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CSE422 Sec-07

ASSIGNMENT-1

CMR

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For consistent

$$h(P) \leq h(C) + c(P \rightarrow C)$$

$$h(A) \leq h(S) + c(A \rightarrow S)$$

$$\rightarrow 10 \leq 9 + 3$$

$$\rightarrow 10 \leq 12$$

$\therefore$  consistent

$$h(A) \leq h(B) + c(A \rightarrow B)$$

$$\rightarrow 10 \leq 2 + 7$$

$$\rightarrow 10 \leq 9$$

NOT consistent

So, Let's consider  $h(A) = 5$

Then it will be consistent

$$h(S) \leq h(R) + c(S \rightarrow R)$$

$$\rightarrow 9 \leq 5 + 5$$

$$\rightarrow 9 \leq 10$$

$\therefore$  consistent

$$h(S) \leq h(F) + c(S \rightarrow F)$$

$$\rightarrow 9 \leq 2 + 11$$

$$\rightarrow 9 \leq 13$$

$\therefore$  consistent

$$h(B) \leq h(G) + c(B \rightarrow G)$$

$$\rightarrow 2 \leq 0 + 4$$

$$\rightarrow 2 \leq 4$$

$\therefore$  consistent

$$h(R) \leq h(C) + c(R \rightarrow C)$$

$$\rightarrow 5 \leq 5 + 2$$

$$\rightarrow 5 \leq 7$$

~~$\therefore$  NOT consistent~~

$\therefore$  consistent

For admissible

$$h(n) \leq g(n)$$

$$h(A) \leq g(A)$$

$$\rightarrow 10 \leq$$

~~A~~  
~~S~~  
~~B~~  
~~F~~  
~~C~~  
~~R~~  
~~G~~  
~~B~~

$$h(C) \leq h(G) + c(C \rightarrow G)$$

$$\rightarrow 5 \leq 0 + 3$$

$$\rightarrow 5 \leq 3$$

NOT consistent

Let's take  $h(C) = 1$

Then consistent.

$$h(F) \leq h(G) + c(F \rightarrow G)$$

$$\rightarrow 2 \leq 0 + 6$$

$$\rightarrow 2 \leq 6$$

$\therefore$  consistent

$$h(G) \leq h(B) + c(G \rightarrow B)$$

$$\rightarrow 0 \leq 11 + 3$$

$$\rightarrow 0 \leq 14$$

Consistent

$$h(B) \leq h(A) + c(B \rightarrow A)$$

$$\rightarrow 11 \leq 5 + 13$$

$$\rightarrow 11 \leq 18$$

$\therefore$  Consistent.

$$h(A) \leq g(n)$$

$$\rightarrow 5 \leq 3+5+2+3$$

$$\rightarrow 5 \leq 13$$

$$h(A) \leq g(n)$$

$$\rightarrow 5 \leq 3+11+6$$

$$\rightarrow 5 \leq 20$$

$$h(A) \leq g(n)$$

$$\rightarrow 5 \leq 7+4$$

$$\rightarrow 5 \leq 11$$

~~A~~  
~~B~~  
~~C~~  
~~D~~  
~~E~~  
~~F~~  
~~G~~

$$h(B) \leq g(n)$$

$$\rightarrow 9 \leq 5+2+3$$

$$\rightarrow 9 \leq 10$$

$$h(B) \leq g(n)$$

$$\rightarrow 9 \leq 11+6$$

$$\rightarrow 9 \leq 17$$

$$h(E) \leq g(n)$$

$$\rightarrow 5 \leq 2+3$$

$$\rightarrow 5 \leq 5$$

$$h(C) \leq g(n)$$

$$\rightarrow 3 \leq 3$$

$$h(G) \leq g(n)$$

$$\rightarrow 0 \leq 0$$

Thus

Admissible

$$h(F) \leq g(n)$$

$$\rightarrow 2 \leq 6$$

$$h(D) \leq g(n)$$

$$\rightarrow 2 \leq 4$$

$$h(B) \leq g(n)$$

$$\rightarrow 11 \leq 13$$

$$\rightarrow 11 \leq 13+7+4$$

$$\rightarrow 11 \leq 24$$

$$\hline 11 \leq 3+11+6+13$$

$$\rightarrow 11 \leq 13+3+5+2+3$$

$$\therefore \begin{cases} h(A) = 5 \\ \text{and} \\ h(C) = 1 \end{cases}$$

$$h5(n) = \frac{h2(n)}{2} \quad | \quad h6(n) = \frac{h1(n) + h2(n)}{2}$$

$h6(n)$  takes the avg. values of both  $h1(n)$  and  $h2(n)$  whereas  $h5(n)$  only takes the value of  $h2(n)$ . So,  $h6(n)$  should always be dominant as it will output a bigger no. than  $h5(n)$ .

