











WORST CASE VS
AVERAGE CASE

MAX

Key idea: We can exploit the knowledge that uncertain outcomes are controlled by chance instead of an adversary

0.5

0.5

0.5

0.5

MAX

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EXPECTIMAX SEARCH

- Previously: Values reflect worst case outcomes (minimax)
- Now: Values reflect average case outcomes (expectimax)
- Expectimax search:
 - Max nodes just like in minimax search
 - Chance nodes instead of min nodes in minimax search
 - Outcomes are uncertain
 - Calculate their expected utilities (i.e., utilities weighted by their likelihood)

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EXPECTIMAX SEARCH

def value(state):

if the state is a terminal state: return the state's utility if the next agent is MAX: return max-value(state) if the next agent is MIN: return exp-value(state)

def max-value(state):

initialize $v = -\infty$ for each successor of state: v = max(v, exp-value(successor))return v def exp-value(state):
 initialize v = 0
 for each successor of state:
 p = probability(successor)
 v += p * max-value(successor)
 return v

EXPECTIMAX SEARCH

| | Minimax | alpha-beta | Expectimax |
|--|----------|------------|------------|
| Correct the solution it finds is optimal | Yes | Yes | Yes |
| Complete it terminates | Yes | Yes | Yes |
| Space Complexity max nodes in memory | O(bm) | O(bm) | O(bm) |
| Time Complexity max nodes generated | $O(b^m)$ | $O(b^m)$ | $O(b^m)$ |

branching factor *b* depth of the goal *d* depth of tree *m*

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OTHER GAMETYPES

- Expectiminimax search:
 - MAX, CHANCE, MIN, CHANCE, MAX, ...
 - Used to model games like backgammon
- Modeling multi-agent problems
 - e.g., two Pacmans solving eat-all-dots problem
 - Utilities are now vectors, with each element representing the utility of one agent



OTHER GAMETYPES

• Expectiminimax search:

• MAX, CHANCE, MIN, CHANCE, MAX, ...

MAX a I

How do you model problems where you can take multiple actions in one turn, and the number of actions depend on some rule?

• e.g., two Pacmans solving eat-all-dots problem

 Utilities are now vectors, with each element representing the utility of one agent 1.2 2.0 1.1 2.10

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