```
(if (null? 1) 0 (+ 1 (length (cdr 1)))))
       (define (append 11 12)
         (if (null? 11) 12
           (cons (car 11) (append (cdr 11) 12))))
       (let x \leftarrow (cons 5 (cons (cons 6 nil) nil) in
         (let y \leftarrow (\cos 3 \text{ nil}) in
            (let z \leftarrow (append x y) in
              (if (null? (car z)) 0 \pi: (length z))))))
                     (a) Example program.
(b) Memory graph at \pi. (
                               ) denotes a closure. Thick edges
```

denote live links. Traversal stops at edges marked  $\times$  during garbage

collection for a liveness-based collector.

(define (length 1)

$$\begin{cases} \emptyset & \text{if } \sigma = \emptyset \\ \{\epsilon\} \cup \mathbf{0}\sigma & \text{otherwise} \end{cases}$$

$$GC(\rho_1, S_1, H_1, (\mathbf{let} \ x \leftarrow s \ \mathbf{in} \ e), \sigma) = (\rho, S, H)$$



$$\langle \mathsf{D}^1_{\mathrm{length}} \rangle \longrightarrow \begin{array}{c} 1,2 \\ 2 \\ 2 \\ \end{array}$$



$$\langle L_a \rangle \rightarrow \bigcirc 2 \rightarrow \bigcirc 0$$



$$GC(\rho_1, S_1, H_1, (\mathbf{let} \ x \leftarrow s \ \mathbf{in} \ e), \sigma) = (\rho, S, H)$$