

# Human Categorization

Kurt Braunlich

# "Classical" View (e.g., Aristotle)

Concepts are combinations of features, or "definitions".

Features are **necessary** and **sufficient**

- Necessary: if category, then features
- Sufficient: if features, then category

e.g.,

- *If car, then steering wheel, seats and an engine*
- *If X has a steering wheel, seats, and an engine, it is a car*

## Classical View: Limitations (1)

- Graded typicality (Rosch & Mervis, 1975).



e.g.,

VS.



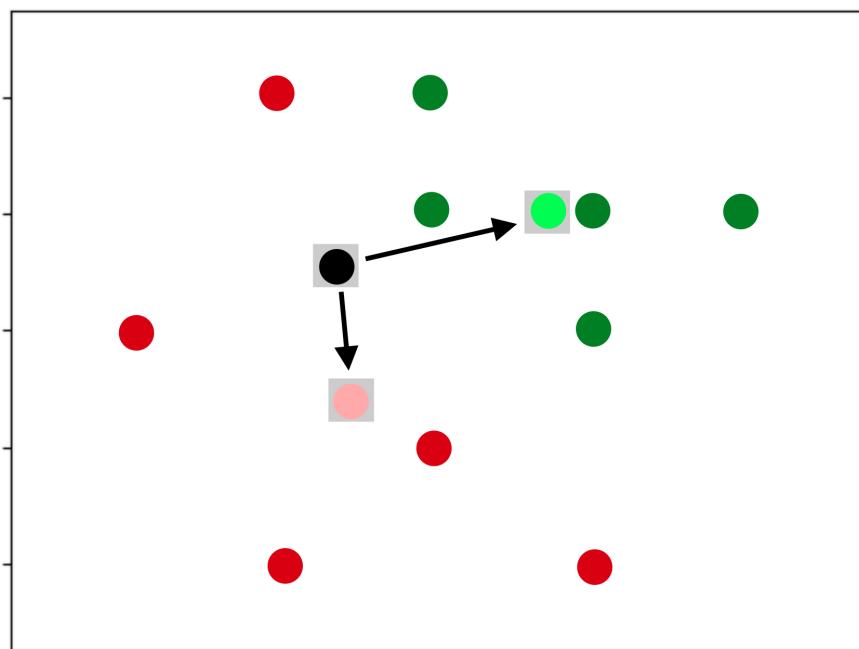
## Classical View: Limitations (2)

- McCloskey & Glucksberg, 1978: Many categories change across time, and differ between participants

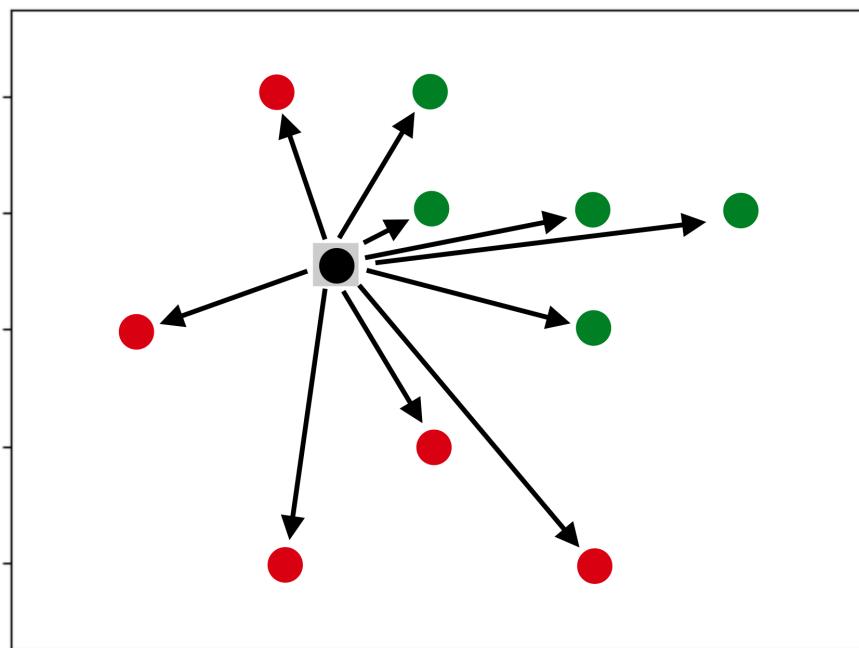


- Uncertainty. e.g.,
- Some concepts/categories don't have clear features or definitions
  - e.g., "just" vs. "unjust"

# Prototype Theory (e.g., Reed, 1972)



# Exemplar Theory (e.g., Nosofsky, 1986)



# Psychological Distance

During object **identification**, individual objects must be differentiated, and all features are relevant.

