

Global and Local Image Warping

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16-726 Learning-based Image Synthesis, Spring 2021

Image Transformations

image filtering: change **range** of image

$$g(x) = T(f(x))$$

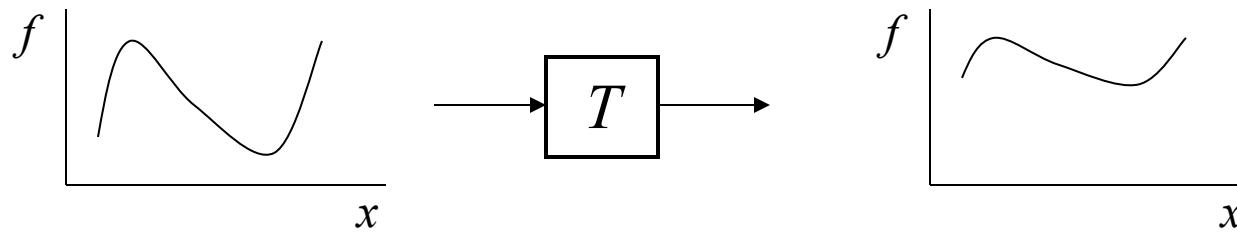


image warping: change **domain** of image

$$g(x) = f(T(x))$$

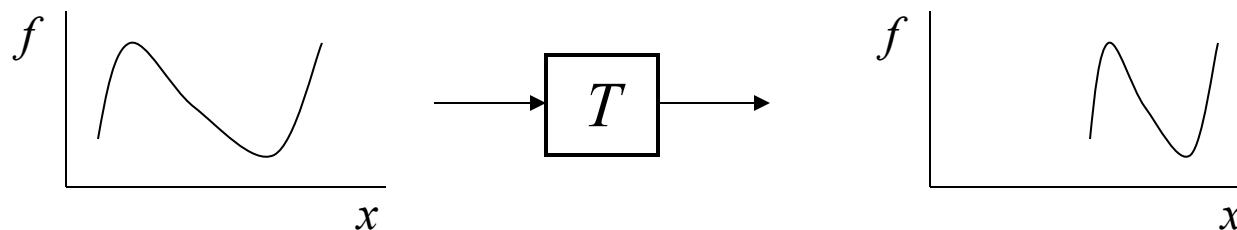


Image Transformations

image filtering: change **range** of image

$$g(x) = T(f(x))$$

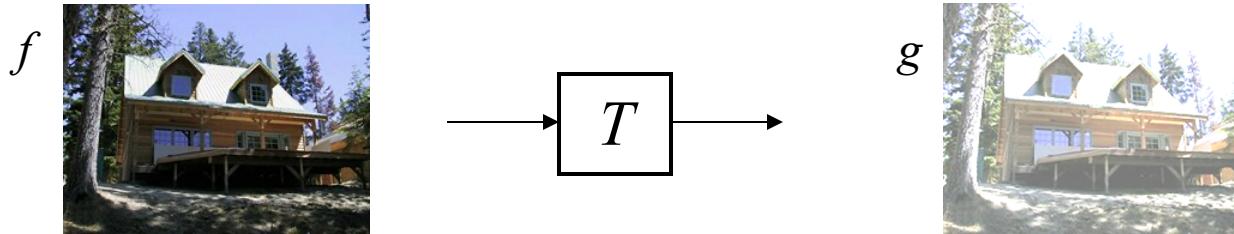
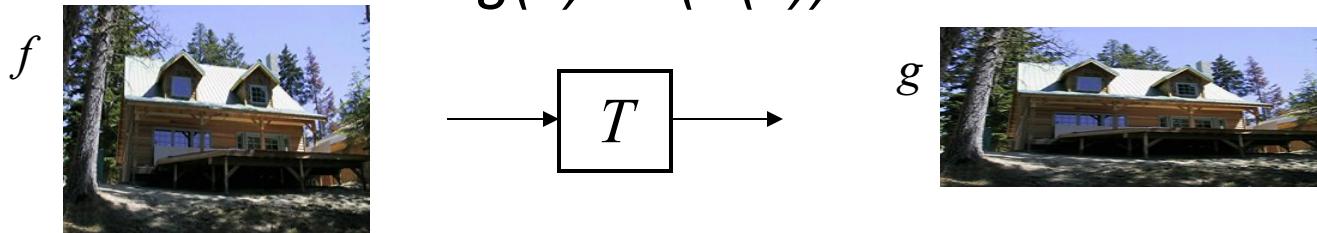


image warping: change **domain** of image

$$g(x) = f(T(x))$$



Parametric (global) warping

Examples of parametric warps:



translation



rotation



aspect



affine

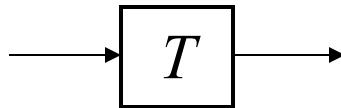


perspective



cylindrical

Parametric (global) warping



$$p = (x, y)$$

$$p' = (x', y')$$

Transformation T is a coordinate-changing machine:

$$p' = T(p)$$

What does it mean that T is global?

- Is the same for any point p
- can be described by just a few numbers (parameters)

Let's represent a linear T as a matrix:

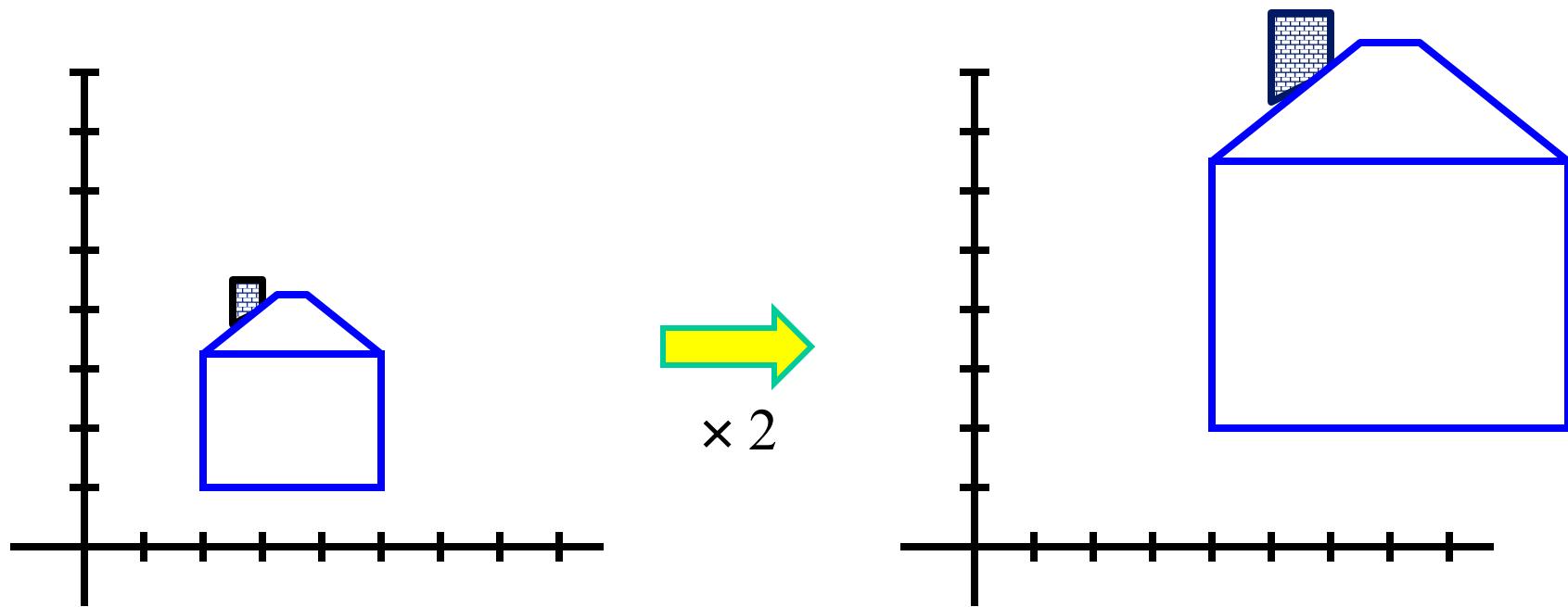
$$p' = \mathbf{M}p$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \mathbf{M} \begin{bmatrix} x \\ y \end{bmatrix}$$

Scaling

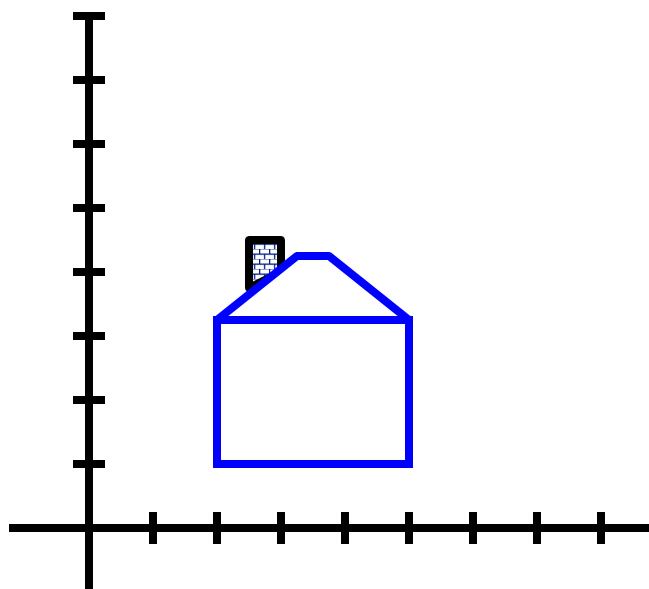
Scaling a coordinate means multiplying each of its components by a scalar

Uniform scaling means this scalar is the same for all components:

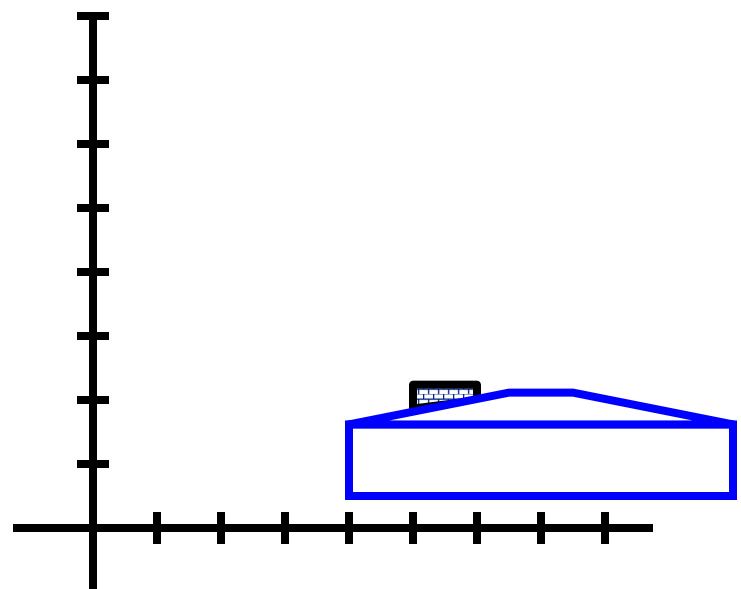


Scaling

Non-uniform scaling: different scalars per component:



\rightarrow
 $X \times 2,$
 $Y \times 0.5$



Scaling

Scaling operation:

$$x' = ax$$

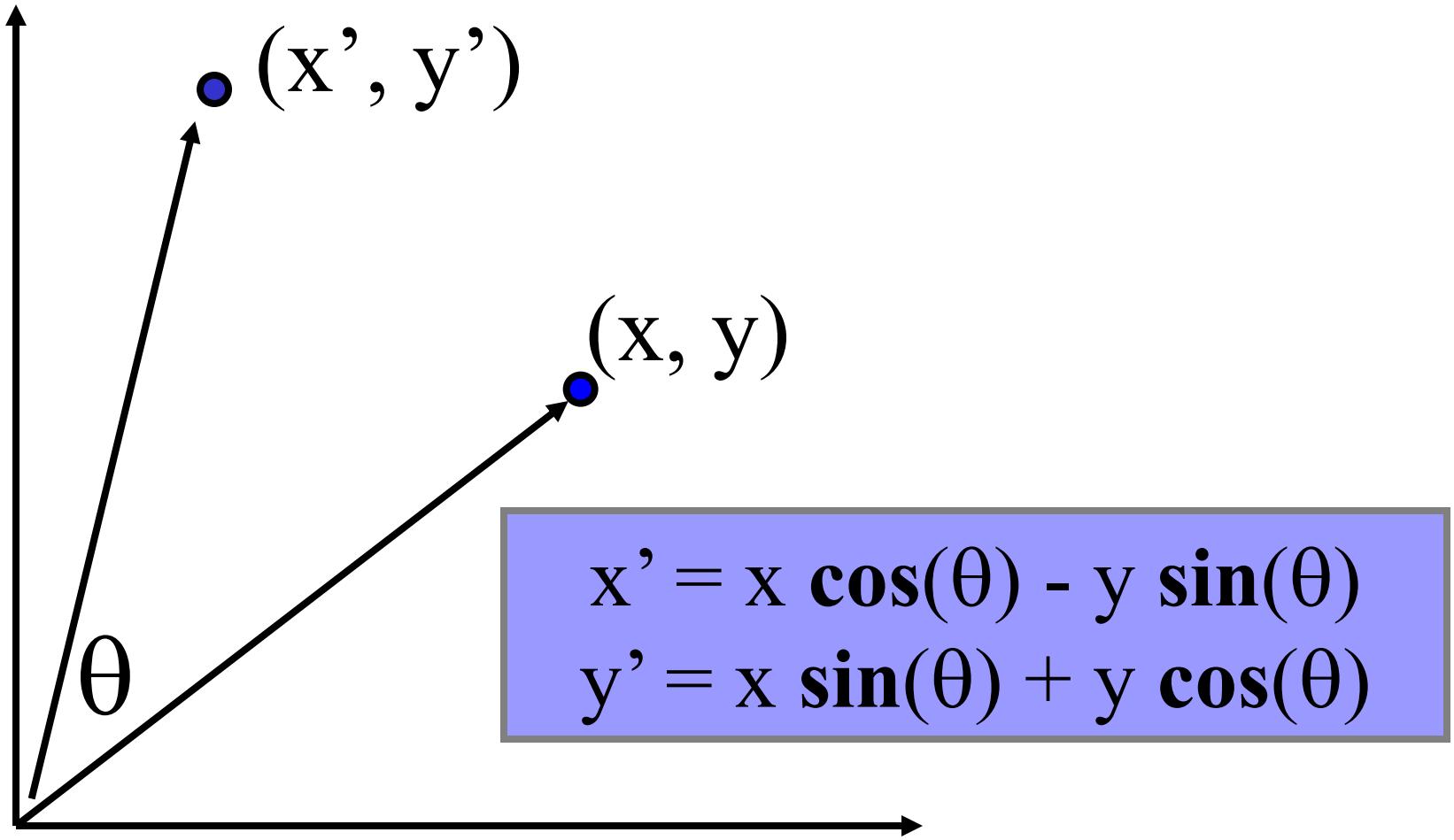
$$y' = by$$

Or, in matrix form:

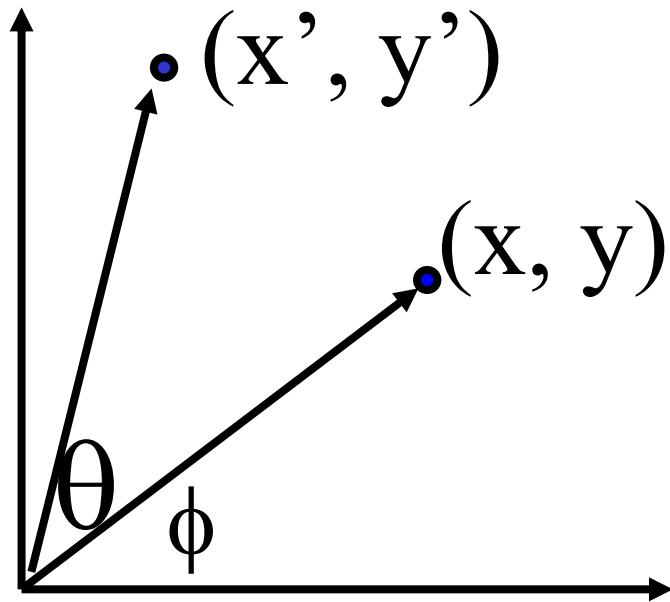
$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \underbrace{\begin{bmatrix} a & 0 \\ 0 & b \end{bmatrix}}_{\text{scaling matrix } S} \begin{bmatrix} x \\ y \end{bmatrix}$$

What's inverse of S?

