

$$f(t, y) = -ay$$

$$\hat{y}_{i+1} = \hat{y}_i + h(-a\hat{y}_i)$$

$$= (1 - ah)(\hat{y}_i)$$

$$\Rightarrow \hat{y}_i = (1 - ah)^i y_0$$

We find that if $|1 - ah| > 1$ then the equation will explode so for Euler's method to work, we need $|1 - ah| < 1$ which implies $0 < ah < 2$ and finally: $h < \frac{2}{a}$

The last part is just an easy rearrangement of the equation:

$$\hat{y}_{i+1} = \hat{y}_i - 10h\hat{y}_{i+1}$$

$$\hat{y}_{i+1} = \frac{\hat{y}_i}{1 + 10h}$$

$$\hat{y}_i = \frac{y_0}{(1+10h)^i} \text{ which is stable since } h \text{ is positive}$$