

Multi-dimensional grids/blocks and coalescence

Oguz Kaya

Assistant Professor
Université Paris-Saclay, Gif-sur-Yvette, France



Objectives

- Use 2D and 3D block indices
- Perform “fast” memory access to the global GPU memory
- Programming exercise on GPU matrix multiplication

Outline

1 Multidimensional indexing of blocks and threads

2 Coalescence

3 Lab assignment: Matrix multiplication

Outline

- 1 Multidimensional indexing of blocks and threads
- 2 Coalescence
- 3 Lab assignment: Matrix multiplication

Multiplication of a 1D array by blocks

Summary of the multiplication example of an 1D array by blocks

```
#include <cstdio>
#include "cuda.h"

#define N 1024
float A[N];
float c = 2.0;

__device__ float dA[N];

__global__ void multiplyArray(int n, float c)
{
    int i = blockIdx.x;
    dA[i] *= c;
}

int main(int argc, char **argv)
{
    // Initialisation
    for (int i = 0; i < N; i++) { A[i] = i; }
    // Copier le tableau vers le GPU
    cudaMemcpyToSymbol(dA, A, N * sizeof(float), 0,
        cudaMemcpyHostToDevice);
    multiplyArray<<<N, 1>>>(N, c);
    // Recopier le tableau multiplié vers le CPU
    cudaMemcpyFromSymbol(A, dA, N * sizeof(float), 0,
        cudaMemcpyDeviceToHost);
    return 0;
}
```

- Multiply each element of a 1D array with constant c using a grid of blocks
- Each block multiplies 1 element
- Execute the kernel using N blocks
- **Question:** What would we do if the array were 2D, i.e. $A[N][N]$?

Multiplication of a 2D array by blocks

```
#include <cstdio>
#include "cuda.h"

#define N 2048
float A[N][N];
float c = 2.0;

__device__ float dA[N][N];

__global__ void multiplyArray2D(int n, float c)
{
    int i = blockIdx.x / n;
    int j = blockIdx.x % n;
    dA[i][j] *= c;
}

int main(int argc, char **argv)
{
    // Initialisation
    for (int i = 0; i < N; i++) {
        for (int j = 0; j < N; j++) { A[i][j] = i + j; }
    }
    // Copier le tableau vers le GPU
    cudaMemcpyToSymbol(dA, A, N * N * sizeof(float), 0,
        cudaMemcpyHostToDevice);
    multiplyArray2D<<<N * N, 1>>>(N, c);
    // Recopier le tableau multiplié vers le CPU
    cudaMemcpyFromSymbol(A, dA, N * N * sizeof(float), 0,
        cudaMemcpyDeviceToHost);
    printf("%f\n", A[1][2]);
    return 0;
}
```

- Multiply each element of $A[N][N]$ by a constant c
- Each block multiplies 1 element
- We need N^2 blocks in total.
- Each group of N consecutive blocks multiply a row of A
- With division and modulus, we can find indices i, j for $A[i][j]$ to be multiplied by each block

Multiplication of a 2D array by a grid of 2D blocks

```
#include <csdio>
#include "cuda.h"

#define N 2048
float A[N][N];
float c = 2.0;

__device__ float dA[N][N];

__global__ void multiplyArray2D(int n, float c)
{
    dA[blockIdx.x][blockIdx.y] *= c;
}

int main(int argc, char **argv)
{
    // Initialisation
    for (int i = 0; i < N; i++) {
        for (int j = 0; j < N; j++) { A[i][j] = i + j; }
    }
    // Copier le tableau vers le GPU
    cudaMemcpyToSymbol(dA, A, N * N * sizeof(float), 0,
        cudaMemcpyHostToDevice);
    dim3 dimGrid;
    dimGrid.x = N;
    dimGrid.y = N;
    dimGrid.z = 1;
    multiplyArray2D<<<dimGrid, 1>>>(N, c);
    // Recopier le tableau multiplié vers le CPU
    cudaMemcpyFromSymbol(A, dA, N * N * sizeof(float), 0,
        cudaMemcpyDeviceToHost);
    printf("%f\n", A[1][2]);
    return 0;
}
```

