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Check if Array Is Sorted and Rotated

- Approach
 - o Brute-force
 - Concatenate array with itself
 - Find the break-point
 - from i=break-point+1 to len(nums) Check if arr[i] ≤ arr[i+1]
 - Time Complexity: O(n)
 - Space Complexity: O(n)
 - Better
 - Find the break-point
 - while (i+1) % len(nums) ≠ break-point Check if nums[i] ≤ nums[i+1]
 - Time Complexity: O(n)
 - Space Complexity: O(1)
 - Optimal
 - There can be at most 1 break-point
 - Count the number of break-points
 - One-Pass
 - Time Complexity: O(n)
 - Space Complexity: O(1)

```
# Python3
# Brute-force Solution
class Solution:
   def check(self, nums: List[int]) -> bool:
       while i < len(nums) - 1 and nums[i] <= nums[i+1]:
           i += 1
        if i == (len(nums) - 1):
            if nums[i-1] <= nums[i]:</pre>
               return True
            if nums[i] < nums[i-1] and nums[i] <= num[0]:
               return True
            return False
        arr = nums + nums
        for j in range(i+1, len(nums)):
            if arr[j] > arr[j+1]:
               return False
        return True
```

```
# Python3
# Better Solution
class Solution:
   def check(self, nums: List[int]) -> bool:
       i = 0
       while i < len(nums) - 1 and nums[i] <= nums[i+1]:
        if i == (len(nums) - 1):
           if nums[i-1] <= nums[i]:</pre>
            if nums[i] < nums[i-1] and nums[i] <= num[0]:
               return True
            return False
        br = i
        i += 1
        while i != br:
           if nums[i] > nums[(i+1)%len(nums)]:
               return False
           i = (i+1) \% len(nums)
        return True
```

```
// C++
// Optimal Solution
class Solution {
public:
    bool check(vector<int>& A) {
        for (int i = 0, k = 0; i < A.size(); ++i)
            if (A[i] > A[(i + 1) % A.size()] && ++k > 1)
                 return false;
        return true;
    }
};
```

Remove Duplicates from Sorted Array

- Approach
 - Brute-force
 - Use set to remove duplicates
 - Time Complexity: O(nlogn)
 - Space Complexity: O(n)
 - Better
 - Use stack

- if stack.top() ≠ curr_element then push curr_element onto the stack
- Time Complexity: O(n)
- Space Complexity: O(n)
- o Optimal
 - Initialize 2 pointers i = 0, j = 1 where i maintains unique elements count
 - if nums[i] == nums[j] then increment j only
 - else swap(nums[i+1], nums[j]) and increment both pointers
 - Time Complexity: O(n)
 - Space Complexity: O(1)

```
# Python3
# Brute-force Solution
def removeDuplicates(self, nums: List[int]) -> int:
    nums[:] = sorted(set(nums))
    return len(nums)
```

```
}
    else {
        swap(nums[i+1], nums[j]);
        i++;
        j++;
        }
    }
    return i+1;
}
```

Rotate Array to the right by k steps

- Approach
 - o Brute-force
 - Rotate one element in every iteration
 - Time Complexity: O(n * k)
 - Space Complexity: O(1)
 - Better
 - Take another array
 - First, Copy the last k elements in the new array
 - Then, Copy the first n-k elements in the new array
 - Time Complexity: O(n)
 - Space Complexity: O(n)
 - Optimal
 - Reverse the last k elements
 - Reverse first n-k elements
 - Reverse the whole array
 - Time Complexity: O(n)
 - Space Complexity: O(1)

```
# Python3
# Brute-force Solution
class Solution:
    def rotate(self, nums: List[int], k: int) -> None:
        for i in range(k % len(nums)):
            temp = nums[-1]
            for j in range(len(nums) - 1, 0, -1):
                 nums[j] = nums[j - 1]
                 nums[0] = temp
```

```
# Python3
# Better Solution
class Solution:
    def rotate(self, nums: List[int], k: int) -> None:
        k = k % len(nums)
        ans = []
```

```
for i in range(len(nums) - k, len(nums)):
    ans += nums[i],
for i in range(len(nums) - k):
    ans += nums[i],
nums[:] = ans
```

```
# Python3
# Optimal Solution
class Solution:
    def reverse(self, nums, start, end):
        while start < end:
            nums[start], nums[end] = nums[end], nums[start]
            start += 1
            end -= 1

def rotate(self, nums: List[int], k: int) -> None:
        n = len(nums)
        k = k % n
        self.reverse(nums, 0, n - k - 1)
        self.reverse(nums, n - k, n - 1)
        self.reverse(nums, 0, n - 1)
```

```
// C++
// Optimal Solution
class Solution {
public:
    void rotate(vector<int>& nums, int k) {
        k = k % nums.size();
        reverse(nums.begin(), nums.end() - k);
        reverse(nums.end() - k, nums.end());
        reverse(nums.begin(), nums.end());
    }
};
```

