

Scivault Physics

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Version 202029

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Chapter 1

Introduction

1.1 Dimensional Analysis and SI units

The **SI** system of units is the standard used by many scientists throughout the world. There are seven *fundamental* or *base* quantities from which all other measurements are derived. These quantities are listed below:

Table 1.1: **SI Units**

Quantity	Unit	Unit Symbol
time	second	s
length	meter	m
mass	kilogram	kg
electrical current	Ampere	A
temperature	Kelvin	K
amount of substance	mole	mol
luminous intensity	candela	cd

Of these quantities, mass, time and length are quite common. Thus, this system is sometimes called the MKS (meter, kilogram, second) system. In order to use any equations, all measurements must have correct units. For example, if a time is expressed in hours, it must first be converted into seconds before any calculations can be attempted.

Dimensional analysis is the process in which the units associated with quantities create *derived units*. For instance, when a distance is divided by a time, the units will be $\frac{m}{s}$ (read *meters per second*).

Dimensional analysis is an important part of solving physics problems. Often, correct dimensional analysis can help you determine if a problem has been solved correctly. One should not even attempt to calculate an answer to a problem until the correct units have been verified.

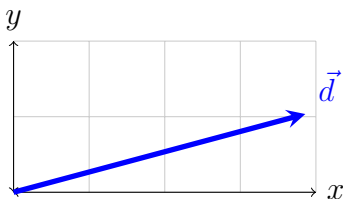
1.2 Vectors and Scalars

In the study of physics, there are two types of quantities that we will deal with on a regular basis: *scalars* and *vectors*.

A **scalar** is a quantity that you are already most likely very familiar with, as it is just a number; scalars have only a *magnitude* (a number that represents how big or strong it is), and can sometimes include units. Examples of scalars might be the number of people in a room, the mass of a car, or your age in years.

Vectors are different from scalars because in addition to a magnitude, they contain a direction as well. Examples of vectors might include 50 feet to the north, 5 m/s at a 33° angle, or 200 miles straight up. There are many ways of expressing vectors. Symbolically, they are often written with an arrow over them. For example, in the equation $\vec{F} = m\vec{a}$ both force and acceleration are vectors – meaning that both force and acceleration have a direction. Sometimes vectors will be expressed in **bold** typeface. Hence, the expression $\mathbf{F} = m \mathbf{a}$ is equivalent to the expression shown above.

The direction for vectors in 1 dimension is easy – all you need is a positive or a negative. Usually, 1-dimensional motion takes place along the x-axis (left and right), but sometimes it will take place in the y- (forward and backward) and z- (up and down) dimensions. For the purposes of this book, positive is to the right and up unless otherwise stated. In two dimensions, a vector requires two pieces of information. One way of expressing a vector is in polar form. Polar form in two dimensions includes a magnitude of the vector and an angle, usually measured from the x-axis. There are several ways for writing this. 4 cm @ 15° , 4 cm $\angle 15^\circ$ and 4 cm at 15° North of East all represent the following displacement vector:



Unit vectors are vectors that have a length of one unit and are oriented along one axis. The unit vector for the x-direction is written as \hat{i} (pronounced i-hat). \hat{i} is a 1-unit long vector that is always parallel to the x-axis, and points in the direction of increasing x values. Likewise, the y-direction and z-direction unit vectors are written as \hat{j} and \hat{k} respectively.

Because the surface of a paper is effectively 2-dimensional, it is very hard to draw lines that are oriented directly into or out of your paper. For this purpose, physicists have agreed to the following convention: vectors that point directly into your paper are notated by \otimes . Vectors that point directly out of your paper are shown by the symbol \odot .

Sometimes, vectors may be expressed in Cartesian coordinates. This vector could either be expressed as an ordered pair (or triple) with square brackets, such as $[3, 4, 5]$ cm, or as a linear combination of the unit vectors shown above, such as $5\hat{i} + 12\hat{j} + 3\hat{k}$. In each case, the distances in each direction are given by the numbers shown.

When converting between polar and cartesian forms for two dimensional vectors, a little trigonometry shows:

$$x = r \cos(\theta) \quad (1.1)$$

$$r = \sqrt{x^2 + y^2} \quad (1.3)$$

$$y = r \sin(\theta) \quad (1.2)$$

$$\theta = \tan^{-1}\left(\frac{y}{x}\right) \quad (1.4)$$

In three dimensions, polar form comes in two types – Cylindrical and Spherical. In cylindrical coordinates, expressed as $[r, \theta, z]$, the above conversions are used, and the z -coordinate remains unchanged from Cartesian form. We will study spherical coordinates more in **INSERT REFERENCE HERE!**

1.3 Vector Mathematics

1.3.1 Vector Addition

1.3.2 The Dot Product

1.3.3 The Cross Product

Chapter 2

Kinematics in One Dimension

2.1 Distance and Displacement

You are probably already familiar with the concept of **distance** – you might get in your car and drive a total of 1.2 miles to school, turning right after 0.45 miles, according to your car’s odometer. Distance is a scalar that tells you how far something traveled. d usually represents distance.

While you may have traveled a total distance of 1.2 miles from your school, you are significantly less than 1.2 miles away from home; in fact, you are approximately 0.874 miles from home, following a direct path directly from your home to the school, at an angle of 59° (not worrying that this path might take you through someone’s back yard or kitchen). **Displacement** is a vector that tell you how far something is from the origin, and is independent of the path taken to get there. The displacement vector is commonly symbolized by \vec{r} though sometimes it may be written as \vec{d} .

2.2 Average and Instantaneous Speed and Velocity

Speed is a scalar value that represents the change in distance per change in time of an object. Speed is usually represented with the symbol v , without the vector sign. You are probably already familiar with this quantity, since the speedometer on your family car measures speed. For the purposes of physics, speed has little value because it is a scalar that tells us nothing of direction. Much more useful is the concept called velocity. Velocity and speed are related much like distance and displacement.

Velocity is the change in displacement of an object per unit time, and as such is a vector. Positive velocities indicate that the object is moving forward, relative to the axis in question, and negative velocities generally mean that the object is moving backward, relative the the axis. The average velocity of an object is given by:

$$\overrightarrow{v_{avg}} = \frac{\Delta \vec{r}}{\Delta t} \quad (2.1)$$

Average velocity is useful if an object's velocity is not changing. However, many times it is more useful to talk about instantaneous velocity. Instantaneous velocity tells us how fast an object is moving at a given instant in time. In order to calculate instantaneous velocity, we must allow our time interval in the above formula to become infinitesimally small. In this case, a little calculus proves:

$$\vec{v} = \frac{d\vec{r}}{dt} \quad (2.2)$$

Calculation of average velocity is rather straightforward, assuming you know both distance traveled and the time it took. If an object is not speeding up or slowing down during a specific time interval, the instantaneous velocity at any time during this interval is equal to the average velocity. If the object does speed up or slow down during the time interval in question, the average velocity and the instantaneous velocity at a certain time during the interval are not necessarily the same.

Example 2.2.1

You ride your bicycle in a straight line for a distance of 73 meters in 12.5 second. What is your average velocity?

Solution:

$$a \quad (2.3)$$

2.3 Relative Motion at Constant Velocity

2.4 Acceleration

2.5 The Kinematic Equations

2.6 Vertical Motion and Gravity

Appendices

Appendix A

Math Skills

A.1 Scientific Notation

A.2 Algebra

A.3 Trigonometry

A.4 Arc Length and Radians

Appendix B

Reference Tables

B.1 Greek Letters

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