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# **Check if Array Is Sorted and Rotated**

- Approach
  - o Brute-force
    - Concatenate array with itself
    - Find the break-point
    - [from i=break-point+1 to len(nums)]  $\mathbf{check}$  if  $\mathbf{arr[i]} \leq \mathbf{arr[i+1]}$
    - Time Complexity: O(n)
    - Space Complexity: O(n)
  - Better
    - Find the break-point
    - while (i+1) % len(nums)  $\neq$  break-point **Check** if nums[i]  $\leq$  nums[i+1]
    - Time Complexity: O(n)
    - Space Complexity: O(1)
  - Optimal
    - There can be at most 1 break-point
    - Count the number of break-points
    - One-Pass
    - Time Complexity: O(n)
    - Space Complexity: O(1)

```
# Python3
# Brute-force Solution
class Solution:
    def check(self, nums: List[int]) -> bool:
        i = 0
        while i < len(nums) - 1 and nums[i] <= nums[i+1]:
            i += 1
        if i == (len(nums) - 1):
            if nums[i-1] <= nums[i]:
                return True
            if nums[i] < nums[i-1] and nums[i] <= num[0]:
    return True</pre>
             return False
        arr = nums + nums
        for j in range(i+1, len(nums)):
            if arr[j] > arr[j+1]:
    return False
        return True
```

```
# Python3
# Better Solution
class Solution:
    def check(self, nums: List[int]) -> bool:
        i = 0
        while i < len(nums) - 1 and nums[i] <= nums[i+1]:
              i += 1

        if i == (len(nums) - 1):
              if nums[i-1] <= nums[i]:
                   return True
        if nums[i] < nums[i] <= num[0]:</pre>
```

```
return True
return False

br = i
i += 1
while i != br:
   if nums[i] > nums[(i+1)%len(nums)]:
      return False
   i = (i+1) % len(nums)
return True
```

```
// C++
// Optimal Solution
class Solution {
public:
    bool check(vector<int>& A) {
        for (int i = 0, k = 0; i < A.size(); ++i)
            if (A[i] > A[(i + 1) % A.size()] && ++k > 1)
            return false;
        return true;
    }
};
```

# **Remove Duplicates from Sorted Array**

- Approach
  - Brute-force
    - Use set to remove duplicates
    - Time Complexity: O(nlogn)
    - Space Complexity: O(n)
  - Better
    - Use stack
    - if stack.top() ≠ curr\_element then push curr\_element onto the stack
    - Time Complexity: O(n)
    - Space Complexity: O(n)
  - Optimal
    - Initialize 2 pointers i = 0, j = 1 where i maintains unique elements count
    - if nums[i] == nums[j] then increment j only
    - else swap(nums[i+1], nums[j]) and increment both pointers
    - Time Complexity: O(n)
    - Space Complexity: O(1)

```
# Python3
# Brute-force Solution
def removeDuplicates(self, nums: List[int]) -> int:
    nums[:] = sorted(set(nums))
    return len(nums)
```

```
# Python3
# Better Solution
```

```
class Solution:
    def removeDuplicates(self, nums: List[int]) -> int:
        stack = [nums[0]]
    for i in range(1, len(nums)):
        if stack[-1] != nums[i]:
            stack += nums[i],
        nums[:] = stack
```

# Rotate Array to the right by k steps

- Approach
  - o Brute-force
    - Rotate one element in every iteration
    - Time Complexity: O(n \* k)
    - Space Complexity: O(1)
  - Better
    - Take another array
    - First, Copy the last k elements in the new array
    - Then, Copy the first n-k elements in the new array
    - Time Complexity: O(n)
    - Space Complexity: O(n)
  - Optimal
    - Reverse the last k elements
    - Reverse first n-k elements
    - Reverse the whole array

- Time Complexity: O(n)
- Space Complexity: O(1)

```
# Python3
# Better Solution
class Solution:
    def rotate(self, nums: List[int], k: int) -> None:
        k = k % len(nums)
        ans = []
    for i in range(len(nums) - k, len(nums)):
        ans += nums[i],
    for i in range(len(nums) - k):
        ans += nums[i],
    nums[:] = ans
```

```
# Python3
# Optimal Solution
class Solution:
    def reverse(self, nums, start, end):
        while start < end:
            nums[start], nums[end] = nums[end], nums[start]
            start += 1
            end -= 1

def rotate(self, nums: List[int], k: int) -> None:
        n = len(nums)
        k = k % n
        self.reverse(nums, 0, n - k - 1)
        self.reverse(nums, 0, n - l)
```

```
// C++
// Optimal Solution
class Solution {
public:
    void rotate(vector<int>& nums, int k) {
        k = k % nums.size();
        reverse(nums.begin(), nums.end() - k);
        reverse(nums.end() - k, nums.end());
        reverse(nums.begin(), nums.end());
    }
};
```