Single Number

Find the number that appears once, and the other numbers twice - Strivers A2Z DSA

Detailed solution for Find the number that appears once, and the other numbers twice - Problem Statement: Given a non-empty array of integers arr, every element appears twice except for one. Find that single one. Examples: Example 1: Input Format: $arr[] = \{2,2,1\}$ Result:



 $\textcolor{red}{\longleftarrow} \ \text{https://takeuforward.org/arrays/find-the-number-that-appears-once-and-the-other-number-stwice/}$

- Approach
 - o Brute-force
 - For every element, count the frequency
 - Time Complexity: $O(n^2)$
 - Space Complexity: O(1)
 - o Better-1
 - Use unordered_map/dict to store the frequency of each element
 - Time Complexity: *O*(*n*)
 - Space Complexity: O(n)

o Better-2

- XOR of two same numbers is always 0 i.e. a ^ a = 0
- XOR of a number with 0 will result in the number itself i.e. 0 ^ a = a
- Perform the XOR of all the numbers of the array elements, we will be left with a single number
- Optimal if array is unsorted
- Time Complexity: O(n)
- Space Complexity: O(1)
- Optimal
 - Works IFF array is sorted
 - Binary Search
 - lacktriangle Time Complexity: O(logn)
 - Space Complexity: O(1)

```
# Python3
# Better Solution - 1
class Solution:
    def singleNumber(self, nums: List[int]) -> int:
        dct = dict()
        for i in nums:
            dct[i] = 0
        for i in nums:
            dct[i] += 1
        for i in dct:
            if dct[i] == 1:
            return i
```

```
// C++
// Better Solution - 1
class Solution {
public:
    int singleNumber(vector<int>& nums) {
        unordered_map<int, int> umap;
        for (int i = 0; i < nums.size(); i++) {
            umap[nums[i]]++;
        }
        for (auto it: umap) {
            if (it.second == 1) return it.first;
        }
        return -1;</pre>
```

```
};
# Python3
# Better Solution - 2
class Solution:
   def search(self, A, N):
       xor = 0
       for i in A:
          xor ^= i
        return xor
# Python3
# Optimal Solution
# Works iff array is sorted
// C++
// Optimal Solution
// Works iff array is sorted
class Solution{
public:
  int search(int A[], int N){
       int low = 0;
        int high = N-1;
        while(low <= high)</pre>
            int mid = low + (high - low) / 2;
           if(mid % 2 == 0)
                if(A[mid] == A[mid+1])
                   low = mid + 1;
                else
                    high = mid - 1;
            }
            else
                if(A[mid] == A[mid + 1])
                   high = mid-1;
                   low = mid + 1;
        }
       return A[low];
```

Next Permutation

- Total Permutations = n!
- $\bullet \ \ \ \ \text{Follow Dictionary Sorted order i.e.} \ \ \{\{1,2,3\},\ \{1,3,2\},\ \{2,1,3\},\ \{2,3,1\},\ \{3,1,2\},\ \{3,2,1\}\}$
- · Approach:

};

- o Brute-force
 - Generate all permutations and apply linear search
 - Time Complexity: O(n! * n)
 - Space Complexity: O(n)

