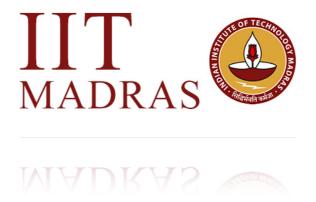
Functional Programming in F*

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Adapted from VTSA 2019 course on Program Verification with F*

Program verification Shall the twain ever meet?

Interactive proof assistants		Semi-automated verifiers of imperative programs
Coq,	air	Dafny,
Agda,		FramaC,
Lean,	gap	Why3,
Isabelle		Liquid Types

- **Left corner:** very expressive higher-order logics, interactive proving, tactics, but mostly only purely functional programming
- **Right corner:** effectful programming, SMT-based automation, but only very weak logics

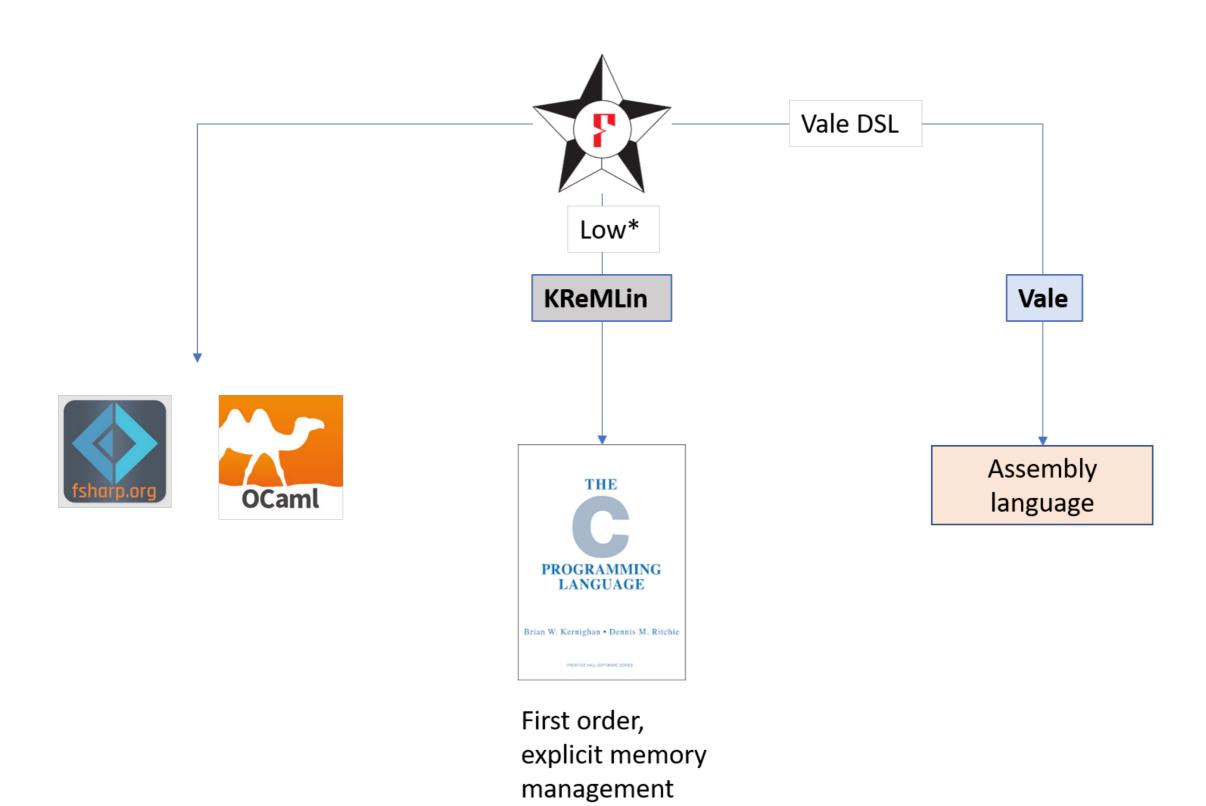
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 - ◆ Like Dafny, Frama-C, Why3, Liquid Types,...
- Expressive core language based on dependent type theory
 - ◆ Like Coq, NuPRL, Agda, Lean,...
- A metaprogramming and tactic framework for interactive proof and user-defined automation
 - ◆ Like Coq, NuPRL, Isabelle, HOL, Lean, ...

