

**Question 1: (10 points)**

For a Correct drawing of the situation - 3 Points

For showing correct vectors for velocity, with units . 1 Point

For showing component vectors of each velocity 1 Point

For indicating  $\theta$  as the direction in which the dart Gun fires 1 Point

For correct Calculations - 6 Points

For any indication (stated or implied) that x-component velocities must be equal 2 Points

For stating:  $\sin(\theta) = \frac{7 \frac{\text{m}}{\text{s}} \cdot \sin(45)}{25 \frac{\text{m}}{\text{s}}}$  or  $\theta = \sin^{-1} \left( \frac{7 \cdot \frac{\text{m}}{\text{s}} \cdot \sin(45)}{25 \cdot \frac{\text{m}}{\text{s}}} \right)$  2 Points

For an answer consistent with previous work 1 Point

For the correct numerical answer 1 Point

For correct units throughout the problem 1 Point

**Question 2: (10 points)**

Part A: 1 Point

For any indication of a parabola in the sketch of the graph 1 Point

Part B: 2 Points

For choosing a transformation that will linearize data (either  $t^2$  or  $\sqrt{h}$ ) 1 Point

For calculation of values consistent with the transformation chosen. 1 Point

Part C: 3 Points

For Labels and Units on both axes 1 Point

For a Graph consistent with calculated values 1 Point

For a Linear Graph 1 Point

Part D: 3 Points

For correctly calculating slope (linear regression or slope formula) 1 Point

For stating (or implying) that  $m = \frac{g_m}{2}$  1 Point

For a numerical answer consistent with previous work 1 Point

Throughout: For correct use of units throughout the problem 1 Point

**Question 3: (10 points)**

## Part A: 4 Points

For showing a Positive Velocity of magnitude 1.5 m/s between 0s and 8 s, inclusive 1 Point

For showing zero velocity between 10s and 18s inclusive 1 Point

For showing a negative velocity of magnitude 2.4 m/s between 20s and 25s inclusive 1 Point

For showing two non-vertical transition regions for  $8s < t < 10s$  and  $18s < t < 20s$  1 Point

## Part B: 5 Points

For a Definition or equation for average acceleration

ie:  $a_{\text{avg}} = \frac{\Delta v}{\Delta t}$  or  $v_f = v_i + a \cdot t$  1 Point

For the correct substitution of numbers from part A 1 Point

For an answer consistent with previous work 1 Point

For the correct magnitude for the numerical answer (0.75) 1 Point

For correct units and sign:  $a_{\text{avg}} = -0.75 \frac{\text{m}}{\text{s}^2}$  1 Point

## Part C: 1 Point

For a correctly drawn vector, with or without a label, pointing downward. 1 Point

**Question 4: (10 points)** For this solution x is to the right, y is up in the second picture and z-is elevation. However, any coordinate system that obeys the right-hand rule is acceptable.

Part A: (3 Points)

For stating  $\Delta d_x = \frac{1}{2} \cdot a_x \cdot \Delta t^2 + v_{ix} \cdot \Delta t$  or  $v_x = \frac{\Delta d_x}{\Delta t}$  1

Point

For stating (or implying)  $\Delta t = \frac{\Delta d_x}{v_x}$  1

Point

For a correct expression for time:  $\Delta t = \frac{L}{2 \cdot v_i \cdot \cos(\theta)}$  or equivalent. 1 Point

Part B: (3 Points)

For stating  $\Delta d_z = \frac{1}{2} \cdot a_z \cdot \Delta t^2 + v_{iz} \cdot \Delta t$  or  $v_z = \frac{\Delta d_z}{\Delta t}$  1 Point

For stating (or implying)  $\Delta t = \sqrt{\frac{2 \Delta d_x}{a_z}}$  1 Point

For a correct expression for time:  $\Delta t = \sqrt{\frac{2 \cdot l}{g}}$  1 Point

Part C: (3 Points)

For stating (or implying) that the total time of flight is the sum of the times in parts A and B 1 Point

For a correct displacement vector of the following form (or equivalent) 2 Points

$$\vec{d} = \left( \frac{L}{2} + v_i \cdot \cos(\theta) \cdot \sqrt{\frac{2 \cdot l}{g}} \right) \cdot \vec{i} + \left( \frac{L}{2} \cdot \tan(\theta) + v_i \cdot \sin(\theta) \cdot \sqrt{\frac{2 \cdot l}{g}} \right) \cdot \vec{j} - L \cdot \vec{k}$$

Throughout: (1 Point)

For defining a coordinate system that obeys the right-hand rule 1 Point

**Question 4: (10 points)****Part A: (3 Points)**

For a correct diagram of the situation, including labels 1 Point

For correctly stating  $a = g \cdot \sin(25)$  1 Point

For an answer consistent with previous work ( $a = g \cdot \sin(25 \cdot \text{deg}) = 4.144 \frac{\text{m}}{\text{s}^2}$ ) 1 Point

**Part B: (3 Points)**

For correctly stating a kinematic equation(s) to find final velocity 1 Point

ie:  $v_f^2 = v_i^2 + 2 \cdot a \cdot \Delta d$  or  $\Delta d = \frac{1}{2} \cdot a \cdot \Delta t^2 + v_i \cdot \Delta t$  and  $a = \frac{v_f - v_i}{\Delta t}$

For substitution of quantities correctly

ie:  $v_f = \sqrt{0^2 + 2 \cdot \left(4.144 \cdot \frac{\text{m}}{\text{s}^2}\right) \cdot 3 \cdot \text{m}}$  1 Point

For an answer consistent with previous work , 1 Point

ie:  $v_f = 4.986 \frac{\text{m}}{\text{s}}$

**Part C: (3 Points)**

For correctly using the z-direction to calculate the time of fall 1 Point

ie:  $10 \cdot \text{m} = \frac{1}{2} \cdot (g) \cdot t^2 + (v_f) \cdot \sin(25 \cdot \text{deg}) \cdot t \rightarrow t = 1.229 \cdot \text{s}$

For an answer consistent with previous work 1 Point

ie:  $\vec{d} = 5.554 \text{m} \cdot \vec{i} - 10 \cdot \text{m} \cdot \vec{k}$

**Part D: (1 Point)**

Correctly answering "yes" with mathematical justification. 1 point

**Throughout: (1 Point)**

For correct use of units 1 Point