(iii)  ~~$h2(n)$~~   <sup>$h3(n)$</sup>  will expand maximum no. of nodes as it will not prune any node and expand nodes till the goal is reached.

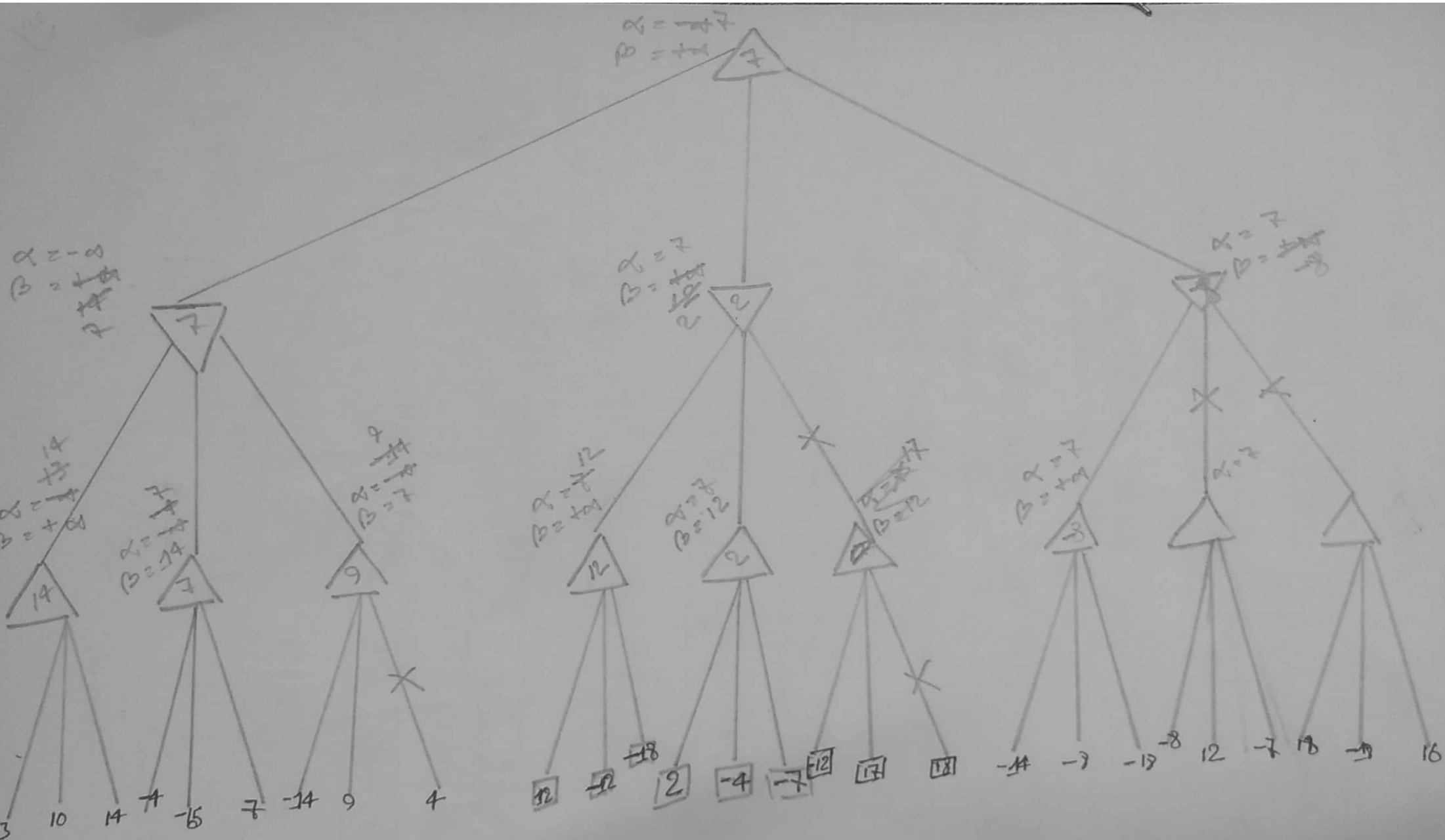
(iv)  $h7(n)$  should be best as it will give the min. value.