- Multiply each element of $A[N][N]$ by a constant c
- Each block multiplies 1 element
- **dim3** defines a 3D index topology for blocks in a grid (**dim3.{x,y,z}**).
- Use **dim3.x = dim3.y = N** and **dim3.z = 1** pour 2D.
- Total number of blocks is **dim3.x * dim3.y * dim3.z**
- No need for division or modulus tricks to find i and j

Multiplication of a 2D array by 2D blocks and 1D threads

```
#include <csstdio>
#include "cuda.h"

#define N 2048
float A[N][N];
float c = 2.0;

__device__ float dA[N][N];

__global__ void multiplyArray2D(int n, float c)
{
    int i = blockIdx.x;
    int j = blockIdx.y * blockDim.x + threadIdx.x;
    if (j < n) { dA[i][j] *= c; }

    int main(int argc, char **argv)
    {
        // Initialisation
        for (int i = 0; i < N; i++) {
            for (int j = 0; j < N; j++) { A[i][j] = i + j; }
        }

        // Copier le tableau vers le GPU
        cudaMemcpyToSymbol(dA, A, N * N * sizeof(float), 0,
                           cudaMemcpyHostToDevice);
        int blockSize = 1024;
        dim3 dimGrid;
        dimGrid.x = N;
        dimGrid.y = N / blockSize;
        dimGrid.z = 1;
        multiplyArray2D<<<dimGrid, blockSize>>>(N, c);
        // Recopier le tableau multiplié vers le CPU
        cudaMemcpyFromSymbol(A, dA, N * N * sizeof(float), 0,
                           cudaMemcpyDeviceToHost);
        printf("%f\n", A[1][2]);
        return 0;
    }
}
```

- Multiply each element of $A[N][N]$ by a constant c
- Each block multiplies **blockSize** elements
- Each thread multiplies 1 element
- Threads in a block work on **blockSize** consecutive elements in a **row** of A .
- Need to launch $N^2 / \text{blockSize}$ blocks in total.
- Each block multiplies a part of a row of A
- Need to make sure not to make out-of-bounds memory accesses for the last threads

Multiplication of a 2D array by 2D blocks and 1D threads

```
#include <csdio>
#include "cuda.h"

#define N 2048
float A[N][N];
float c = 2.0;

__device__ float dA[N][N];

__global__ void multiplyArray2D(int n, float c)
{
    int i = blockIdx.x * blockDim.x + threadIdx.x;
    int j = blockIdx.y;
    if (i < n) { dA[i][j] *= c; }

    int main(int argc, char **argv)
    {
        // Initialisation
        for (int i = 0; i < N; i++) {
            for (int j = 0; j < N; j++) { A[i][j] = i + j; }
        }
        // Copier le tableau vers le GPU
        cudaMemcpyToSymbol(dA, A, N * N * sizeof(float), 0,
                           cudaMemcpyHostToDevice);
        int blockSize = 1024;
        dim3 dimGrid;
        dimGrid.x = N / blockSize;
        dimGrid.y = N;
        dimGrid.z = 1;
        multiplyArray2D<<<dimGrid, blockSize>>>(N, c);
        // Recopier le tableau multiplié vers le CPU
        cudaMemcpyFromSymbol(A, dA, N * N * sizeof(float), 0,
                           cudaMemcpyDeviceToHost);
        printf("%f\n", A[1][2]);
        return 0;
    }
}
```

- Each thread multiplies 1 element
- Need to launch $N^2/\text{blockSize}$ blocks in total.
- Threads in a block work on **blockSize** consecutive elements in a **column** of A .
- Need to launch $N^2/\text{blockSize}$ blocks in total.
- Each block multiplies a part of a column of A
- Need to make sure not to make out-of-bounds memory accesses for the last threads
- Which one is better (row-based or col-based)?
- What happens if A has few rows/columns?