Optimal

- First, we find the breakpoint i.e. point where this condition <code>nums[i] < nums[i+1]</code> is met from the back. If there is no such point then the list is already in descending order and the next permutation is the reverse of the given list.
- When a breakpoint is found we swap it with the first greater element from the back of the list and reverse the list elements on the right of breakpoint.
- Time Complexity: O(n)
- Space Complexity: O(1)

```
# Python3
# Optimal Solution
class Solution:
   def reverse(self, nums, start, stop):
       size = stop + start
       for i in range(start, (size + 1) // 2):
            nums[i], nums[size - i] = nums[size - i], nums[i]
    def nextPermutation(self, nums: List[int]) -> None:
       ind = -1
        # find breakpoint from back
       for i in range(len(nums)-2, -1, -1):
            if nums[i] < nums[i+1]:
               ind = i
                         # breakpoint found
       if ind == -1: # no breakpoint found
           nums.reverse() # in-place
            # nums[:] = nums[::-1] # also works but is not in-place
            \# Note that nums = nums[::-1] doesn't work as it is not in-place
           # nums[::-1] creates and returns new list object
        else:
            for i in range(len(nums)-1, ind, -1):
                if nums[i] > nums[ind]:
                    nums[i], nums[ind] = nums[ind], nums[i]
            # reverse list elements on the right of breakpoint
           self.reverse(nums, ind+1, len(nums)-1) # in-place
            \# nums[ind+1:] = nums[ind+1:][::-1] \# also works but is not in-place
            # but nums[2:4].reverse() is not correct
```

```
// C++
// Optimal Solution
class Solution {
public:
    void nextPermutation(vector<int>& nums) {
        int ind = -1;
        for (int i = nums.size()-2; i >= 0; i--) {
            if (nums[i] < nums[i+1]) {</pre>
                ind = i;
                break;
            }
        }
        if (ind == -1) {
            reverse(nums.begin(), nums.end());
        }
        else {
            for (int i = nums.size()-1; i >= 0; i--) {
                if (nums[i] > nums[ind]) {
                    swap(nums[i], nums[ind]);
                    break;
                }
```

```
}
reverse(nums.begin()+ind+1, nums.end());
}
}
```

Maximum Subarray Sum (Kadane's Algorithm)

- Approach
 - o Brute-force
 - Check the sum of every possible subarray and consider the maximum among them
 - Time Complexity: $O(n^3)$
 - Space Complexity: O(1)
 - Better
 - If we carefully observe, we can notice that to get the sum of the current subarray we just need to add the current element(i.e. arr[j]) to the sum of the previous subarray i.e. arr[i....j-1].
 - Time Complexity: $O(n^2)$
 - Space Complexity: O(1)
 - o Optimal
 - The intuition of the algorithm is not to consider the subarray as a part of the answer if its sum is less than 0. A subarray with a sum less than 0 will always reduce our answer and so this type of subarray cannot be a part of the subarray with maximum sum.
 - Here, we will iterate the given array with a single loop and while iterating we will add the elements in a sum variable. Now, if at any point the sum becomes less than 0, we will set the sum as 0 as we are not going to consider any subarray with a negative sum. Among all the sums calculated, we will consider the maximum one.
 - Time Complexity: O(n)
 - Space Complexity: O(1)

```
# Python3
# Brute-force Solution
def maxSubarraySum(arr, n):
    maxi = -sys.maxsize - 1  # maximum sum

for i in range(n):
    for j in range(i, n):
        # subarray = arr[i.....j]
        sum = 0

        # add all the elements of subarray:
        for k in range(i, j+1):
            sum += arr[k]

        maxi = max(maxi, sum)

return maxi
```

```
# Python3
# Better Solution
def maxSubarraySum(arr, n):
    maxi = -sys.maxsize - 1 # maximum sum

for i in range(n):
    sum = 0
    for j in range(i, n):
        # current subarray = arr[i....j]

    #add the current element arr[j]
    # to the sum i.e. sum of arr[i...j-1]
    sum += arr[j]

    maxi = max(maxi, sum) # getting the maximum

return maxi
```

```
# Python3
# Optimal Solution (Kadane's Algorithm)
class Solution:
    def maxSubArray(self, nums: List[int]) -> int:
        maxsum = nums[0]
        tempsum = 0

    for i in nums:
        tempsum += i
        maxsum = max(maxsum, tempsum)
        if tempsum < 0: tempsum = 0
    return maxsum</pre>
```

```
// C++
// Optimal Solution (Kadane's Algorithm)
class Solution {
public:
   int maxSubArray(vector<int>& nums) {
        int maxsum = nums[0];
        int tempsum = 0;
        for (auto i: nums) {
            tempsum += i;
            if (tempsum > maxsum) {
               maxsum = ts;
            if (tempsum < 0) {
                tempsum = 0;
           }
        }
        return maxsum;
   }
};
```

Print Subarray with Maximum Sum (variation of Kadane's Algorithm)

- Approach
 - Optimal
 - Store the starting index and the ending index of the subarray. Thus we can easily get the subarray afterwards without actually storing the subarray elements.