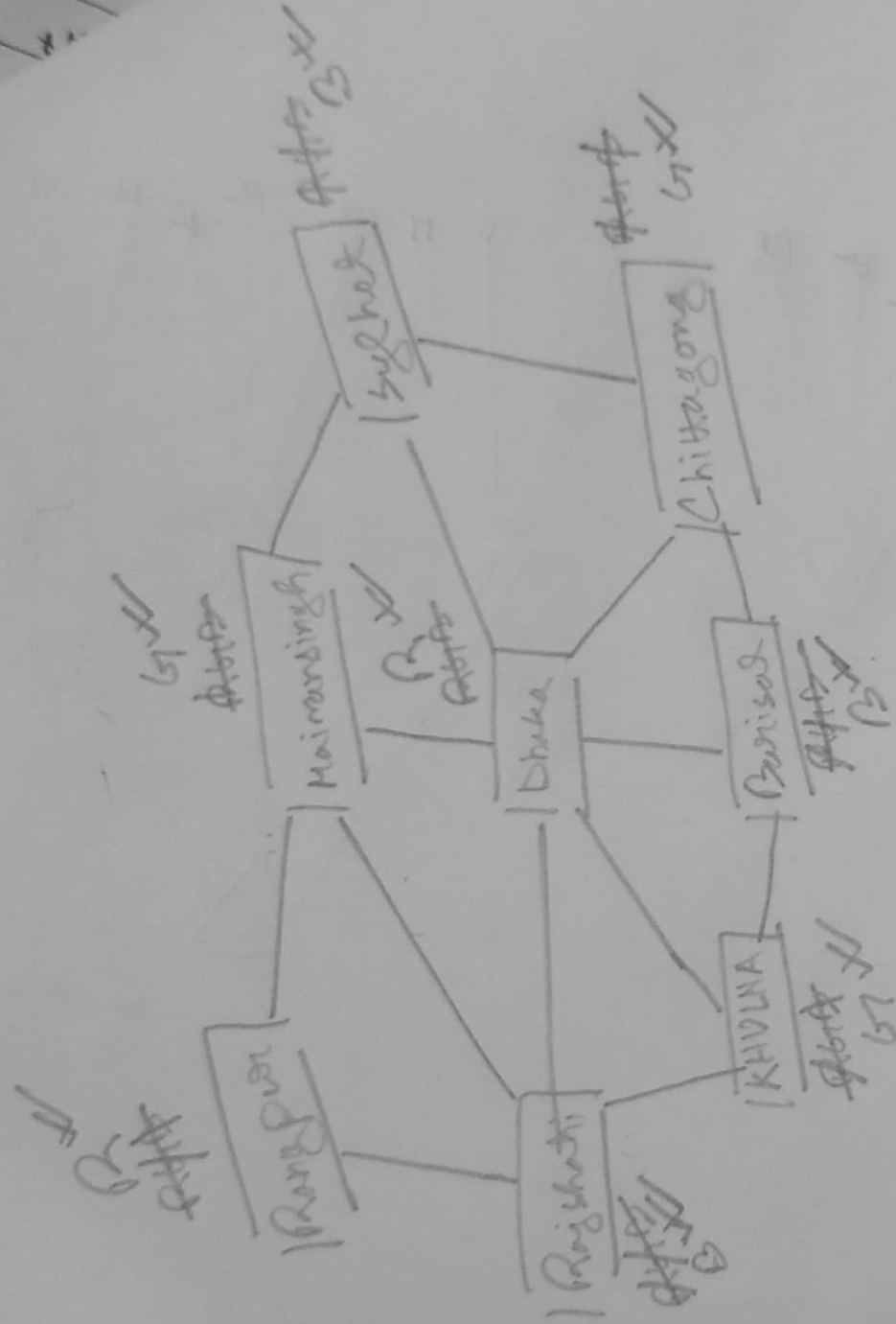
(i)  $h3(n)$  is possibly inadmissible.

3) Temperature is a control parameter that regulates the probability of making a bad move i.e. moving to a worse sol<sup>n</sup>. The amount of exploration vs exploitation on the search depends on the temperature.