Multiplication of a 2D array by 2D blocks and 1D threads

```
#include <csstdio>
#include "cuda.h"

#define N 2048
float A[N][N];
float c = 2.0;

__device__ float dA[N][N];

__global__ void multiplyArray2D(int n, float c)
{
    int i = blockIdx.x * blockDim.x + threadIdx.x / blockDim.y;
    int j = blockIdx.y * blockDim.y + threadIdx.x % blockDim.y;
    if (i < n && j < n) { dA[i][j] *= c; }

    int main(int argc, char **argv)
    {
        // Initialisation
        for (int i = 0; i < N; i++) {
            for (int j = 0; j < N; j++) { A[i][j] = i + j; }
        }
        // Copier le tableau vers le GPU
        cudaMemcpyToSymbol(dA, A, N * N * sizeof(float), 0,
                           cudaMemcpyHostToDevice);
        int blockSize = 1024;
        dim3 dimGrid;
        dimGrid.x = N / 32;
        dimGrid.y = N / 32;
        dimGrid.z = 1;
        multiplyArray2D<<<dimGrid, blockSize>>>(N, c);
        // Recopier le tableau multiplié vers le CPU
        cudaMemcpyFromSymbol(A, dA, N * N * sizeof(float), 0,
                           cudaMemcpyDeviceToHost);
        printf("%f\n", A[1][2]);
        return 0;
    }
}
```

- Organize **blockSize = 1024** threads in 2D
- Each block works on a submatrix of size 32×32
- Consecutive threads work on the same **row**
- Find i and j with division and modulus

Multiplication of a 2D array by 2D blocks and 1D threads

```
#include <csdio>
#include "cuda.h"

#define N 2048
float A[N][N];
float c = 2.0;

__device__ float dA[N][N];

__global__ void multiplyArray2D(int n, float c)
{
    int i = blockIdx.x * blockDim.x + threadIdx.x / blockDim.y;
    int j = blockIdx.y * blockDim.y + threadIdx.x % blockDim.y;
    if (i < n && j < n) { dA[i][j] *= c; }

    int main(int argc, char **argv)
    {
        // Initialisation
        for (int i = 0; i < N; i++) {
            for (int j = 0; j < N; j++) { A[i][j] = i + j; }
        }
        // Copier le tableau vers le GPU
        cudaMemcpyToSymbol(dA, A, N * N * sizeof(float), 0,
                           cudaMemcpyHostToDevice);
        int blockSize = 1024;
        dim3 dimGrid;
        dimGrid.x = N / 32;
        dimGrid.y = N / 32;
        dimGrid.z = 1;
        multiplyArray2D<<<dimGrid, blockSize>>>(N, c);
        // Recopier le tableau multiplié vers le CPU
        cudaMemcpyFromSymbol(A, dA, N * N * sizeof(float), 0,
                           cudaMemcpyDeviceToHost);
        printf("%f\n", A[1][2]);
        return 0;
    }
}
```

- Organize **blockSize = 1024** threads in 2D
- Each block works on a submatrix of size 32×32
- Consecutive threads work on the same **column**
- Find i and j with division and modulus
- Which one is better (row-based or col-based)?

Multiplication of a 2D array by 2D blocks and 1D threads

```
#include <csstdio>
#include "cuda.h"

#define N 2048
float A[N][N];
float c = 2.0;

__device__ float dA[N][N];

__global__ void multiplyArray2D( int n, float c )
{
    int i = blockIdx.x * blockDim.x + threadIdx.x;
    int j = blockIdx.y * blockDim.y + threadIdx.y;
    if ( i < n && j < n ) { dA[i][j] *= c; }

}

int main( int argc, char **argv )
{
    // Initialisation
    for ( int i = 0; i < N; i++ ) {
        for ( int j = 0; j < N; j++ ) { A[i][j] = i + j; }
    }

    // Copier le tableau vers le GPU
    cudaMemcpyToSymbol(dA, A, N * N * sizeof(float), 0,
                      cudaMemcpyHostToDevice);
    dim3 dimBlock;
    dimBlock.x = 32;
    dimBlock.y = 32;
    dimBlock.z = 1;
    dim3 dimGrid;
    dimGrid.x = N / 32;
    dimGrid.y = N / 32;
    dimGrid.z = 1;
    multiplyArray2D<<<dimGrid, dimBlock>>>(N, c);
    // Recopier le tableau multiplié vers le CPU
    cudaMemcpyFromSymbol(A, dA, N * N * sizeof(float), 0,
                      cudaMemcpyDeviceToHost);
    printf("%f\n", A[1][2]);
    return 0;
}
```

