

Subject: Greedy BFS

Date:

B → Branching
m → Max Depth

Time and space complexity of Greedy BFS $\Rightarrow b^{d^m}$
DFS $\Rightarrow b^m$

Approximate

Heuristic (h) \Rightarrow Distance from the Goal State.

1	2	3	Goal State	B = Blank
4	5	6	$h = 0$	Up = Blank Up
7	8			

Manhattan

Manhattan Distance is a Distance Measure that is calculated by taking the sum of distances between the x and y coordinates.

Goal
Given State

1	2	3
4	5	6
7	8	-

Given
Goal State

1	3	2
4	7	8
6	5	

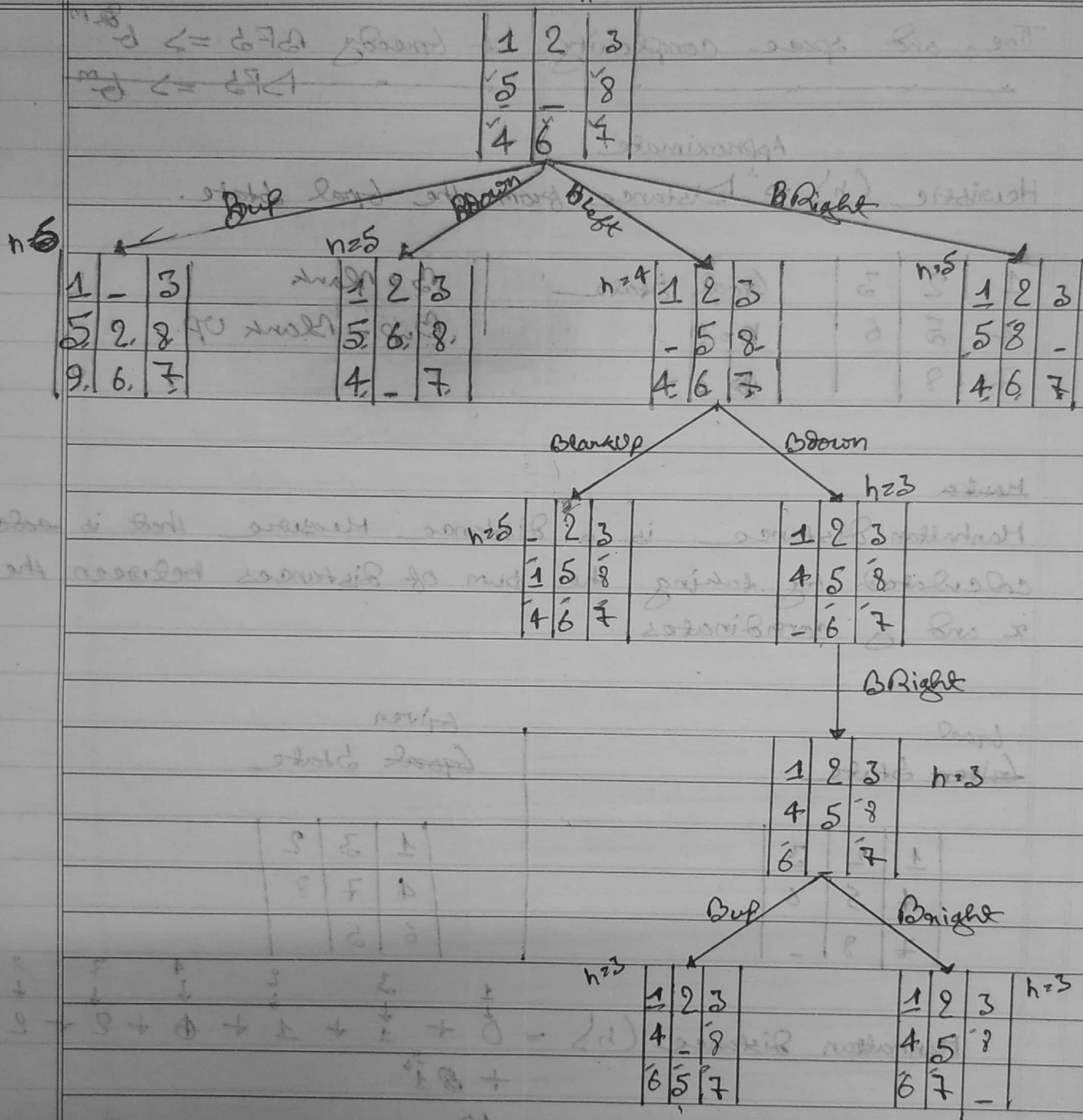
$$\text{Manhattan Distance (h)} = \overset{1}{\downarrow} 0 + \overset{3}{\downarrow} 1 + \overset{2}{\downarrow} 1 + \overset{4}{\downarrow} 1 + \overset{7}{\downarrow} 2 + \overset{8}{\downarrow} 2 + \overset{6}{\downarrow} 3 + \overset{5}{\downarrow} 1 = 10$$

