    3rd Qu.: 5.000
                                     3rd Qu.: 5.000
                                                     3rd Qu.: 4.000
          :10.000
                          :10.000
                                           :10.000
                                                     Max.
                                                            :10.000
       mitoses
                          class
         : 1.000
                    Benign :458
   1st Qu.: 1.000
                    Malignant:241
   Median : 1.000
         : 1.589
   3rd Qu.: 1.000
          :10.000
## Max.
```

## Step (2) Data Visualization





#### Step (2) Data Visualization (Cont.)



## Hypothesis Testing

## Step (1) Set Up a Null Hypothesis

$$H_0: \mu_{1} = \mu_2$$

$$H_1: \mu_{1\neq}\mu_2$$

- The means of thickness from Benign and Malignant groups
- $\blacksquare H_0$ : The two means of thickness are same.
- $\blacksquare H_1$ : The two means of thickness are not same.

#### Step (2) Data Extract

Divided into two groups by class attribute

```
groupBenign <- CancerData[CancerData$class == 'Benign',]
groupMalignant <- CancerData[CancerData$class == 'Malignant',]</pre>
```

```
## # A tibble: 458 x 10

## thickness unif_cell_size unif_cell_shape marginal_adhesion cell_size

## (dbl> (db) (dbl> (db) (dbl> (dbl> (dbl> (dbl> (dbl) (dbl> (dbl> (dbl) (db
```

groupMalignant

band cromatin <dbl>, normal nucleoli <dbl>, mitoses <dbl>, class <fct>

### Step (3) F-test

- Assumed the variances are unknown and equal.
- Conducted a F-test first to compare two variances at  $\alpha = 0.05$

```
##
## F test to compare two variances
##
## data: groupBenign$thickness and groupMalignant$thickness
## F = 0.4752, num df = 457, denom df = 240, p-value = 1.092e-11
## alternative hypothesis: true ratio of variances is not equal to 1
## 95 percent confidence interval:
## 0.3793569 0.5906700
## sample estimates:
## ratio of variances
## 0.4751982
```

#### P-value $< \alpha = 0.05$

- $1.092 \times 10^{-11}$
- 0.0000000001092

#### Reject H<sub>0</sub> and Select H<sub>1</sub>

- Select the alternative hypothesis
- The confidence interval (0.38, 0.59)
- There is a difference in the two variances

### Step (4) T-test

- Assumed the variances are not equal based on the F-test.
- Assumed the two samples are normally distributed and independent.

```
t.test(groupBenign$thickness, groupMalignant$thickness, var.equal = FALSE)
```

```
##
## Welch Two Sample t-test
##
## data: groupBenign$thickness and groupMalignant$thickness
## t = -24.231, df = 363.11, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
    -4.582685 -3.894693
## sample estimates:
## mean of x mean of y
    2.956332    7.195021</pre>
```

#### P-value $< \alpha = 0.05$

•  $2.2 \times 10^{-16}$  (0.00000000000000022)

#### Reject H<sub>0</sub> and Select H<sub>1</sub>

- Select the alternative hypothesis
- The confidence interval (-4.58, -3.89)
- The mean of Benign is 2.96
- The mean of Malignant is 7.20

### Step (5) Conclusion

- Reject  $H_0$  and Select  $H_1$
- Malignant cells are much thicker than Benign cells.



## Linear Regression & Prediction

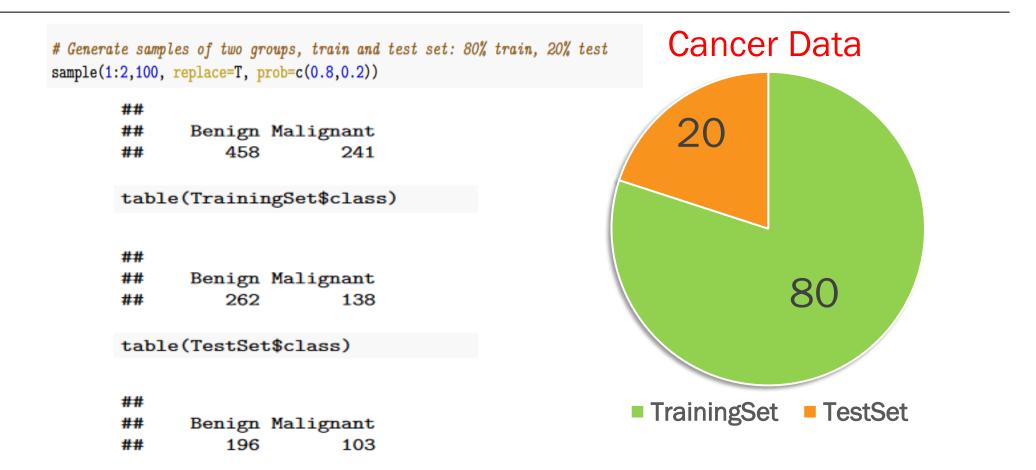
### Step (1) Concept of the Regression

 Measures the relationship between the dependent variable and the one or more independent variables.

#### Step (2) Regression Function

- f(x) = E(Y|X = x)
- $class \approx f(all other features)$
- class = a response, target or outcome
  - Benign or Malignant
  - family=binomial
- thickness or bare\_nuclei = a predictor or input

#### Step (3) Generates Train & Test Sets



## Step (3) Train & Test Sets (Cont.)

	Original	TrainingSet	TestSet
Benign	66 %	67 %	64 %
Malignant	34 %	33 %	36 %