- Use a **dim3** for 2D indexing of threads, with **dim3.x = dim3.y = 32** and **dim3.z = 1**
- Threads with consecutive **threadIdx.x** are put in the same warp (then using **threadIdx.y**, then **threadIdx.z**)
- Therefore, each warp touches a **column** of **A**

Multiplication of a 2D array by 2D blocks and 1D threads

```
#include <csdio>
#include "cuda.h"

#define N 2048
float A[N][N];
float c = 2.0;

__device__ float dA[N][N];

__global__ void multiplyArray2D(int n, float c)
{
    int i = blockIdx.x * blockDim.x + threadIdx.x;
    int j = blockIdx.y * blockDim.y + threadIdx.y;
    if (i < n && j < n) { dA[i][j] *= c; }

}

int main(int argc, char **argv)
{
    // Initialisation
    for (int i = 0; i < N; i++) {
        for (int j = 0; j < N; j++) { A[i][j] = i + j; }
    }
    // Copier le tableau vers le GPU
    cudaMemcpyToSymbol(dA, A, N * N * sizeof(float), 0,
                      cudaMemcpyHostToDevice);
    dim3 dimBlock;
    dimBlock.x = 32;
    dimBlock.y = 32;
    dimBlock.z = 1;
    dim3 dimGrid;
    dimGrid.x = N / 32;
    dimGrid.y = N / 32;
    dimGrid.z = 1;
    multiplyArray2D<<<dimGrid, dimBlock>>>(N, c);
    // Recopier le tableau multiplié vers le CPU
    cudaMemcpyFromSymbol(A, dA, N * N * sizeof(float), 0,
                      cudaMemcpyDeviceToHost);
    printf("%f\n", A[1][2]);
    return 0;
}
```

- Use a **dim3** for 2D indexing of threads, with **dim3.x = dim3.y = 32** and **dim3.z = 1**
- Threads with consecutive **threadIdx.x** are put in the same warp (then using **threadIdx.y**, then **threadIdx.z**)
- Therefore, each warp touches a **row** of **A**
- Which one is better (row-based or col-based)?

Dimension limits for grids and blocks

For a grid, need to have

- **dim3.x** $\leq 2^{31} - 1$
- **dim3.y** ≤ 65535
- **dim3.z** ≤ 65535

For a block, need to have

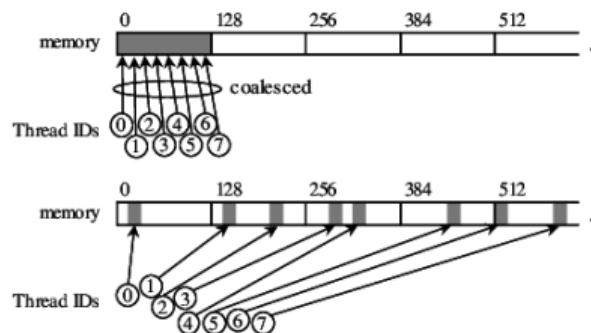
- **dim3.x** ≤ 1024
- **dim3.y** ≤ 1024
- **dim3.z** ≤ 64
- Total number of threads in a block ≤ 1024

Outline

- 1 Multidimensional indexing of blocks and threads
- 2 Coalescence
- 3 Lab assignment: Matrix multiplication

Coalescence

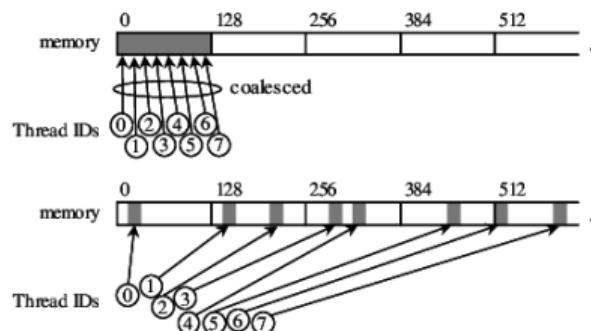
Coalescence pertains to accesses to the main memory from threads within a warp.