2-D Rotation



2-D Rotation



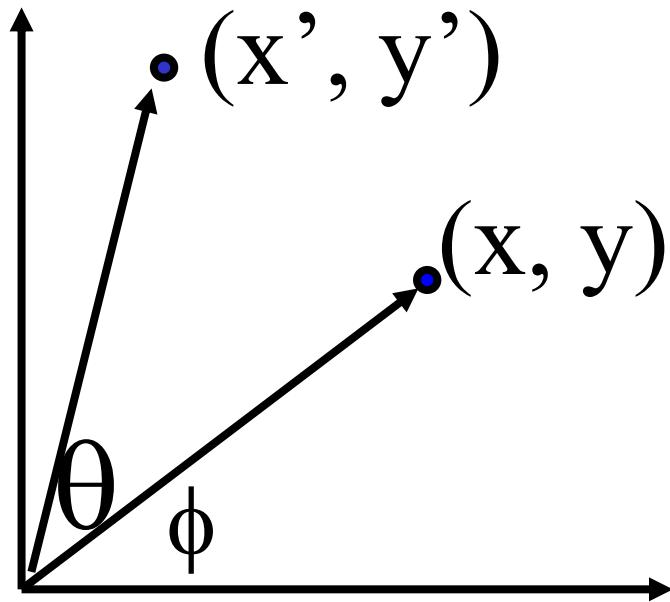
$$x = r \cos (\phi)$$

$$y = r \sin (\phi)$$

$$x' = r \cos (\phi + \theta)$$

$$y' = r \sin (\phi + \theta)$$

2-D Rotation



$$x = r \cos(\phi)$$

$$y = r \sin(\phi)$$

$$x' = r \cos(\phi + \theta)$$

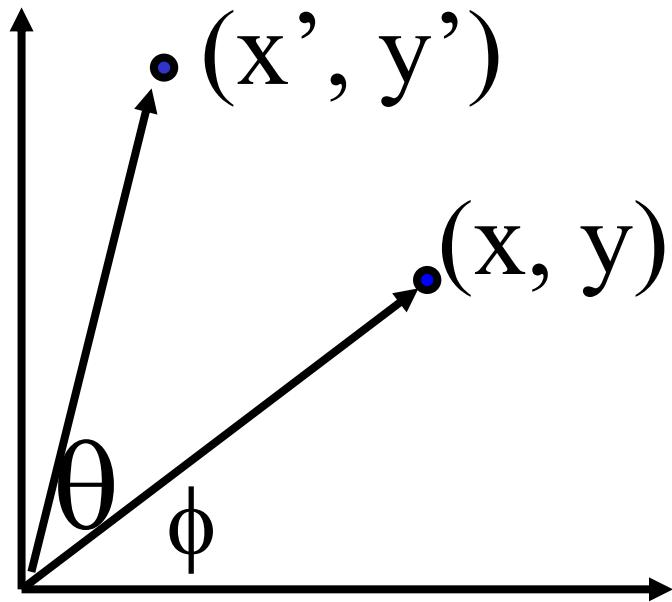
$$y' = r \sin(\phi + \theta)$$

Trig Identity...

$$x' = r \cos(\phi) \cos(\theta) - r \sin(\phi) \sin(\theta)$$

$$y' = r \sin(\phi) \cos(\theta) + r \cos(\phi) \sin(\theta)$$

2-D Rotation



$$x = r \cos(\phi)$$

$$y = r \sin(\phi)$$

$$x' = r \cos(\phi + \theta)$$

$$y' = r \sin(\phi + \theta)$$

Trig Identity...

$$x' = r \cos(\phi) \cos(\theta) - r \sin(\phi) \sin(\theta)$$

$$y' = r \sin(\phi) \cos(\theta) + r \cos(\phi) \sin(\theta)$$

Substitute...

$$x' = x \cos(\theta) - y \sin(\theta)$$

$$y' = x \sin(\theta) + y \cos(\theta)$$

2-D Rotation

This is easy to capture in matrix form:

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \underbrace{\begin{bmatrix} \cos(\theta) & -\sin(\theta) \\ \sin(\theta) & \cos(\theta) \end{bmatrix}}_{\mathbf{R}} \begin{bmatrix} x \\ y \end{bmatrix}$$

Even though $\sin(\theta)$ and $\cos(\theta)$ are nonlinear functions of θ ,

- x' is a linear combination of x and y
- y' is a linear combination of x and y

What is the inverse transformation?

- Rotation by $-\theta$
- For rotation matrices $\mathbf{R}^{-1} = \mathbf{R}^T$

2x2 Matrices

What types of transformations can be represented with a 2x2 matrix?

2D Identity?

$$x' = x$$

$$y' = y$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

2D Scale around (0,0)?

$$x' = s_x * x$$

$$y' = s_y * y$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} s_x & 0 \\ 0 & s_y \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

2x2 Matrices

What types of transformations can be represented with a 2x2 matrix?

2D Rotate around (0,0)?

$$\begin{aligned}x' &= \cos \Theta * x - \sin \Theta * y \\y' &= \sin \Theta * x + \cos \Theta * y\end{aligned}$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos \Theta & -\sin \Theta \\ \sin \Theta & \cos \Theta \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

2D Shear?

$$\begin{aligned}x' &= x + sh_x * y \\y' &= sh_y * x + y\end{aligned}$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & sh_x \\ sh_y & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

2x2 Matrices

What types of transformations can be represented with a 2x2 matrix?

2D Mirror about Y axis?

$$\begin{aligned}x' &= -x \\y' &= y\end{aligned}$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

2D Mirror over (0,0)?

$$\begin{aligned}x' &= -x \\y' &= -y\end{aligned}$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

2x2 Matrices

What types of transformations can be represented with a 2x2 matrix?

2D Translation?

$$x' = x + t_x \quad \text{NO!}$$

$$y' = y + t_y$$

Only linear 2D transformations
can be represented with a 2x2 matrix

All 2D Linear Transformations

Linear transformations are combinations of ...

- Scale,
- Rotation,
- Shear, and
- Mirror

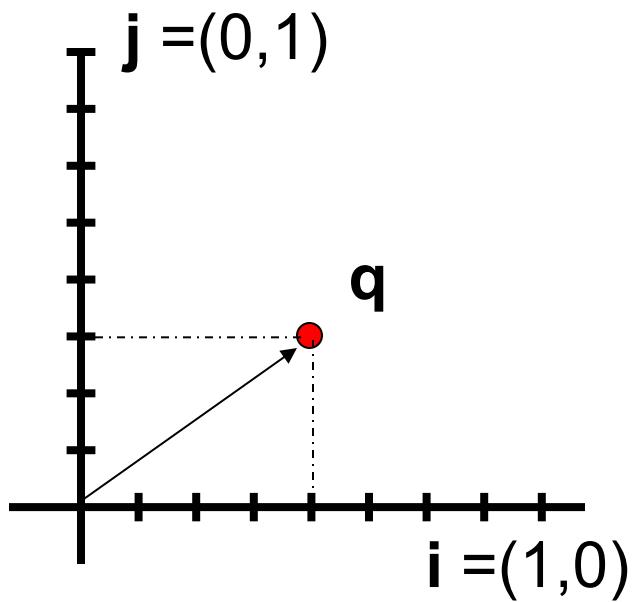
$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

Properties of linear transformations:

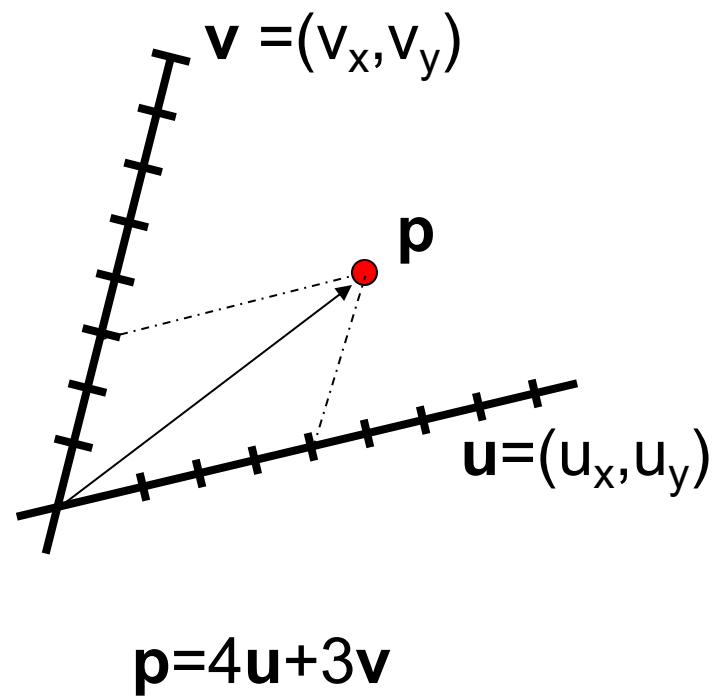
- Origin maps to origin
- Lines map to lines
- Parallel lines remain parallel
- Ratios are preserved
- Closed under composition

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} e & f \\ g & h \end{bmatrix} \begin{bmatrix} i & j \\ k & l \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

Consider a different Basis

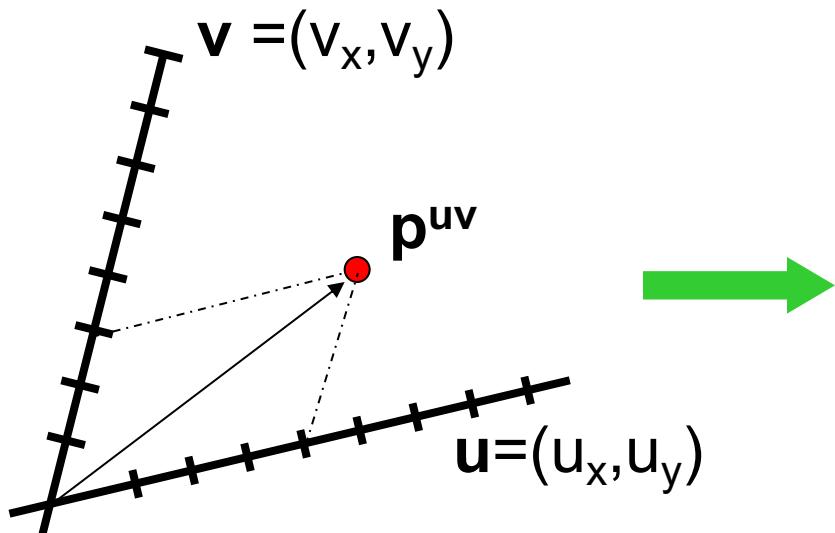


$$\mathbf{q} = 4\mathbf{i} + 3\mathbf{j} = (4, 3)$$



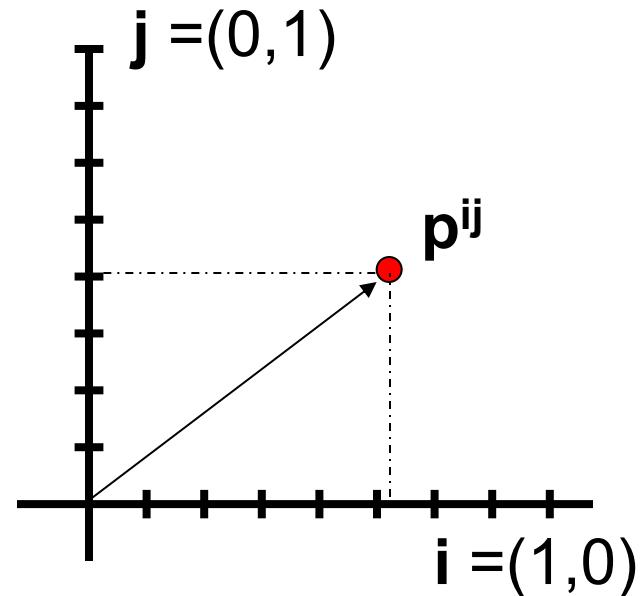
$$\mathbf{p} = 4\mathbf{u} + 3\mathbf{v}$$

Linear Transformations as Change of Basis



$$p^{uv} = (4, 3)$$

$$\begin{aligned} p_x &= 4u_x + 3v_x \\ p_y &= 4u_y + 3v_y \end{aligned}$$

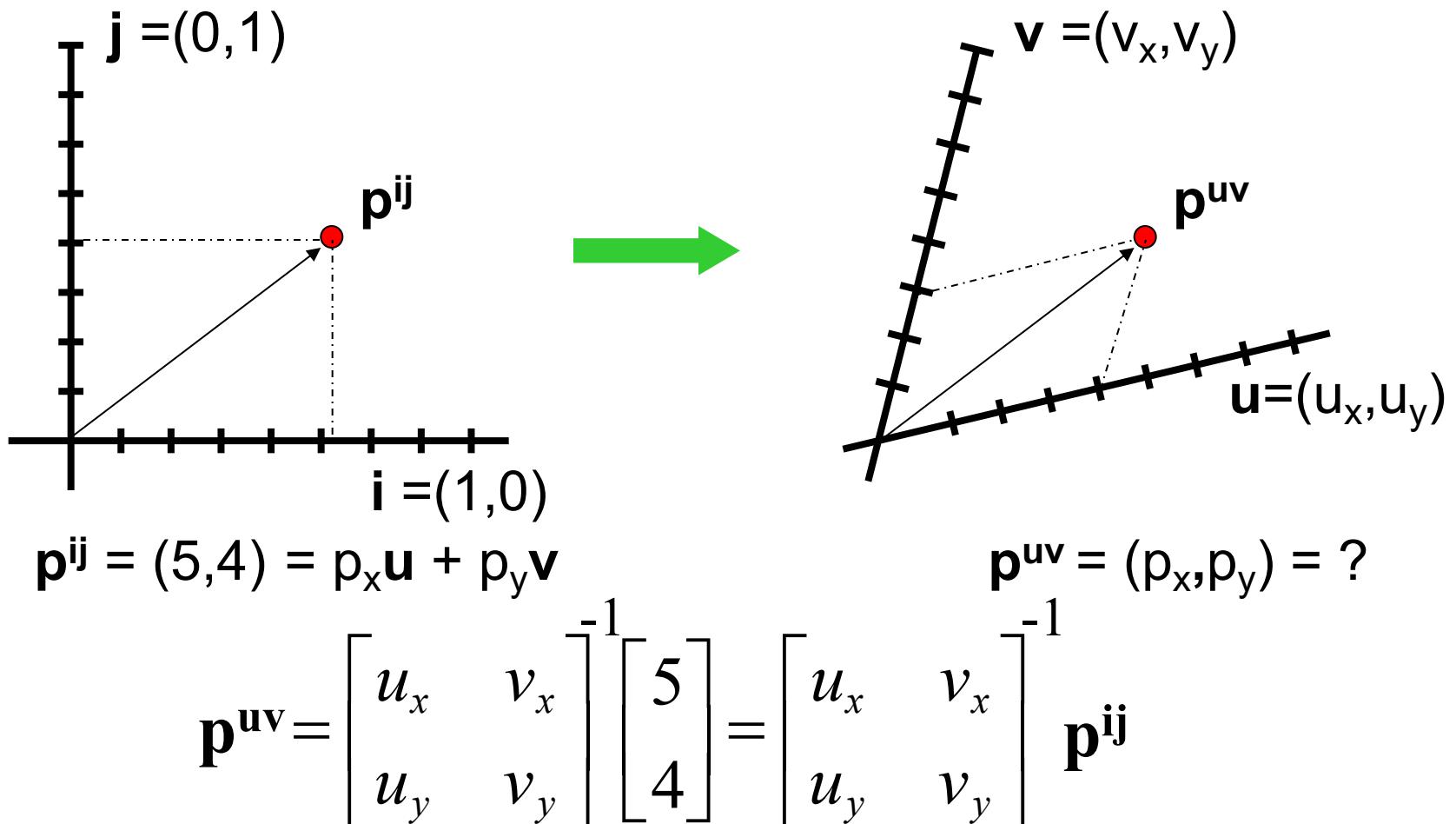


$$p^{ij} = 4u + 3v$$

$$p^{ij} = \begin{bmatrix} u_x & v_x \\ u_y & v_y \end{bmatrix} \begin{bmatrix} 4 \\ 3 \end{bmatrix} = \begin{bmatrix} u_x & v_x \\ u_y & v_y \end{bmatrix} p^{uv}$$

