

Things to Memorize: Circular Motion and Orbits

### Centripetal Force and Acceleration

- Any force that causes an object to move in a circle is a **centripetal force**.
- A centripetal force is always directed toward the center of the circle the object moves in. (The word *centripetal* means "center-seeking".)

### Kepler's Laws

- 1. All planets move about the Sun in elliptical orbits, having the Sun as one of the foci.
  - The eccentricity determines how close to a circle an objects orbit is.

Shape	Eccentricity
Circle	$\varepsilon = 0$
Elipse	$0 < \varepsilon < 1$
Parabola	$\varepsilon = 1$
Hyperbola	$\varepsilon > 1$

- All 8 planets have very low eccentricity. (For example,  $\varepsilon_{Earth} = 0.0167086$ )
- Some comets follow hyperbolic paths.
- 2. A radius vector joining any planet to the Sun sweeps out equal areas in equal lengths of time.
  - This means planets move faster when closer to the sun and slower when farther from the sun.
- 3. The squares of the sidereal periods (of revolution) of the planets are directly proportional to the cubes of their mean distances from the Sun.
  - This law works for any set of objects that orbit the same central body. So two planets, a planet and a comet, and even two moons of Jupiter will work. It does NOT work when the two objects do not orbit the same central body.

#### Universal Gravitation

• Universal Gravitation is used when you wish to find the force of gravity between two objects when they are separated by significant distances.

#### Orbital Motion

- In order for an object to have a stable orbit, **gravity** must act as a **centripetal force**.
- Combining Newton's Law of Universal Gravitation with centripetal force allows Kepler's 3rd Law to be derived.



• Most orbital motion problems will require you to equate the formula for Universal Gravitation with the formula for centripetal force.

## Angular Velocity and Acceleration

Before Beginning this section, be sure to review the section on Arc Length.

- Angular Velocity measures how quickly something is rotating.
  - Units: rad/s
  - Symbol:  $\omega$
- **Angular Acceleration** measure how quickly an object's angular velocity is changing (speeding up or slowing down).
  - Units:  $rad/s^2$
  - Symbol:  $\alpha$

## **Angular Kinematics**

## Torque

# **Angular Momentum**