- Threads within a warp execute instructions **synchronously**
- Each memory access is equally treated **synchronously**
- If threads access to consecutive elements in the memory, it requires reading/writing one memory line (thus performs 1 memory access)

Coalescence (cont.)

Il s'agit d'accès à la mémoire globale des threads dans un warp.



- If the access is scattered, each touched line will be read
 - In the worst case, 32 lines might be read for a single warp access
 - Most read elements will not be used; bandwidth wasted.
- **Rule:** Design the kernel so that the accesses are contiguous on **threadIdx.x** (and then **threadIdx.y**, then **threadIdx.z**)

Example: Multiplication of a 2D array

Multiply each element of an array $A[N][N]$ with a scalar c

```
#include <csdio>
#include "cuda.h"

#define N 2048
float A[N][N];
float c = 2.0;

__device__ float dA[N][N];

__global__ void multiplyArray2D(int n, float c)
{
    int i = blockIdx.x;
    int j = blockIdx.y * blockDim.x + threadIdx.x;
    if (j < n) { dA[i][j] *= c; }
}

int main(int argc, char **argv)
{
    // Initialisation
    for (int i = 0; i < N; i++) {
        for (int j = 0; j < N; j++) { A[i][j] = i + j; }
    }
    // Copier le tableau vers le GPU
    cudaMemcpyToSymbol(dA, A, N * N * sizeof(float), 0,
        cudaMemcpyHostToDevice);
    int blockSize = 1024;
    dim3 dimGrid;
    dimGrid.x = N;
    dimGrid.y = N / blockSize;
    dimGrid.z = 1;
    multiplyArray2D<<<dimGrid, blockSize>>>(N, c);
    // Recopier le tableau multiplié vers le CPU
    cudaMemcpyFromSymbol(A, dA, N * N * sizeof(float), 0,
        cudaMemcpyDeviceToHost);
    printf("%f\n", A[1][2]);
    return 0;
}
```

- Is this **coalescent**?
- Yes! Matrix is stored by rows, **threadIdx.x** aligned with rows

Example: Multiplication of a 2D array

Multiply each element of an array $A[N][N]$ with a scalar c

```
#include <csdio>
#include "cuda.h"

#define N 2048
float A[N][N];
float c = 2.0;

__device__ float dA[N][N];

__global__ void multiplyArray2D(int n, float c)
{
    int i = blockIdx.x * blockDim.x + threadIdx.x;
    int j = blockIdx.y;
    if (i < n) { dA[i][j] *= c; }
}

int main(int argc, char **argv)
{
    // Initialisation
    for (int i = 0; i < N; i++) {
        for (int j = 0; j < N; j++) { A[i][j] = i + j; }
    }
    // Copier le tableau vers le GPU
    cudaMemcpyToSymbol(dA, A, N * N * sizeof(float), 0,
                      cudaMemcpyHostToDevice);
    int blockSize = 1024;
    dim3 dimGrid;
    dimGrid.x = N / blockSize;
    dimGrid.y = N;
    dimGrid.z = 1;
    multiplyArray2D<<<dimGrid, blockSize>>>(N, c);
    // Recopier le tableau multiplié vers le CPU
    cudaMemcpyFromSymbol(A, dA, N * N * sizeof(float), 0,
                      cudaMemcpyDeviceToHost);
    printf("%f\n", A[1][2]);
    return 0;
}
```

- Is this **coalescent**?
- No! Matrix is stored by rows, **threadIdx.x** aligned with columns
- 32 lines will be read for each memory access performed by a warp

