

Lab 2: Convolution

ENGR 451 Digital Signal Processing



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Questions:

1. **Why do we have to pad these sequences with zeros?**
 - a. We pad the sequence with zeros to be able to easily add all the sequences in matlab. Matlab only lets you effectively add sequences of the same length
2. **In general, how does the number of sequences we have to sum the length of these sequences depend on the sizes of $x[n]$ and $h[n]$?**
 - a. When convolving X and H , the length always turns out to be the length of X and length of H minus 1
3. **Why the difference?**
 - a. There is a difference because the length is going to be the same no matter how you convolve it but X and H could have different lengths so the one with the shorter length will require more sequences to complete the convolution.
4. **Why the difference?**
 - a. There is a difference in matrix size because the lengths of X and H are different. Due to the difference property of matrices, the shorter length will have a small matrix.
5. **In, general how do the number of rows and columns of matrix depend on the lengths of the sequences $x[n]$ and $h[n]$?**
 - a. When multiplying the two vectors with size i and k to make a matrix of the size $i \times k$, we know that since we pad on the matrices that i won't change, what we can change is k . The smaller the vector, the smaller the size which means we will not to calculate as much when creating the new matrix.
6. **When is it more advantageous to compute $x[n]*h[n]$ and when is it better to compute $h[n]*x[n]$?**
 - a. The factor that really dictates what will be the most efficient way to calculate the convolution is the length of the X and H vectors. Whichever is the shorter length is the one you want to convolve with to make all the calculations shorter even though in the end, both will give the same result. Essentially, it is better to convolve the signal with the shortest length

Matlab Published Code

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```
% lab2.m
% Please place lab2.m in your working directory
% Provide the print-out from running this function
% using 'publish lab2'
%
% T. Holton 10 Sept 08

test_lab2;
```

Convolution, Part I

Convolution #1

```
x = sequence([1 2 6 -3 5], 1);
h = sequence([4 -1 5 3 2], -3);
test_lab2(x, h);
```

```
% Convolution #2
test_lab2(h, x);
```

```
% Convolution #3
h = sequence(1, 0);
test_lab2(x, h);
```

```
% Convolution #4
test_lab2(h, x);
```

```
% Convolution #5
x = sequence(cos(2 * pi * (1:50000) / 16), -5); % nice, big sequence
h = sequence(ones(1, 10), 10);
test_lab2(x, h);
```

```
% Convolution #6
test_lab2(h, x);
```

```
% Convolution #7
x = sequence(1, 2);
h = sequence(1, -1);
test_lab2(x, h);
```

```
% Convolution #8
test_lab2(h, x);
```

Problem #1

Your data are correct
Your offset is correct
Your elapsed time is 30.437 usecs
which is 3.05 times Holton's elapsed time (9.995 usecs)
and 3.89 times Matlab's elapsed time (7.831 usecs)

Problem #2

Your data are correct
Your offset is correct
Your elapsed time is 21.691 usecs
which is 3.1 times Holton's elapsed time (7.007 usecs)
and 8.39 times Matlab's elapsed time (2.584 usecs)

Problem #3

Your data are correct
Your offset is correct
Your elapsed time is 45.585 usecs
which is 0.527 times Holton's elapsed time (86.475 usecs)
and 0.459 times Matlab's elapsed time (99.265 usecs)

Problem #4

Your data are correct
Your offset is correct
Your elapsed time is 24.63 usecs
which is 0.875 times Holton's elapsed time (28.143 usecs)
and 3.66 times Matlab's elapsed time (6.722 usecs)

Problem #5

Your data are correct
Your offset is correct
Your elapsed time is 1854.75 usecs
which is 1.4 times Holton's elapsed time (1327.47 usecs)
and 18.6 times Matlab's elapsed time (99.553 usecs)

Problem #6

Your data are correct
Your offset is correct
Your elapsed time is 2039.65 usecs
which is 1.46 times Holton's elapsed time (1395.56 usecs)
and 22.8 times Matlab's elapsed time (89.622 usecs)

Problem #7

Your data are correct

Your offset is correct

Your elapsed time is 21.07 usecs

which is 3.28 times Holton's elapsed time (6.425 usecs)

and 3.79 times Matlab's elapsed time (5.562 usecs)

Problem #8

Your data are correct

Your offset is correct

Your elapsed time is 13.614 usecs

which is 3.84 times Holton's elapsed time (3.547 usecs)

and 7.16 times Matlab's elapsed time (1.901 usecs)

Real-time Convolution

Real-time convolution #1

