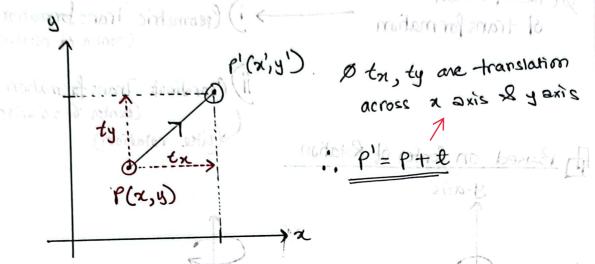
1) Translation:

& It is the repositionging of an object / pixel in a straight line



p'(x',y') & tn, ty are translation across x axis & y exis

o Representing as an equation:

Translation across y axis
$$y = y + ty - ii$$

$$(0,0,0)$$

& Motix representation:

i) Contesian Representation: montator to istno

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \end{bmatrix}$$
 ratio $\begin{bmatrix} 2x \\ x \end{bmatrix}$ are to conceptal

ii) Homogeneous Representation:

1) Iranslation

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & 0 & \text{fix} \\ 0 & 1 & \text{fiy} \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

S) Shearing

$$\begin{cases}
\chi' \\
y'
\end{cases} = \begin{bmatrix}
\chi + \ell\chi \\
y + \ell\chi
\end{bmatrix}$$

- (2) He mainly prefer to use Homogeneous containate system in Computer Graphics. But why?
 - -> Using Homogeneous coordinate eystem all an extra dimension to the 2D/3D Cantesian eystem. This allows us to be do alline /subtraction, but also allows us to perform multiplication of division. It can be used to generate composite Matrices combining multiple transformations that can be represented into a single matrix to reduce computations.
 - Ø So in Homogeneous Coordinate system:

 → for 20 we use (3x3) matrix

 → for 30 we use (4x4) matrix

3D Translation matrix representation (7, y, 2)

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & t_{x} \\ 0 & 1 & 0 & t_{y} \\ 0 & 0 & 1 & t_{z} \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

() (g)

Translate the point (3,2,7), 3 units in x-axis 4 units in y-axis & -3 units in the z-axis? $t_{z=3}$, $t_{y=4}$, $t_{z=-3}$

An

$$\begin{bmatrix} x' \\ y' \\ 2' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 3 \\ 0 & 1 & 0 & 4 \\ 0 & 0 & 1 & -3 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 3 \\ 2 \\ 7 \\ 1 \end{bmatrix}$$

=
$$\begin{pmatrix} 3 + 3 \\ \times 2 + 4 \\ \end{pmatrix}$$

$$= \begin{pmatrix} 3 + 3 \\ \times 2 + 4 \\ \end{pmatrix}$$

$$= \begin{pmatrix} 6 \\ 6 \\ 6 \end{pmatrix}$$

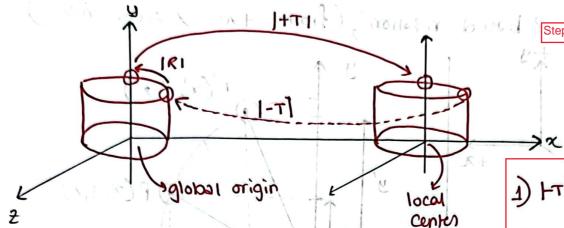
$$= \begin{pmatrix} 6 \\ 6 \\ 6 \end{pmatrix}$$

$$= \begin{pmatrix} 6 \\ 6 \\ 6 \end{pmatrix}$$

$$= \begin{pmatrix} 6 \\ 6 \\ 4 \end{pmatrix}$$

$$= \begin{pmatrix} 6 \\ 6 \\$$

Hon do me work on Rotation ?



generales a composite

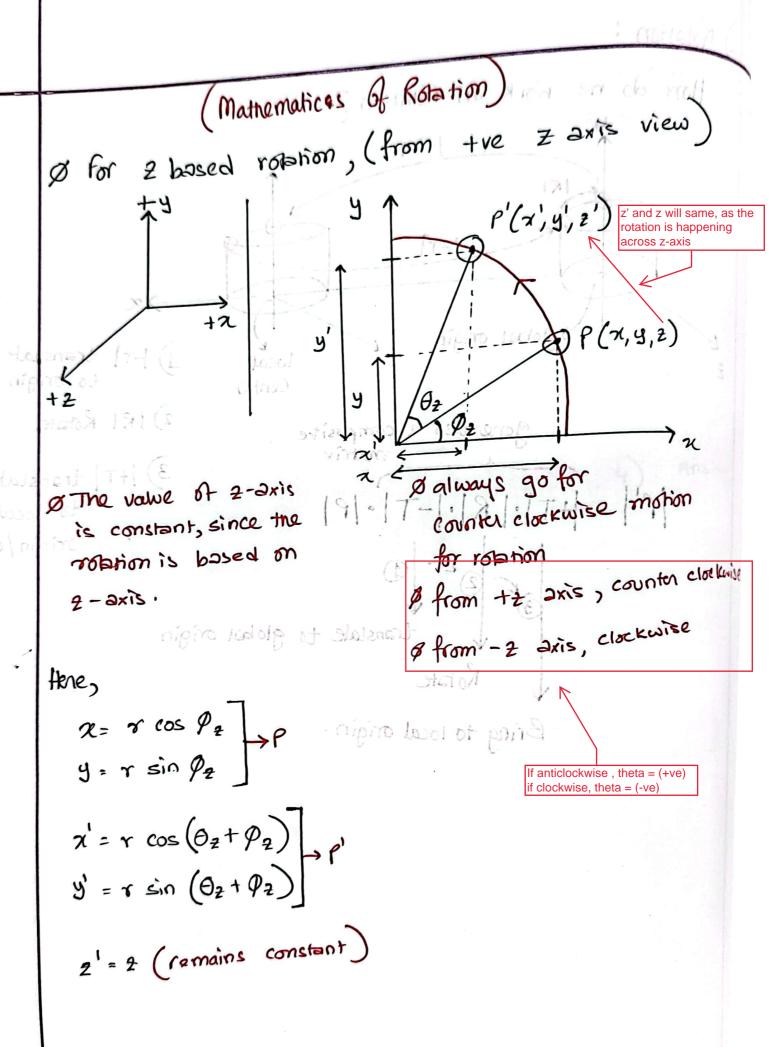
- - 2) IRI Robbe
 - 3) I+T | translake origin/center.

