

Tangent Function

In right triangle trigonometry (for acute angles only), the tangent is defined as the ratio of the opposite side to the adjacent side. The unit circle definition is $\tan(\theta) = y/x$ or $\tan(\theta) = \sin(\theta)/\cos(\theta)$. The **tangent function** is negative whenever sine or cosine, but not both, are negative: the second and fourth quadrants. Tangent is also equal to the slope of the terminal side.

Domain: $\{x | x = \pi + k\pi, k = \dots, -1, 0, 1, \dots\} = \{x | x = \dots, -3\pi, -\pi, \pi, 3\pi, \dots\}$

Range: Real numbers (R)

Characteristics: Period = π

- x intercepts: $x = k\pi$, where k is an integer.
- y intercepts: $y = 0$
- Symmetry: since $\tan(-x) = -\tan(x)$ then $\tan(x)$ is an odd function and its graph is symmetric with respect to the origin.
- Intervals of increase/decrease: over one period and from $-\pi/2$ to $\pi/2$, $\tan(x)$ is increasing.
- Vertical asymptotes: $x = \pi/2 + k\pi$, where k is an integer.

