## knn nosol

January 30, 2024

# 0.1 This is the k-nearest neighbors workbook for ECE C147/C247 Assignment #2

Please follow the notebook linearly to implement k-nearest neighbors.

Please print out the workbook entirely when completed.

The goal of this workbook is to give you experience with the data, training and evaluating a simple classifier, k-fold cross validation, and as a Python refresher.

#### 0.2 Import the appropriate libraries

```
[]: import numpy as np # for doing most of our calculations import matplotlib.pyplot as plt# for plotting from utils.data_utils import load_CIFAR10 # function to load the CIFAR-10_u dataset.

# Load matplotlib images inline

# matplotlib inline

# These are important for reloading any code you write in external .py files.

# see http://stackoverflow.com/questions/1907993/

dautoreload-of-modules-in-ipython

%load_ext autoreload

%autoreload 2
```

The autoreload extension is already loaded. To reload it, use: %reload\_ext autoreload

```
[]: # Set the path to the CIFAR-10 data
cifar10_dir = '/Users/tilboon/Documents/UCLA/Courses/C247/HW2/HW2_code/
cifar-10-batches-py' # You need to update this line
X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)

# As a sanity check, we print out the size of the training and test data.
print('Training data shape: ', X_train.shape)
print('Training labels shape: ', y_train.shape)
print('Test data shape: ', X_test.shape)
print('Test labels shape: ', y_test.shape)
```

```
Training labels shape: (50000,)
    Test data shape: (10000, 32, 32, 3)
    Test labels shape: (10000,)
[]: # Visualize some examples from the dataset.
    # We show a few examples of training images from each class.
    classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse', _
     num_classes = len(classes)
    samples_per_class = 7
    for y, cls in enumerate(classes):
        idxs = np.flatnonzero(y_train == y)
        idxs = np.random.choice(idxs, samples_per_class, replace=False)
        for i, idx in enumerate(idxs):
            plt_idx = i * num_classes + y + 1
            plt.subplot(samples_per_class, num_classes, plt_idx)
            plt.imshow(X_train[idx].astype('uint8'))
            plt.axis('off')
            if i == 0:
                plt.title(cls)
    plt.show()
```

Training data shape: (50000, 32, 32, 3)



```
[]: # Subsample the data for more efficient code execution in this exercise
   num_training = 5000
   mask = list(range(num_training))
   X_train = X_train[mask]
   y_train = y_train[mask]

   num_test = 500
   mask = list(range(num_test))
   X_test = X_test[mask]
   y_test = y_test[mask]

# Reshape the image data into rows
   X_train = np.reshape(X_train, (X_train.shape[0], -1))
   X_test = np.reshape(X_test, (X_test.shape[0], -1))
   print(X_train.shape, X_test.shape)
```

(5000, 3072) (500, 3072)

# 1 K-nearest neighbors

In the following cells, you will build a KNN classifier and choose hyperparameters via k-fold cross-validation.

```
[]: # Import the KNN class
from nndl import KNN
```

```
[]: # Declare an instance of the knn class.
knn = KNN()

# Train the classifier.
# We have implemented the training of the KNN classifier.
# Look at the train function in the KNN class to see what this does.
knn.train(X=X_train, y=y_train)
```

#### 1.1 Questions

- (1) Describe what is going on in the function knn.train().
- (2) What are the pros and cons of this training step?

#### 1.2 Answers

- (1) This is a pretty simple function. It is simply storing the training data in the class instance.
- (2) This is a very simple and easy to implement training function. But, this could lead to a large amount of memory usage and eventually slow down your computations.

#### 1.3 KNN prediction

In the following sections, you will implement the functions to calculate the distances of test points to training points, and from this information, predict the class of the KNN.

Time to run code: 45.17984080314636 Frobenius norm of L2 distances: 7906696.077040902

**Really slow code** Note: This probably took a while. This is because we use two for loops. We could increase the speed via vectorization, removing the for loops.

If you implemented this correctly, evaluating np.linalg.norm (dists\_L2, 'fro') should return:  $\sim\!7906696$ 

#### 1.3.1 KNN vectorization

The above code took far too long to run. If we wanted to optimize hyperparameters, it would be time-expensive. Thus, we will speed up the code by vectorizing it, removing the for loops.

Time to run code: 0.21989989280700684
Difference in L2 distances between your KNN implementations (should be 0): 0.0

**Speedup** Depending on your computer speed, you should see a 10-100x speed up from vectorization. On our computer, the vectorized form took 0.36 seconds while the naive implementation

took 38.3 seconds.