Example: Multiplication of a 2D array

Multiply each element of an array $A[N][N]$ with a scalar c

```
#include <csdio>
#include "cuda.h"

#define N 2048
float A[N][N];
float c = 2.0;

__device__ float dA[N][N];

__global__ void multiplyArray2D(int n, float c)
{
    int i = blockIdx.x * blockDim.x + threadIdx.x;
    int j = blockIdx.y * blockDim.y + threadIdx.y;
    if (i < n && j < n) { dA[i][j] *= c; }
}

int main(int argc, char **argv)
{
    // Initialisation
    for (int i = 0; i < N; i++) {
        for (int j = 0; j < N; j++) { A[i][j] = i + j; }
    }
    // Copier le tableau vers le GPU
    cudaMemcpyToSymbol(dA, A, N * N * sizeof(float), 0,
                      cudaMemcpyHostToDevice);
    dim3 dimBlock;
    dimBlock.x = 32;
    dimBlock.y = 32;
    dimBlock.z = 1;
    dim3 dimGrid;
    dimGrid.x = N / 32;
    dimGrid.y = N / 32;
    dimGrid.z = 1;
    multiplyArray2D<<<dimGrid, dimBlock>>>(N, c);
    // Recopier le tableau multiplié vers le CPU
    cudaMemcpyFromSymbol(A, dA, N * N * sizeof(float), 0,
                      cudaMemcpyDeviceToHost);
    printf("%f\n", A[1][2]);
}
```

- Is this **coalescent**?
- No! Matrix is stored by rows, **threadIdx.x** is aligned with columns.
- 32 lines will be read for each memory access performed by a warp

Example: Multiplication of a 2D array

Multiply each element of an array $A[N][N]$ with a scalar c

```
#include <cstdio>
#include "cuda.h"

#define N 2048
float A[N][N];
float c = 2.0;

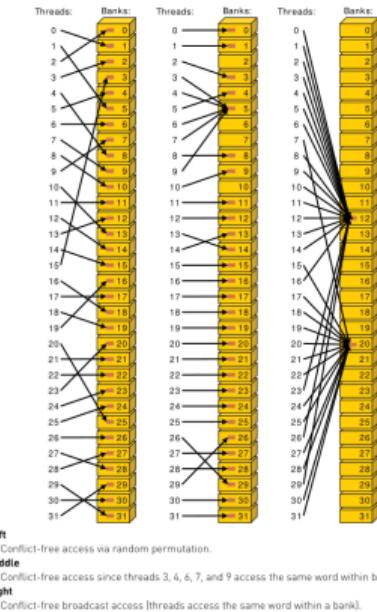
__device__ float dA[N][N];

__global__ void multiplyArray2D(int n, float c)
{
    int i = blockIdx.x * blockDim.y + threadIdx.y;
    int j = blockIdx.y * blockDim.x + threadIdx.x;
    if (i < n && j < n) { dA[i][j] *= c; }
}

int main(int argc, char **argv)
{
    // Initialisation
    for (int i = 0; i < N; i++) {
        for (int j = 0; j < N; j++) { A[i][j] = i + j; }
    }
    // Copier le tableau vers le GPU
    cudaMemcpyToSymbol(dA, A, N * N * sizeof(float), 0,
                      cudaMemcpyHostToDevice);
    dim3 dimBlock;
    dimBlock.x = 32;
    dimBlock.y = 32;
    dimBlock.z = 1;
    dim3 dimGrid;
    dimGrid.x = N / 32;
    dimGrid.y = N / 32;
    dimGrid.z = 1;
    multiplyArray2D<<<dimGrid, dimBlock>>>(N, c);
    // Recopier le tableau multiplié vers le CPU
    cudaMemcpyFromSymbol(A, dA, N * N * sizeof(float), 0,
                      cudaMemcpyDeviceToHost);
    printf("%f\n", A[1][2]);
}
```

- Is this **coalescent**?
- Yes! Matrix is stored by rows, **threadIdx.x** is aligned with rows

