

# MID-POINT LINE ALGORITHM (contd\*)

LECTURE 4

Equation of a line:

Implicit form  $\left\{ \begin{array}{l} y = mx + c \dots\dots (i) \end{array} \right.$ , where  $m = \frac{dy}{dx}$

↓

$\Rightarrow y = \frac{dy}{dx} \cdot x + c \dots\dots$  (multiply both sides with  $dx$ )

$\Rightarrow dx \cdot y = dy \cdot x + dx \cdot c \dots\dots$  (take  $dx \cdot y$  to the right hand side)

$\Rightarrow \underbrace{dy \cdot x}_{\downarrow} - \underbrace{dx \cdot y}_{\downarrow} + \underbrace{dx \cdot c}_{\downarrow} = 0 \dots\dots$

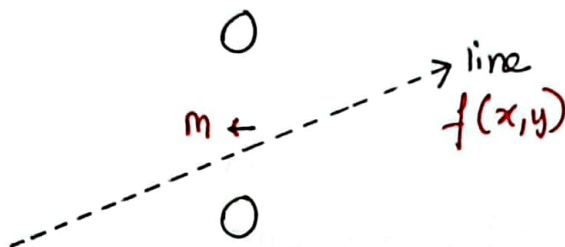
Explicit form  $\left\{ \right.$

$Ax + By + C = 0 \dots\dots (ii)$

(replace,  
✓  $dy = A$   
✓  $-dx = B$   
✓  $dx \cdot c = C$ )

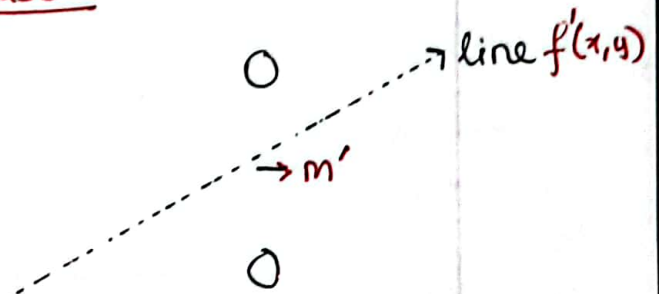
case 1

case 2



if we plug in the coordinates of  $M$  into the eqn of the line, the resulting value of the function will be (+ve)

$f(M) = +ve$



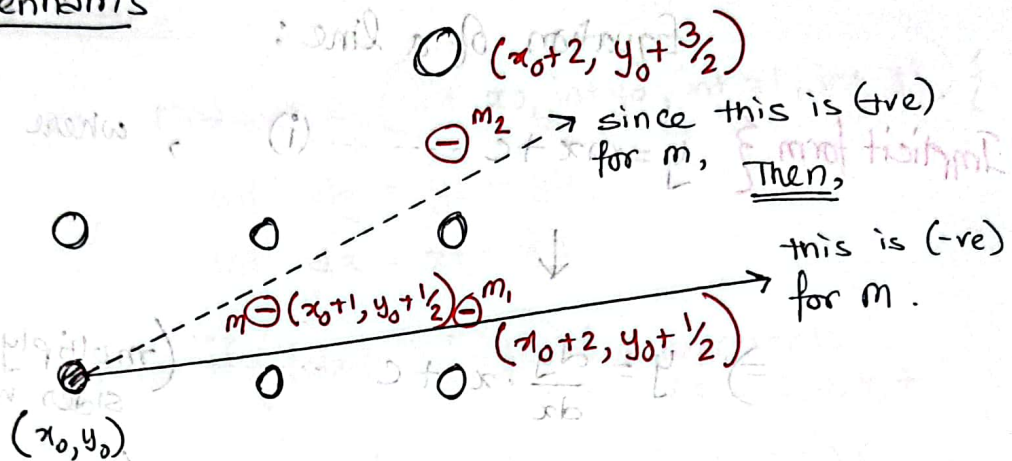
if we plug in the coordinates of  $M'$  into the eqn of the line, the resulting value of the function will be (-ve)