```
x = [1 4 2 6 5];  
h = [4 -1 3 -5 2];  
test_lab2a;  
test_lab2a(x, h);
```

```
% Real-time convolution convolution #2
```

```
test_lab2a(h, x);
```

```
% Real-time convolution #3
```

```
x = cos(2 * pi * (1:50000) / 16); % nice, big sequence  
h = ones(1, 10);  
test_lab2a(x, h);
```

Real-time convolution #1

Your data are correct

Real-time convolution #2

Your data are correct

Real-time convolution #3

Your data are correct

Deconvolution

Deconvolution #1

```
h = sequence([1 3 2], 2);  
y = sequence([1 6 15 20 15 7 2], -1);  
test_lab2b;  
test_lab2b(y, h);
```

% Deconvolution #1

```
y = sequence([-1 -2 0 0 0 0 1 2], 2);  
test_lab2b(y, h);
```

Deconvolution problem #1

Your data are correct
Your offset is correct

Deconvolution problem #2

Your data are correct
Your offset is correct

Code

```
disp('-----')  
disp('          Code')  
disp('-----')  
type sequence  
type conv_rt
```

Code

```
classdef sequence  
    properties  
        data  
        offset  
    end  
  
    methods  
        function s = sequence(data, offset)  
            % SEQUENCE Sequence object  
            % S = SEQUENCE(DATA, OFFSET) creates sequence S  
            % using DATA and OFFSET  
            %  
            % Kevin Baltazar Reyes 13 Feb 2019  
            s.data = data;
```

```

    s.offset = offset;
end

```

```

function display(s)
    var = inputname(1);
    if (isempty(var))
        disp('ans =');
    else
        disp([var ' =']);
    end
    switch length(s.data)
        case 0
            disp(' data: []')
        case 1
            disp([' data: ', num2str(s.data)])
        otherwise
            disp([' data: [' num2str(s.data) ']'])
        end
    end
    disp([' offset: ' num2str(s.offset)])
end

```

```

function y = flip(x)
    % FLIP Flip a Matlab sequence structure, x, so y = x[-n]
    tempData = x.data(end:-1:1); %start with the end of the sequence then count down 1 each time

    tempOffset = -(x.offset+length(x.data) - 1);
    y = sequence(tempData,tempOffset);
end

```

```

function y = shift(x, no)
    % SHIFT Shift a Matlab sequence structure, x, by integer amount no so that y[n] = x[n - no]

    sameDataX=x.data; %data sequence remains the same, we are only shifting the offset
    newOffset=(x.offset+no); %new offset = previous offset + value you are shifting
    y=sequence(sameDataX,newOffset);
end

```

```

function x = trim(x)
    %takes zeros off from each side of sequence

    while x.data(end)==0
        x.data(end)=[];
    end

    while x.data(1)==0
        x.data(1)=[];
        x.offset=x.offset+1;
    end

end

```

```

function z = plus(x, y)
    % PLUS Add x and y. Either x and y will both be sequence structures, or one of them may be a number.

    if isa(x,'sequence')==0    %checks if x is a constant
        z=sequence(y.data+x,y.offset); %if x is a constant, add constant x to every data pt in y sequence, leave offset
untouched
        z=trim(z);
        return;
    end

    if isa(y,'sequence')==0    %same as above but instead
        z=sequence(x.data+y,x.offset);
        z=trim(z);
        return;
    end

    lx=length(x.data); %length of data in sequence x
    ly=length(y.data); %length of data in sequence y

    ody=y.offset-x.offset; %difference between sequence offsets IF Y HAS GREATER OFFSET THAN X
    odx=x.offset-y.offset; %%difference between sequence offsets IF X HAS GREATER OFFSET THAN Y

    x.data=[zeros(1,odx) x.data zeros(1,ody-(lx-ly))]; %add zeros to the beginning & end of sequence x as a "filler".
    You cannot perform operations between x & y if there is no data at a given index. The zeros are put in to fill these
    empty spots.
    y.data=[zeros(1,ody) y.data zeros(1,odx-(ly-lx))];

    off=min(x.offset,y.offset); %minimum offset between x & y
    z=sequence(x.data+y.data,off); %create sequence z as a result of adding sequence x & y together

    z=trim(z);

end

function z = minus(x, y)
    % MINUS Subtract x and y. Either x and y will both be sequence structures, or one of them may be a number.

    if isa(x,'sequence')==0
        z=sequence(x-y.data,y.offset);
        z=trim(z);
        return;
    end
    if isa(y,'sequence')==0
        z=sequence(x.data-y,x.offset);
        z=trim(z);
        return;
    end
end

```



```
Lx=length(x.data);
```

```
Ly=length(y.data);
```

```
ody=y.offset-x.offset;
```

```
odx=x.offset-y.offset;
```

```
x.data=[zeros(1,odx) x.data zeros(1,ody-(Lx-Ly))];
```

```
y.data=[zeros(1,ody) y.data zeros(1,odx-(Ly-Lx))];
```

```
off=min(x.offset,y.offset);
```

```
z=sequence(x.data-y.data,off);
```

```
z=trim(z);
```

```
end
```

```
function z = times(x, y)
```

% TIMES Multiply x and y (i.e. .*) Either x and y will both be sequence structures, or one of them may be a number.

