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import numpy as np
import pdb
This code was originally written for CS 231n at Stanford University
(cs231n.stanford.edu). It has been modified in various areas for use in the
ECE 239AS class at UCLA. This includes the descriptions of what code to
implement as well as some slight potential changes in variable names to be
consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for
permission to use this code. To see the original version, please visit
cs231n.stanford.edu.
def affine forward(x, w, b):
 Computes the forward pass for an affine (fully-connected) layer.
 The input x has shape (N, d 1, \ldots, d k) and contains a minibatch of N
 examples, where each example x[i] has shape (d_1, \ldots, d_k). We will
 reshape each input into a vector of dimension D = d \ 1 \ * \ldots \ * \ d \ k, and
 then transform it to an output vector of dimension M.
 Inputs:
 - x: A numpy array containing input data, of shape (N, d 1, ..., d k)
 - w: A numpy array of weights, of shape (D, M)
 - b: A numpy array of biases, of shape (M,)
 Returns a tuple of:
 - out: output, of shape (N, M)
  - cache: (x, w, b)
  # ------ #
  # YOUR CODE HERE:
  # Calculate the output of the forward pass. Notice the dimensions
    of w are D x M, which is the transpose of what we did in earlier
    assignments.
  # ----- #
 reshaped input = np.reshape(x, (x.shape[0], -1))
 out = np.dot(reshaped input, w) + b
  # END YOUR CODE HERE
  # ----- #
 cache = (x, w, b)
 return out, cache
def affine_backward(dout, cache):
 Computes the backward pass for an affine layer.
 Inputs:
 - dout: Upstream derivative, of shape (N, M)
 - cache: Tuple of:
    - x: A numpy array containing input data, of shape (N, d 1, ..., d k)
   - w: A numpy array of weights, of shape (D, M)
   - b: A numpy array of biases, of shape (M,)
 Returns a tuple of:
  - dx: Gradient with respect to x, of shape (N, d1, ..., d k)
 - dw: Gradient with respect to w, of shape (D, M)
  - db: Gradient with respect to b, of shape (M,)
 x, w, b = cache
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dx, dw, db = None, None, None
 # YOUR CODE HERE:
  Calculate the gradients for the backward pass.
 # Notice:
 # dout is N x M
   dx should be N x d1 x ... x dk; it relates to dout through multiplication with w, which
is D x M
   dw should be D x M; it relates to dout through multiplication with x, which is N x D
after reshaping
 # db should be M; it is just the sum over dout examples
 dx = np.dot(dout, w.T).reshape(x.shape)
 dw = np.dot(x.reshape(x.shape[0], -1).T, dout)
 db = np.sum(dout, axis=0)
 # ----- #
 # END YOUR CODE HERE
 # ============== #
 return dx, dw, db
def relu forward(x):
 Computes the forward pass for a layer of rectified linear units (ReLUs).
 - x: Inputs, of any shape
 Returns a tuple of:
 - out: Output, of the same shape as x
 # ------ #
 # YOUR CODE HERE:
  Implement the ReLU forward pass.
 # ----- #
 out = np.maximum(x, 0)
 # ------ #
 # END YOUR CODE HERE
 # ------ #
 cache = x
 return out, cache
def relu_backward(dout, cache):
 Computes the backward pass for a layer of rectified linear units (ReLUs).
 Input:
 - dout: Upstream derivatives, of any shape
 - cache: Input x, of same shape as dout
 Returns:
 - dx: Gradient with respect to x
 x = cache
 # ------ #
 # YOUR CODE HERE:
 # Implement the ReLU backward pass
 # ------ #
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# ReLU directs linearly to those > 0
 dx = dout * (x >= 0)
  # ------ #
  # END YOUR CODE HERE
  return dx
def batchnorm_forward(x, gamma, beta, bn_param):
 Forward pass for batch normalization.
 During training the sample mean and (uncorrected) sample variance are
 computed from minibatch statistics and used to normalize the incoming data.
 During training we also keep an exponentially decaying running mean of the mean
 and variance of each feature, and these averages are used to normalize data
 at test-time.
 At each timestep we update the running averages for mean and variance using
 an exponential decay based on the momentum parameter:
 running mean = momentum * running mean + (1 - momentum) * sample mean
 running var = momentum * running var + (1 - momentum) * sample var
 behavior: they compute sample mean and variance for each feature using a
 large number of training images rather than using a running average. For
 this implementation we have chosen to use running averages instead since
 they do not require an additional estimation step; the torch7 implementation
 of batch normalization also uses running averages.