- **Exemplar:** The distance,  $d$ , between object  $i$  and  $j$ :

$$d_{ij} = \sum_k |x_{ik} - x_{jk}|$$

- **Prototype<sup>\*</sup>:** The distance,  $d$ , between object  $i$  and prototype  $A$ :

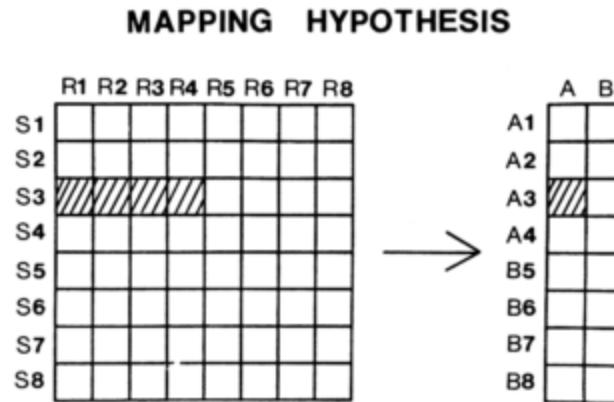
$$d_{iA} = \sum_k |x_{ik} - x_{Ak}|,$$

where  $k$  : dimension

\* For comparison, throughout, we assume Multiplicative Prototype Model...

# The "Mapping" Hypothesis

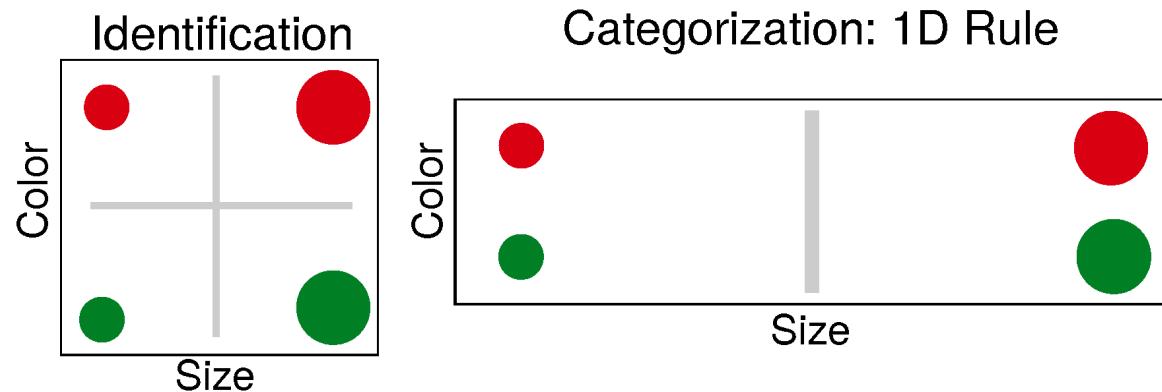
Human categorization is closely related to identification. It should be possible to predict categorization accuracy from identification confusions.



**Shepard (1961):** mapping does not explain categorization.

- Categorization involves abstraction and/or attention

# Attention "Warps" Psychological Space



... increasing the ratio of within- to between-category similarity.

# Psychological Distance: Categorization

Much flexibility in human categorization can be modeled by including attentional parameters,  $w$ :

e.g., in the Generalized Context Model (an exemplar model; Nosofsky, 1986):

$$d_{ij} = \sum_k w_k |x_{ik} - x_{jk}|,$$

# Integral vs. Separable Dimensions

Garner (1976): Can dimensions be ignored?

- **Separable:** reaction time same for 2D stimuli with 1D rule, and 1D stim with 1D rule. E.g., [red square and red circle vs. green square and green circle] vs. [red square vs. green square]
- **Integral:** Dimensions interact. E.g., when categorizing 2D auditory stim based on 1D "frequency" rule:
  - Faster RT\* when intensity is positively correlated with frequency
  - Slower RT\* when intensity is orthogonal to frequency

\* relative to a 1D rule with 1D stimuli (e.g., intensity held constant).

# The Minkowski $r$ Metric

Using the Minkowski distance metric, the  $r$  parameter allows us to use **Euclidean** ( $r=2$ ) or **City Block** ( $r=1$ ) distance measures, which are appropriate for **integral** vs. **separable** dimension stimuli:

$$d_{ij} = \left( \sum_k w_k |x_{ik} - x_{jk}|^r \right)^{1/r}$$

# Similarity

Similarity is an exponential function of distance, and is influenced by the sensitivity parameter,  $c$ .