```
if isa(x,'sequence')==0
```

```
    z=sequence(y.data*x,y.offset);
```

```
    return;
```

```
end
```

```
if isa(y,'sequence')==0
```

```
    z=sequence(x.data*y,x.offset);
```

```
    return;
```

```
end
```

```
Lx=length(x.data);
```

```
Ly=length(y.data);
```

```
ody=y.offset-x.offset;
```

```
odx=x.offset-y.offset;
```

```
x.data=[zeros(1,odx) x.data zeros(1,ody-(Lx-Ly))];
```

```
y.data=[zeros(1,ody) y.data zeros(1,odx-(Ly-Lx))];
```

```
off=min(x.offset,y.offset);
```

```
z=sequence(x.data.*y.data,off);
```

```
z=trim(z);
```

```
end
```

```
function stem(x)
```

% STEM Display a Matlab sequence, x, using a stem plot.

```
stem( x.offset : length(x.data )+x.offset-1,x.data);
```

```
end
```

```
function y = conv(x,h)
```

```

%CONV two finite-length Matlab sequence objects, x and h
% returning sequence object y

if (length(x.data) > length(h.data)) %if sequence h is shorter, convolve sequence h with matrix X (y=h*X)
    X = zeros(length(h.data), ((length(h.data)+length(x.data))-1)); %define X's dimensions and stuff with zeros:
    i=1; %X row length = sequence h data length
    j=1; %Y column length = length(h.data)+length(x.data)-1
    P = [x.data zeros(1,length(h.data)-1)]; %sequence x duplicated in P. length(x.data) + length of zeros stuffed
after MUST EQUAL length of sequence y for flip&shift method
    for n = 1:(length(h.data)) %outer loop for row increment
        for m = 1:((length(h.data)+length(x.data))-1) %inner loop for column increment
            X(i,j)=P(j); %value stored in P's current index goes to corresponding X index
            j=j+1; %index points to next column (next value of data in P)
        end
        P = circshift(P,[0,1]); %circular shift-right on vector P. Value of o inputted one time to open data slot
(leftmost slot)
        i=i+1; %index points to next row (P[k-n])
        j=1; %start from P's first data point (leftmost column)
    end
    y = sequence((h.data*X),(x.offset+h.offset)); %now that the matrix dimensions are correct, we can multiply
them together

else %convolve x with matrix H (y=x*H)
    H = zeros(length(x.data), ((length(h.data)+length(x.data))-1));
    i=1;
    j=1;
    P = [h.data zeros(1,length(x.data)-1)];

    for n=1:(length(x.data))
        for m = 1:((length(x.data)+length(h.data))-1)
            H(i,j)=P(j);
            j=j+1;
        end
        P = circshift(P,[0,1]);
        i=i+1;
        j=1;
    end
    y=sequence((x.data*H),(x.offset+h.offset));
end
end

function x = deconv(y,h) % x = y*H^(-1)
% DECONV Convolve finite-length Matlab sequence object, y,
% given impulse response object, h
% returning sequence object, x.

Lx = length(y.data)-length(h.data)+1; %length of sequence x
h_hat = zeros(Lx,Lx); %define Lx by Lx matrix
F = [h.data zeros(1, Lx-length(h.data))]; %sequence h duplicated in F. Add zeros after h.data so the length of F
== Lx

```

```

        %traverse vector F through Lx by Lx matrix h_hat. Shift right, cut
        %off data shifted out at the end of the vector
        for i=1:Lx
            h_hat(i,:) = [zeros(1,i-1) F(1:Lx-i+1)]; %shift right by 1 each row by adding one zero per row in front, and
            cutting 1 data per row at end
        end
        x = sequence(y.data(1:Lx)*inv(h_hat), y.offset-h.offset); %only need to sample enough y.data to equal
        length(x.data). (length(y.data) MUST equal row & column length for h_hat
        end

    end
end

function y = conv_rt(x,h)
% Convolve two finite-length arrays, x and h returning array, y
h_hat = h(end:-1:1);
x_hat = [zeros(1,length(h)-1) x zeros(1,length(h)-1)];
y = zeros(1,length(x)+length(h)-1);

for i=1:length(x)+length(h)-1
    y(i) = sum(h_hat.*x_hat(i:i+length(h)-1));
end
end

```