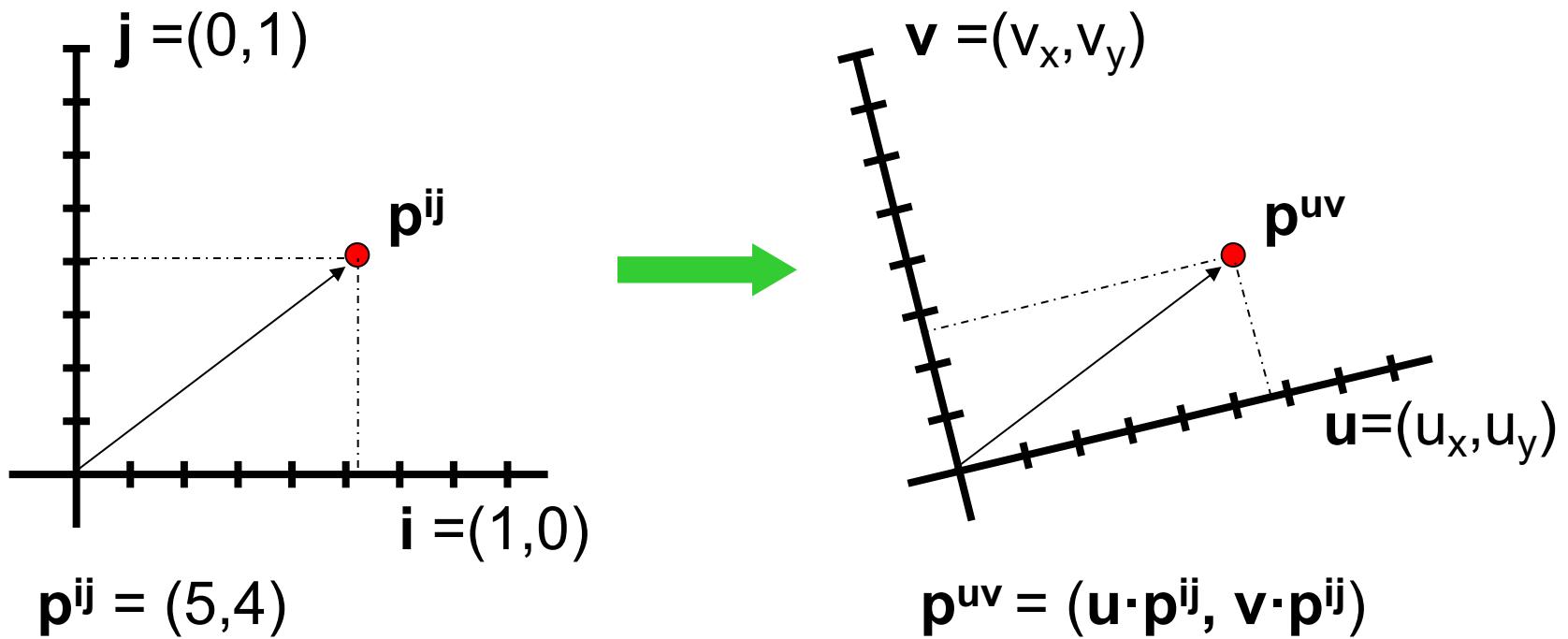
Any linear transformation is a basis!!!

What's the inverse transform?



- How can we change from any basis to any basis?
- What if the basis are orthogonal?

Projection onto orthogonal basis



$$p^{uv} = \begin{bmatrix} u_x & u_x \\ v_y & v_y \end{bmatrix} \begin{bmatrix} 5 \\ 4 \end{bmatrix} = \begin{bmatrix} u_x & u_y \\ v_x & v_y \end{bmatrix} p^{ij}$$

Homogeneous Coordinates

Q: How can we represent translation as a 3x3 matrix?

$$x' = x + t_x$$

$$y' = y + t_y$$

Homogeneous Coordinates

Homogeneous coordinates

- represent coordinates in 2 dimensions with a 3-vector

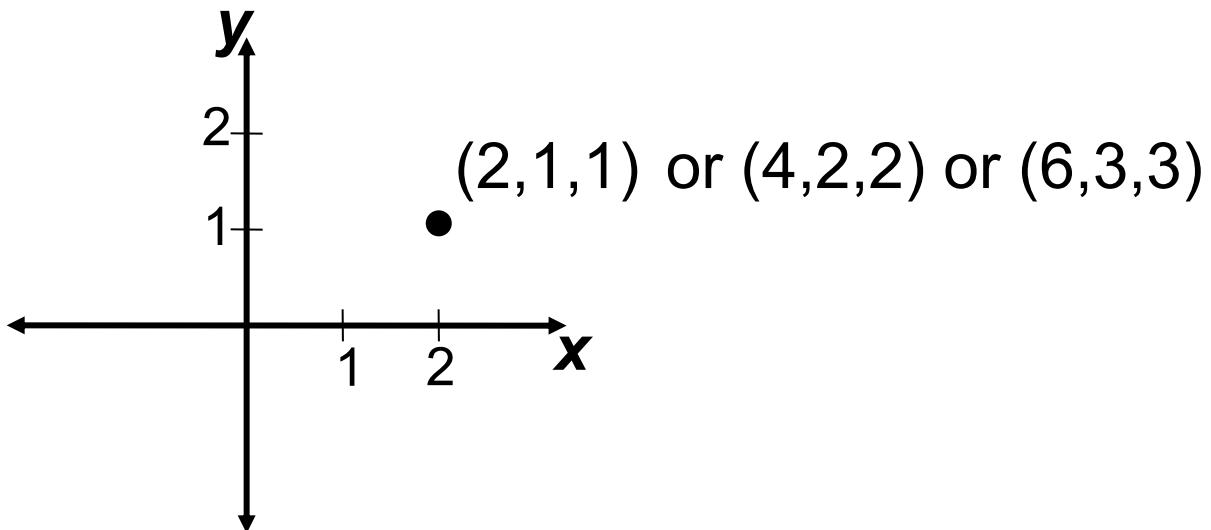
$$\begin{bmatrix} x \\ y \end{bmatrix} \xrightarrow{\text{homogeneous coords}} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Homogeneous Coordinates

Add a 3rd coordinate to every 2D point

- (x, y, w) represents a point at location $(x/w, y/w)$
- $(x, y, 0)$ represents a point at infinity
- $(0, 0, 0)$ is not allowed

Convenient
coordinate system to
represent many
useful
transformations



Homogeneous Coordinates

Q: How can we represent translation as a 3x3 matrix?

$$x' = x + t_x$$

$$y' = y + t_y$$

A: Using the rightmost column:

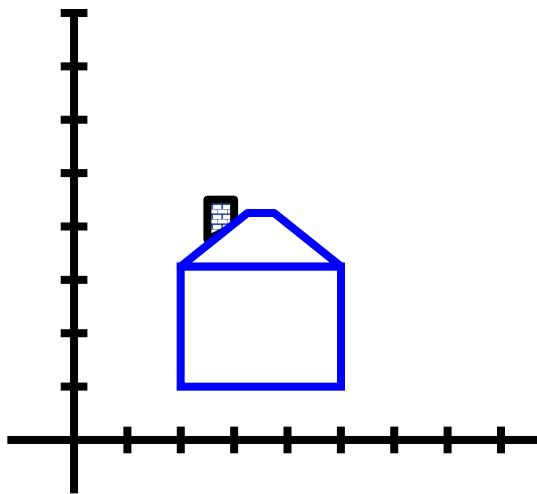
$$\text{Translation} = \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix}$$

Translation

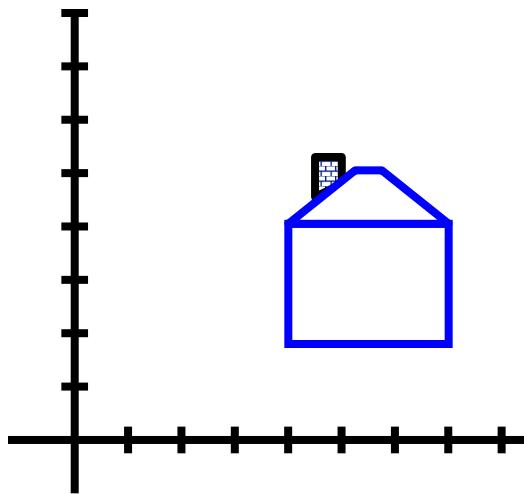
Example of translation

Homogeneous Coordinates

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} x + t_x \\ y + t_y \\ 1 \end{bmatrix}$$



$$\begin{aligned} t_x &= 2 \\ t_y &= 1 \end{aligned}$$



Basic 2D Transformations

Basic 2D transformations as 3x3 matrices

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Translate

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} s_x & 0 & 0 \\ 0 & s_y & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Scale

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \Theta & -\sin \Theta & 0 \\ \sin \Theta & \cos \Theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Rotate

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & sh_x & 0 \\ sh_y & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Shear

Matrix Composition

Transformations can be combined by
matrix multiplication

$$\begin{bmatrix} x' \\ y' \\ w' \end{bmatrix} = \left(\begin{bmatrix} 1 & 0 & tx \\ 0 & 1 & ty \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \cos \Theta & -\sin \Theta & 0 \\ \sin \Theta & \cos \Theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} sx & 0 & 0 \\ 0 & sy & 0 \\ 0 & 0 & 1 \end{bmatrix} \right) \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$
$$p' = T(t_x, t_y) R(\Theta) S(s_x, s_y) p$$

Does the order of multiplication matter?

Affine Transformations

Affine transformations are combinations of ...

- Linear transformations, and
- Translations

$$\begin{bmatrix} x' \\ y' \\ w \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$

Properties of affine transformations:

- Origin does not necessarily map to origin
- Lines map to lines
- Parallel lines remain parallel
- Ratios are preserved
- Closed under composition
- Models change of basis

Will the last coordinate w always be 1?

Projective Transformations

Projective transformations ...

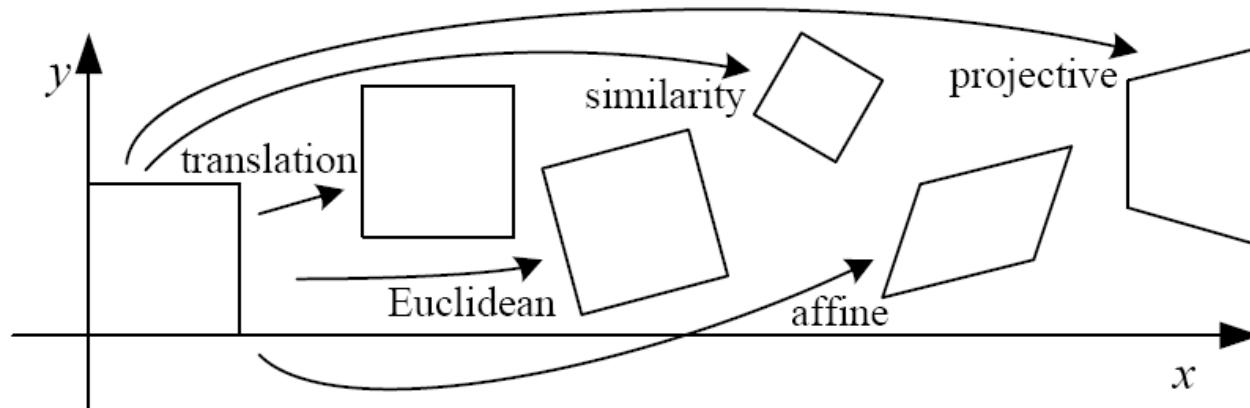
- Affine transformations, and
- Projective warps

$$\begin{bmatrix} x' \\ y' \\ w' \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$

Properties of projective transformations:

- Origin does not necessarily map to origin
- Lines map to lines
- Parallel lines do not necessarily remain parallel
- Ratios are not preserved
- Closed under composition
- Models change of basis

2D image transformations



Name	Matrix	# D.O.F.	Preserves:	Icon
translation	$\left[\begin{array}{c c} \mathbf{I} & \mathbf{t} \end{array} \right]_{2 \times 3}$			
rigid (Euclidean)	$\left[\begin{array}{c c} \mathbf{R} & \mathbf{t} \end{array} \right]_{2 \times 3}$			
similarity	$\left[\begin{array}{c c} s\mathbf{R} & \mathbf{t} \end{array} \right]_{2 \times 3}$			
affine	$\left[\begin{array}{c} \mathbf{A} \end{array} \right]_{2 \times 3}$			
projective	$\left[\begin{array}{c} \tilde{\mathbf{H}} \end{array} \right]_{3 \times 3}$			