Simulated Annealing has a higher probability of making a bad move at high temperatures. This allows the algo to consider more potential solutions. This helps the algo to escape a local optima and land on a global optima sol<sup>n</sup>. The probability of making a poor decision declines as the temperature drops, making it less likely that the algorithm would take a step that produces a worse outcome. As a result, the algorithm can maximize the benefits of the current sol<sup>n</sup> and move closer to the local optimum.

The tendency to go down from a higher place to a lower place decreases with decreasing temp. After a certain temp it stops going down and behaves like hill climb.





$A^7$   $B_A^{10}$   $B_A^6$   $C_A^9$

$B_A^6$   $B_A^{10}$   $C_A^9$   $H_{AE}^6$   $F_{AE}^9$

$H_{AE}^6$   $B_A^{10}$   $C_A^9$   ~~$F_{AE}^9$~~   $F_{AE}^9$   $X_{AEH}^9$

$C_A^9$   $B_A^{10}$   ~~$C_A^9$~~   $F_{AE}^9$   $X_{AEH}^9$   $E_{AC}^8$   $F_{AC}^9$   $G_{AC}^9$

$E_{AC}^8$   $B_A^{10}$   $F_{AE}^9$   $X_{AEH}^9$   ~~$E_{AC}^8$~~   $F_{AC}^8$   $G_{AC}^9$   $H_{ACE}^8$   $F_{ACE}^{11}$

$F_{AC}^8$   $B_A^{10}$   $F_{AE}^9$   $X_{AEH}^9$   $G_{AC}^9$   $H_{ACE}^8$   $F_{ACE}^{11}$   $H_{ACE}^7$

$H_{ACE}^7$   $B_A^{10}$   $F_{AE}^9$   $X_{AEH}^9$   $G_{AC}^9$   $H_{ACE}^8$   $F_{ACE}^{11}$   $X_{ACFH}^{10}$

$H_{ACE}^8$   $B_A^{10}$   $F_{AE}^9$   $X_{AEH}^9$   $G_{AC}^9$   $F_{ACE}^{11}$   $X_{ACFH}^{10}$   $X_{ACEH}^{11}$

$F_{AE}^9$   $B_A^{10}$   ~~$F_{AE}^9$~~   $X_{AEH}^9$   $G_{AC}^9$   $F_{ACE}^{11}$   $X_{ACFH}^{10}$   $X_{ACEH}^{11}$   $H_{AEF}^8$

$H_{AEF}^8$   $B_A^{10}$   $X_{AEH}^9$   $G_{AC}^9$   $F_{ACE}^{11}$   $X_{ACFH}^{10}$   $X_{ACEH}^{11}$   ~~$H_{AEF}^8$~~   $X_{AEFG}^{11}$

$G_{AC}^9$   $B_A^{10}$   $X_{AEH}^9$   ~~$G_{AC}^9$~~   $F_{ACE}^{11}$   $X_{ACFH}^{10}$   $X_{ACEH}^{11}$   $X_{AEFG}^{11}$   $X_{ACG}^8$

$X_{ACG}^8$   $B_A^{10}$   $X_{AEH}^9$   $F_{ACE}^{11}$   $X_{ACFH}^{10}$   $X_{ACEH}^{11}$   $X_{AEFG}^{11}$   ~~$X_{ACG}^8$~~

As the goal node is reached, the algo terminates.