Running F* programs



Uses of F* in Project Everest

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- Project Everest: verify and deploy new, efficient HTTPS stack
 - → miTLS: Verified reference implementation of TLS (1.2 and 1.3)
 - ◆ EverParse: Verified parsers and formatter generators
 - ◆ EverCrypt: Agile Cryptographic Provider
 - ◆ HACL*: High-Assurance Cryptographic Library
 - ♦ Vale: Verified Assembly Language for Everest

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 - ♦ Vale: Verified Assembly Language for Everest
- Verified Everest code deployed in
 - Firefox (Mozilla NSS crypto), Windows (WinQUIC), Azure Confidential Consortium (Verified Merkle tree for the blockchain), WireGuard VPN, Zinc crypto library for Linux, Tezos and Concordium blockchains

Refinement Types

```
type nat = x:int{x >= 0}
```

Refinements introduced by type annotations (code unchanged)

```
val factorial : nat -> nat
let rec factorial n = if n = 0 then 1 else n * (factorial (n - 1))
```

Logical obligations discharged by SMT (for else branch, simplified)

```
n \ge 0, n <> 0 \mid = n - 1 >= 0

n \ge 0, n <> 0, (factorial (n - 1)) >= 0 \mid = n * (factorial <math>(n - 1)) >= 0
```

Refinement Types

• Refinements eliminated by subtyping: nat <: int

```
let i : int = factorial 42
let f : x:nat{x > 0} -> int = factorial
```

Total Functions

- The F* functions we saw so far were all total
- Tot effect (default) = no side-effects, terminates on all inputs

```
val factorial : nat -> Tot nat
let rec factorial n =
  if n = 0 then 1 else n * (factorial (n - 1))
```

Quiz: How about giving this weaker type to factorial?

```
val factorial : int -> Tot int
```

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factorial (-1) loops! (int type in F* is unbounded)

Semantic Termination Checking

- based on well-founded ordering on expressions (<<)
 - naturals related by < (negative integers unrelated)
 - inductives related by subterm ordering
 - lex tuples % [a;b;c] with lexicographic ordering
- order constraints discharged by the SMT solver
- arbitrary total expression as decreases metric

```
val ackermann: m:nat -> n:nat -> Tot nat (decreases %[m;n])
let rec ackermann m n =
   if m = 0 then n + 1
   else if n = 0 then ackermann (m - 1) 1
   else ackermann (m - 1) (ackermann m (n - 1))
```

default metric is lex ordering of all (non-function) args

```
val ackermann: m:nat -> n:nat -> Tot nat
```

Divergence Effect (Dv)

We might not want to prove that our code always terminates

```
val factorial : int -> Dv int
```

- Some useful code might not always terminate
 - ◆ An evaluator for lambda expressions

- ♦ A webserver
- In Coq, we had to write such code as an inductive type and not a Fixpoint

Effect System

- Pure code cannot call potentially divergent code
- Only pure code can appear in specifications

```
val factorial : int -> Dv int
type tau = x:int{x = factorial (-1)}
```

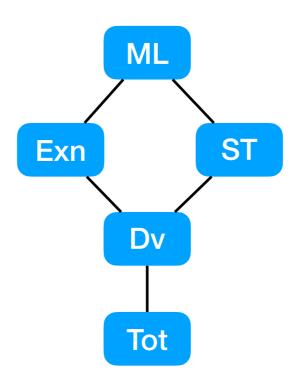
- Sub-effecting: Tot t <: Dv t
- So, divergent code can include pure code

```
incr 2 + factorial (-1) : Dv int
```

Effect System: Other effects

- Tot and Dv are just two of the possible effects. Some others include:
 - ◆ ST the effect of a computation that may diverge, read, write or allocate new references in the heap
 - ★ Exn the effect of a computation that may diverge or raise an exception
 - ◆ ML the effect of a computation that may diverge, read, write or allocate, or raise an exception

Effect System: Lattice



• **Sub-effecting:** Computations at a particular effect can be considered to be computations at an effect higher up the lattice

```
let baz () : Dv int = incr 2 + factorial3 (-1)
```

Switch to Code Example

Fin!