These transformations are a nested set of groups

- Closed under composition and inverse is a member

Image Warping in Biology

D'Arcy Thompson

<http://www-groups.dcs.st-and.ac.uk/~history/Miscellaneous/darcy.html>

http://en.wikipedia.org/wiki/D'Arcy_Thompson

Importance of shape and structure in evolution

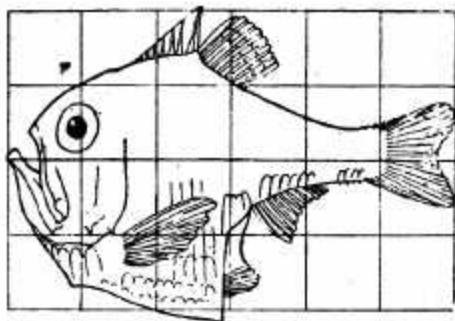
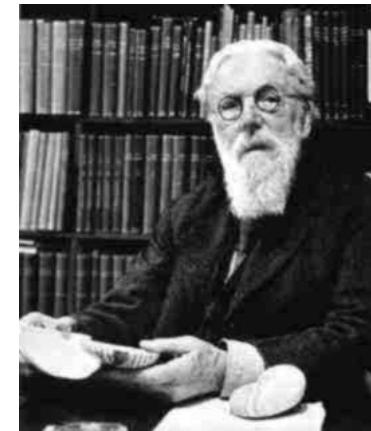
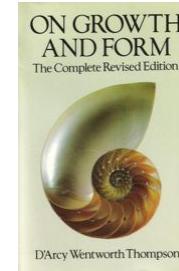


Fig. 517. *Argyropelecus Olfersi.*

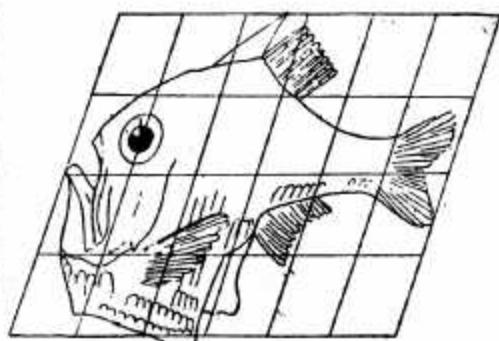
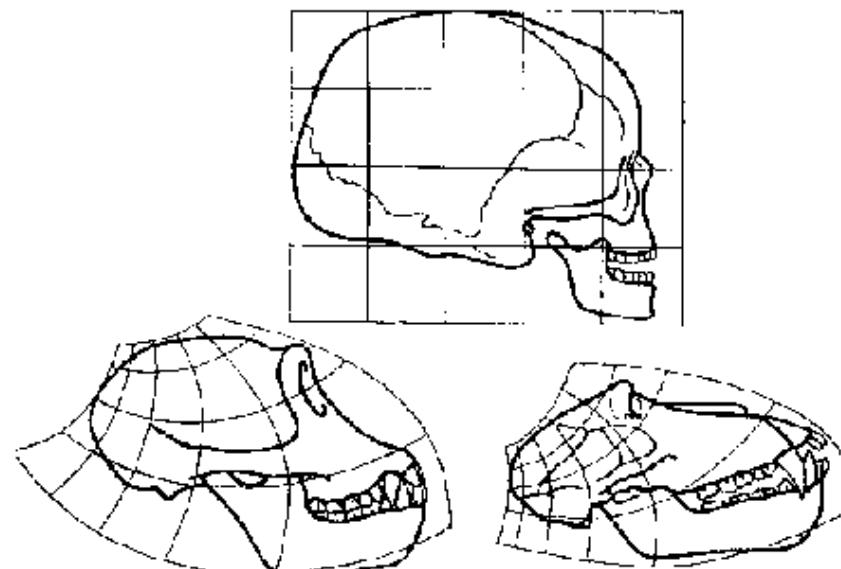
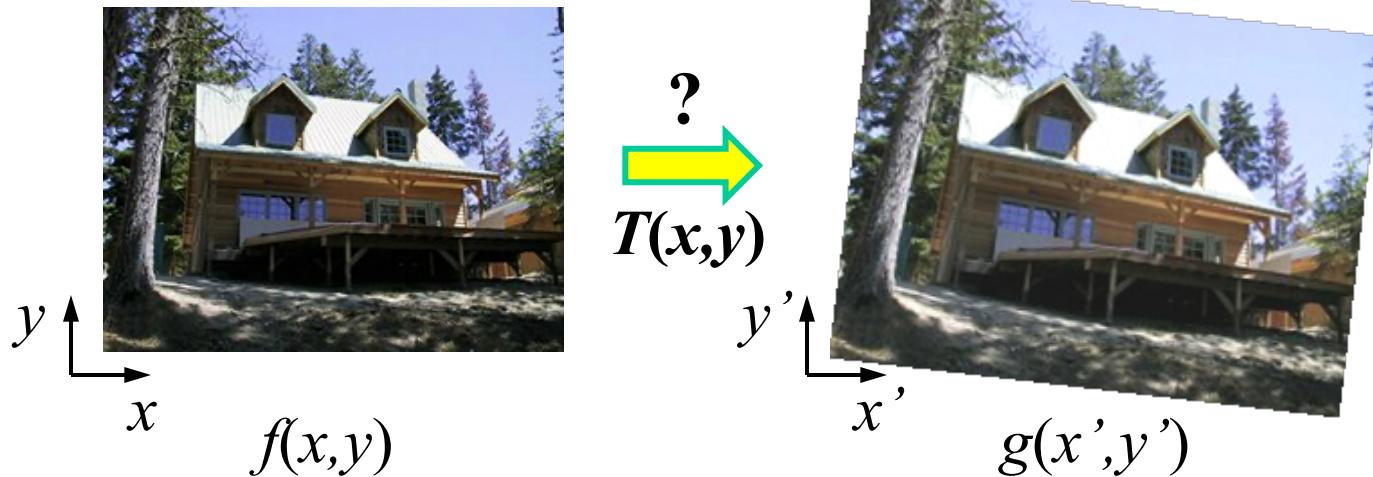


Fig. 518. *Sternopyx diaphana.*



Skulls of a human, a chimpanzee and a baboon
and transformations between them

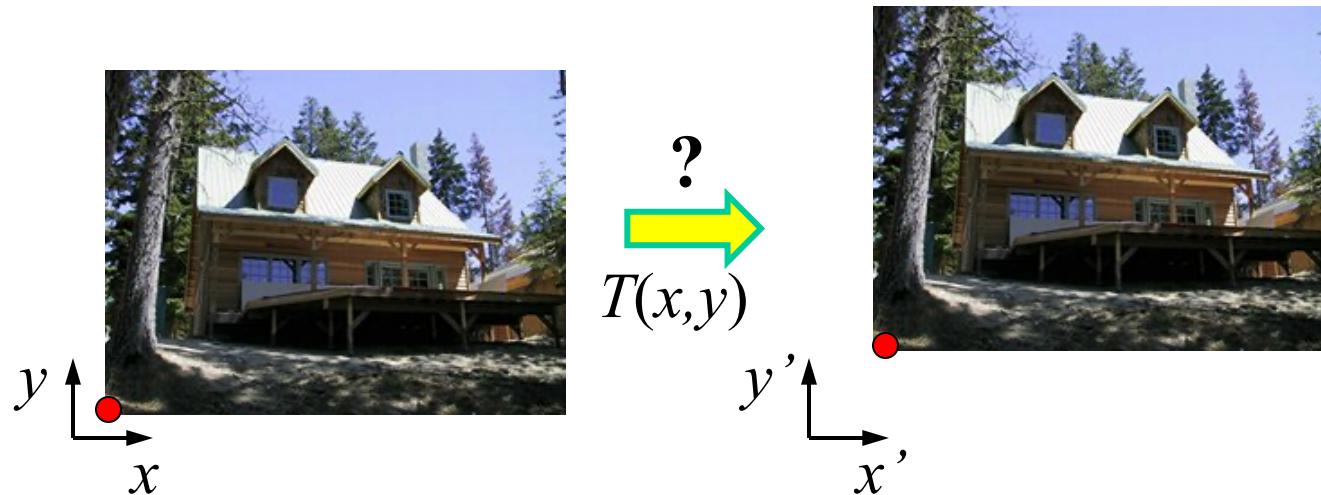
Recovering Transformations



What if we know f and g and want to recover the transform T ?

- e.g. better align images from Project 1
- willing to let user provide correspondences
 - How many do we need?

Translation: # correspondences?



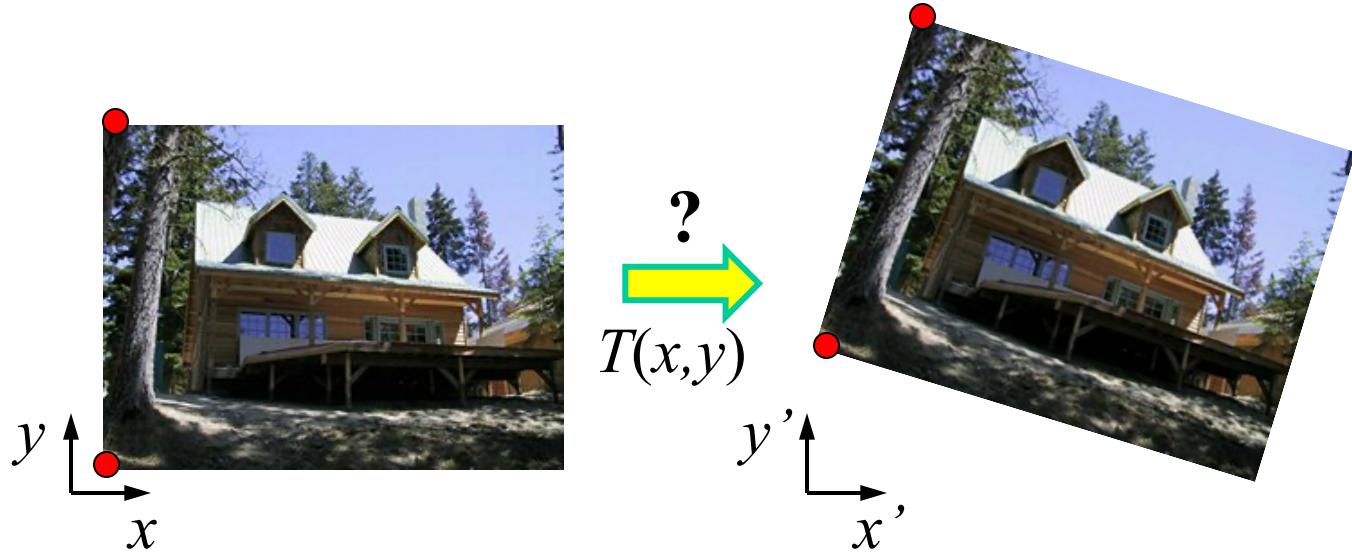
How many correspondences needed for translation?

How many Degrees of Freedom?

What is the transformation matrix?

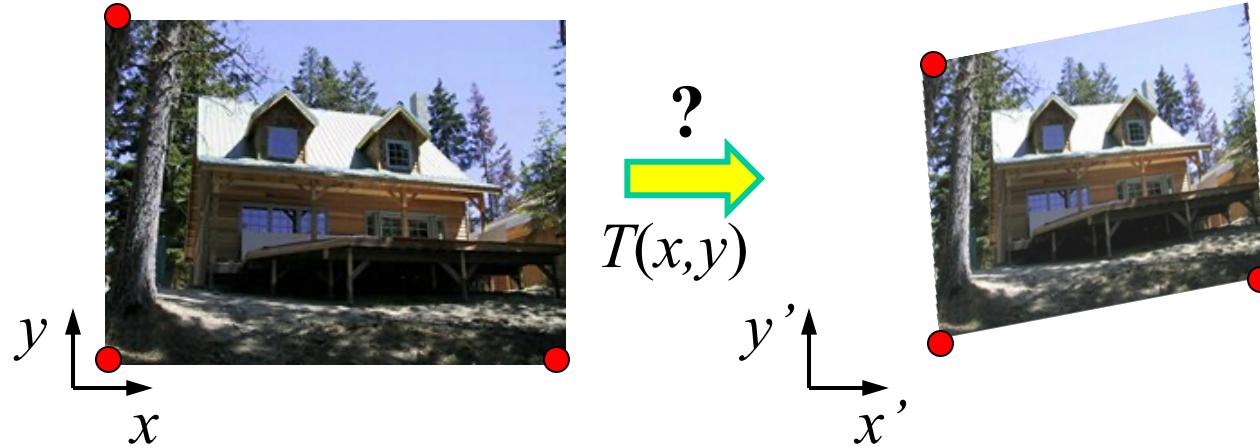
$$\mathbf{M} = \begin{bmatrix} 1 & 0 & p'_x - p_x \\ 0 & 1 & p'_y - p_y \\ 0 & 0 & 1 \end{bmatrix}$$

Euclidian: # correspondences?



How many correspondences needed for translation+rotation?
How many DOF?

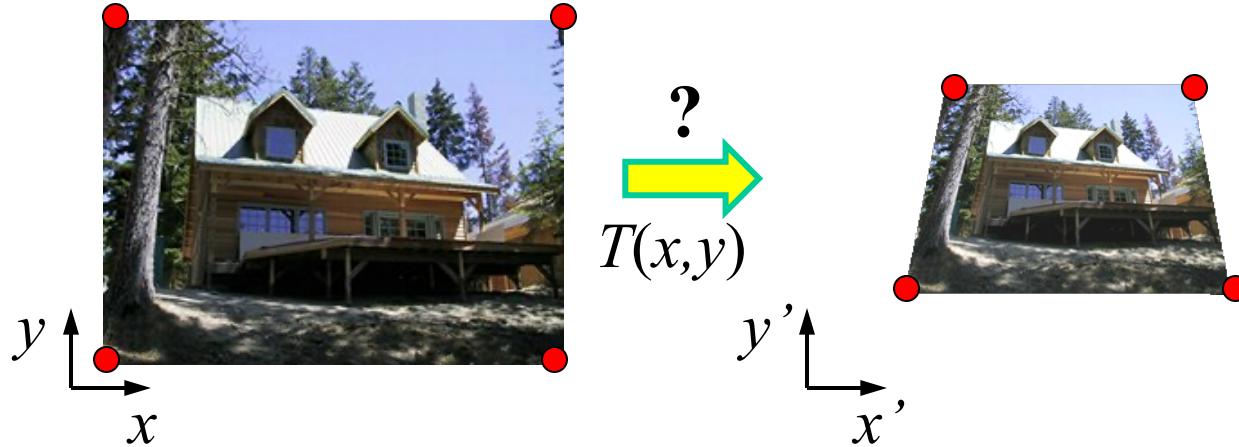
Affine: # correspondences?



How many correspondences needed for affine?

How many DOF?

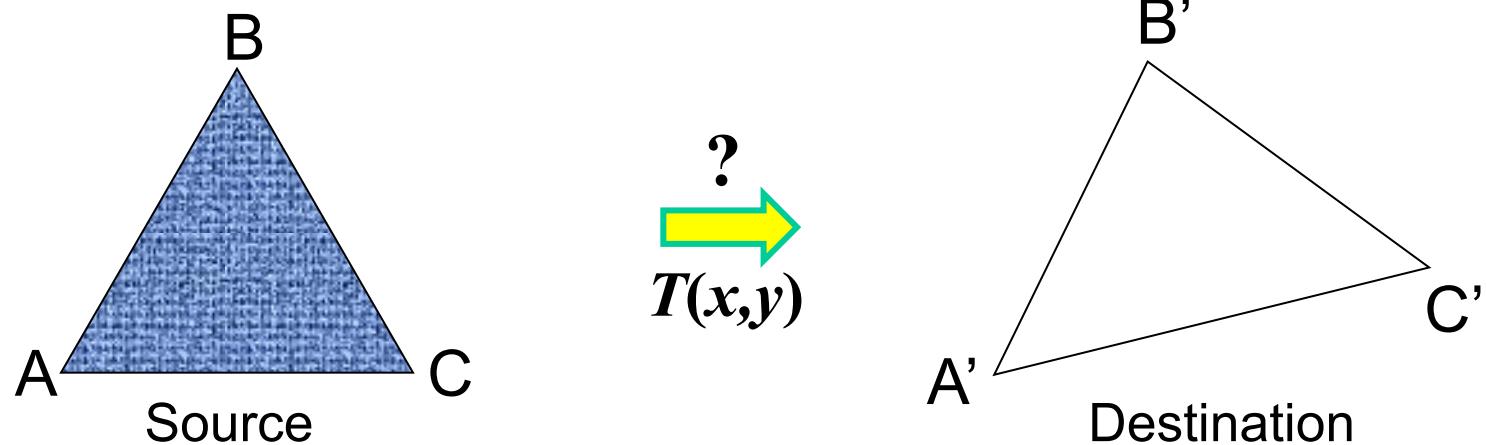
Projective: # correspondences?