$A \rightarrow B \rightarrow A \rightarrow B \rightarrow$

$$A \rightarrow C \rightarrow G \rightarrow X$$

Cost: 8

⑥  $h(A) \leq h(B) + c(A \rightarrow B)$

$$\rightarrow 7 \leq 5 + 5$$

$$\rightarrow 7 \leq 10$$

$$h(A) \leq h(E) + c(A \rightarrow E)$$

$$\rightarrow 7 \leq 4 + 2$$

$$\rightarrow 7 \leq 6 \text{ NOT consistent}$$

$$h(A) \leq h(C) + c(A \rightarrow C)$$

$$\rightarrow 7 \leq 6 + 3$$

$$\rightarrow 7 \leq 9$$

$$h(B) \leq h(D) + c(B \rightarrow D)$$

$$\rightarrow 5 \leq 3 + 2$$

$$\rightarrow 5 \leq 5$$

$$h(B) \leq h(E) + c(B \rightarrow E)$$

$$\rightarrow 5 \leq 4 + 1$$

$$\rightarrow 5 \leq 5$$

$$h(C) \leq h(E) + c(C \rightarrow E)$$

$$\rightarrow 6 \leq 4 + 1$$

$$\rightarrow 6 \leq 5$$

$$\therefore \text{NOT consistent}$$

$$h(C) \leq h(F) + c(C \rightarrow F)$$

$$\rightarrow 6 \leq 4 + 1$$

$$\rightarrow 6 \leq 5$$

$$\therefore \text{NOT consistent}$$

$$h(C) \leq h(G) + c(C \rightarrow G)$$

$$\rightarrow 6 \leq 2 + 4$$

$$\rightarrow 6 \leq 6$$

$$h(D) \leq h(H) + c(D \rightarrow H)$$

$$\rightarrow 3 \leq 2 + 2$$

$$\rightarrow 3 \leq 4$$

$$\therefore \text{NOT consistent}$$

$$h(D) \leq h(X) + c(D \rightarrow X)$$

$$\rightarrow 3 \leq 0 + 4$$

$$\rightarrow 3 \leq 4$$

$$h(E) \leq h(H) + c(E \rightarrow H)$$

$$\rightarrow 4 \leq 2 + 2$$

$$\rightarrow 4 \leq 4$$

$$h(E) \leq h(F) + c(E \rightarrow F)$$

$$\rightarrow 4 \leq 4 + 3$$

$$\rightarrow 4 \leq 7$$

$$h(F) \leq h(H) + c(F \rightarrow H)$$

$$\rightarrow 4 \leq 2 + 1$$

$$\rightarrow 4 \leq 3$$

$$\} \text{NOT consistent}$$

~~A~~  
~~B~~  
~~C~~  
~~D~~  
~~E~~  
~~F~~  
~~G~~  
~~H~~  
~~X~~



$$\begin{aligned}
 &h(a) \leq h(x) + c(a \rightarrow x) \\
 &\rightarrow 2 \leq 0 + 1 \\
 &\rightarrow 2 \leq 1 \text{ NOT consistent}
 \end{aligned}$$

$$\begin{aligned}
 &h(h) \leq h(x) + c(h \rightarrow x) \\
 &\rightarrow 2 \leq 0 + 5 \\
 &\rightarrow 2 \leq 5
 \end{aligned}$$

$$\begin{aligned}
 &h(x) \leq h(x) + c(x \rightarrow x) \\
 &\rightarrow 0 \leq 0 + 0 \\
 &\rightarrow 0 \leq 0
 \end{aligned}$$

$\therefore$  The Heuristic is not consistent for 6 cases.

~~$$\begin{aligned}
 h(A) &= 1 \\
 h(B) &= 2 \\
 h(C) &= 3 \\
 h(D) &= 4 \\
 h(H) &= 2
 \end{aligned}$$~~