# **Single Number**

Find the number that appears once, and the other numbers twice - Strivers A2Z DSA

Detailed solution for Find the number that appears once, and the other numbers twice - Problem Statement: Given a non-empty array of integers arr, every element appears twice except for one. Find that single one. Examples: Example 1: Input Format:  $arr[] = \{2,2,1\}$  Result: 1 Explanation: In this array, only the element 1



https://takeuforward.org/arrays/find-the-number-that-appears-once-and-the-other-numbers-twice/

- Approach
  - Brute-force
    - For every element, count the frequency
    - Time Complexity:  $O(n^2)$
    - Space Complexity: O(1)

#### o Better-1

- Use unordered\_map/dict to store the frequency of each element
- Time Complexity: O(n)
- Space Complexity: O(n)

#### o Better-2

- XOR of two same numbers is always 0 i.e. a ^ a = 0
- XOR of a number with 0 will result in the number itself i.e.  $0 ^ a = a$
- Perform the XOR of all the numbers of the array elements, we will be left with a single number
- Optimal if array is unsorted
- Time Complexity: O(n)
- Space Complexity: O(1)
- Optimal
  - Works IFF array is sorted
  - Binary Search
  - Time Complexity: O(logn)
  - Space Complexity: O(1)

```
# Python3
# Better Solution - 1
class Solution:
    def singleNumber(self, nums: List[int]) -> int:
        dct = dict()
        for i in nums:
            dct[i] = 0
        for i in nums:
            dct[i] += 1
        for i in dct:
            if dct[i] == 1:
                 return i
```

```
// C++
// Better Solution - 1
class Solution {
public:
    int singleNumber(vector<int>& nums) {
        unordered_map<int, int> umap;
        for (int i = 0; i < nums.size(); i++) {
            umap[nums[i]]++;
        }
        for (auto it: umap) {
            if (it.second == 1) return it.first;
        }
        return -1;
    }
};</pre>
```

```
# Python3
# Better Solution - 2
class Solution:
```

```
def search(self, A, N):
    xor = 0
    for i in A:
        xor ^= i
    return xor
```

```
# Python3
# Optimal Solution
# Works iff array is sorted
```

```
// C++
// Optimal Solution
// Works iff array is sorted
class Solution{
public:
  int search(int A[], int N){
        int low = 0;
        int high = N-1;
        while(low <= high)
            int mid = low + (high - low) / 2;
            if(mid \% 2 == 0)
                if(A[mid] == A[mid+1])
                    low = mid + 1;
                    high = mid - 1;
            else
                if(A[mid] == A[mid + 1])
                    high = mid-1;
                    low = mid + 1;
        return A[low];
};
```