How many correspondences needed for projective?

How many DOF?

Example: warping triangles



Given two triangles: ABC and A'B'C' in 2D (12 numbers)

Need to find transform T to transfer all pixels from one to the other.

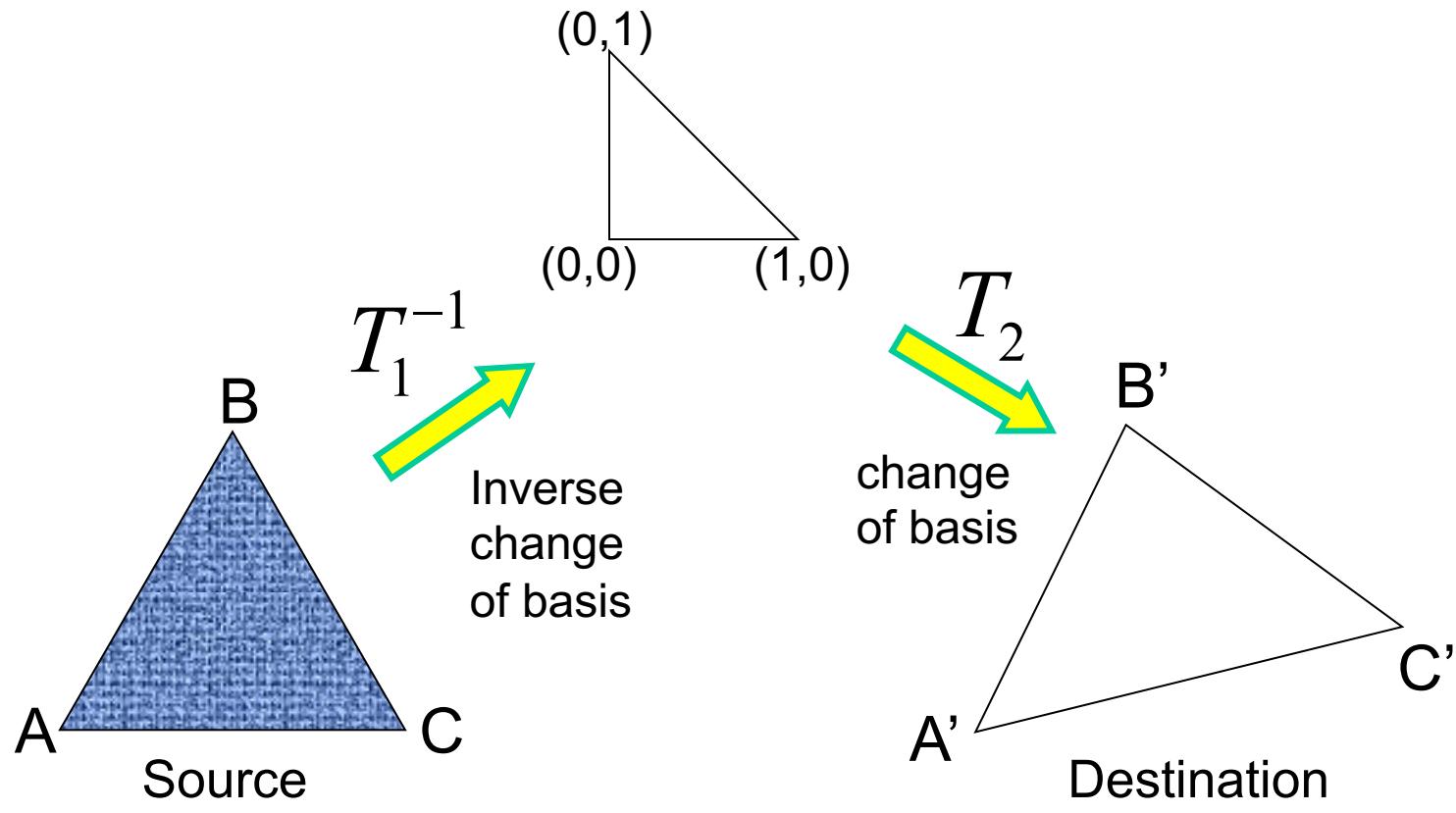
What kind of transformation is T ?

How can we compute the transformation matrix:

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Two ways:
Algebraic and
geometric

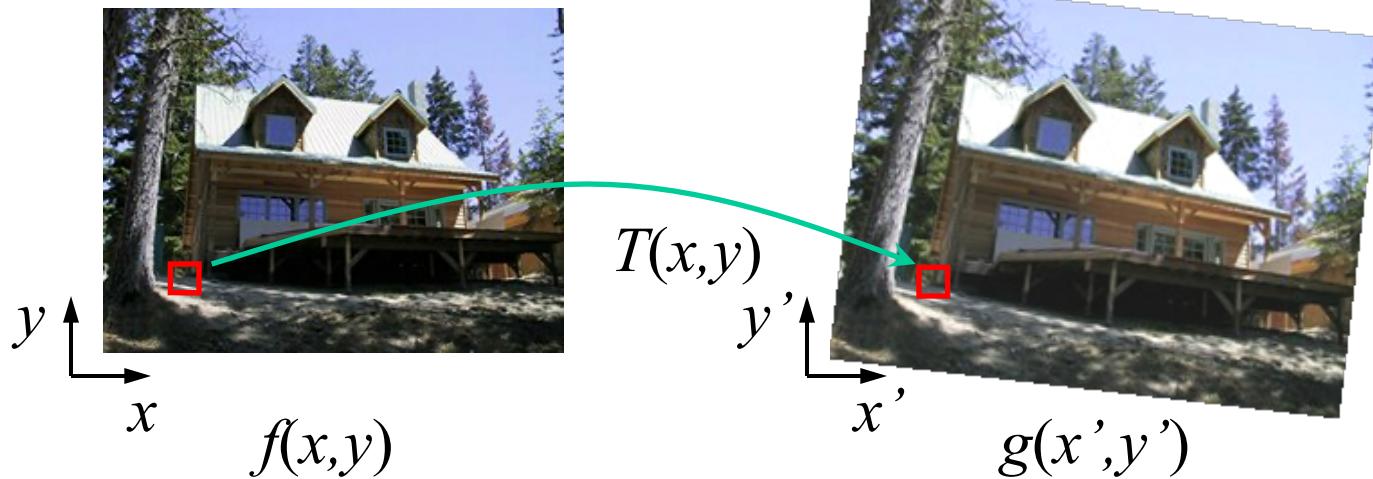
warping triangles (Barycentric Coordinates)



Don't forget to move the origin too!

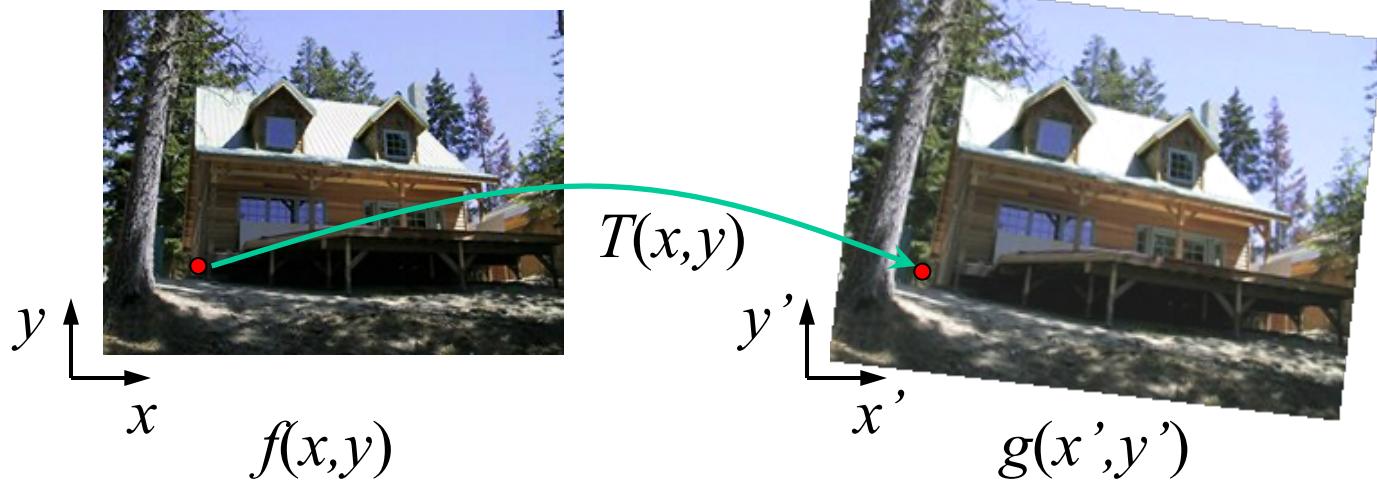
Very useful for Project 4... (hint,hint,nudge,nudge)

Image warping



Given a coordinate transform $(x',y') = T(x,y)$ and a source image $f(x,y)$, how do we compute a transformed image $g(x',y') = f(T(x,y))$?

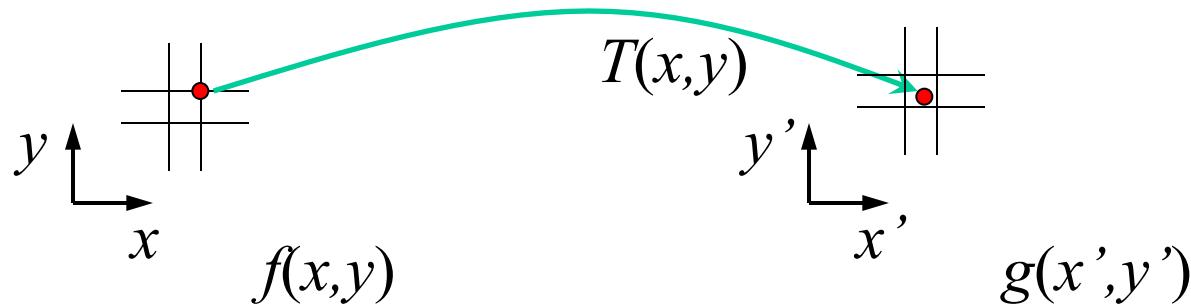
Forward warping



Send each pixel $f(x,y)$ to its corresponding location
 $(x',y') = T(x,y)$ in the second image

Q: what if pixel lands “between” two pixels?

Forward warping



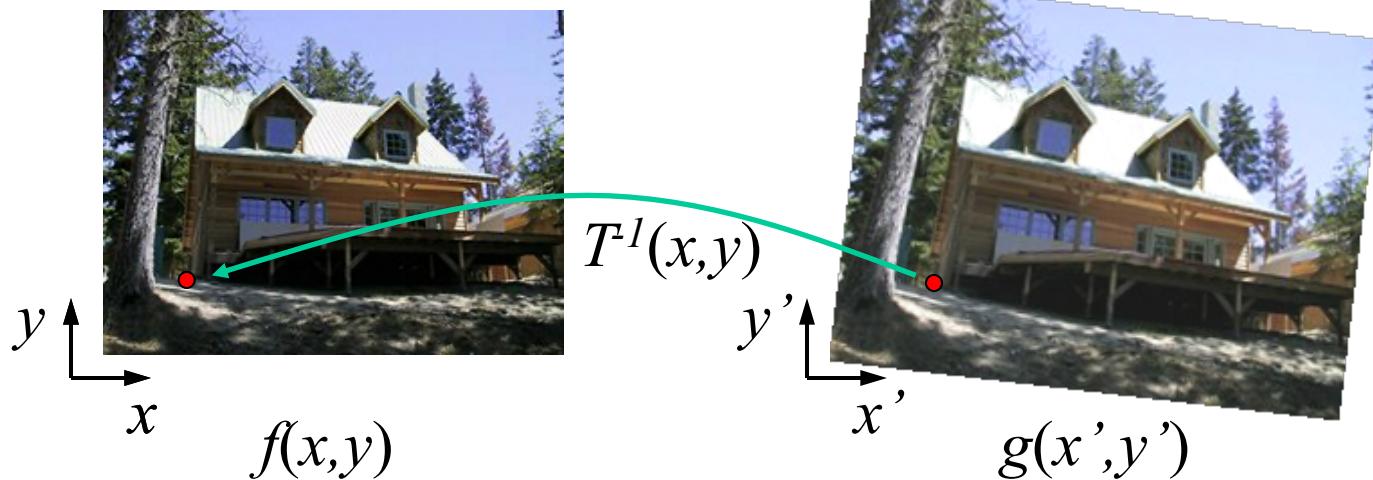
Send each pixel $f(x, y)$ to its corresponding location
 $(x', y') = T(x, y)$ in the second image

Q: what if pixel lands “between” two pixels?

A: distribute color among neighboring pixels (x', y')

- Known as “splatting”
- Check out `griddata` in Matlab

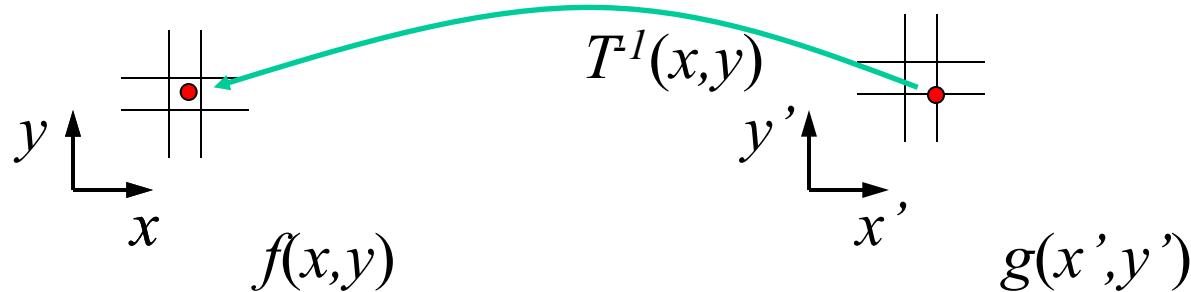
Inverse warping



Get each pixel $g(x',y')$ from its corresponding location
 $(x,y) = T^{-1}(x',y')$ in the first image

Q: what if pixel comes from “between” two pixels?

Inverse warping



Get each pixel $g(x',y')$ from its corresponding location
 $(x,y) = T^{-1}(x',y')$ in the first image

Q: what if pixel comes from “between” two pixels?

A: *Interpolate* color value from neighbors

- nearest neighbor, bilinear, Gaussian, bicubic
- Check out `interp2` in Matlab

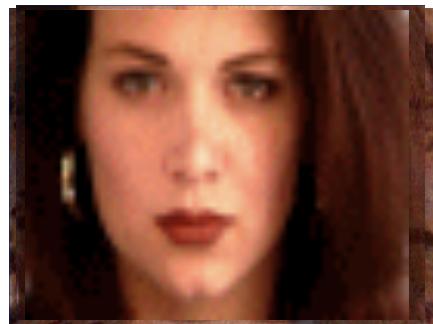
Forward vs. inverse warping

Q: which is better?