A single problem can have multiple heuristic function. In such a case, we should choose the heuristic function that gives larger values.

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8 Puzzle state space Tree

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Say we have two heuristic functions named h_1 and h_2 . For all the nodes, if $h_1(n) \geq h_2(n)$, then we can say that h_1 dominates h_2 .

$$h_1(A) = 12, h_1(B) = 8, h_1(C) = 20, h_1(D) = 9$$

$$h_2(A) = 7, h_2(B) = 9, h_2(C) = 17, h_2(D) = 8$$

If we have two heuristic functions where for some of the nodes $h_1(n) \geq h_2(n)$ and for other nodes $h_2(n) \geq h_1(n)$ then we choose the heuristic function that happens to be true for more of the nodes. Otherwise, we can also take the best of both worlds i.e.

$h_1(A) \geq h_2(A)$. So for node A we will choose the heuristic function h_1 . Similarly for B we will choose h_2 and so on. In short, we will choose the heuristic function that provides a larger value than the other for function for that very node.

* For Tree and Heuristic Table, look A* search notes.

A³⁶⁶

GBFS \rightarrow NOT optimal

A³⁶⁶ [C³²⁹ E²⁵³ B³⁷⁴

Complete ?

E²⁵³ [C³²⁹ B³⁷⁴ G¹⁹³ F¹⁷⁸

Tree \rightarrow Incomplete

Graph \rightarrow Finite \rightarrow Complete

Infinite \rightarrow Incomplete

F¹⁷⁸ [C³²⁹ B³⁷⁴ G¹⁹³ I⁰

I⁰ [C³²⁹ B³⁷⁴ G¹⁹³

Time and Space Complexity :
 $\rightarrow O(b^m)$

When the goal node is expanded, the searching algorithm stops.

A \rightarrow E \rightarrow F \rightarrow I

Path cost = $140 + 99 + 211$
 $= 450$

A \rightarrow E \rightarrow G \rightarrow H \rightarrow I

path-cost = $140 + 80 + 97 + 101$
 $= 418$

Thus, optimal result is not achieved.

Optimal / sub-optimal path is defined using True cost whereas Greedy BFS is in its simulation does not even consider True path cost. It is entirely based on approximate path cost. So, the path output given by this algorithm will also be an approximate path.

All the search has two versions :

(i) Tree

(ii) Graph

Tree version has the tendency to get stuck in a loop.

In a Tree Search version, whether a parent has been visited or not is not kept track of. But in a graph search version, it is kept track of.

Tree Greedy BFS is not ^{Complete} optimal in any case. This infinite loop issue can be prevented using Graph Search version.

For finite trees, Graph GBFS is Complete.

" infinite " Incomplete.

Based upon the quality of the heuristic, the actual implementation time will come down lower if it is a good heuristic Function. So, if we use a decent quality heuristic that gives a good approximation, in practical implementation the time complexity decreases significantly compared to uninformed search.

A* search is the better version of GBFS.