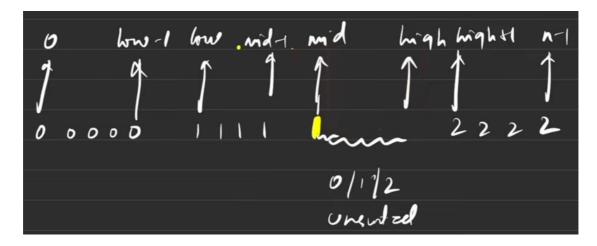
• Time Complexity: O(n)

• Space Complexity: O(1)

```
# Python3
# Optimal Solution
def maxSubarraySum(arr, n):
   maxi = -sys.maxsize - 1 # maximum sum
   sum = 0
   start = 0
   ansStart, ansEnd = -1, -1
   for i in range(n):
       if sum == 0:
           start = i # starting index
       sum += arr[i]
       if sum > maxi:
           maxi = sum
           ansStart = start
           ansEnd = i
       if sum < 0:
           sum = 0
   print(arr[ansStart:ansEnd+1])
```

Sort an array of 0's, 1's and 2's (Dutch National Flag Algorithm)

- Approach
 - Brute-force
 - Apply Merge-Sort Algorithm or any in-built Sorting Algorithm
 - Time Complexity: O(nlogn)
 - Space Complexity: O(n)
 - Better
 - Maintain 3 counter variables that store the number of occurrences of 0's, 1's and 2's
 - Two-Pass
 - Time Complexity: O(n)
 - Space Complexity: O(1)
 - Optimal
 - Maintain 3 pointers low=0 , mid=0 , high=len(nums)-1
 - Note that the array is sorted between 0 to low-1, low to mid-1, and high to len(nums)-1 and unsorted between mid to high-1
 - while mid ≤ high we check nums[mid] and swap it with low/high accordingly and maintain pointers as necessary



- One-Pass
- Time Complexity: O(n)
- Space Complexity: O(1)

```
# Python3
# Brute-force Solution
class Solution:
   def sortColors(self, nums: List[int]) -> None:
        nums.sort()
```

```
# Python3
# Better Solution (Two Pass)
class Solution:
   def sortColors(self, nums: List[int]) -> None:
       zero = 0
       one = 0
       two = 0
       for i in nums:
           if i == 0:
               zero += 1
            elif i == 1:
               one += 1
            else:
               two += 1
        for i in range(zero):
           nums[i] = 0
        for i in range(zero, one+zero):
           nums[i] = 1
        for i in range(one+zero, two+one+zero):
           nums[i] = 2
```

```
# Python3
# Optimal Solution (Dutch National Flag Algorithm - One Pass)
class Solution:
    def sortColors(self, nums: List[int]) -> None:
        low = 0
        mid = 0
        high = len(nums) - 1

    while mid <= high:
        if nums[mid] == 0:
            nums[low], nums[mid] = nums[low]
        low += 1</pre>
```

```
mid += 1
elif nums[mid] == 1:
    mid += 1
else:
    nums[mid], nums[high] = nums[high], nums[mid]
    high -= 1
```

```
// C++
// Optimal Solution (Dutch National Flag Algorithm)
#include <bits/stdc++.h>
class Solution {
public:
   void sortColors(vector<int>& nums) {
       int low = 0;
       int mid = 0;
       int high = nums.size() - 1;
        while (mid <= high) {
            if (nums[mid] == 0) {
                swap(nums[low], nums[mid]);
                low++;
                mid++;
            }
            else if (nums[mid] == 1) {
                mid++;
            }
            else {
                swap(nums[mid], nums[high]);
                high--;
           }
       }
   }
};
```