#### 1.3.2 Implementing the prediction

Now that we have functions to calculate the distances from a test point to given training points, we now implement the function that will predict the test point labels.

#### 0.726

If you implemented this correctly, the error should be: 0.726.

This means that the k-nearest neighbors classifier is right 27.4% of the time, which is not great, considering that chance levels are 10%.

# 2 Optimizing KNN hyperparameters

In this section, we'll take the KNN classifier that you have constructed and perform cross-validation to choose a best value of k, as well as a best choice of norm.

#### 2.0.1 Create training and validation folds

First, we will create the training and validation folds for use in k-fold cross validation.

```
[]: # Create the dataset folds for cross-valdiation.
num_folds = 5

X_train_folds = []
y_train_folds = []
```

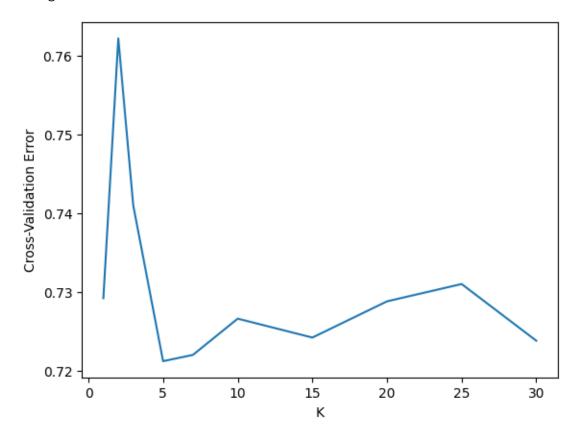
```
# ----- #
# YOUR CODE HERE:
  Split the training data into num_folds (i.e., 5) folds.
  X_train_folds is a list, where X_train_folds[i] contains the
#
     data points in fold i.
   y_train_folds is also a list, where y_train_folds[i] contains
     the corresponding labels for the data in X_train_folds[i]
# Randomization
np.random.seed(0)
indices = np.arange(num_training)
np.random.shuffle(indices)
X_train_shuffled = X_train[indices]
y_train_shuffled = y_train[indices]
X_train_folds = np.array_split(X_train_shuffled, num_folds)
y_train_folds = np.array_split(y_train_shuffled, num_folds)
# END YOUR CODE HERE
# ----- #
```

### 2.0.2 Optimizing the number of nearest neighbors hyperparameter.

In this section, we select different numbers of nearest neighbors and assess which one has the lowest k-fold cross validation error.

```
errors = []
  for i in range(num_folds):
    # Find validation set
    X_current_validation = X_train_folds[i]
    y_current_validation = y_train_folds[i]
    # Find training set and concatenate folds
    X_current_train = np.concatenate(X_train_folds[:i] + X_train_folds[(i + 1):
  →])
    y_current_train = np.concatenate(y_train_folds[:i] + y_train_folds[(i + 1):
  →])
    # Train model with current 'k' value
    knn = KNN()
    knn.train(X=X_current_train, y=y_current_train)
    current_dists_arr = knn.
 →compute_L2_distances_vectorized(X=X_current_validation)
    y_prediction = knn.predict_labels(current_dists_arr, k=k)
    # Error computation
    errors.append(np.count_nonzero(y_current_validation - y_prediction)/
  →float(len(y_current_validation)))
  # Add average erros to final_errors array
  final_errors.append(np.mean(errors))
  print('K: %d, Avg Error: %f' % (k, final_errors[-1]))
# Plot
plt.plot(ks, final_errors)
plt.xlabel('K')
plt.ylabel('Cross-Validation Error')
plt.show()
# ----- #
# END YOUR CODE HERE
# ----- #
print('Computation time: %.2f'%(time.time()-time_start))
K: 1, Avg Error: 0.729200
K: 2, Avg Error: 0.762200
K: 3, Avg Error: 0.741000
K: 5, Avg Error: 0.721200
K: 7, Avg Error: 0.722000
K: 10, Avg Error: 0.726600
```

K: 15, Avg Error: 0.724200K: 20, Avg Error: 0.728800K: 25, Avg Error: 0.731000K: 30, Avg Error: 0.723800



Computation time: 20.98

#### 2.1 Questions:

(1) What value of k is best amongst the tested k's?

(2) What is the cross-validation error for this value of k?