Coalescence rules



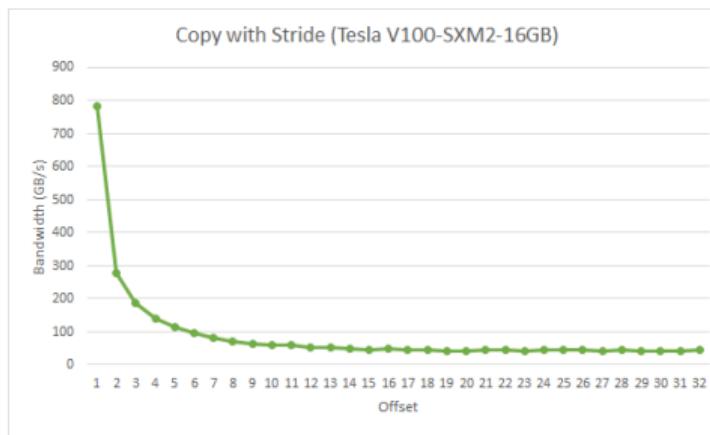
- Threads in a warp accessing the same memory slot = good performance (however, bandwidth is still potentially wasted).
- Threads in a warp accessing the same **memory line** in a **random** order = still good performance in new architectures (Volta and later).
- If coalescent access is difficult to do, **shared memory** might be useful (we will see soon).

Example: Strided memory access to an array

```
--device__ float dA[N];  
--global__ void stridedAccess(int stride)  
{  
    float f = dA[threadIdx.x * stride];  
    // ...  
}
```

- How does performance evolve in terms of **stride**?
- For **stride** = 1, reading a single line of 128 bytes.
- For **stride** = 2, reading two lines of 128 bytes (half of which is unused).
- ...
- For **stride** = 32, reading 32 lines of 128 bytes (31/32 of which is unused).

Example: Strided memory access to an array (cont.)



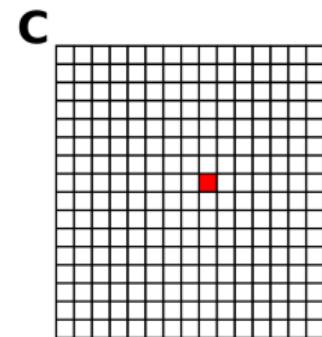
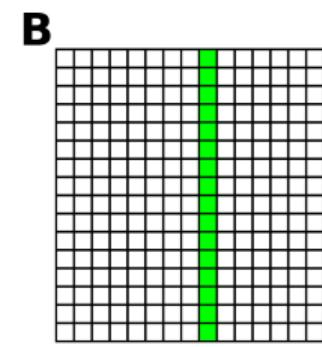
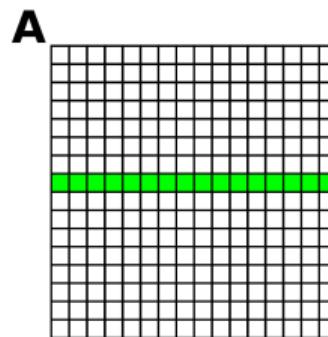
- Effective bandwidth falls rapidly.

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Matrix multiplication

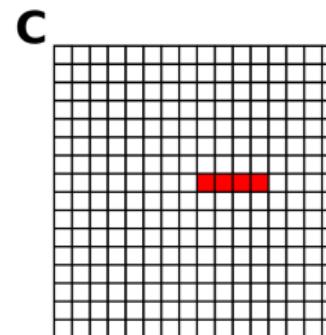
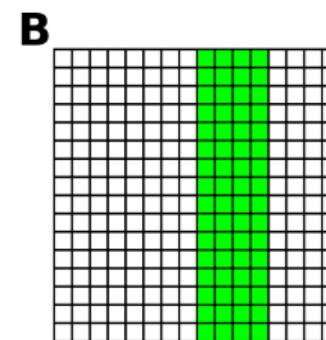
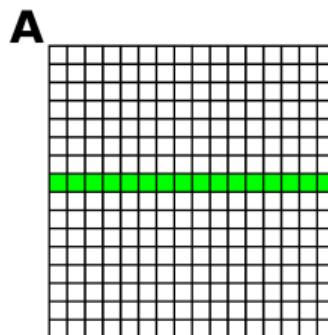
Let A, B, C be $N \times N$ matrices.



- The multiplication $C = AB$ corresponds to the computation $C[i][j] = \sum_{k=0}^{N-1} A[i][k]B[k][j]$.
- First kernel: Create one block/thread to compute each $C[i][j]$.