Best Time to Buy and Sell Stock

- Approach
 - Brute-force
 - Use 2 loops and track every transaction and maintain a variable to contain the max value among all transactions.
 - Time Complexity: $O(n^2)$
 - Space Complexity: O(1)
 - o Optimal
 - Iterate over the array and check whether cur_price min_price > max_profit and if cur_price < min_price</p>
 - Time Complexity: O(n)
 - Space Complexity: O(1)

```
# Python3
# Brute-force Solution
class Solution:
    def maxProfit(self, prices: List[int]) -> int:
        max_profit = 0
        for i in range(len(prices)):
            for j in range(i+1, len(prices)):
```

```
max_profit = max(max_profit, prices[j]-prices[i])
return max_profit
```

```
# Python3
# Optimal Solution
class Solution:
    def maxProfit(self, prices: List[int]) -> int:
        min_price = prices[0]
    max_profit = 0
    for i in range(1, len(prices)):
        # if current_price - min_price is greater than max_profit, update max_profit
        max_profit = max(max_profit, prices[i]-min_price)

# if current_price is less than min_price, update min_price
    min_price = min(min_price, prices[i])
return max_profit
```

```
// C++
// Optimal Solution
int maxProfit(vector<int> &arr) {
    int maxPro = 0;
    int n = arr.size();
    int minPrice = INT_MAX;

for (int i = 0; i < arr.size(); i++) {
        minPrice = min(minPrice, arr[i]);
        maxPro = max(maxPro, arr[i] - minPrice);
    }

return maxPro;</pre>
```

Using Kadane's Algorithm

• Will also work when the prices array is given as price_difference array i.e. {1, 7, 4, 11} will be given as {0, 6, -3, 7}

```
# Python3
# Optimal Solution (variation of Kadane's Algorithm)
class Solution:
    def maxProfit(self, prices: List[int]) -> int:
        n = len(prices)
        ans = 0
        curSum = 0
        for i in range(n-1):
            curSum += prices[i+1] - prices[i]
        if curSum < 0:
            curSum = 0
        ans = max(ans, curSum)
    return ans</pre>
```

Merge 2 Sorted Arrays

- Approach
 - o Brute-force
 - Concatenate both arrays and apply any (in-built) sorting algorithm
 - Time Complexity: O((m+n)log(m+n))

■ Space Complexity: *O*(1) (in-place)

Better

- Maintain a separate array res and two pointers a and b (for given arrays).
- while (a < m and b < n) Check if nums1[a] < nums2[b]
- Time Complexity: O(m+n)
- Space Complexity: O(m+n)

Optimal

- Maintain three pointers and iterate from backwards of both arrays and take the larger element between the two and store it at the back of nums1 array
- Time Complexity: O(m+n)
- Space Complexity: O(1)

```
# Python3
# Better Solution
class Solution:
    def merge(self, nums1: List[int], m: int, nums2: List[int], n: int) -> None:
       a = b = 0
        res = []
        while (a < m \text{ and } b < n):
           if nums1[a] < nums2[b]:
               res.append(nums1[a])
                a += 1
                res.append(nums2[b])
                b += 1
        while (a < m):
            res.append(nums1[a])
            a += 1
        while (b < n):
           res.append(nums2[b])
        nums1[:] = res.copy()
```

```
# Python3
# Optimal Solution
class Solution:
    def merge(self, nums1: List[int], m: int, nums2: List[int], n: int) -> None:
        a, b, write_index = m-1, n-1, m + n - 1

    while b >= 0:
        if a >= 0 and nums1[a] > nums2[b]:
            nums1[write_index] = nums1[a]
        a -= 1
    else:
        nums1[write_index] = nums2[b]
        b -= 1

    write_index -= 1
```

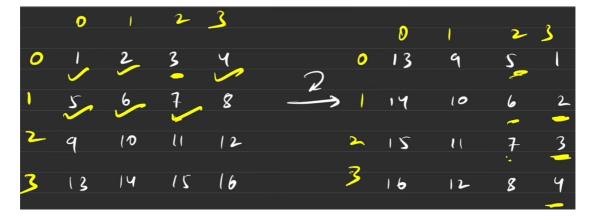
```
// C++
// Optimal Solution
class Solution {
public:
    void merge(vector<int>& nums1, int m, vector<int>& nums2, int n) {
```

```
int a = m - 1;
int b = n - 1;
int c = m + n - 1;

while (b >= 0) {
    if (a >= 0 && nums1[a] > nums2[b]) {
        nums1[c] = nums1[a];
        a--;
    }
    else {
        nums1[c] = nums2[b];
        b--;
    }
    c--;
}
```

Rotate the Matrix by 90 Degrees (Clockwise)

- Approach
 - o Brute-force
 - Take an element in the matrix and put it in its proper place in another matrix.
 - Time Complexity: $O(n^2)$
 - Space Complexity: $O(n^2)$





- o Optimal
 - Transpose the matrix and reverse all the rows.