 Input:
 - x: Data of shape (N, D)
 - gamma: Scale parameter of shape (D,)
  - beta: Shift paremeter of shape (D,)
 - bn param: Dictionary with the following keys:
   - mode: 'train' or 'test'; required
   - eps: Constant for numeric stability
   - momentum: Constant for running mean / variance.
   - running mean: Array of shape (D,) giving running mean of features
   - running_var Array of shape (D,) giving running variance of features
 Returns a tuple of:
 - out: of shape (N, D)
  - cache: A tuple of values needed in the backward pass
 mode = bn param['mode']
 eps = bn param.get('eps', 1e-5)
 momentum = bn_param.get('momentum', 0.9)
 N, D = x.shape
 running mean = bn param.get('running mean', np.zeros(D, dtype=x.dtype))
 running var = bn param.get('running var', np.zeros(D, dtype=x.dtype))
 out, cache = None, None
 if mode == 'train':
   # ----- #
   # YOUR CODE HERE:
      A few steps here:
        (1) Calculate the running mean and variance of the minibatch.
        (2) Normalize the activations with the sample mean and variance.
        (3) Scale and shift the normalized activations. Store this
            as the variable 'out'
        (4) Store any variables you may need for the backward pass in
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the 'cache' variable.
   \# compute the mean and covariance from minibatch examples x
   mu = x.mean(axis=0)
   var = x.var(axis=0)
   # keep an exponentially decaying running mean and variance
   # these averages are used to normalize data at test-time
   running_mean = momentum * running_mean + (1 - momentum) * mu
   running_var = momentum * running_var + (1 - momentum) * var
   # normalize the activations x with the current mean and variance
   # subtract the mean and divide by the variance
   xc = x - mu
   xn = (xc) / (np.sqrt(var + eps))
   # scale and shift the normalized activations
   out = (gamma * xn) + beta
   # store variables you need for the backward pass in the 'cache' variable
   cache = [eps, mu, var, gamma, beta, x, xc, xn]
   # ----- #
   # END YOUR CODE HERE
   # ______ #
 elif mode == 'test':
   # ------ #
   # YOUR CODE HERE:
     Calculate the testing time normalized activation. Normalize using
     the running mean and variance, and then scale and shift appropriately.
   # Store the output as 'out'.
   # ----- #
   # calculate the testing time normalized activation
   # normalize using the running mean and variance from training statistics
   xn = (x - running mean) / (np.sqrt(running var + eps))
   # scale and shift appropriately
   out = (gamma * xn) + beta
   # ----- #
   # END YOUR CODE HERE
   else:
   raise ValueError ('Invalid forward batchnorm mode "%s"' % mode)
 # Store the updated running means back into bn param
 bn param['running_mean'] = running_mean
 bn param['running var'] = running var
 return out, cache
def batchnorm backward(dout, cache):
 Backward pass for batch normalization.
 For this implementation, you should write out a computation graph for
 batch normalization on paper and propagate gradients backward through
 intermediate nodes.
 Inputs:
 - dout: Upstream derivatives, of shape (N, D)
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- cache: Variable of intermediates from batchnorm_forward.
 Returns a tuple of:
 - dx: Gradient with respect to inputs x, of shape (N, D)
 - dgamma: Gradient with respect to scale parameter gamma, of shape (D,)
  - dbeta: Gradient with respect to shift parameter beta, of shape (D,)