$f'(M') = -ve$



If  $dinit = +ve$ , under the mid point  
If  $dinit = -ve$ , over the mid point

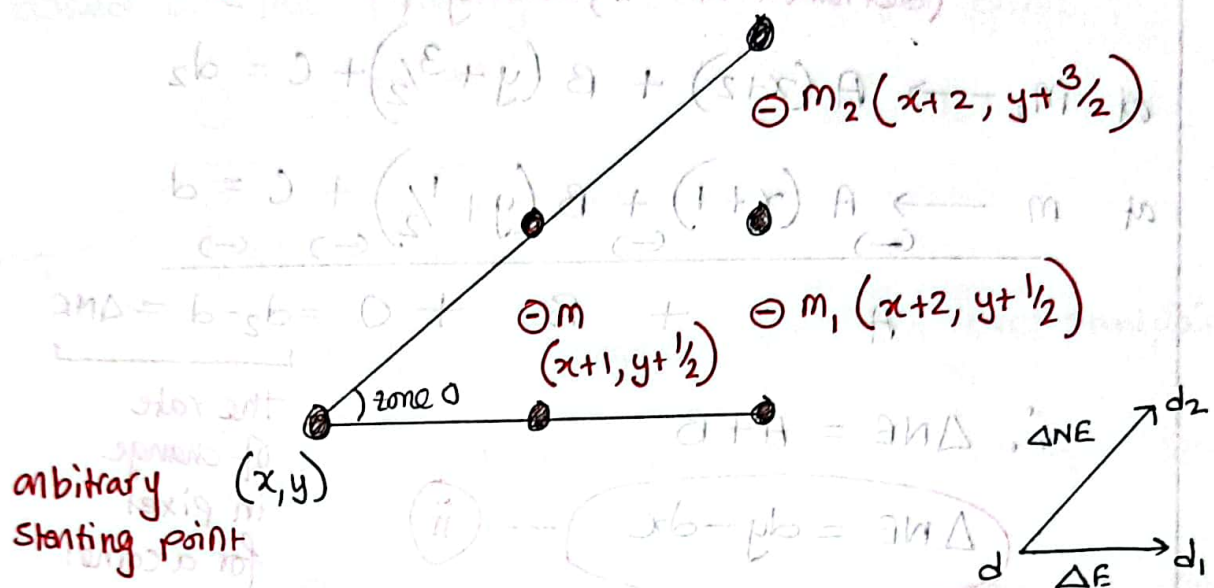
# Bresenham's



we will be considering the rate of change (in the deviation from the midpoint)

to further locate the pixels in the path.

# Designing the Algo for Zone 0.



(deviation at  $m_1$ , solving for  $\Delta E$ )

$$\text{at } m_1, \rightarrow A(x+2) + B(y+\frac{1}{2}) + C = d_1$$

$$\text{at } m, \rightarrow A(x+1) + B(y+\frac{1}{2}) + C = d$$

$$\text{Subtracting: } A + 0 + 0 = d_1 - d \approx \Delta E$$

$$\therefore A = \Delta E$$

meaning,  $\Delta E = dy$

(i)

the rate of change of pixel for a horizontal movement.



(deviation at  $m_2$ , solving for  $\Delta NE$ )

$$\text{at } m_2 \rightarrow A(x+2) + B(y+3/2) + C = d_2$$

$$\text{at } m \rightarrow A(x+1) + B(y+1/2) + C = d$$

$$A + B + 0 = d_2 - d = \Delta NE$$

$$\therefore \Delta NE = A + B$$

$$\Delta NE = dy - dx$$

ii

the rate of change in pixel for a corner movement.

we still need to solve for the initial deviation /  $d_{init}$  at  $m$ , for starting points  $(x_0, y_0)$

$$\text{at } m, A(x_0+1) + B(y_0+1/2) + C = d_{init}$$

It decide the next move of the pixel. Mostly for the first move.

$$\Rightarrow Ax_0 + By_0 + C + A + B/2 = d_{init}$$

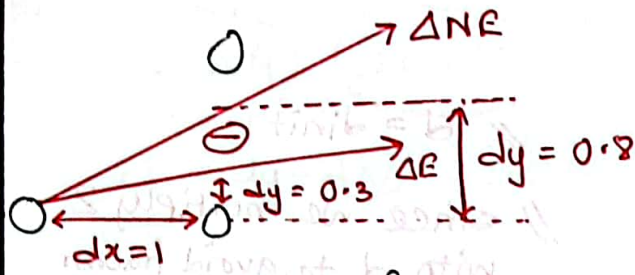
$$\Rightarrow d_{init} = A + B/2$$

since  $(x_0, y_0)$  is a coordinate from the line  $Ax_0 + By_0 + C = 0$

$$\Rightarrow d_{init} = dy - dx/2$$

iii

Ø Now, we need figure out if we'll move to  $\Delta E / \Delta NE$  based on the polarity of the value for  $d_{init}$ :



Ø for  $\Delta NE$ , where line goes over midpoint.

$$d_{init} = dy - \frac{dx}{2} = 0.8 - \frac{1}{2} = 0.3 (+ve)$$

Ø for  $\Delta E$ , where line goes below midpoint.

$$d_{init} = 0.3 - \frac{1}{2} = -0.2 (-ve)$$

\*  
∴ We can conclude that for a +ve value for  $d$  the movement will be  $\Delta NE$ ,  
AND,  
for a -ve value for  $d$  the movement will be  $\Delta E$ .