$$s_{ij} = d^{-cd_{ij}}$$

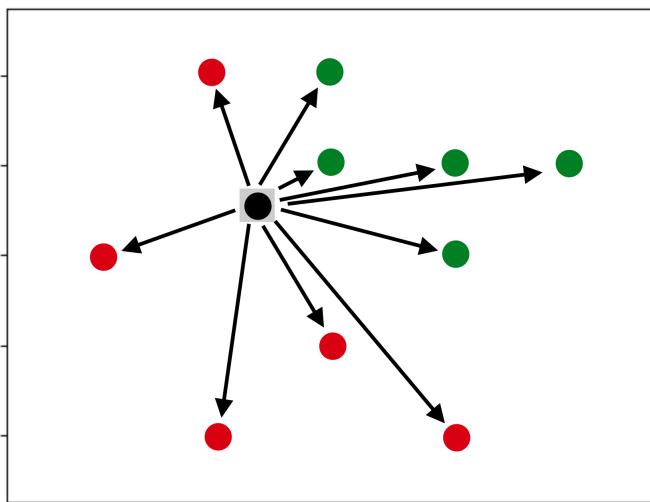
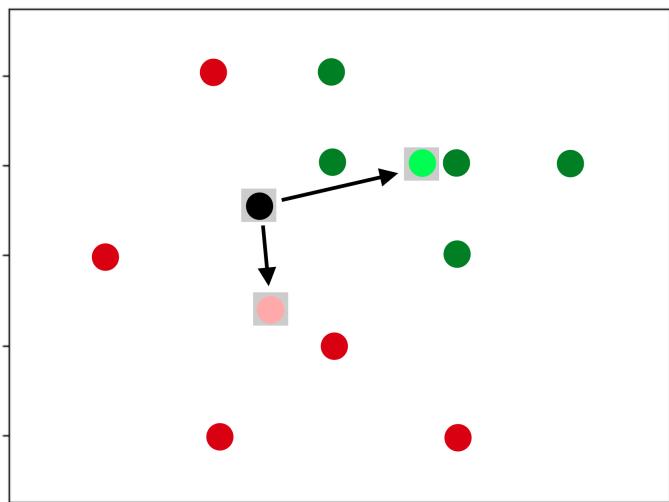
- when  $c$  is high, insensitive to  $w$
- when  $c$  is low,  $w$  more influential

## Choice (Luce, 1963; Shepard, 1957)

The probability of choosing category  $A$ , given stimulus,  $i$ , is given by the choice rule :

$$P(A|i) = \frac{\sum_{a \in A} s_{ia}}{\sum_{a \in A} s_{ia} + \sum_{b \in B} s_{ib}}$$

# Prototypes vs. Exemplars



# The 5/4 Category Structure

*The 5–4 Category Structure*

Stimulus	Dimension diagnosticity			
	High 1	Low	High 2	Medium
Category A items				
A1	1	1	1	0
A2	1	0	1	0
A3	1	0	1	1
A4	1	1	0	1
A5	0	1	1	1
Category B items				
B1	1	1	0	0
B2	0	1	1	0
B3	0	0	0	1
B4	0	0	0	0

**Prototype** predicts A1 easier to learn

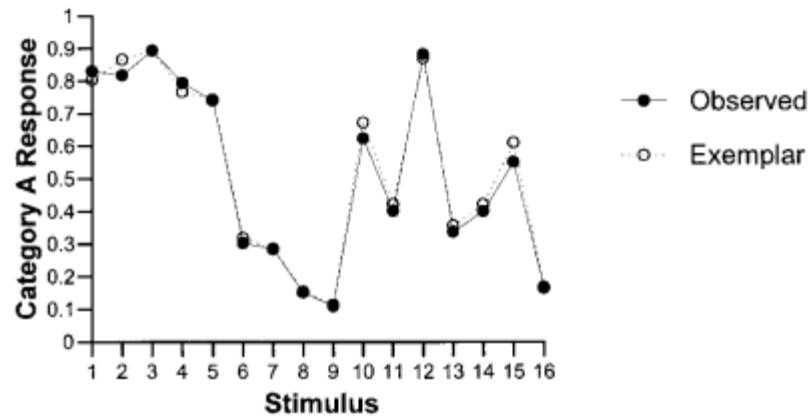
- A1 shares 3 features with the *A* prototype (0000 is most common on each D) but only one with the *B* prototype (1111)

**Exemplar** predicts A2 easier to learn

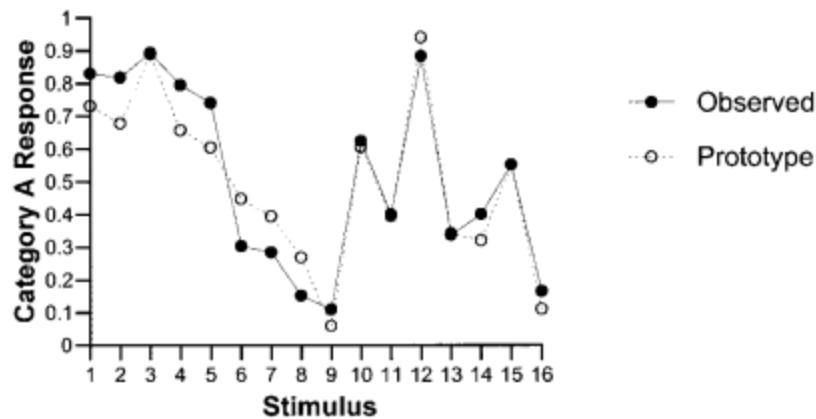
- A2 shares 3 features with 2 *A* members (A1 and A3) and less than or equal to 2 with any B member.
- Inconsistent experimental results...