### **Next Permutation**

- Total Permutations = n!
- Follow Dictionary Sorted order i.e.  $\{\{1,2,3\},\ \{1,3,2\},\ \{2,1,3\},\ \{2,3,1\},\ \{3,1,2\},\ \{3,2,1\}\}$
- Approach:
  - o Brute-force
    - Generate all permutations and apply linear search
    - Time Complexity: O(n! \* n)
    - Space Complexity: O(n)
  - Optimal
    - First, we find the breakpoint i.e. point where this condition <code>nums[i] < nums[i+1]</code> is met from the back. If there is no such point then the list is already in descending order and the next permutation is the reverse of the given list.
    - When a breakpoint is found we swap it with the first greater element from the back of the list and reverse the list elements on the right of breakpoint.
    - Time Complexity: O(n)
    - Space Complexity: O(1)

```
# Python3
# Optimal Solution
class Solution:
    def reverse(self, nums, start, stop):
        size = stop + start
        for i in range(start, (size + 1) // 2):
            nums[i], nums[size - i] = nums[size - i], nums[i]
```

```
def nextPermutation(self, nums: List[int]) -> None:
    # find breakpoint from back
    for i in range(len(nums)-2, -1, -1):
       if nums[i] < nums[i+1]:
           ind = i # breakpoint found
           break
    if ind == -1: # no breakpoint found
        nums.reverse() # in-place
        \# \ nums[:] = nums[::-1] \# \ also \ works \ but \ is \ not \ in-place
        # Note that nums = nums[::-1] doesn't work as it is not in-place
        # nums[::-1] creates and returns new list object
       for i in range(len(nums)-1, ind, -1):
           if nums[i] > nums[ind]:
                nums[i], nums[ind] = nums[ind], nums[i]
                break
        # reverse list elements on the right of breakpoint
        self.reverse(nums, ind+1, len(nums)-1) # in-place
        \# nums[ind+1:] = nums[ind+1:][::-1] \# also works but is not in-place
        # but nums[2:4].reverse() is not correct
```

```
// C++
// Optimal Solution
class Solution {
public:
    void nextPermutation(vector<int>& nums) {
        int ind = -1;
        for (int i = nums.size()-2; i >= 0; i--) {
            if (nums[i] < nums[i+1]) {
                ind = i;
                break;
        if (ind == -1) {
            reverse(nums.begin(), nums.end());
        else {
            for (int i = nums.size()-1; i >= 0; i--) {
                if (nums[i] > nums[ind]) {
                    swap(nums[i], nums[ind]);
                    break;
                }
            reverse(nums.begin()+ind+1, nums.end());
};
```

#### Maximum Subarray Sum (Kadane's Algorithm)

- Approach
  - o Brute-force
    - Check the sum of every possible subarray and consider the maximum among them
    - Time Complexity:  $O(n^3)$
    - Space Complexity: O(1)
  - Better
    - If we carefully observe, we can notice that to get the sum of the current subarray we just need to add the current element(i.e. arr[j]) to the sum of the previous subarray i.e. arr[i....j-1].
    - Time Complexity:  $O(n^2)$
    - Space Complexity: O(1)
  - Optimal
    - The intuition of the algorithm is not to consider the subarray as a part of the answer if its sum is less than 0. A subarray with a sum less than 0 will always reduce our answer and so this type of subarray cannot be a part of the subarray with maximum sum.
    - Here, we will iterate the given array with a single loop and while iterating we will add the elements in a sum variable. Now, if at any point the sum becomes less than 0, we will set the sum as 0 as we are not going to

consider any subarray with a negative sum. Among all the sums calculated, we will consider the maximum one.

- Time Complexity: O(n)
- Space Complexity: O(1)

```
# Python3
# Brute-force Solution
def maxSubarraySum(arr, n):
    maxi = -sys.maxsize - 1  # maximum sum

for i in range(n):
    for j in range(i, n):
        # subarray = arr[i.....j]
        sum = 0

        # add all the elements of subarray:
        for k in range(i, j+1):
            sum += arr[k]

        maxi = max(maxi, sum)

return maxi
```

```
# Python3
# Better Solution
def maxSubarraySum(arr, n):
    maxi = -sys.maxsize - 1 # maximum sum

for i in range(n):
    sum = 0
    for j in range(i, n):
        # current subarray = arr[i.....j]

    #add the current element arr[j]
    # to the sum i.e. sum of arr[i...j-1]
    sum += arr[j]

    maxi = max(maxi, sum) # getting the maximum

return maxi
```

```
# Python3
# Optimal Solution (Kadane's Algorithm)
class Solution:
    def maxSubArray(self, nums: List[int]) -> int:
        maxsum = nums[0]
    tempsum = 0

    for i in nums:
        tempsum += i
        maxsum = max(maxsum, tempsum)
        if tempsum < 0: tempsum = 0
    return maxsum</pre>
```

```
// C++
// Optimal Solution (Kadane's Algorithm)
class Solution {
public:
    int maxSubArray(vector<int>& nums) {
        int maxsum = nums[0];
        int tempsum = 0;

    for (auto i: nums) {
            tempsum += i;
            if (tempsum > maxsum) {
                 maxsum = ts;
            }
            if (tempsum < 0) {
                 tempsum = 0;
            }
        }
        return maxsum;
    }
}</pre>
```