Matrix multiplication

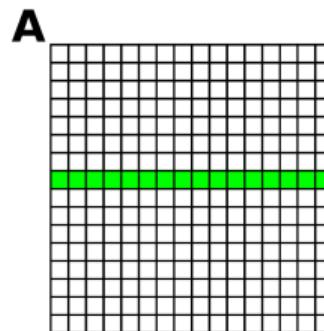
Let A, B, C be $N \times N$ matrices.



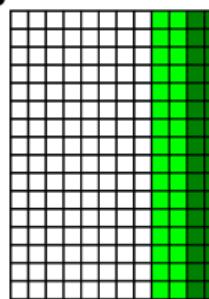
- The multiplication $C = AB$ corresponds to the computation $C[i][j] = \sum_{k=0}^{N-1} A[i][k]B[k][j]$.
- Second kernel: Use P threads per block, each block computing P consecutive elements of a row of C ($P = 4$ in this figure).
- Suppose that N is divisible by P .

Matrix multiplication

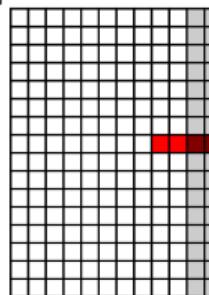
Let A, B, C be $N \times N$ matrices.



B



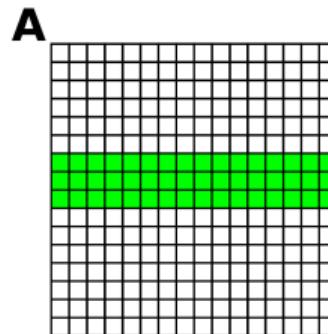
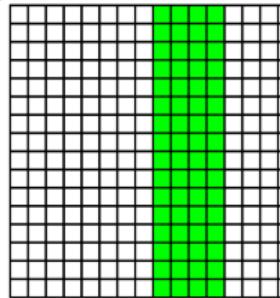
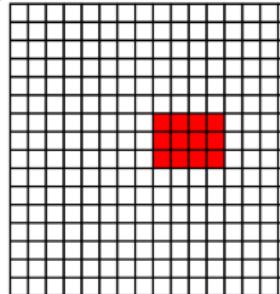
C



- The multiplication $C = AB$ corresponds to the computation $C[i][j] = \sum_{k=0}^{N-1} A[i][k]B[k][j]$.
- Second kernel: Use P threads per block, each block computing P consecutive elements of a row of C ($P = 4$ in this figure).
- Suppose that N is **not** divisible by P .

Matrix multiplication

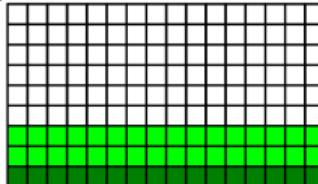
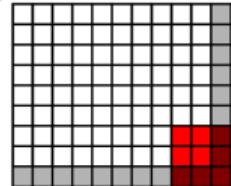
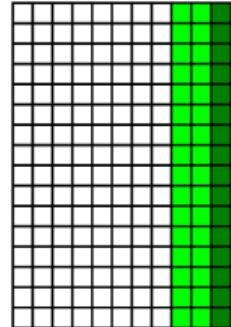
Let A, B, C be $N \times N$ matrices.

**B****C**

- The multiplication $C = AB$ corresponds to the computation $C[i][j] = \sum_{k=0}^{N-1} A[i][k]B[k][j]$.
- Fourth kernel: Use $P \times Q$ threads per block, each block computing $P \times Q$ consecutive elements in a tile of C ($P = 4$ et $Q = 3$ in this figure).
- Suppose that N is divisible by P and Q .

Matrix multiplication

Let A, B, C be $N \times N$ matrices.

A**C****B**

- The multiplication $C = AB$ corresponds to the computation $C[i][j] = \sum_{k=0}^{N-1} A[i][k]B[k][j]$.
- Fourth kernel: Use $P \times Q$ threads per block, each block computing $P \times Q$ consecutive elements in a tile of C ($P = 4$ et $Q = 3$ in this figure).
- Suppose that N is **not** divisible by P and Q .

Contact

Oguz Kaya

Université Paris-Saclay and LISN, Paris, France

oguz.kaya@universite-paris-saclay.fr

www.oguzkaya.com