# Model Comparison

B. Exemplar Model



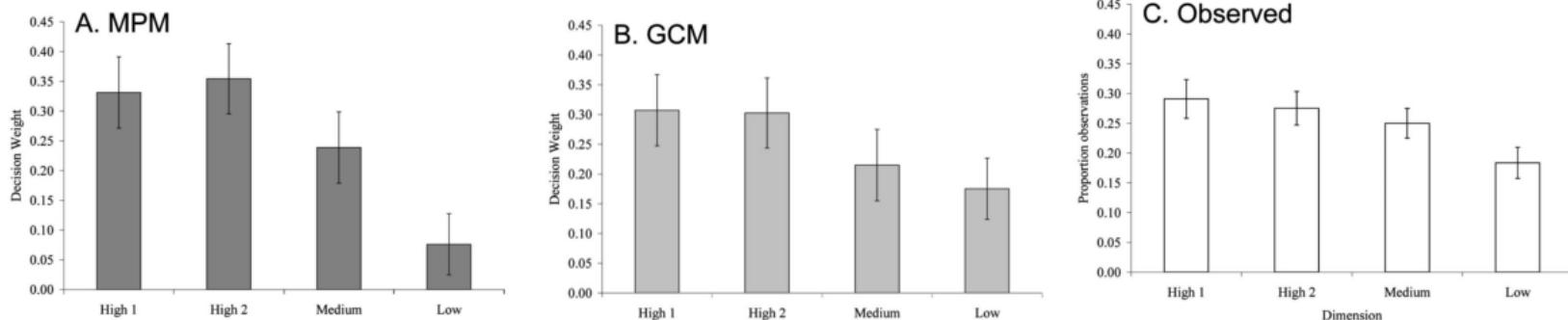
A. Prototype Model



Smith & Minda (2000): Exemplar models typically provide a better fit to choice data than prototype models, particularly on trained items (stim 1-9)

# Eye Tracking

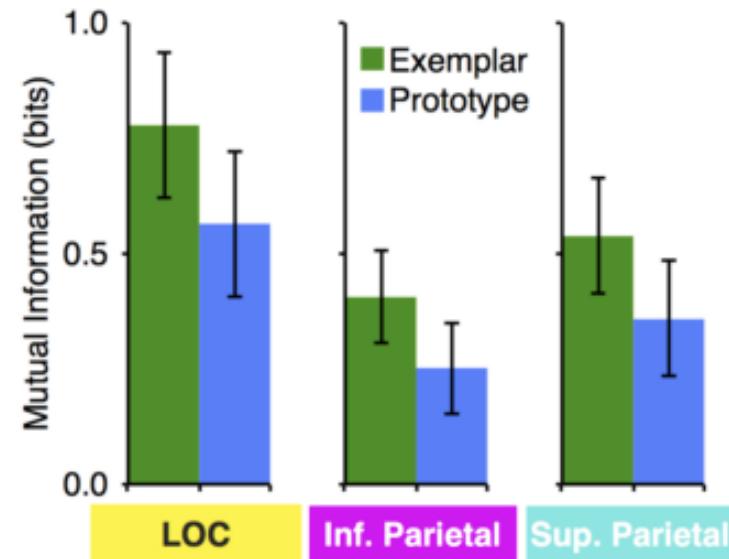
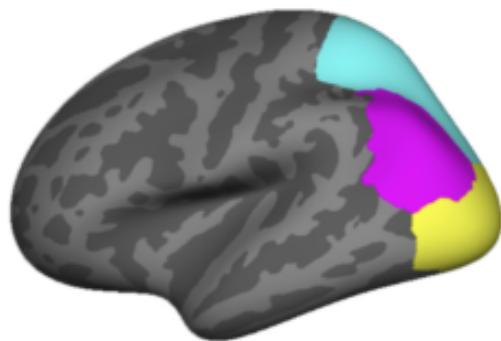
**Smith Minda (2000): GCM posits suboptimal attention weights (i.e., attention to uninformative dimensions)**