## Print Subarray with Maximum Sum (variation of Kadane's Algorithm)

- Approach
  - o Optimal
    - Store the starting index and the ending index of the subarray. Thus we can easily get the subarray afterwards without actually storing the subarray elements.
    - Time Complexity: O(n)
    - Space Complexity: O(1)

```
# Python3
# Optimal Solution
def maxSubarraySum(arr, n):
   maxi = -sys.maxsize - 1 # maximum sum
    start = 0
    ansStart, ansEnd = -1, -1
    for i in range(n):
       if sum == 0:
            start = i # starting index
        sum += arr[i]
        if sum > maxi:
maxi = sum
            ansStart = start
            ansEnd = i
        if sum < 0:
            sum = 0
    print(arr[ansStart:ansEnd+1])
```

## Sort an array of 0's, 1's and 2's (Dutch National Flag Algorithm)

- Approach
  - o Brute-force
    - Apply Merge-Sort Algorithm or any in-built Sorting Algorithm
    - Time Complexity: O(nlogn)
    - Space Complexity: O(n)
  - Better
    - Maintain 3 counter variables that store the number of occurrences of 0's, 1's and 2's
    - Two-Pass
    - Time Complexity: O(n)
    - Space Complexity: O(1)
  - Optimal
    - Maintain 3 pointers low=0, mid=0, high=len(nums)-1
    - Note that the array is sorted between 0 to low-1, low to mid-1, and high to len(nums)-1 and unsorted between mid to high-1
    - while mid ≤ high we check nums[mid] and swap it with low/high accordingly and maintain pointers as necessary

9

One-Pass

lacktriangleright Time Complexity: O(n)

• Space Complexity: O(1)

```
# Python3
# Brute-force Solution
class Solution:
   def sortColors(self, nums: List[int]) -> None:
        nums.sort()
```

```
# Python3
# Better Solution (Two Pass)
class Solution:
    def sortColors(self, nums: List[int]) -> None:
        zero = 0
        one = 0
        two = 0
        for i in nums:
            if i == 0:
                zero += 1
        elif i == 1:
            one += 1
        else:
            two += 1
```

```
for i in range(zero):
    nums[i] = 0
for i in range(zero, one+zero):
    nums[i] = 1
for i in range(one+zero, two+one+zero):
    nums[i] = 2
```

```
# Python3
# Optimal Solution (Dutch National Flag Algorithm - One Pass)
class Solution:
    def sortColors(self, nums: List[int]) -> None:
        low = 0
        mid = 0
        high = len(nums) - 1
        while mid <= high:
           if nums[mid] == 0:
                nums[low], nums[mid] = nums[mid], nums[low]
                mid += 1
            \verb|elif nums[mid]| == 1:
               mid += 1
            else:
                nums[mid], nums[high] = nums[high], nums[mid]
                high -= 1
```

```
// C++
// Optimal Solution (Dutch National Flag Algorithm)
#include <bits/stdc++.h>
class Solution {
public:
    void sortColors(vector<int>& nums) {
        int low = 0;
         int mid = 0;
        int high = nums.size() - 1;
         while (mid <= high) {
   if (nums[mid] == 0) {
                  swap(nums[low], nums[mid]);
                  mid++;
             else if (nums[mid] == 1) {
                  mid++;
             else {
                  swap(nums[mid], nums[high]);
             }
        }
    }
};
```

## Best Time to Buy and Sell Stock

- Approach
  - o Brute-force
    - Use 2 loops and track every transaction and maintain a variable to contain the max value among all transactions.
    - Time Complexity:  $O(n^2)$
    - Space Complexity: O(1)
  - Optimal
    - Iterate over the array and check whether cur\_price min\_price > max\_profit and if cur\_price < min\_price
    - Time Complexity: O(n)
    - Space Complexity: O(1)

```
# Python3
# Brute-force Solution
class Solution:
   def maxProfit(self, prices: List[int]) -> int:
        max_profit = 0
```

```
for i in range(len(prices)):
    for j in range(i+1, len(prices)):
        max_profit = max(max_profit, prices[j]-prices[i])
return max_profit
```

```
# Python3
# Optimal Solution
class Solution:
    def maxProfit(self, prices: List[int]) -> int:
        min_price = prices[0]
        max_profit = 0
        for i in range(1, len(prices)):
            # if current_price - min_price is greater than max_profit, update max_profit
        max_profit = max(max_profit, prices[i]-min_price)

# if current_price is less than min_price, update min_price
        min_price = min(min_price, prices[i])
return max_profit
```

```
// C++
// Optimal Solution
int maxProfit(vector<int> &arr) {
    int maxPro = 0;
    int n = arr.size();
    int minPrice = INT_MAX;

for (int i = 0; i < arr.size(); i++) {
        minPrice = min(minPrice, arr[i]);
        maxPro = max(maxPro, arr[i] - minPrice);
    }

return maxPro;</pre>
```