3 2 1 1 translate to global origin

For global center rotation

$$\mathsf{P'} = |\mathsf{R}|.|\mathsf{P}|$$

Bring to local origin.



```
He Know,

Cos (A+B) = cos A cos B - sin A sin B

sin (A+B) = cos A sin B - sin A cos B

Since,

x' = r cos (P+O)

y' = r sin (P+O)
```

$$y'=\tau \sin (\varphi + \theta)$$
 $z'=\tau \sin (\varphi + \theta)$
 $z'=\tau \sin (\varphi + \theta)$

He know,

21 = 2

Then,
$$\chi' = \chi \cos \theta - y \sin \theta$$

$$y' = \chi \sin \theta + y \cos \theta$$
Formula for x', y' and z'
$$y'' = \chi \sin \theta + y \cos \theta$$

x = r cos p

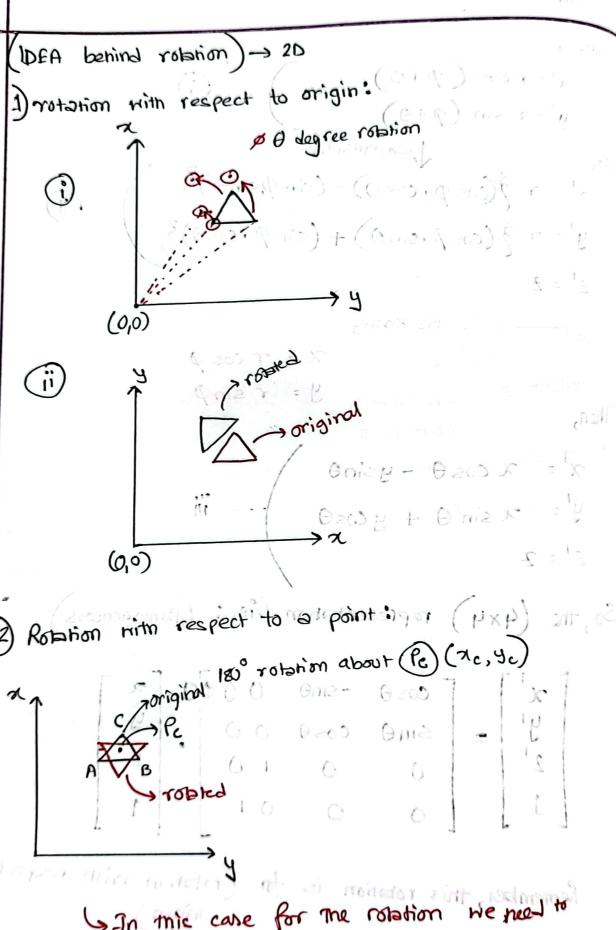
So, the (4x4) representation is (Homogeneous)

$$\begin{bmatrix} x' \\ y' \\ 2' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos\theta & -\sin\theta & 0 & 0 \\ \sin\theta & \cos\theta & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Homogeneous matrix representation for rotation on z-axis

Remember, this robin is for (robin with respect to the origin)

hence me don't need the 1+T/ & 1-T/ motrices.



Franciale to origin first, robbe, then translate back to local origin.

Robbte the point (9,2) at an angle of 45°, with respect to origin an find the result?

I since, we are dealing with a 2d point, we can eliminate the use of 2 axis for this.

$$\begin{bmatrix} \chi' \\ y' \end{bmatrix} = \begin{bmatrix} \cos 45 & -\sin 45 & 0 \\ \sin 45 & \cos 45 & 0 \end{bmatrix} \cdot \begin{bmatrix} 9 \\ 2 \\ 1 \end{bmatrix}$$

$$= \begin{cases} 4.95 \\ 7.78 \\ 7.78 \end{cases}$$
(Ans.)

OP nie - OP 200 OP nie

Robbte the point
$$(6,2)$$
 at an angle of 190° with respect to the point, $(2,2)$?

Hith respect to the point, $(2,2)$?

 $P' = \{ (2,2) : (2,3) : (2,2)$