

## Name: KEY - DO NOT REPRODUCE

## Assignment 4.02: Projectiles - KEY

- 1. A cannon is placed on level ground. It is aimed 25 degrees above horizontal. The cannonball leaves the cannon with an initial speed of 300 m/s.
  - (a) What is the horizontal component of the initial velocity  $(v_{ix})$ ?

$$v_{ix} = v_i \cos(\theta) = 300 m/s \cos(25^\circ) \approx 271.892 \text{ m/s}$$

(b) What is the vertical component of the initial velocity  $(v_{iy})$ ?

Using up as Positive: 
$$v_{iy} = v_i \sin(\theta) = 300 m/s \sin(25^\circ) \approx 126.786 \text{ m/s}$$

(c) What is the time it takes for the cannonball to reach its maximum height?

$$v_{fy} = v_{iy} + a_y t \longrightarrow t = \frac{v_{fy} - v_{iy}}{a_y} = \frac{0m/s - 126.786m/s}{-9.81m/s^2} \approx 12.924 \text{ s}$$

(d) What is the maximum height of the cannonball?

$$d_y = v_{iy}t + \frac{1}{2}a_yt^2 = (126.786m/s)(12.924s) + \frac{1}{2}(-9.81m/s^2)(12.924s)^2 \approx 819.294m$$

(e) What is the total time of flight for the cannonball?

$$t_{total} = 2 \times t = 2 \times 12.924s = 25.848s$$

(f) How far from the cannon does the cannonball land?

$$d_x = v_{ix}t + \frac{1}{2}a_xt^{-1} = (271.892m/s)(25.848s) \approx 7027.864m$$

- 2. A golfer hits a ball on a level golf-course at 35 m/s, 45° above horizontal.
  - (a) What is the amount of time it takes the golf-ball to reach its maximum height (hint: find  $v_{ix}$  and  $v_{iy}$  first).

$$v_{ix} = v_i \cos(\theta) = 35m/s \cos(45^\circ) \approx 24.749 \text{ m/s}$$
  
 $v_{iy} = v_i \sin(\theta) = 35m/s \sin(45^\circ) \approx 24.749 \text{ m/s}$   
 $v_{fy} = v_{iy} + a_y t \longrightarrow t = \frac{v_{fy} - v_{iy}}{a_y} = \frac{0m/s - 24.749m/s}{-9.81m/s^2} \approx 2.523 \text{ s}$ 

(b) What is the total time the golf ball is in the air?

$$t_{total} = 2 \times t = 2 \times 2.523s = 5.046s$$

(c) How far away does the golf ball land?

$$d_x = v_{ix}t + \frac{1}{2}a_xt^{2^{-0}} = (24.749m/s)(5.046s) \approx 124.873m$$



- 3. Kay is attempting to kick a football through the field-goal posts. She kicks the ball at 18 m/s at a  $35^{\circ}$  angle to the ground. She is 20 meters from the goal-post.
  - (a) What are the initial vertical and horizontal velocities of the football?

$$v_{ix} = v_i \cos(\theta) = 18m/s \cos(35^\circ) \approx 14.745 \text{ m/s}$$
  
 $v_{iy} = v_i \sin(\theta) = 18m/s \sin(35^\circ) \approx 10.324 \text{ m/s}$ 

(b) How long does it take the football to travel the distance to the goal post? (Hint – does this depend on the vertical direction or the horizontal direction?)

$$d_x = v_{ix}t + \frac{1}{2}a_xt^{2^{-0}} \longrightarrow t = \frac{d_x}{v_{ix}} = \frac{20m}{14.745m/s} \approx 1.356s$$

(c) What is the height of the football when it passes the goal-post?

$$d_y = v_{iy}t + \frac{1}{2}a_yt^2 = (10.324m/s)(1.356s) + \frac{1}{2}(-9.81m/s^2)(1.356s)^2 \approx 4.980m$$

(d) Assuming the football is kicked straight, does she score 3 points for her team?

Yes! (The field-goal crossbar in American Football is 10 feet, or a little over 3 meters high.)

- 4. Briana is hunting wild turkeys. She sees a turkey sitting on a branch at the top of a tree that is 35 meters away. She aims her bow at a 25° angle, and shoots the arrow with a speed of 65 m/s. The turkey is hit, and falls to the ground. Briana picks up the turkey and takes it home to save for thanksgiving dinner.
  - (a) What are the initial vertical and horizontal velocities of the arrow?  $v_{ix} = v_i \cos(\theta) = 65m/s\cos(25^\circ) \approx 58.910 \text{ m/s}$  $v_{iy} = v_i \sin(\theta) = 65m/s\sin(25^\circ) \approx 27.470 \text{ m/s}$
  - (b) How long does it take for the arrow to hit the turkey?

$$d_x=v_{ix}t+\frac{1}{2}a_xt^2$$
  $\longrightarrow t=\frac{d_x}{v_{ix}}=\frac{35m}{58.910m/s}\approx 0.594s$ 

(c) How high up was the turkey sitting?

$$d_y = v_{iy}t + \frac{1}{2}a_yt^2 = (27.470m/s)(0.594s) + \frac{1}{2}(-9.81m/s^2)(0.594s)^2 \approx 14.589m$$

(d) How long does the turkey take to fall to the ground?

For the turkey, using up as positive:

$$d_y = v_{ig}t^0 + \frac{1}{2}a_yt^2 \longrightarrow t = \sqrt{\frac{2d}{a}} = \sqrt{\frac{2\times(-14.589m)}{-9.81m/s^2}} \approx 1.725s$$