

New Subroutine:

```
import numpy as np

def fixedpt(f, x0, tol, Nmax):

    x = np.zeros((Nmax, 1))

    count = 0
    while (count < Nmax):
        x1 = f(x0)
        if (abs(x1-x0) < tol):
            xstar = x1
            ier = 0
            a = count
            x0 = x1
            x[count] = x1
            count += 1

    xstar = x1
    ier = 1
    return (x, a)

f = lambda x: (10/(x+4))**(1/2)
tol = 10**-10
Nmax = 100

x0 = 1.5
(x, a) = fixedpt(f, x0, tol, Nmax)
print(a)
```

★ x is vector of approximations
 a is number of iterations to converge with tol

$$1) \lim_{n \rightarrow \infty} \frac{|\hat{p}_{n+1} - p|}{|\hat{p}_n - p|^\alpha} = \lambda$$

$$\frac{|\hat{p}_{n+1} - p|}{\lambda} = |\hat{p}_n - p|^\alpha$$

$$\lim_{n \rightarrow \infty} \log_{|\hat{p}_n - p|} \left(\frac{|\hat{p}_{n+1} - p|}{\lambda} \right) = \alpha$$

2a) 1) (from new subroutine)

$$2b) \log_{|\hat{p}_n - p|} \left(\frac{|\hat{p}_{n+1} - p|}{\lambda} \right) = \alpha$$

$\alpha = 1, \lambda < 1$ (linear convergence)