

MAE 101C

Ch 6

MAE 101C: Final study sheet

$$c = \lambda f \quad \frac{[Hz]}{[nm]} \quad \text{speed of light, } 3 \times 10^8 \text{ m/s}$$

$$\alpha + \rho = 1 \quad \begin{matrix} \text{absorptivity} \\ \text{reflectivity} \end{matrix}$$

ϵ : emittance

$\epsilon = 1$ for blackbody

$J = \text{outgoing radiation energy}$
 $G = \text{incoming radiation energy}$
 reciprocal rule

$$F_{21} = \frac{A_1}{A_2} F_{12}$$

gray surface

why $\alpha = \epsilon$

string rule pg 464

Black body: absorbs all radiation falling upon it
 Emission is diffuse: no preferred direction
 Max Emission

Stefan-Boltzmann law

$$E_b = \sigma T^4$$

$$\sigma = 5.67 \times 10^{-8} \text{ W/m}^2 \text{K}^4$$

Shape factor

F_{12} : fraction of energy leaving A_1 that is intercepted by A_2

$$\dot{Q}_{12} = E_{b1} A_1 F_{12} - E_{b2} A_2 F_{21}$$

Emittance ratio of radiant emittance of object / "blackbody"

Absorptance: ratio of radiative flux absorbed / received

absorbs all incident radiation

$$J = \epsilon_1 \sigma T_1^4 + (1 - \epsilon_1) [F_{12} J_2 + F_{13} J_3]$$

Refractory: $\dot{Q} = 0$

$$\dot{Q} = 0 = J - G$$

$$J = G$$

Ch 6

MAE 101C: Final study sheet

$c = \lambda f$ [Hz] [mm]
 speed of light, 3×10^8 m/s

Black body: absorbs all radiation falling upon it
 Emission is diffuse: no preferred direction
 Max Emission

$\alpha + \rho = 1$
 absorptivity reflectivity

Stefan-Boltzmann law

$E_b = \sigma T^4$
 $\sigma = 5.67 \times 10^{-8} \text{ W/m}^2 \text{K}^4$

ϵ : emittance

$\epsilon = 1$ for blackbody
 outgoing

Radiosity

$J = \text{incoming radiation energy}$
 $G = \text{incoming}$
 reciprocal rule

Shape factor

F_{12} : fraction of energy leaving A_1 that is intercepted by A_2

$\dot{Q}_{12} = E_{b1} A_1 F_{12} - E_{b2} A_2 F_{21}$

$F_{21} = \frac{A_1}{A_2} F_{12}$

Emittance ratio of radiant emittance of object / "blackbody"

gray surface

Absorptance: ratio of radiant flux absorbed / received

why $\alpha = \epsilon$

absorbs all incident radiation

string rule pg 464

$J = \epsilon_1 \sigma T_1^4 + (1 - \epsilon_1) [F_{12} J_2 + F_{13} J_3]$

Refractory: $\dot{Q} = 0$

$\dot{Q} = 0 = J - G$

$J = G$

101C Notes

ch1

$$q = -k \frac{dT}{dx}$$

$$\text{Thermal resistance: } R = \frac{L}{kA}$$

air = low conductivity = high resistance

$$\frac{U}{A} = \frac{1}{hA}$$

thermal conductivity

overall heat transfer coefficient

U? problem
How to find?

Lumped thermal capacity

valid if $\text{conductive} \gg \text{convective}$

$$Bi = \frac{\text{convective}}{\text{conductive}} \quad \text{If } < 0.1, \text{ valid}$$

$$= \frac{h_c L_{eff}}{k} \quad \sim \frac{V}{A}$$

$$\frac{T - T_e}{T_0 - T_e} = \exp\left(-\frac{t}{t_c}\right) \quad t_c = \frac{\rho V c}{h_c A}$$

ρ : density

c : thermal capacity

h : heat transfer coeff

convection

Equilibrium temp:

$$M_1 C_1 (T_{0,1} - T_2) = M_2 C_2 (T_2 - T_{0,2})$$

$$q = h_c \Delta T$$

Radiative heat transfer b/w bodies

emittance

$$Q_{12} = \epsilon_1 A_1 \sigma (T_1^4 - T_2^4)$$

$$\epsilon_1 = \text{emissivity factor}$$

$$q = \sigma (T_1^4 - T_2^4)$$

First Law

$$\rho C V \frac{dT}{dt} = \dot{Q} + \dot{Q}_r$$

$$\rho V = \text{mass}$$

σ = Stefan-Boltzmann constant

$$\dot{Q}_{\text{net}} = \dot{Q}_{\text{in}} - \dot{Q}_{\text{out}}$$

ch2

$$q = -k \frac{dT}{dx}$$

Fourier's law: $\dot{Q} = 4\pi r^2 (-k \frac{dT}{dr})$ for shell

\dot{Q}_v''' = volumetric thermal energy generation rate

$$\dot{Q}_{\text{loss}} = \frac{T(r_0) - T_e}{R_{\text{tot}}}$$

Energy balance \rightarrow governing equation

Apply BCs

$$\dot{Q}_x - \dot{Q}_{x+\Delta x} + \dot{Q}_v''' A \Delta x = 0$$

Fin

$$B = \sqrt{\frac{h_c p}{kA}}$$

p = perimeter

$$\dot{Q}_{\text{fin}} = h_c P L (T_b - T_e) \frac{\tanh(BL)}{BL}$$

Prandtl number (Pr)

$$Pr = \frac{\nu}{\alpha} = \frac{\text{viscous diffusion rate}}{\text{thermal diffusion rate}}$$

ch 3 pg

$$\frac{T_A - T_i}{T_i - T_B} = \left(\frac{(k\rho c)_B}{(k\rho c)_A} \right)^{1/2}$$

$$\frac{310 - T_i}{T_i - 263} = \left(\frac{(0.1)(500)(2400)}{(990)(4180)(0.628)} \right)^{1/2}$$

$$310 - T_i = 0.2149 (T_i - 263)$$

$$310 - T_i = 0.2149 T_i - 56.5$$

$$1.2149 T_i = 366.5$$

$$T_i = 301.671$$

$$T_i = 28.7^\circ$$

Ch 3: conduction

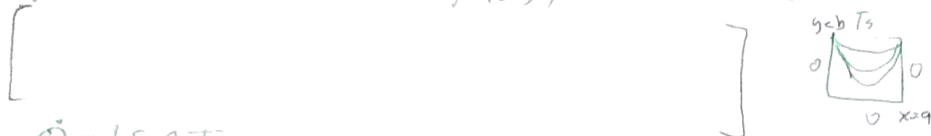
$\theta = T - T_0$ to have non-zero sides ^{fewer}

Superposition: $\theta(x,y) = c_1 \theta_1(x,y) + c_2 \theta_2(x,y)$

Eq. (3.30) rotate to match Figure 3.7

$\theta_1(y, 1-x)$ 90° CW

$\theta_2(1-y, x)$ 90° CW



$$\dot{Q} = kS \Delta T$$

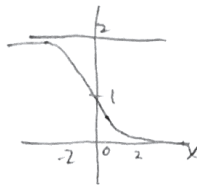
shape factor [m]

$$\text{erfc}(\eta) = \frac{2}{\sqrt{\pi}} \int_{\eta}^{\infty} e^{-t^2} dt$$

$$\eta = \frac{x}{2\sqrt{\alpha t}}$$

$$\theta = \frac{T - T_0}{T_s - T_0} \text{ dimensionless temp}$$

α = thermal diffusivity



1. energy balance

$$qA|_x - qA|_{x+\Delta x} + \dot{Q}''' \Delta V = 0$$

$$- \epsilon A \sigma T^4$$

$$- h_c \Delta x \Delta T_p$$

Laplace's equation

$$\frac{\partial^2 \theta}{\partial x^2} + \frac{\partial^2 \theta}{\partial y^2} = 0$$

$$\theta(x,y) = X(x)Y(y)$$

$$X'' - \lambda^2 X = 0, Y'' + \lambda^2 Y = 0$$

$$\theta = X\bar{Y} = (A_1 e^{\lambda x} + A_2 e^{-\lambda x})(B_1 \sin \lambda y + B_2 \cos \lambda y)$$

Convection problems:

find equation and calculate \dot{Q}

Ch 4: convection

$$Re = \frac{\rho V D}{\mu}$$

Turbulent flow: $Re_0 \approx 2300$ in pipe, $Re_0 \approx 50,000$ for flat plate

Nusselt number: $\frac{\text{convective}}{\text{conductive}}$ heat transfer, across fluid boundary

~~Bi = $\frac{hL_c}{k}$~~ ~~convective~~ ~~conductive~~ ~~inside~~ ~~outside~~

solid body vs. fluid
(Bi) (Nu)

If $Bi < 0.1$, conductive \Rightarrow convective inside outside

$$Bi = \frac{hL_c}{k}$$

Pipes: evaluate at average temp properties