A: usually inverse—eliminates holes

- however, it requires an invertible warp function—not always possible...

Morphing = Object Averaging



The aim is to find “an average” between two objects

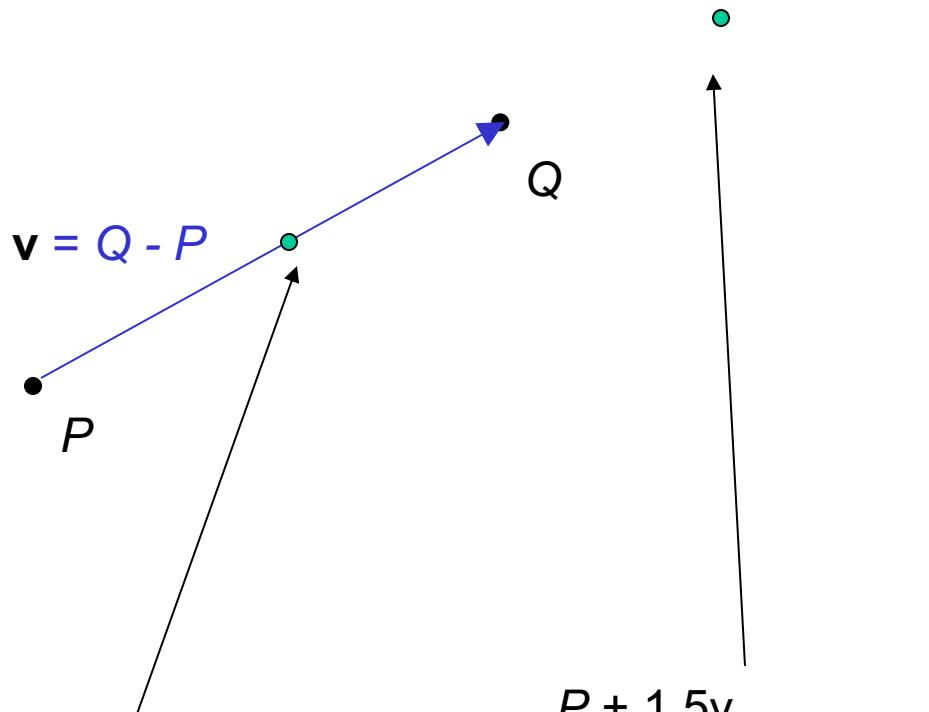
- Not an average of two images of objects...
- ...but an image of the average object!
- How can we make a smooth transition in time?
 - Do a “weighted average” over time t

How do we know what the average object looks like?

- We haven't a clue!
- But we can often fake something reasonable
 - Usually required user/artist input

Averaging Points

What's the average
of P and Q?



$$\begin{aligned}P + 0.5v \\= P + 0.5(Q - P) \\= 0.5P + 0.5Q\end{aligned}$$

$$\begin{aligned}P + 1.5v \\= P + 1.5(Q - P) \\= -0.5P + 1.5Q \\(\text{extrapolation})\end{aligned}$$

Linear Interpolation
(Affine Combination):
New point $aP + bQ$,
defined only when $a+b = 1$
So $aP+bQ = aP+(1-a)Q$

P and Q can be anything:

- points on a plane (2D) or in space (3D)
- Colors in RGB or HSV (3D)
- Whole images (m-by-n D)... etc.

Idea #1: Cross-Dissolve



Interpolate whole images:

$$\text{Image}_{\text{halfway}} = (1-t) * \text{Image}_1 + t * \text{Image}_2$$

This is called **cross-dissolve** in film industry

But what is the images are not aligned?

Idea #2: Align, then cross-dissolve



Align first, then cross-dissolve

- Alignment using global warp – picture still valid

Global warp not always enough!



What to do?

- Cross-dissolve doesn't work
- Global alignment doesn't work
 - Cannot be done with a global transformation (e.g. affine)
- Any ideas?

Feature matching!

- Nose to nose, tail to tail, etc.
- This is a local (non-parametric) warp

Local (non-parametric) Image Warping

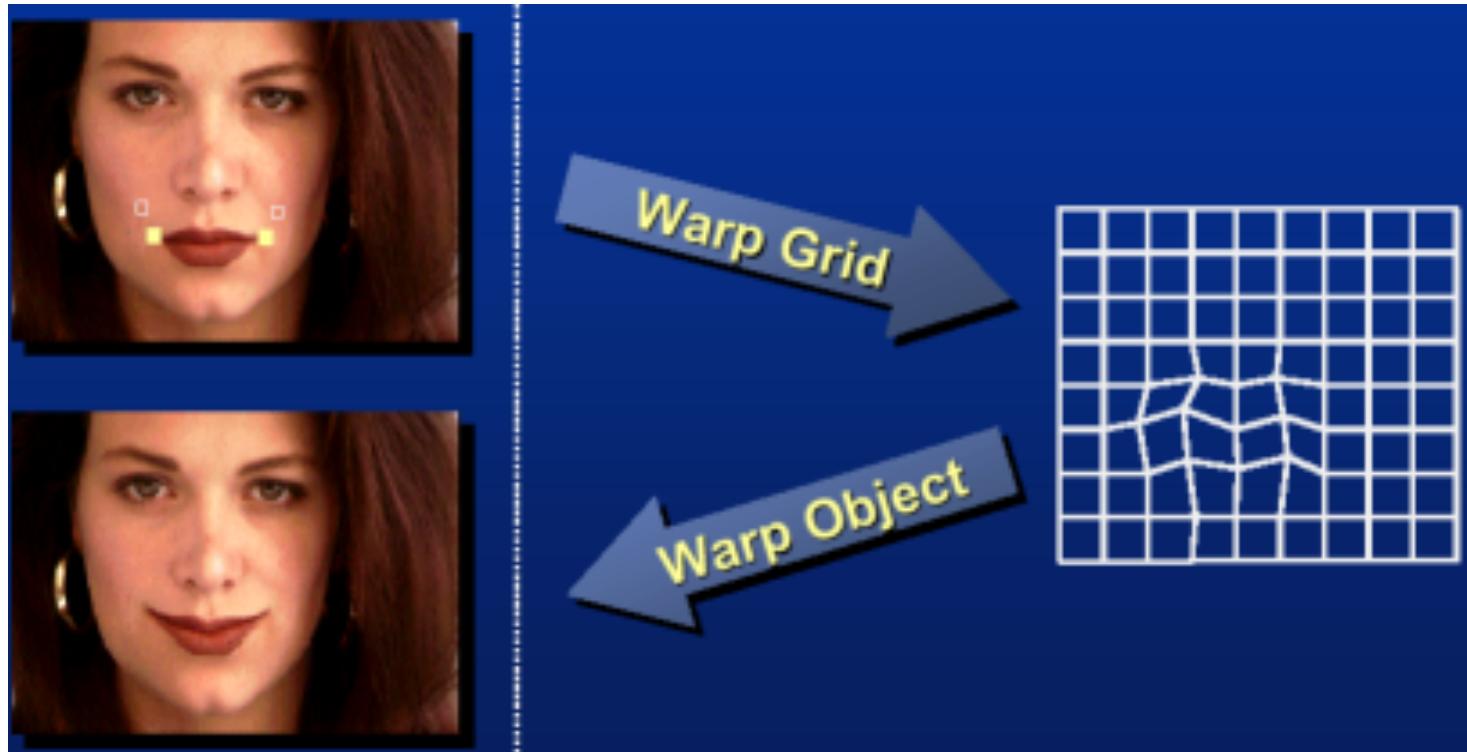


Need to specify a more detailed warp function

- Global warps were functions of a few (2,4,8) parameters
- Non-parametric warps $u(x,y)$ and $v(x,y)$ can be defined independently for every single location x,y !
- Once we know vector field u,v we can easily warp each pixel (use backward warping with interpolation)

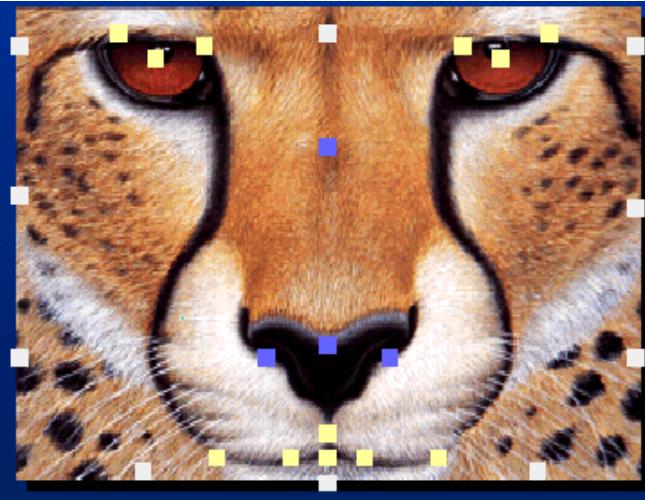
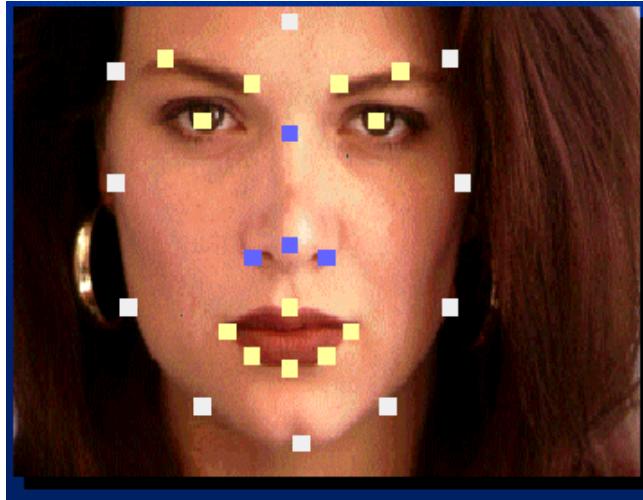
Warp specification -- dense

Define vector field to specify a dense warp



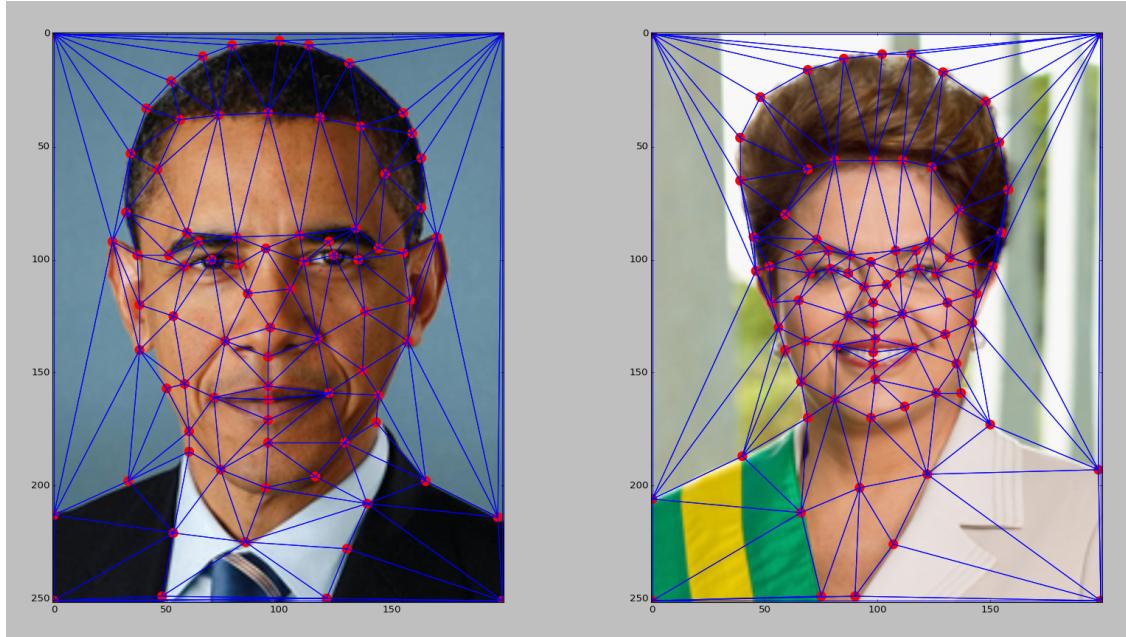
Warp specification - sparse

How can we specify a sparse warp?

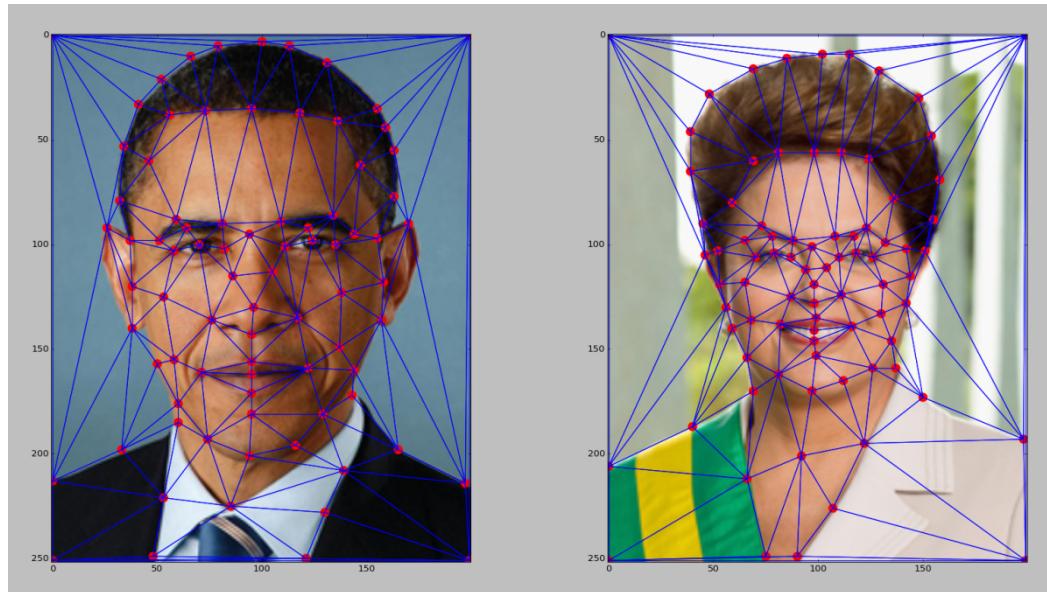


How do we go from feature points to pixels?