## 2.2 Answers:

- (1) This value varies dependent on the random seed selected, but for this example (0) k = 5
- (2) This value varies dependent on the random seed selected, but for this example (0) cross-validation error = 0.721200

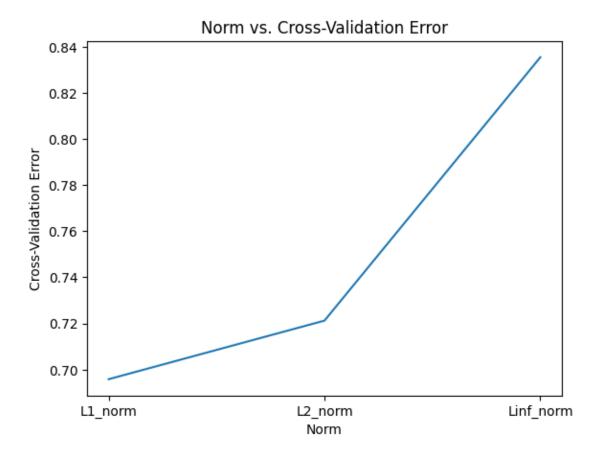
#### 2.2.1 Optimizing the norm

Next, we test three different norms (the 1, 2, and infinity norms) and see which distance metric results in the best cross-validation performance.

```
[]: time_start =time.time()
    L1_norm = lambda x: np.linalg.norm(x, ord=1)
    L2_norm = lambda x: np.linalg.norm(x, ord=2)
    Linf_norm = lambda x: np.linalg.norm(x, ord= np.inf)
    norms = [L1_norm, L2_norm, Linf_norm]
    # YOUR CODE HERE:
    # Calculate the cross-validation error for each norm in norms, testing
       the trained model on each of the 5 folds. Average these errors
     # together and make a plot of the norm used vs the cross-validation error
        Use the best cross-validation k from the previous part.
    # Feel free to use the compute distances function. We're testing just
    # three norms, but be advised that this could still take some time.
    # You're welcome to write a vectorized form of the L1- and Linf- norms
     # to speed this up, but it is not necessary.
    final_norm_errors = []
    for norm in norms:
      errors = []
      for i in range(num folds):
        # Find validation set
        X_current_validation = X_train_folds[i]
        y_current_validation = y_train_folds[i]
        # Find training set and concatenate folds
        X_current_train = np.concatenate(X_train_folds[:i] + X_train_folds[(i + 1):
      →])
        y_current_train = np.concatenate(y_train_folds[:i] + y_train_folds[(i + 1):
     →])
        # Train model with current 'k' value
        knn = KNN()
        knn.train(X=X_current_train, y=y_current_train)
        current_dists_arr = knn.compute_distances(X_current_validation, norm)
        y_prediction = knn.predict_labels(current_dists_arr, k=5)
        # Error computation
        errors.append(np.count_nonzero(y_current_validation - y_prediction)/
      →float(len(y_current_validation)))
```

```
# Add average erros to final_errors array
 final_norm_errors.append(np.mean(errors))
print('L1_norm: Avg Error = %f' % (final_norm_errors[0]))
print('L2_norm: Avg Error = %f' % (final_norm_errors[1]))
print('Linf_norm: Avg Error = %f' % (final_norm_errors[2]))
# Plot
plt.plot(final_norm_errors)
plt.title("Norm vs. Cross-Validation Error")
plt.xlabel('Norm')
plt.ylabel('Cross-Validation Error')
plt.xticks(np.arange(3), ['L1_norm', 'L2_norm', 'Linf_norm'])
plt.show()
# ----- #
# END YOUR CODE HERE
# ======== #
print('Computation time: %.2f'%(time.time()-time_start))
```

L1\_norm: Avg Error = 0.695800 L2\_norm: Avg Error = 0.721200 Linf\_norm: Avg Error = 0.835400



Computation time: 531.58

## 2.3 Questions:

- (1) What norm has the best cross-validation error?
- (2) What is the cross-validation error for your given norm and k?

## 2.4 Answers:

- (1) L1 norm
- (2) k = 5 and CVE = 0.695800

# 3 Evaluating the model on the testing dataset.

Now, given the optimal k and norm you found in earlier parts, evaluate the testing error of the k-nearest neighbors model.

Error rate achieved: 0.698

#### 3.1 Question:

How much did your error improve by cross-validation over naively choosing k = 1 and using the L2-norm?

#### 3.2 Answer:

```
0.726 - 0.698 = 0.028 \sim 2.8\%
```