```
glm.fit <- glm(class~., data=TrainingSet, family = binomial)
summary(glm.fit)</pre>
```

```
call:
glm(formula = class ~ ., family = binomial, data = TrainingSet)
Deviance Residuals:
     Min
                     Median
                                    3Q
                                             Max
-2.75062 -0.14191
                               0.02105
                    -0.07453
                                         2.32846
Coefficients:
                   Estimate Std. Error z value Pr(>|z|)
(Intercept)
                  -9.638266
                             1.319450
                                        -7.305 2.78e-13
thickness
                  0.528409
                              0.168876
                                         3.129
                                                0.00175
unif_cell_size
                  -0.097515
                              0.273424
                                        -0.357
                                                0.72136
unif_cell_shape
                  0.263986
                              0.272529
                                        0.969
                                               0.33272
marginal_adhesion 0.345806
                              0.166802
                                        2.073 0.03816 *
cell_size
                  0.004148
                              0.182814
                                        0.023
                                               0.98190
bare_nuclei
                                                0.00108
                              0.114905
                                         3.269
                  0.375644
band_chromatin
                                         2.727
                0.501770
                             0.183968
                                               0.00638 **
normal_nucleoli
                              0.152506
                                         1.137
                                                0.25552
                  0.173406
                              0.501148
                                         1.236 0.21650
mitoses
                  0.619365
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
    Null deviance: 507.343 on 399 degrees of freedom
Residual deviance: 74.866 on 390 degrees of freedom
AIC: 94.866
Number of Fisher Scoring iterations: 8
```

### Step (4) Linear Regression

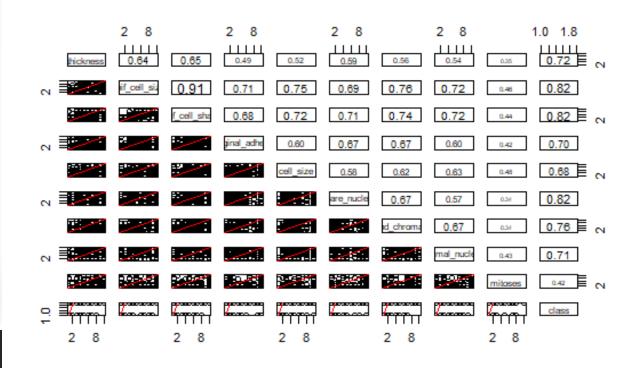
P-Value is close to 0

## Step (4) Linear Regression (Cont.)

Is there a relationship between predictors and response?

Yes, there is a significant relationship between predictors and response.

 The scatter plots matrix about the relationship between predictors and response.



## Step (4) Linear Regression (Cont.)

The statistically significant variables

thickness

Bare\_nuclei

The coefficient for thickness

0.52. Hence, it is a positive relationship between class and thickness.

## Each value of yield\_glm has the probability placing between 0 and 1 which means how much close to Malignant (1)

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 0.0009837 0.0027611 0.0158238 0.3553679 0.9767362 0.9999998
```