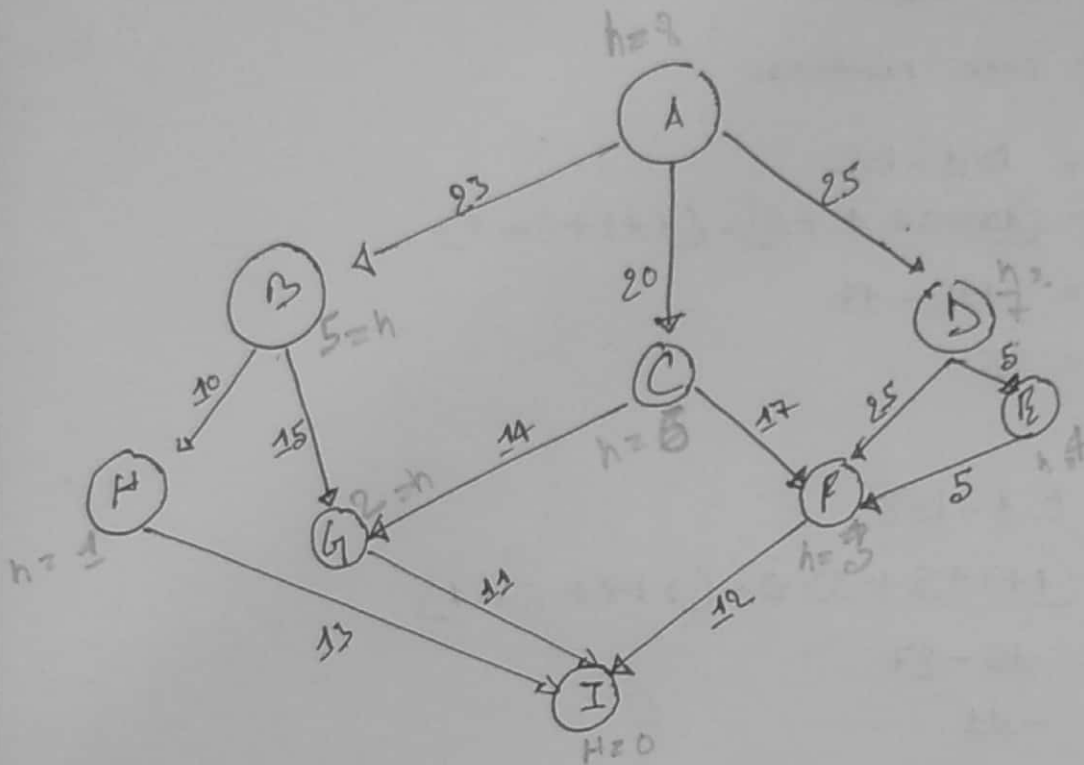
$$h(A) \leq h(I) + c(A \rightarrow I)$$

$$\rightarrow 2 \leq 0 + 11$$

$$h(H) \leq h(I) + c(H \rightarrow I)$$

$$\rightarrow 1 \leq 0 + 13$$

So, all the heuristic values are consistent



~~A~~  
~~B~~  
~~C~~  
~~D~~  
~~E~~  
~~F~~  
~~G~~  
~~H~~  
~~I~~

$$h(A) \leq h(B) + c(A \rightarrow B)$$

$$\rightarrow 8 \leq 5 + 23$$

$$h(A) \leq h(G) + c(A \rightarrow G)$$

$$\rightarrow 8 \leq 6 + 20$$

$$h(A) \leq h(D) + c(A \rightarrow D)$$

$$\rightarrow 8 \leq 7 + 25$$

$$h(B) \leq h(H) + c(B \rightarrow H)$$

$$\rightarrow 5 \leq 1 + 10$$

$$h(B) \leq h(G) + c(B \rightarrow G)$$

$$\rightarrow 5 \leq 2 + 15$$

$$h(C) \leq h(G) + c(C \rightarrow G)$$

$$\rightarrow 6 \leq 2 + 14$$

$$h(C) \leq h(F) + c(C \rightarrow F)$$

$$\rightarrow 6 \leq 3 + 17$$

$$h(D) \leq h(F) + c(D \rightarrow F)$$

$$\rightarrow 7 \leq 3 + 25$$

$$h(D) \leq h(E) + c(D \rightarrow E)$$

$$\rightarrow 7 \leq 5 + 5$$

$$h(E) \leq h(F) + c(E \rightarrow F)$$

$$\rightarrow 4 \leq 3 + 5$$

$$h(F) \leq h(I) + c(F \rightarrow I)$$

$$\rightarrow 3 \leq 0 + 12$$

② 100 1 3 2 4 1 5 1 - PC1

1 9 7 9 5 6 3 4 2 - PC2

These are generated randomly.

⑥ D1 ← Sum of odd numbers

D2 ← Sum of even numbers.

$$\begin{aligned}\therefore \text{Fitness - PC1} &= D1 - D2 \\ &= (100 + 3 + 4 + 5) - (1 + 2 + 6 + 1) \\ &= 112 - 11 \\ &= 95\end{aligned}$$

$$\begin{aligned}\text{Fitness - PC2} &= D1 - D2 \\ &= (1 + 7 + 5 + 3) - (9 + 9 + 6 + 4) \\ &= 16 - 27 \\ &= -11\end{aligned}$$

### Crossovers

① 100 1 3 2 5 6 3 4  
1 9 7 8 4 6 5 9

② 100 1 3 2 10 6 3 4  
1 9 20 8 4 6 5 9

Mutation

$$\begin{aligned}\text{Fitness - CC1} &= D1 - D2 \\ &= (100 + 3 + 10 + 3) - (1 + 2 + 6 + 4) \\ &= 116 - 13 \\ &= 103\end{aligned}$$

$$D1 - D2 = D1 - D2$$

$$= (1+20+4+5) - (9+8+6+8)$$

$$= 30 - 31$$

$$= -1$$

$\therefore$  Child Chromosome 2 is better.