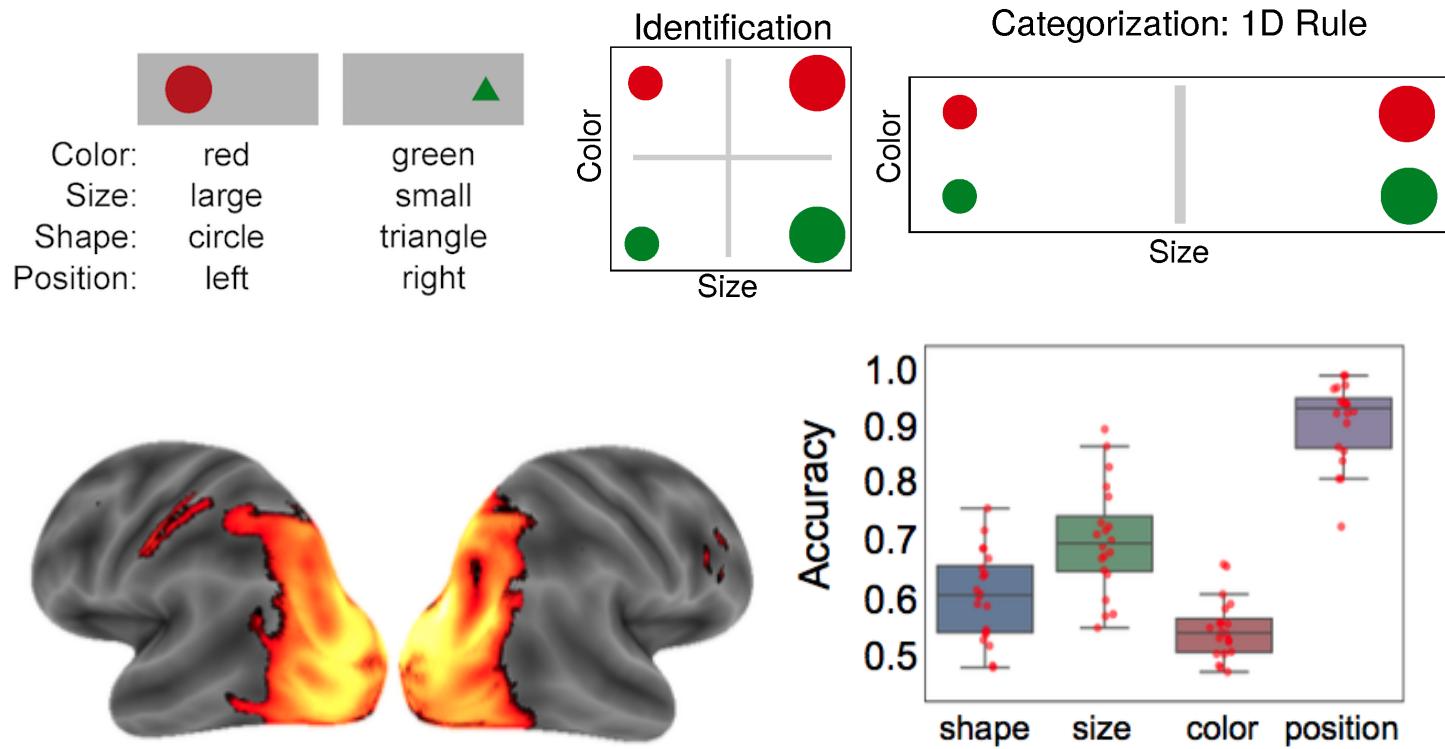
**Rehder & Hoffman, (2005): Eye fixation data more closely matched predictions of GCM**

# FMRI

Mack et al. (2013): Neural stimulus representations were more consistent with exemplar model than prototype model.



Braunlich & Love, (in prep.): Discriminability of neural feature representations covary with individual differences in attentional parameters. Better match for GCM than MPM.



# Flexible Clustering

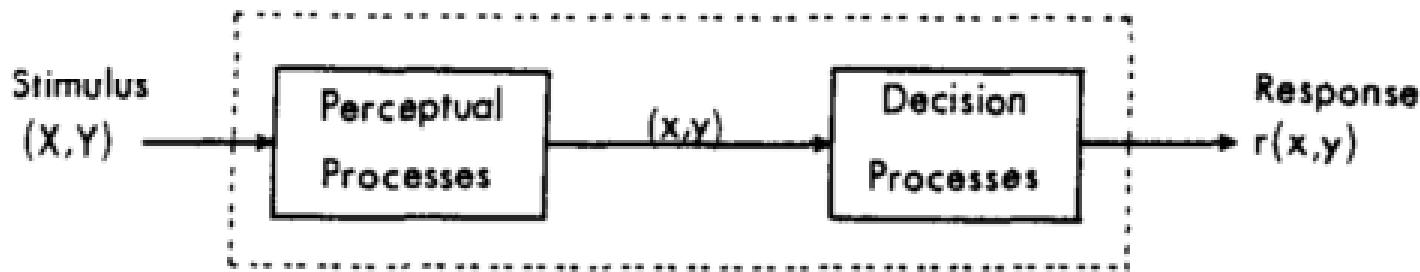
Anderson (1991): Rational Model of Categorization

Love & Gureckis (2004): SUSTAIN

- Based on structure in external world, and our experiences with it, we can flexibly learn intermediate category representations.

# Rules

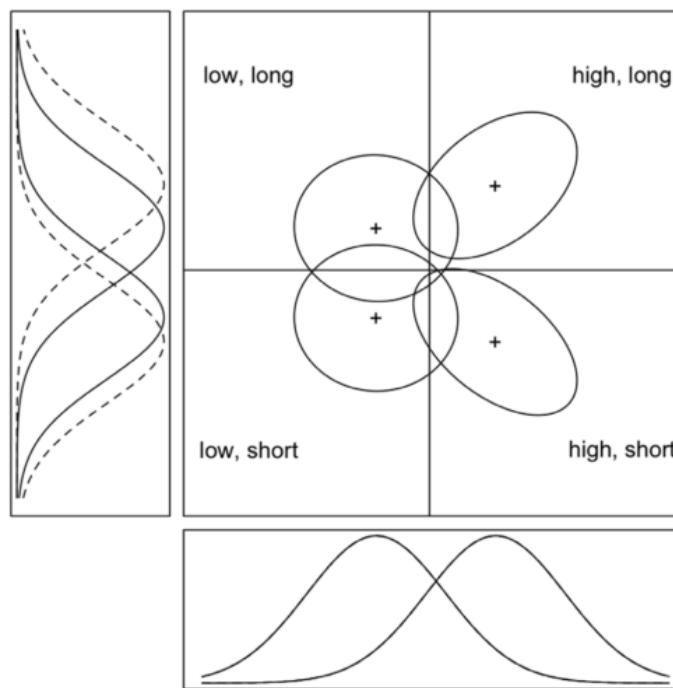
Ashby & Townsend (1986): General Recognition Theory