- Time Complexity: $O(n^2)$
- Space Complexity: O(1) (in-place)

```
# Python3
# Brute-force Solution
class Solution:
    def rotate(self, matrix: List[List[int]]) -> None:
        n = len(matrix)
        ans = [[0 for i in range(n)]for j in range(n)]

    for i in range(n):
        for j in range(n):
        ans[j][n-i-1] = matrix[i][j]

    for i in range(n):
        for j in range(n):
        matrix[i][j] = ans[i][j]
```

```
# Python3
# Optimal Solution
class Solution:
    def rotate(self, matrix: List[List[int]]) -> None:
        n = len(matrix)
        for i in range(1, n):
            for j in range(i):
                matrix[i][j], matrix[j][i] = matrix[j][i], matrix[i][j]

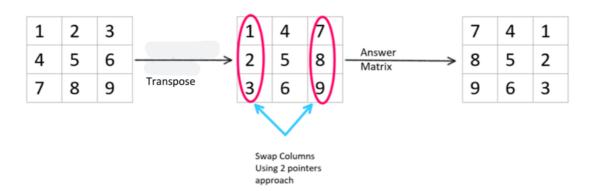
        for i in matrix:
            i.reverse()
```

```
// C++
// Optimal Solution
void rotate(vector<vector<int>>& m) {
    int n = m.size();

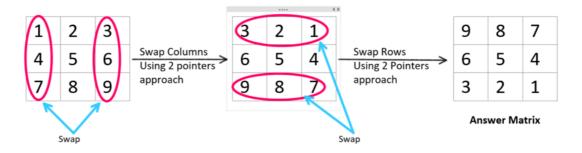
    for(int i=0; i<n; i++)
        for(int j=0; j<i; j++)
            swap(m[i][j], m[j][i]);

    for(int i=0; i<n; i++)
        reverse(m[i].begin(), m[i].end());
}</pre>
```

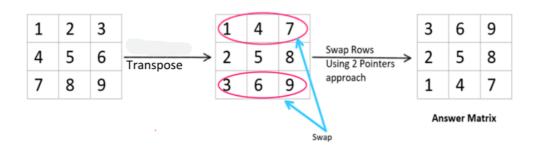
Rotate 90°



Rotate 180°



Rotate 270°



Merge Overlapping Sub-intervals

- Approach
 - Brute-force

- Sort the array first and then check for every interval[i], what all intervals[i+1] to intervals[n-1] could be merged with the current interval.
- Time Complexity: O(nlogn) + O(2n)
- Space Complexity: O(n)
- Optimal
 - Sort the array
 - Use stack to check if interval[i] ≤ stack.top()[1] then update the stack top with max(stack.top()[1], interval[i][1]) else push the interval[i] onto the stack
 - Time Complexity: O(nlogn) + O(n)
 - Space Complexity: O(n)

```
# Python3
# Brute-force Solution
def mergeOverlappingIntervals(arr: List[List[int]]) -> List[List[int]]:
   n = len(arr) # size of the array
   # sort the given intervals:
   arr.sort()
   ans = []
    for i in range(n): # select an interval:
       start, end = arr[i][0], arr[i][1]
       # Skip all the merged intervals:
       if ans and end <= ans[-1][1]:
        # check the rest of the intervals:
        for j in range(i + 1, n):
            if arr[j][0] \le end:
               end = max(end, arr[j][1])
            else:
                break
        ans.append([start, end])
    return ans
```

```
// C++
// Optimal Solution
vector<vector<int>> mergeOverlappingIntervals(vector<vector<int>> &arr) {
   int n = arr.size(); // size of the array

//sort the given intervals:
```

Template

- Approach
 - o Brute-force

- Time Complexity: $O(n^3)$
- Space Complexity: O(1)
- o Better

•

- Time Complexity: $O(n^3)$
- Space Complexity: O(1)
- Optimal

•

- Time Complexity: $O(n^3)$
- Space Complexity: O(1)

```
# Python3
# Brute-force Solution

# Python3
# Better Solution

# Python3
# Optimal Solution

// C++
// Optimal Solution
```