# Step (5) Prediction to the Response

Let's apply the model to a New Data, TestSet

#### Step (6) The Importance of Variables

#### **Packages**

```
library(tidyverse) # includes tibbles, ggplot2, dplyr, and more.
library(caret)
                 # analyzes variable importance_
library(MLmetrics)
                                                table(TrainingSet$bare_nuclei, TrainingSet$class)
 varImp(glm.fit)
                                                         Benign Malignant
  ##
                          Overall
                                                            225
  ## thickness
                         3.077160
                                                             13
                         1.151258
  ## unif_cell_size
  ## unif_cell_shape
                         1.872451
                                                                       16
  ## marginal_adhesion 2.206841
  ## cell size
                         1.602011
  ## bare nuclei
                         3.096287
                                                                       10
  ## band_chromatin
                         2.297884
  ## normal_nucleoli
                         1.472362
                                                                       73
  ## mitoses
                         1.458283
```



# The Model Evaluation

```
MAE(y_pred = yield_glm, y_true = as.numeric(TestSet$class))
## [1] 1.009181

MSE(y_pred = yield_glm, y_true = as.numeric(TestSet$class))
## [1] 1.035692
```

- The Mean Absolute Error (MAE)
- The Mean Squared Error (MSE)
- MAE and MSE are good to close to 0

# Step (1) MAE & MSE

# Step (2) AIC Evaluation : Stepwise Regression - Backward

```
call:
glm(formula = class ~ ., family = binomial, data = TrainingSet)
                                                                  glm(formula = class ~ thickness + unif_cell_size + unif_cell_shape +
Deviance Residuals:
                                                                      marginal_adhesion + bare_nuclei + band_chromatin + normal_nucleoli +
     Min
                      Median
                                     3Q
                                                                      mitoses, family = binomial, data = TrainingSet)
                                              Max
                                0.02105
-2.75062 -0.14191 -0.07453
                                          2.32846
                                                                  Deviance Residuals:
Coefficients:
                                                                                       Median
                                                                       Min
                                                                                                             Max
                   Estimate Std. Error z value Pr(>|z|)
                                                                  -2.75414 -0.14210 -0.07438
                                                                                                0.02086
                                                                                                         2.32520
(Intercept)
                   -9.638266
                               1.319450
                                        -7.305 2.78e-13
                                                                  Coefficients:
                               0.168876
thickness
                   0.528409
                                          3.129
                                                 0.00175 **
                                                                                   Estimate Std. Error z value Pr(>|z|)
unif_cell_size
                  -0.097515
                               0.273424
                                         -0.357
                                                 0.72136
                                                                                   -9.63477
                                                                  (Intercept)
                                                                                               1.31029 -7.353 1.94e-13 ***
                               0.272529
                                                 0.33272
unif_cell_shape
                   0.263986
                                          0.969
                                                                  thickness
                                                                                   0.52838
                                                                                               0.16881
                                                                                                        3.130 0.001748 **
marginal_adhesion 0.345806
                               0.166802
                                          2.073
                                                 0.03816 *
                                                                  unif_cell_size
                                                                                   -0.09693
                                                                                               0.27239
                                                                                                       -0.356 0.721943
cell size
                   0.004148
                               0.182814
                                          0.023
                                                 0.98190
                                                                  unif_cell_shape
                                                                                    0.26402
                                                                                               0.27263
                                                                                                        0.968 0.332836
                                          3.269
                                                 0.00108 **
bare_nuclei
                   0.375644
                               0.114905
                                                                  marginal_adhesion 0.34705
                                                                                               0.15742
                                                                                                        2.205 0.027478 *
band_chromatin
                   0.501770
                               0.183968
                                          2.727
                                                 0.00638 **
                                                                  bare_nuclei
                                                                                    0.37600
                                                                                               0.11391
                                                                                                        3.301 0.000964 ***
normal_nucleoli
                   0.173406
                               0.152506
                                          1.137
                                                 0.25552
                                                                  band_chromatin
                                                                                    0.50240
                                                                                               0.18188
                                                                                                        2.762 0.005741 **
                   0.619365
                               0.501148
                                          1.236
mitoses
                                                 0.21650
                                                                  normal_nucleoli
                                                                                    0.17390
                                                                                               0.15117
                                                                                                        1.150 0.249997
                                                                  mitoses
                                                                                    0.62038
                                                                                               0.49932
                                                                                                        1.242 0.214069
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
                                                                  Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
                                                                  (Dispersion parameter for binomial family taken to be 1)
    Null deviance: 507.343 on 399 degrees of freedom
Residual deviance: 74.866 on 390 degrees of freedom
                                                                      Null deviance: 507.343 on 399 degrees of freedom
                                                                  Residual deviance: 74.866 on 391 degrees of freedom
AIC: 94.866
                                                                  AIC: 92.866
```