- Noise in perception/identification: stimuli are represented as multivariate distributions. If multivariate normal, then GRT is a multivariate extension of Signal Detection Theory.
- Noise in decision-boundary: "criterial noise"

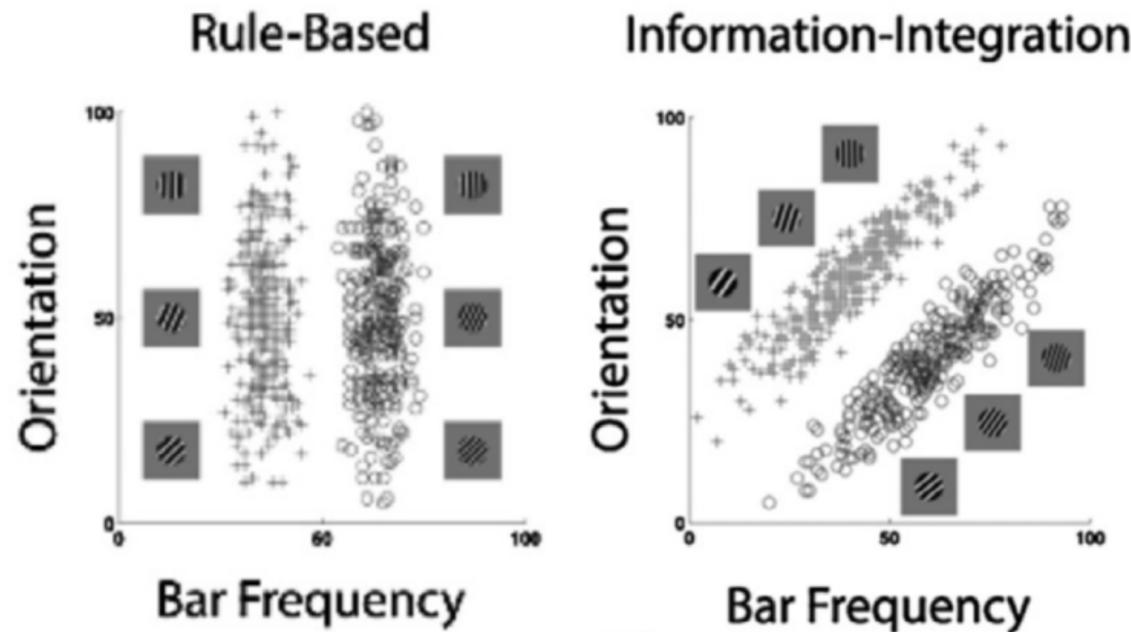
## Ashby & Townsend (1986): General Recognition Theory

Decision bounds (straight lines) parcellate perceptual space into response regions:



# Multiple-Process Models (1)

Ashby et al. (1998): COVIS (Competition between verbal and implicit systems



RB: fast learning, strong generalization

II: slow, reward-dependent learning, poor generalization

## Multiple-Process Models (2)

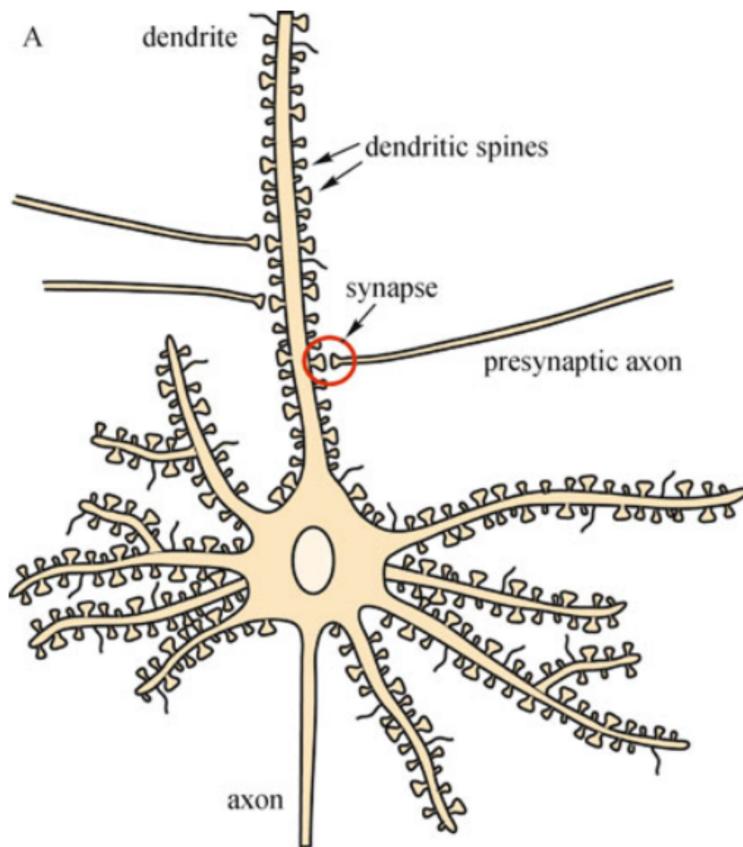
Nosofsky et. al. (1994): RULEX: Rule + Exception