 dx, dgamma, dbeta = None, None, None
 # ------ #
 # YOUR CODE HERE:
 # Implement the batchnorm backward pass, calculating dx, dgamma, and dbeta.
  # first pull out relevant variables
 eps, mu, var, gamma, beta, x, xc, xn = cache
 N, D = dout.shape
 # the easy ones: dbeta, dgamma
 dbeta = np.sum(dout, axis=0)
 dgamma = np.sum(dout * xn, axis=0)
 # the hard one: dx
 dxn = dout * gamma
 # intermediate variables
 sqrtvar = np.sqrt(var + eps)
 ivar = 1 / sqrtvar
 # intermediate steps for dvar
 dvar = np.sum(dxn * xc, axis=0) * (-0.5) * np.power(sqrtvar, -3)
 # intermediate steps for dmu
 \# dmu = -np.sum(dxn * ivar, axis=0) + dvar * np.sum(-2. * xc, axis=0) / N
 dmu = -ivar * np.sum(dxn, axis=0) - (2.0 * dvar / N) * np.sum(xc, axis=0)
 # final step for dx
 \# dx = (dxn * ivar) + (dvar * 2 * xc / N) + (dmu / N)
 dx = (ivar * dxn) + (dmu * np.ones like(dout) / N) + (2.0 * xc / N) * dvar
 # ------ #
  # END YOUR CODE HERE
  # ------ #
 return dx, dgamma, dbeta
def dropout forward(x, dropout param):
 Performs the forward pass for (inverted) dropout.
 Inputs:
 - x: Input data, of any shape
 - dropout param: A dictionary with the following keys:
   - p: Dropout parameter. We keep each neuron output with probability p.
   - mode: 'test' or 'train'. If the mode is train, then perform dropout;
     if the mode is test, then just return the input.
   - seed: Seed for the random number generator. Passing seed makes this
     function deterministic, which is needed for gradient checking but not in
    real networks.
 Outputs:
  - out: Array of the same shape as x.
 - cache: A tuple (dropout param, mask). In training mode, mask is the dropout
   mask that was used to multiply the input; in test mode, mask is None.
 p, mode = dropout param['p'], dropout param['mode']
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if 'seed' in dropout_param:
  np.random.seed(dropout param['seed'])
 mask = None
 out = None
 if mode == 'train':
  # ----- #
  # YOUR CODE HERE:
    Implement the inverted dropout forward pass during training time.
    Store the masked and scaled activations in out, and store the
   dropout mask as the variable mask.
  # ----- #
  mask = (np.random.rand(*x.shape) < p) / p</pre>
  out = x * mask
  # END YOUR CODE HERE
  # ----- #
 elif mode == 'test':
  # ----- #
  # YOUR CODE HERE:
   Implement the inverted dropout forward pass during test time.
  # ----- #
  out = x
  # ----- #
  # END YOUR CODE HERE
  cache = (dropout param, mask)
 out = out.astype(x.dtype, copy=False)
 return out, cache
def dropout backward(dout, cache):
 Perform the backward pass for (inverted) dropout.
 Inputs:
 - dout: Upstream derivatives, of any shape
 - cache: (dropout param, mask) from dropout forward.
 dropout_param, mask = cache
 mode = dropout_param['mode']
 dx = None
 if mode == 'train':
  # ------ #
  # YOUR CODE HERE:
  # Implement the inverted dropout backward pass during training time.
  # ----- #
  dx = dout * mask
  # ----- #
  # END YOUR CODE HERE
  elif mode == 'test':
  # ------ #
  # YOUR CODE HERE:
   Implement the inverted dropout backward pass during test time.
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dx = dout
   # ------ #
   # END YOUR CODE HERE
   # ============= #
 return dx
def svm loss(x, y):
 Computes the loss and gradient using for multiclass SVM classification.
 Inputs:
 - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
   for the ith input.
  - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
   0 <= y[i] < C
 Returns a tuple of:
  - loss: Scalar giving the loss
  - dx: Gradient of the loss with respect to x
 N = x.shape[0]
 correct class scores = x[np.arange(N), y]
 margins = np.maximum(0, x - correct class scores[:, np.newaxis] + 1.0)
 margins[np.arange(N), y] = 0
 loss = np.sum(margins) / N
 num pos = np.sum(margins > 0, axis=1)
 dx = np.zeros like(x)
 dx[margins > 0] = 1
 dx[np.arange(N), y] -= num pos
 dx /= N
 return loss, dx
def softmax_loss(x, y):
 Computes the loss and gradient for softmax classification.
 Inputs:
 - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
   for the ith input.
  - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
   0 <= y[i] < C
 Returns a tuple of:
 - loss: Scalar giving the loss
  - dx: Gradient of the loss with respect to x
 probs = np.exp(x - np.max(x, axis=1, keepdims=True))
 probs /= np.sum(probs, axis=1, keepdims=True)
 N = x.shape[0]
 loss = -np.sum(np.log(probs[np.arange(N), y])) / N
 dx = probs.copy()
 dx[np.arange(N), y] -= 1
 dx /= N
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return loss, dx