#### Using Kadane's Algorithm

• Will also work when the prices array is given as price\_difference array i.e. {1, 7, 4, 11} will be given as {0, 6, -3, 7}

```
# Python3
# Optimal Solution (variation of Kadane's Algorithm)
class Solution:
    def maxProfit(self, prices: List[int]) -> int:
        n = len(prices)
        ans = 0
        curSum = 0
        for i in range(n-1):
            curSum += prices[i+1] - prices[i]
        if curSum < 0:
            curSum = 0
        ans = max(ans, curSum)
    return ans</pre>
```

# **Merge 2 Sorted Arrays**

- Approach
  - o Brute-force
    - Concatenate both arrays and apply any (in-built) sorting algorithm
    - lacktriangle Time Complexity: O((m+n)log(m+n))
    - Space Complexity: O(1) (in-place)
  - Better
    - Maintain a separate array res and two pointers a and b (for given arrays).
    - while (a < m and b < n) Check if nums1[a] < nums2[b]
    - Time Complexity: O(m+n)
    - Space Complexity: O(m+n)
  - o Optimal

- Maintain three pointers and iterate from backwards of both arrays and take the larger element between the two and store it at the back of nums1 array
- Time Complexity: O(m+n)
- Space Complexity: O(1)

```
# Python3
# Better Solution
class Solution:
    def merge(self, nums1: List[int], m: int, nums2: List[int], n: int) -> None:
        while (a < m \text{ and } b < n):
           if nums1[a] < nums2[b]:
               res.append(nums1[a])
                a += 1
            else:
                res.append(nums2[b])
                b += 1
        while (a < m):
            res.append(nums1[a])
            a += 1
        while (b < n):
            res.append(nums2[b])
            b += 1
        nums1[:] = res.copy()
```

```
# Python3
# Optimal Solution
class Solution:
    def merge(self, nums1: List[int], m: int, nums2: List[int], n: int) -> None:
        a, b, write_index = m-1, n-1, m + n - 1

    while b >= 0:
        if a >= 0 and nums1[a] > nums2[b]:
            nums1[write_index] = nums1[a]
        a -= 1
    else:
        nums1[write_index] = nums2[b]
        b -= 1

    write_index -= 1
```

```
// C++
// Optimal Solution
class Solution {
public:
    void merge(vector<int>& nums1, int m, vector<int>& nums2, int n) {
       int a = m - 1;
        int b = n - 1;
       int c = m + n - 1;
        while (b \ge 0) {
           if (a \ge 0 \& nums1[a] > nums2[b]) {
               nums1[c] = nums1[a];
            else {
               nums1[c] = nums2[b];
               b--;
           c--;
       }
};
```

# Rotate the Matrix by 90 Degrees (Clockwise)

- Approach
  - o Brute-force
    - Take an element in the matrix and put it in its proper place in another matrix.
    - Time Complexity:  $O(n^2)$

				_	/ 2\
•	Space	Comp	olexity:	O	$(n^2)$

Ta

```
    Optimal

        • Transpose the matrix and reverse all the rows.
        ■ Time Complexity: O(n^2)
        • Space Complexity: O(1) (in-place)
# Python3
# Brute-force Solution
```

class Solution:

def rotate(self, matrix: List[List[int]]) -> None: n = len(matrix)
ans = [[0 for i in range(n)]for j in range(n)]

for i in range(n):
 for j in range(n):
 ans[j][n-i-1] = matrix[i][j]

for i in range(n):
 for j in range(n):
 matrix[i][j] = ans[i][j]