Pseudo Code (MPL Zone 0):

drawline ( $x_0, y_0, x_1, y_1$ ) {

$$dy = y_1 - y_0$$

$$dx = x_1 - x_0$$

$$d = 2dy - dx$$

//  $d = d_{init}$ .

$$dE = 2dy$$

// since we multiply 2 with  $d$  to avoid fraction

$$dNE = 2(dy - dx)$$

// we need to multiply

$dE$  &  $dNE$  with 2 as well.

$$x = x_0$$

$$y = y_0$$

draw( $x, y$ );

while ( $x \leq x_2$ ) {

if ( $d \leq 0$ ) {

// for  $dE$  movement only  $x$  increases.

$x++$

$$d += dE$$

// add  $dE$  to current value of  $d$

} else {

// for  $dNE$  movement  $x, y$  both increase by 1.

$x++$

$y++$

$$d += dNE$$

// add  $dNE$  to current value of  $d$ .

}

draw( $x, y$ )

}

}



For zone 0,3,4,7 >> x increase by 1  
As all this zone x goes parallel  
For zone 1,2,5,6 >> y increase by 1  
As all this zone y goes parallel

Q1) Draw (30,50) to (40,54) using MPL

$dy = 4$ ,  $dx = 10$

$d = dy - dx/2 = 2(dy) - dx = 8 - 10 = -2$   
use this to avoid fraction.

$\Delta E = 2 \cdot dy = +8$

$\Delta NE = 2(dy - dx) = 2(4 - 10) = -12$

If  $dinit \geq 0$ , it is over the mid point or y increases by 1 which is NE.

If  $dinit < 0$ , it is under the mid point or y remains same which is E.

x	y	d	$\Delta E / \Delta NE$	(PIXEL)
30	50	-2	$\Delta E$	(30,50)
31	50	6	$\Delta NE$	(31,50)
32	51	-6	$\Delta E$	(32,51)
33	51	2	$\Delta NE$	(33,51)
34	52	-10	$\Delta E$	(34,52)
35	52	-2	$\Delta E$	(35,52)
36	52	6	$\Delta NE$	(36,52)
37	53	-6	$\Delta E$	(37,53)
38	53	2	$\Delta NE$	(38,53)
39	54	-10	$\Delta E$	(39,54)
40	54	-2	$\Delta E$	(40,54)

If move to E,  $dinit += \Delta E$

if move to NE,  $dinit += \Delta NE$

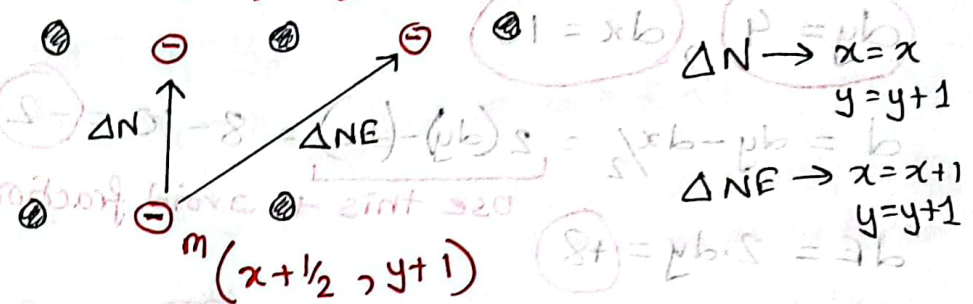
done

$x_b - x_s = \text{len}$

# Ø Home Assignment Design for Zone 1 & Zone 5

Zone 1

$$m_1(x+\frac{1}{2}, y+2) \quad m_2(x+\frac{3}{2}, y+2)$$



$$\Delta N \rightarrow x=x, y=y+1$$

$$\Delta NE \rightarrow x=x+1, y=y+1$$

Ø  $\Delta N$

at  $m_1$   
at  $m$

$$A(x+\frac{1}{2}) + B(y+2) + C = d_1$$

$$\hookrightarrow A(x+\frac{1}{2}) + B(y+1) + C = d$$

$$0 + B + 0 = \Delta N$$

$$\therefore \Delta N = -dx \rightarrow \text{we'll use } [-2dx]$$

Ø  $\Delta NE$

at  $m_2$   
at  $m$

$$A(x+\frac{3}{2}) + B(y+2) + C = d_2$$

$$\hookrightarrow A(x+\frac{1}{2}) + B(y+1) + C = d$$

$$A + B = \Delta NE$$

$$\therefore \Delta NE = dy - dx \rightarrow \text{we'll use } [2(dy - dx)]$$

Ø  $d_{init}$

at  $m$   
 $(x_0, y_0)$

$$A(x_0+\frac{1}{2}) + B(y_0+1) + C = d_{init}$$

$$A/\frac{1}{2} + B = d_{init}$$

$$\therefore d_{init} = dy/\frac{1}{2} - dx \rightarrow \text{we'll use } [dy - 2dx]$$