- People learn simple rules and specific exceptions.
- Very good fits to learning data

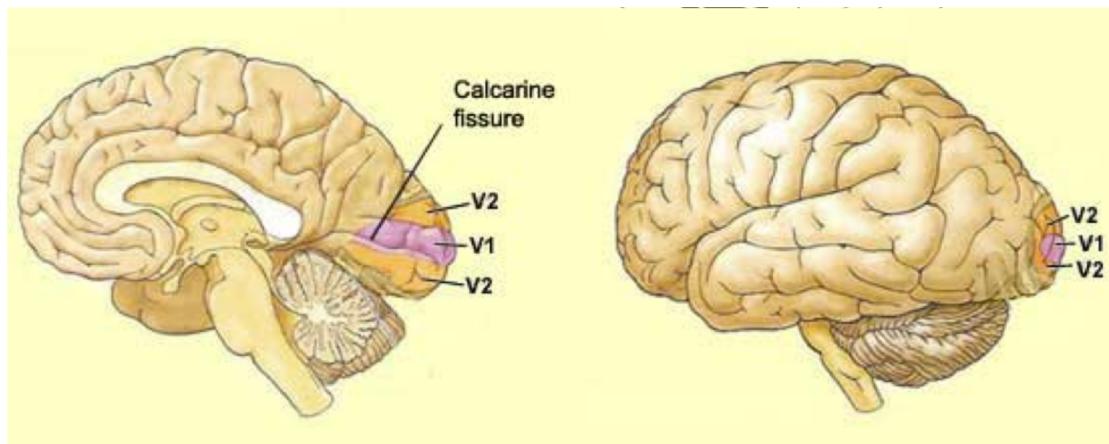
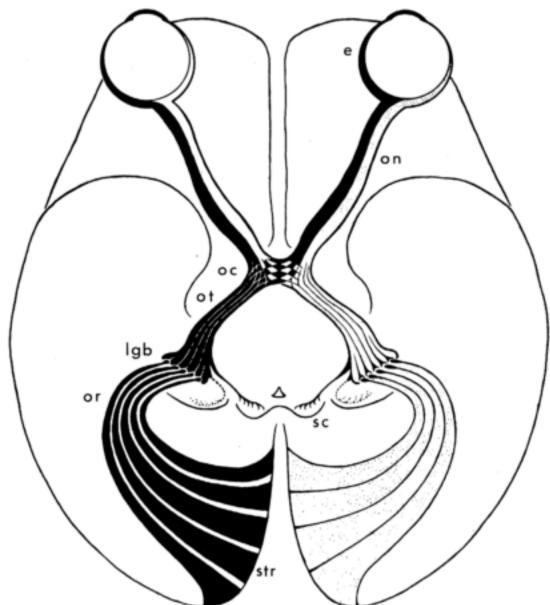
# Summary

- Low number of stimuli, high reps favor exemplars
- Initial learning characterized by hypothesis testing over simple rules
- High number of reps/ high number of stimuli, might facilitate direct stimulus  response associations (e.g., Information-Integration Structure)

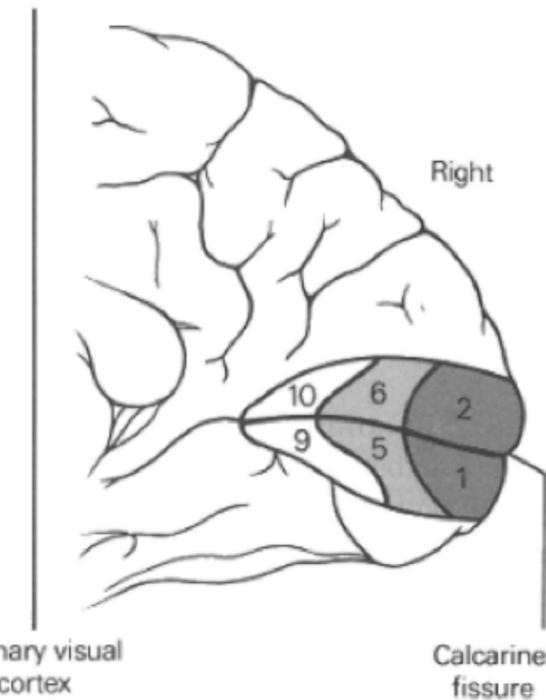
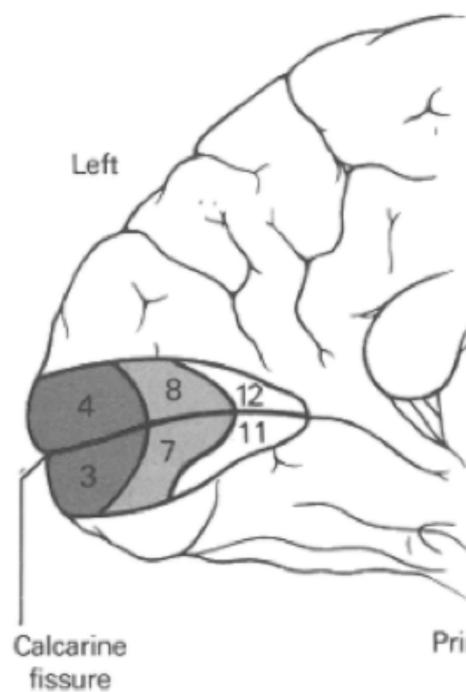
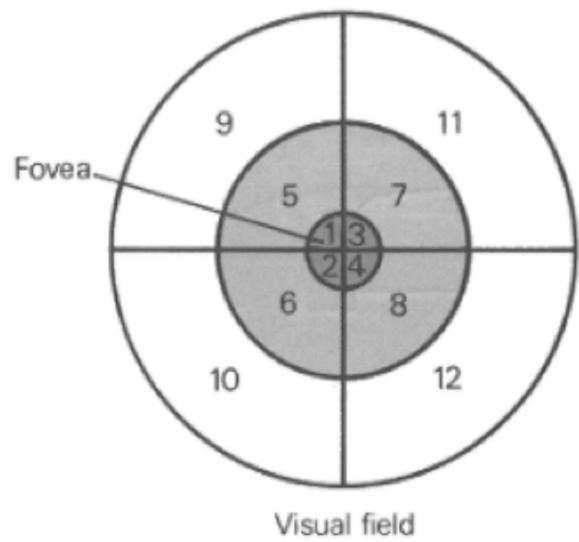
# The Neuron