Triangular Mesh

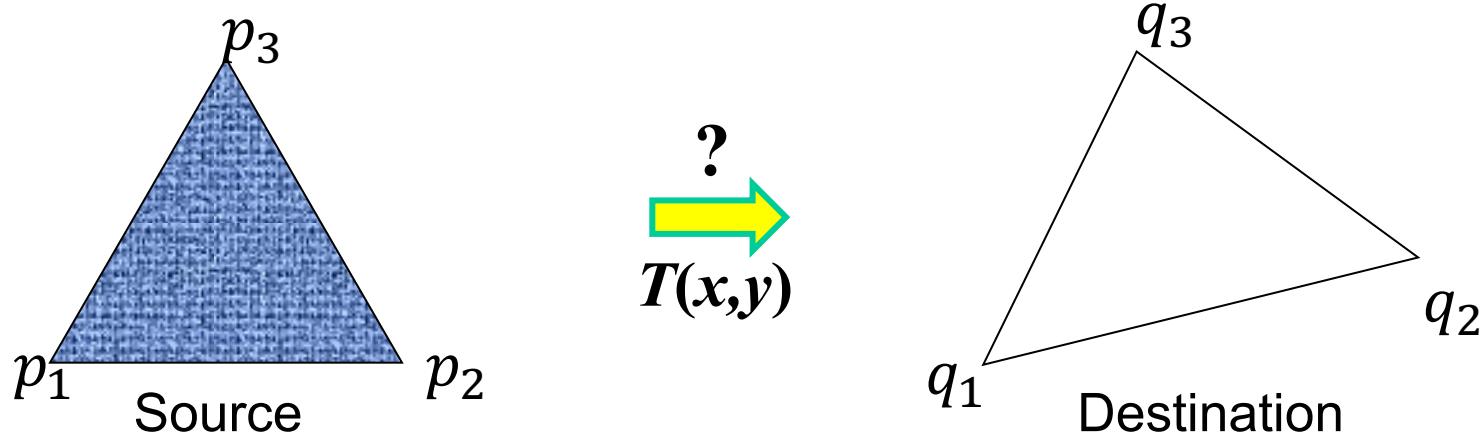


1. Input correspondences at key feature points
2. Define a triangular mesh over the points
 - Same mesh in both images!
 - Now we have triangle-to-triangle correspondences
3. Warp each triangle separately from source to destination
 - How do we warp a triangle?



(c) Ian Albuquerque Raymundo da Silva

Warping triangles



Given two triangles: $p_1p_2p_3$ and $q_1q_2q_3$ in 2D (12 numbers)

Need to find transform T to transfer all pixels from one to the other.

What kind of transformation is T ?

How can we compute the transformation matrix:

$$p = (x, y)$$

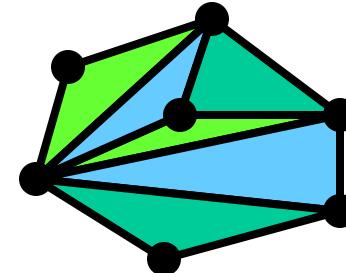
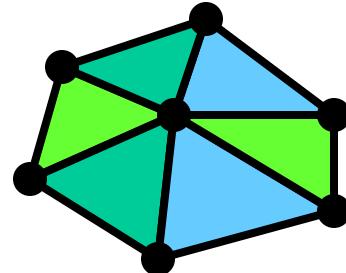
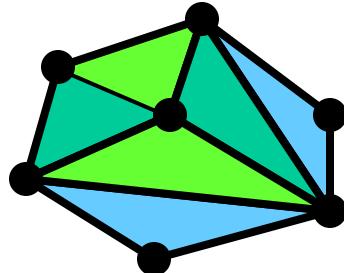
$$q = (x', y')$$

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

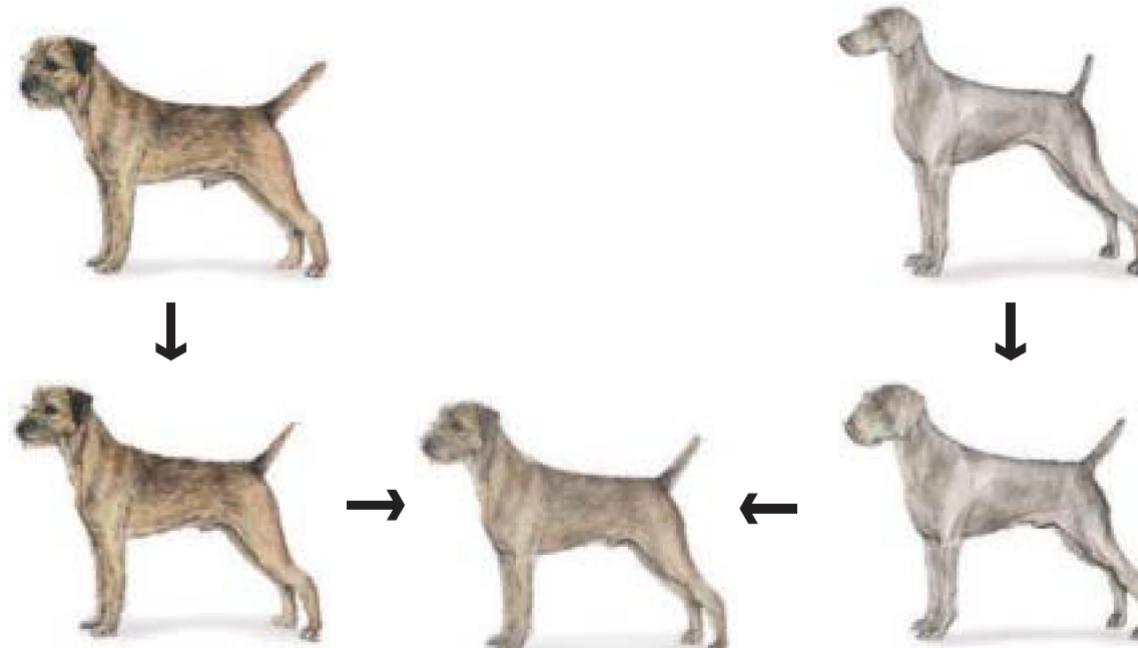
Triangulations

A *triangulation* of set of points in the plane is a *partition* of the convex hull to triangles whose vertices are the points, and do not contain other points.

There are an exponential number of triangulations of a point set.



Full Morphing Procedure



Morphing procedure:

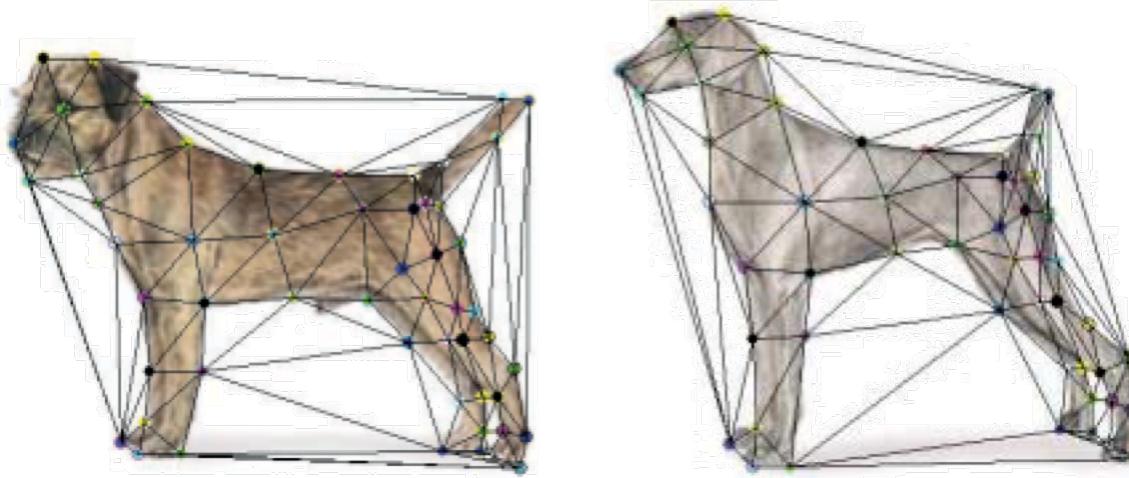
for every t ,

1. Find the average shape (the “mean dog”😊)
 - local warping
2. Find the average color
 - Cross-dissolve the warped images

1. Create Average Shape

How do we create an intermediate warp at time t?

- Assume $t = [0, 1]$
- Simple linear interpolation of each feature pair
 - $p \rightarrow q$
 - $(1 - t) \cdot p + t \cdot q$ for corresponding features p and p'



2. Create Average Color



Interpolate whole images:

$$\text{Image}_{\text{halfway}} = (1-t) * \text{Image} + t * \text{image}'$$

cross-dissolve!

Morphing & matting

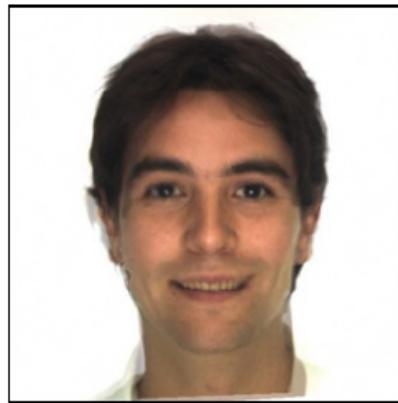
Extract foreground first to avoid artifacts in the background



(c) $\alpha = 0.0$



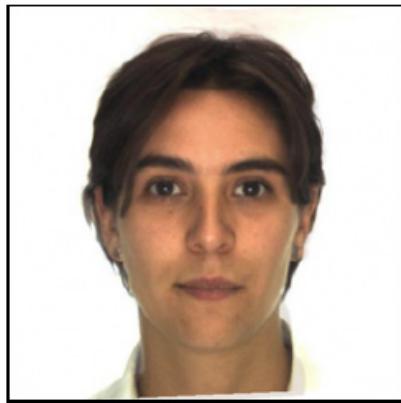
(d) $\alpha = 0.2$



(e) $\alpha = 0.4$



(f) $\alpha = 0.6$

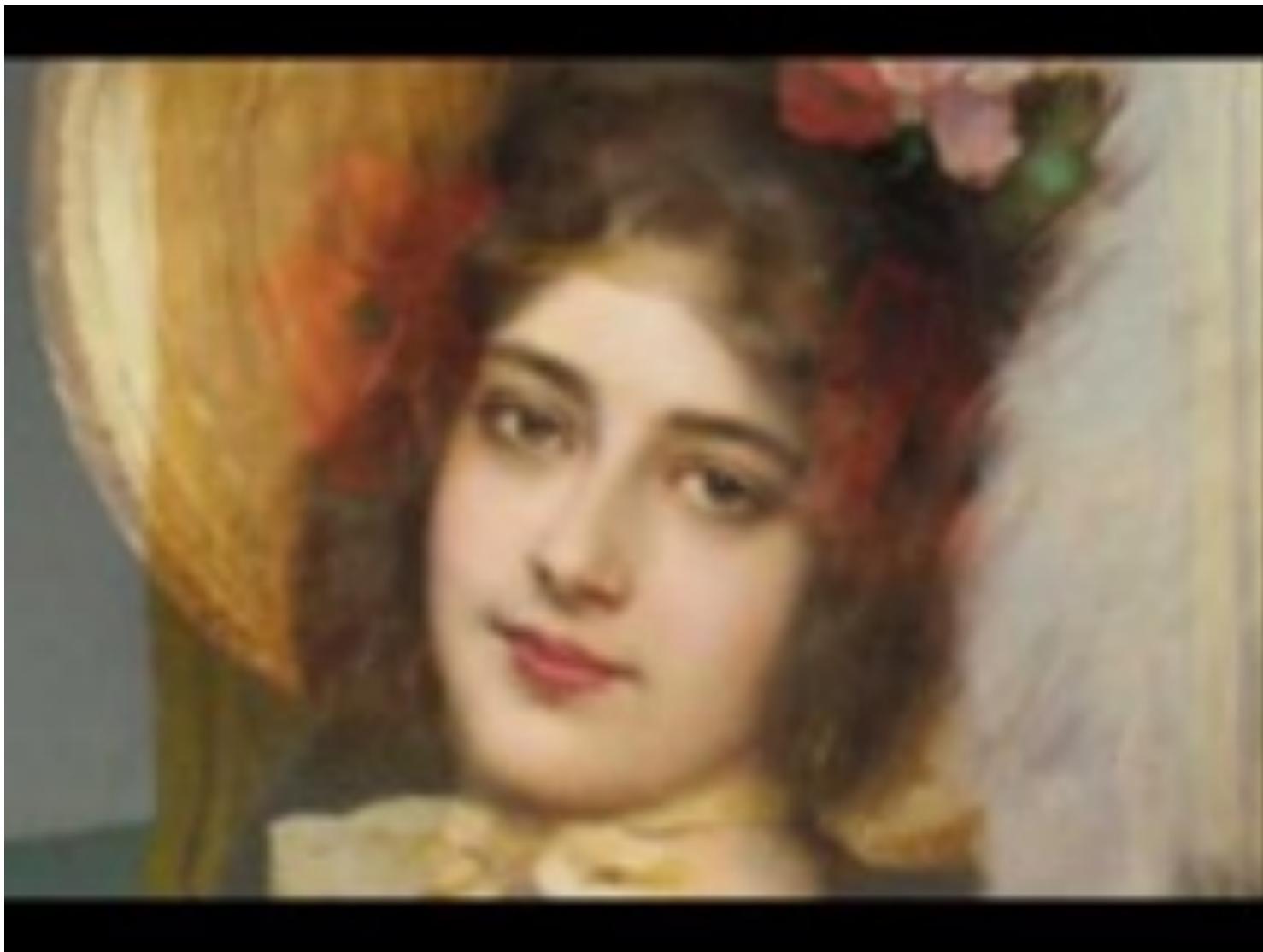


(g) $\alpha = 0.8$



(h) $\alpha = 1.0$

Amuse-bouche



By Philip Scott Johnson

Music: Bach's Sarabande from Suite for Solo Cello No. 1 in G Major, BWV 1007 performed by Yo-Yo Ma

Moving Least Square

What is a good local warping function $T(p) \rightarrow q$?

