

Modified Pseudocode

The original pseudo code had the counter incrementing only when elements got moved around, but what we want is for the counter to increment with every comparison.

The solution was to move the `A[j] > v` comparison outside the while loop into it's own if clause right after incrementing count as long as '`j >= 0`' is true.

```
SortAnalysis(A[0 .. n-1])
//input: Array A[0..n-1] of n orderable elements
//output: Total number of key comparisons made

count <- 0
for i <- 1 to n-1 do
  v <- A[i]
  j <- i-1
  while j>=0 do
    count <- count + 1
    if A[j] > v then
      A[j+1] <- A[j]
      j <- j - 1
    else
      break
  A[j+1] <- v
```

Summary of Results

Based on our analysis, we found that the *comparisons per n^2* stayed relatively consistent (around 0.25)

Raw Data

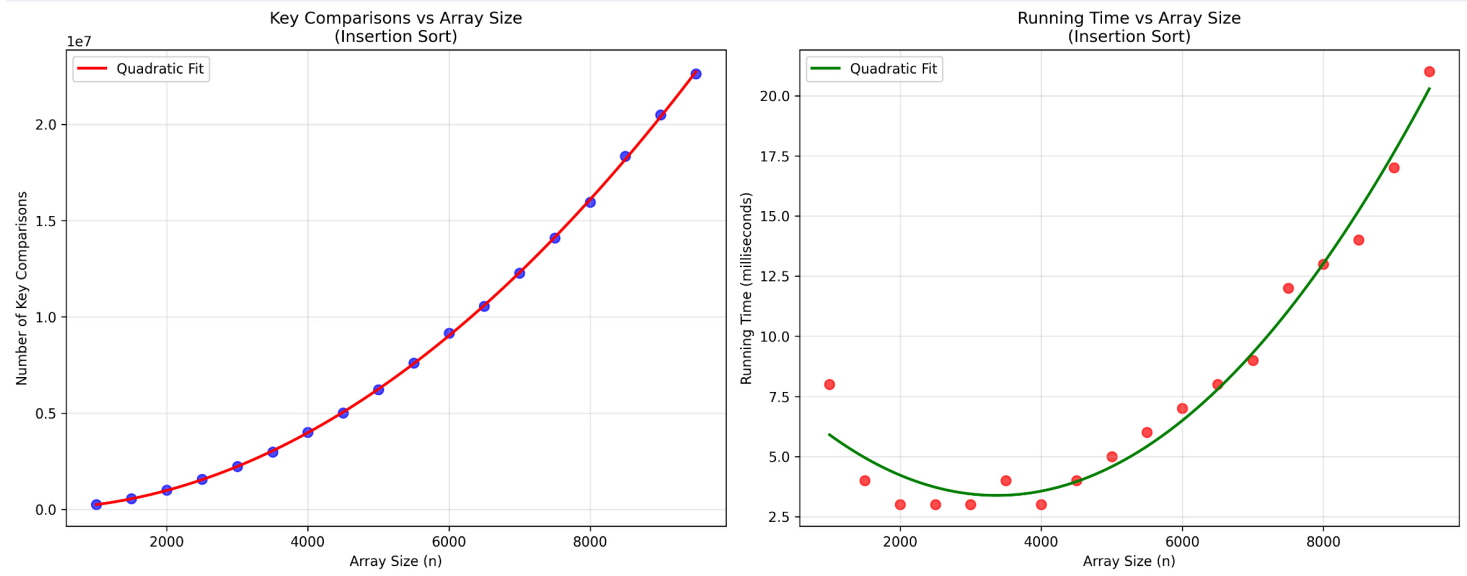
```
!!python3 /home/dev/projects/school/CSC401-Project1/analysis.py
=== DATA SUMMARY ===
Data points analyzed: 18
Array size range: 1000 - 9500
Minimum comparisons: 244,783
Maximum comparisons: 22,127,480

Predicted comparisons for n=10,000: 24,801,693
Predicted running time for n=10,000: 20.8 ms

=== DETAILED RESULTS TABLE ===
Size | Comparisons | Time (ms) | Comp/n2 | Theoretical
-----
1000 | 244,783 | 4.0 | 0.244783 | 249,750
1500 | 559,028 | 13.0 | 0.248457 | 562,125
2000 | 997,692 | 1.0 | 0.249423 | 999,500
2500 | 1,580,953 | 2.0 | 0.252952 | 1,561,875
3000 | 2,270,047 | 3.0 | 0.252227 | 2,249,250
3500 | 3,069,543 | 2.0 | 0.250575 | 3,061,625
4000 | 4,020,316 | 3.0 | 0.251270 | 3,999,000
4500 | 5,033,262 | 3.0 | 0.248556 | 5,061,375
5000 | 6,191,463 | 4.0 | 0.247659 | 6,248,750
5500 | 7,524,604 | 5.0 | 0.248747 | 7,561,125
6000 | 8,909,020 | 7.0 | 0.247473 | 8,998,500
6500 | 10,621,300 | 7.0 | 0.251392 | 10,560,875
7000 | 12,164,766 | 9.0 | 0.248261 | 12,248,250
7500 | 14,166,612 | 12.0 | 0.251851 | 14,060,625
8000 | 16,191,149 | 13.0 | 0.252987 | 15,998,000
8500 | 18,027,718 | 13.0 | 0.249519 | 18,060,375
9000 | 20,180,375 | 15.0 | 0.249140 | 20,247,750
9500 | 22,127,480 | 17.0 | 0.245180 | 22,560,125

Press ENTER or type command to continue
```

Graph



From the data, we can conclude that comparisons roughly quadruple when we double the array size, which implies a time complexity of $O(n^2)$

The theoretical analysis on insertion sort expects about $(n^2)/4$ comparisons for any given random data. This is consistent with our ratio of ~ 0.249 .

Predicting $n=10,000$

Based on our program, our predictions would be:

- **24,801,693 comparisons**
- **~ 20.8 milliseconds**

The theoretical prediction would be:

$$T(10000) = \frac{10000^2}{4} = 25,000,000 \text{ comparisons}$$

This is pretty close to our results we got.

Algorithm Analysis

For Insertion sort:

- Best case – when array is already sorted $\rightarrow O(n)$
- Average case – for random data $\rightarrow O(n^2)$
- Worst case – reverse sorted array $\rightarrow O(n^2)$

This confirms our experiment which was testing for the average case.