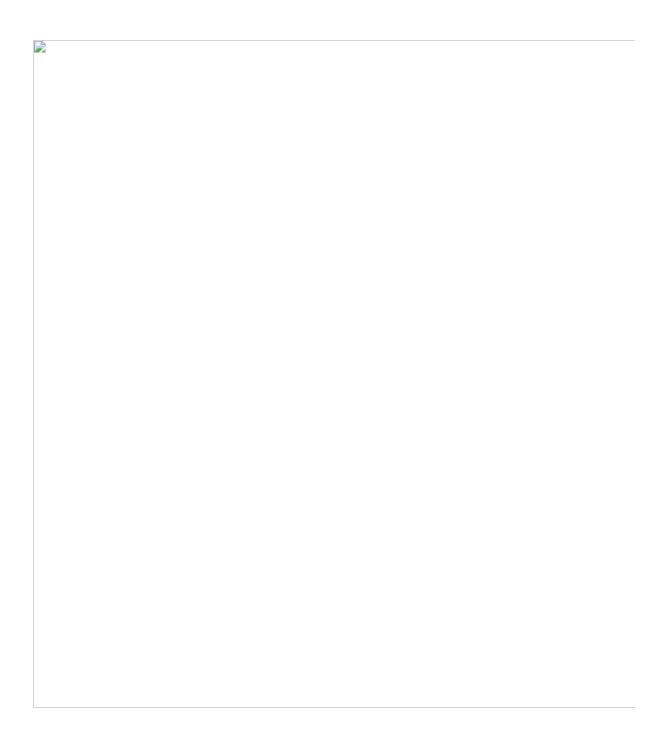
```
# Python3
# Optimal Solution
class Solution:
    def rotate(self, matrix: List[List[int]]) -> None:
        n = len(matrix)
        for i in range(1, n):
            for j in range(i):
                 matrix[i][j], matrix[j][i] = matrix[j][i], matrix[i][j]

        for i in matrix:
            i.reverse()
```

```
// C++
// Optimal Solution
void rotate(vector<vector<int>>& m) {
    int n = m.size();

    for(int i=0; i<n; i++)
        for(int j=0; j<i; j++)
            swap(m[i][j], m[j][i]);

    for(int i=0; i<n; i++)
        reverse(m[i].begin(), m[i].end());
}</pre>
```



# **Merge Overlapping Sub-intervals**

- Approach
  - Brute-force
    - Sort the array first and then check for every interval[i], what all intervals[i+1] to intervals[n-1] could be merged with the current interval.
    - lacktriangledown Time Complexity: O(nlogn) + O(2n)
    - Space Complexity: O(n)
  - Optimal
    - Sort the array
    - Use stack to check if interval[i] < stack.top()[1]</pre> then update the stack top with max(stack.top()[1], interval[i][1])
      else push the interval[i] onto the stack
    - lacktriangle Time Complexity: O(nlogn) + O(n)
    - Space Complexity: O(n)

```
# Python3
# Brute-force Solution
def mergeOverlappingIntervals(arr: List[List[int]]) -> List[List[int]]:
   n = len(arr) # size of the array
    # sort the given intervals:
    arr.sort()
    ans = []
    for i in range(n): # select an interval:
        start, end = arr[i][0], arr[i][1]
        \ensuremath{\text{\#}} Skip all the merged intervals:
        if ans and end <= ans[-1][1]:
            continue
        # check the rest of the intervals:
        for j in range(i + 1, n):
    if arr[j][0] <= end:
                end = max(end, arr[j][1])
             else:
                break
        ans.append([start, end])
```

```
// C++
// Optimal Solution
vector<vector<int>>> mergeOverlappingIntervals(vector<vector<int>>> &arr) {
   int n = arr.size(); // size of the array
   //sort the given intervals:
   sort(arr.begin(), arr.end());
    vector<vector<int>> ans;
    for (int i = 0; i < n; i++) {
        // if the current interval does not
        \ensuremath{//} lie in the last interval:
        if (ans.empty() || arr[i][0] > ans.back()[1]) {
           ans.push_back(arr[i]);
        // if the current interval
        // lies in the last interval:
           ans.back()[1] = max(ans.back()[1], arr[i][1]);
       }
   return ans:
```

## **Template**

- Approach
  - o Brute-force
    - •
    - Time Complexity:  $O(n^3)$
    - Space Complexity: O(1)

Better

```
■ Time Complexity: O(n^3)
■ Space Complexity: O(1)

Optimal

■ Time Complexity: O(n^3)
■ Space Complexity: O(1)

# Python3
# Brute-force Solution

# Python3
# Better Solution

# Python3
# Optimal Solution
```