- Interpolation: need to satisfy control points $T(p_i) = q_i$
- Smoothness: T should be smooth;
- Identity: if $p_i = q_i$, T should be an identity mapping

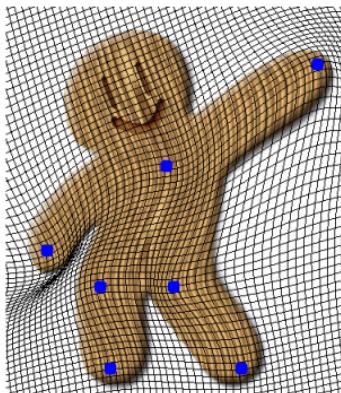
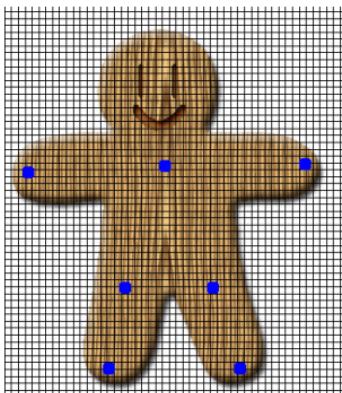
Triangulation-based methods:

$$\operatorname{argmin}_T \|T(p_i) - q_i\|^2 \text{ for 3 vertices in each triangle}$$

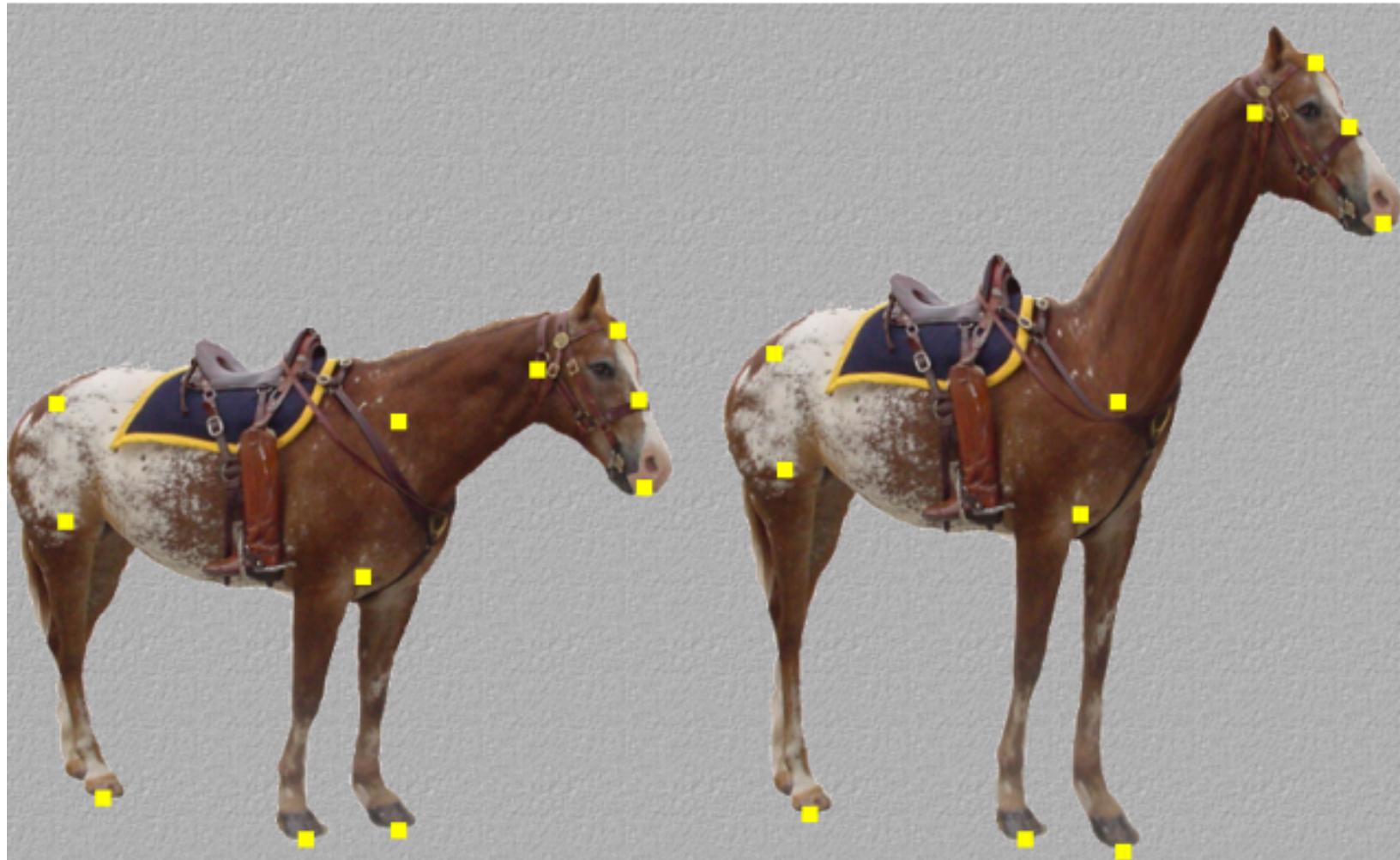
Moving least squares:

$$\operatorname{argmin}_T w_i \|T(p_i) - q_i\|^2 \text{ for all the control points}$$

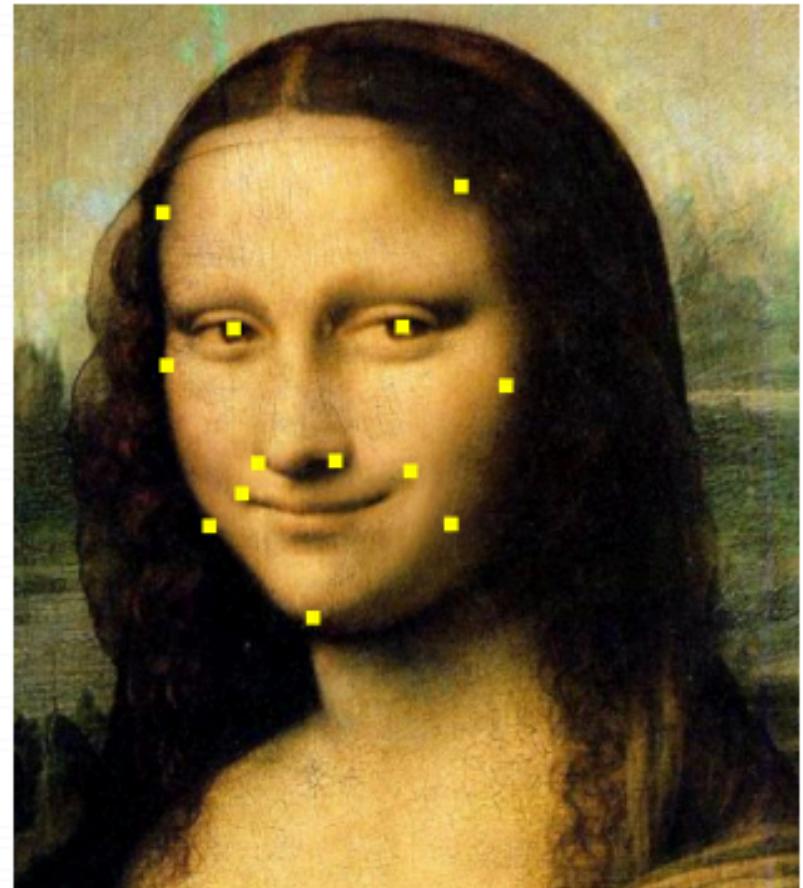
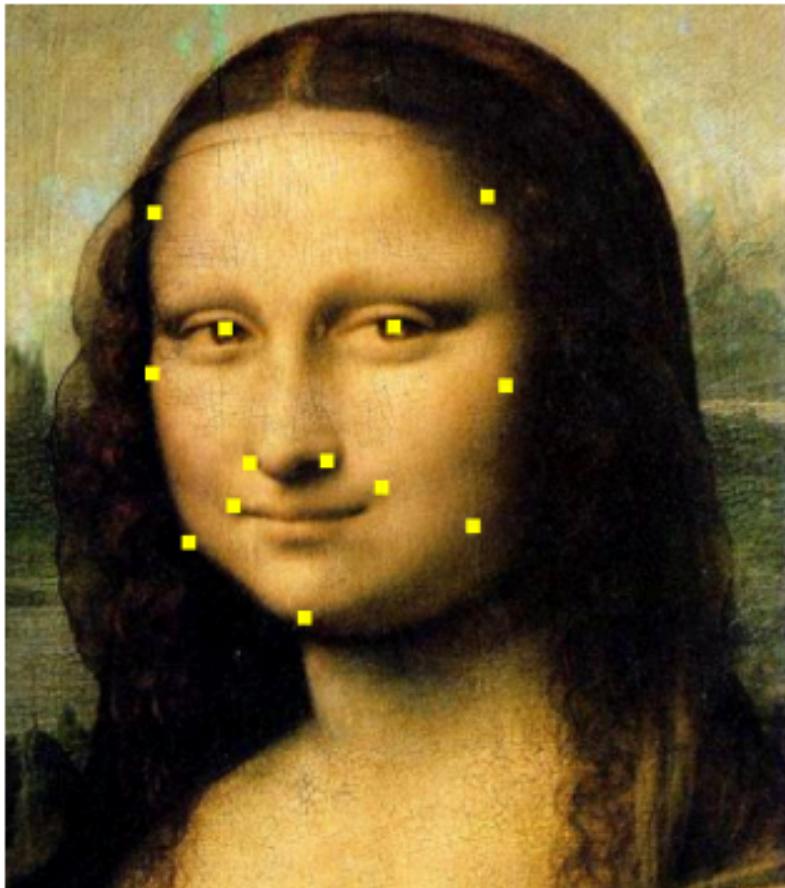
$$\text{Where } w_i = \frac{1}{|p_i - v|^{2\alpha}}$$



Moving Least Square

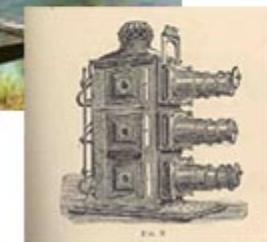
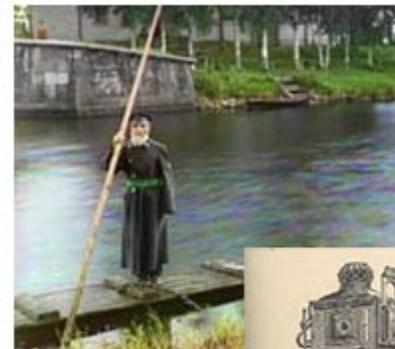
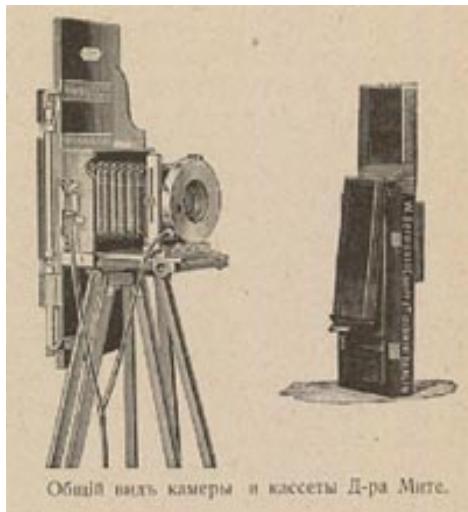


Moving Least Square

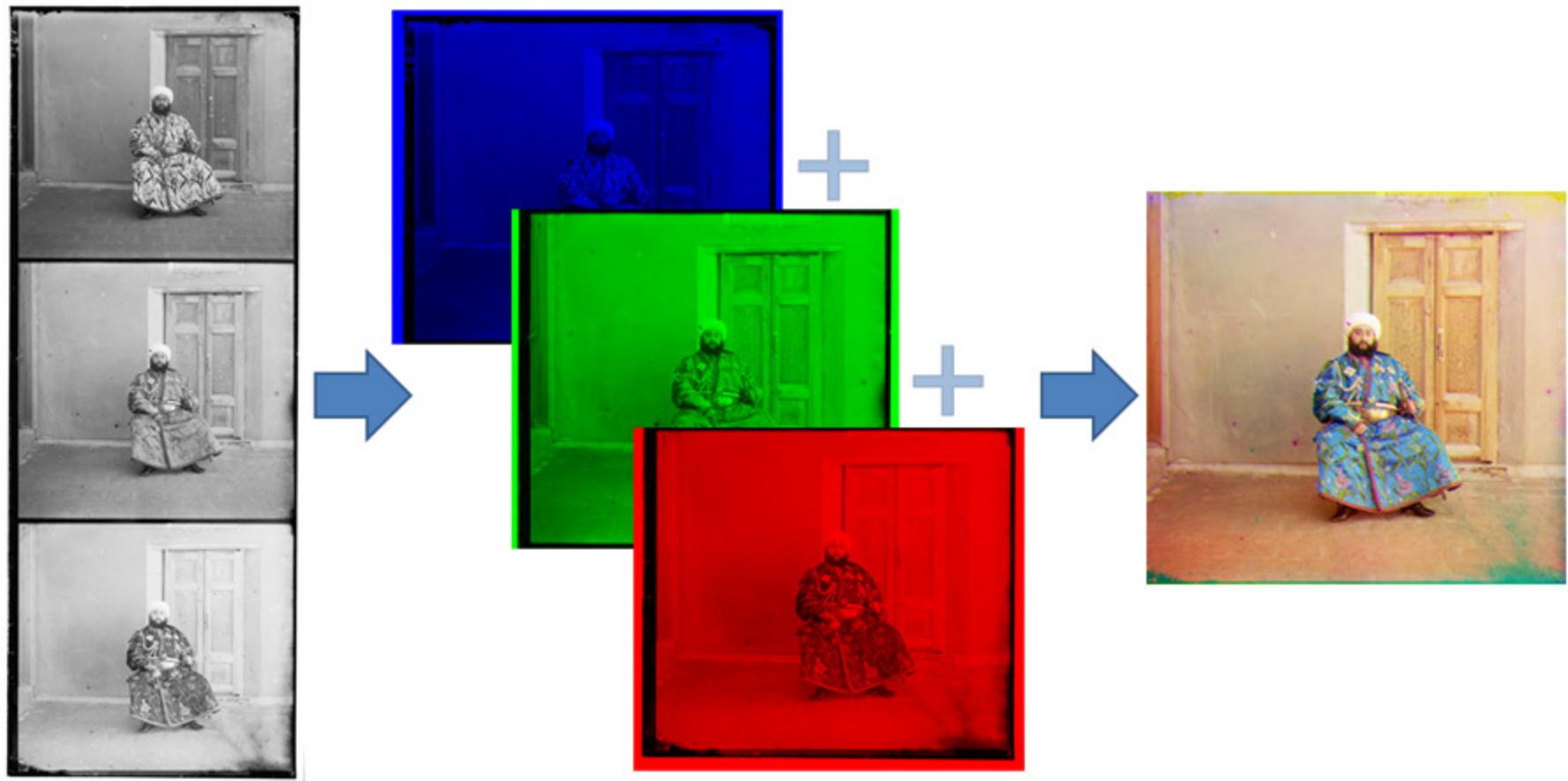


Programming Project #1

Prokudin-Gorskii's Color Photography (1907)



Programming Project #1



Programming Project #1

- How to compare R,G,B channels?
- No right answer
 - Sum of Squared Differences (SSD):

$$ssd(u, v) = \sum_{(x,y) \in N} [I(u + x, v + y) - P(x, y)]^2$$

- Normalized Correlation (NCC):

$$ncc(u, v) = \frac{\sum_{(x,y) \in N} [I(u + x, v + y) - \bar{I}] [P(x, y) - \bar{P}]}{\sqrt{\sum_{(x,y) \in N} [I(u + x, v + y) - \bar{I}]^2} \sum_{(x,y) \in N} [P(x, y) - \bar{P}]^2}$$



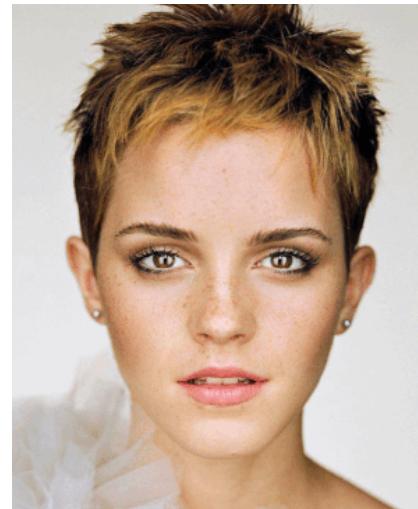
Student Presentation

Data-Driven Graphics (2000-2010)

- Graphcut Texture, SIGGRAPH 2003.
- Interactive Digital Photomontage, SIGGRAPH 2004.
- GrabCut, SIGGRAPH 2004.
- Hybrid Images, SIGGRAPH 2006.
- Photo Clip Art, SIGGRAPH 2007.
- Image Deformation Using Moving Least Squares. SIGGRAPH 2006.
- Seam Carving for Content-Aware Image Resizing, SIGGRAPH 2007.
- Sketch2Photo, SIGGRAPH Asia 2009.
- Coordinates for Instant Image Cloning, SIGGRAPH 2009
- ...



Thank You!



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16-726, Spring 2021

<https://learning-image-synthesis.github.io/>