Number of Fisher Scoring iterations: 8

Number of Fisher Scoring iterations: 8

```
yield_glm_backward <- predict(glm.fit.backward, newdata = TestSet, type='response')
MAE(y_pred = yield_glm_backward, y_true = as.numeric(TestSet$class))

## [1] 1.009169

MSE(y_pred = yield_glm_backward, y_true = as.numeric(TestSet$class))

## [1] 1.03568</pre>
```

MAE and MSE have the lower values.

# Step (3) MAE & MSE Again

```
glm.probs <- predict(glm.fit, TestSet, type="response")</pre>
glm.probs[1:20]
##
## 0.8958529825 0.0116622814 0.9999513801 0.0079474817 0.0009266467 0.0013256881
                                                 10
                                                             11
## 0.0063174258 0.9986258191 0.0022763852 0.6528355793 0.5329421765 0.0013465175
##
                        14
                                     15
                                                 16
                                                             17
                                                                          18
            13
## 0.0016872540 0.0021474490 0.0038237546 0.5692245457 0.9837381726 0.9987921929
            19
## 0.9991824692 0.8609674823
glm.predict <- rep(0, NROW(TestSet))</pre>
glm.predict[glm.probs > .5] = 1
glm.predict[1:20]
```

## Step (4) Accuracy

# Predicted Values Data Set

```
predictions <- prediction(glm.probs, TestSet$class)
t_performance <- performance(predictions, measure = "tpr", x.measure = "fpr")
performance(predictions, "auc")@y.values[[1]]</pre>
```

## [1] 0.9963786

**Accuracy 99.63%** 

## Step (4) Accuracy

modelFit <- train(class~., data=TrainingSet, method="glm")

Applying glm to TrainingSet to get model as an input

predictions <- predict(modelFit, newdata=TestSet)
confusionMatrix(predictions, TestSet\$class)</pre>

Predicted values in the frame new data, TestSet.

Predictions is categorized by confusionMatrix

#### Confusion Matrix and Statistics

Reference
Prediction Benign Malignant
Benign 187 4
Malignant 3 105

Accuracy : 0.9766

95% CI: (0.9524, 0.9905)

No Information Rate: 0.6355 P-Value [Acc > NIR]: <2e-16

Kappa : 0.9494

Mcnemar's Test P-Value : 1

Sensitivity: 0.9842
Specificity: 0.9633
Pos Pred Value: 0.9791
Neg Pred Value: 0.9722
Prevalence: 0.6355
Detection Rate: 0.6254
Detection Prevalence: 0.6388

'Positive' Class : Benign

Balanced Accuracy: 0.9738

# (Bonus) Confusion Matrix



# Step (3) Conclusion

THE MULTIPLE LINEAR REGRESSION MODEL WORKS WELL TO PREDICT THE RESPONSE.



# Q & A

#### Citations

- https://archive.ics.uci.edu/ml/machine-learningdatabases/breast-cancer-wisconsin/
- https://visualsonline.cancer.gov/details.cfm?imageid=2512

## Thank You!