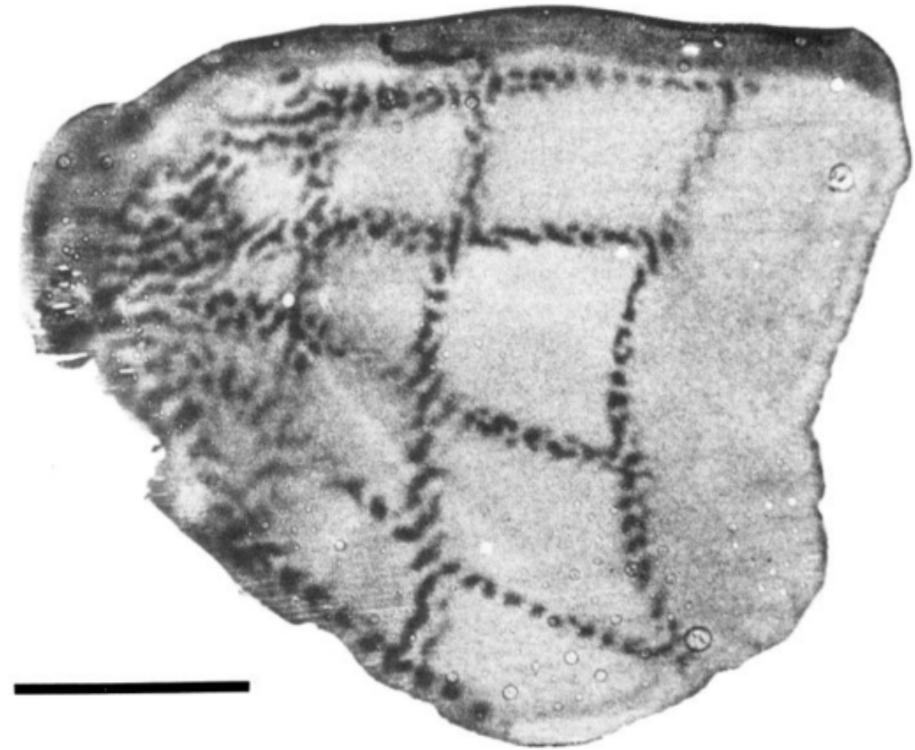
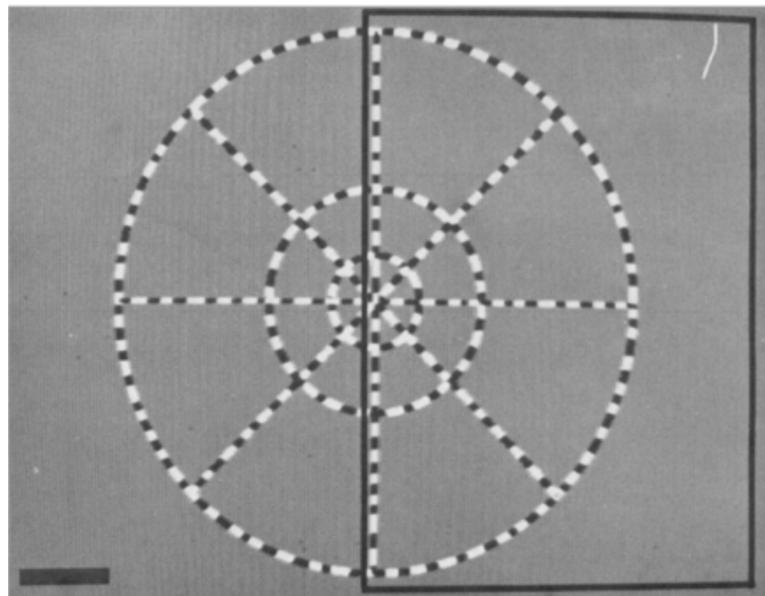
# From Eyes to Cortex:



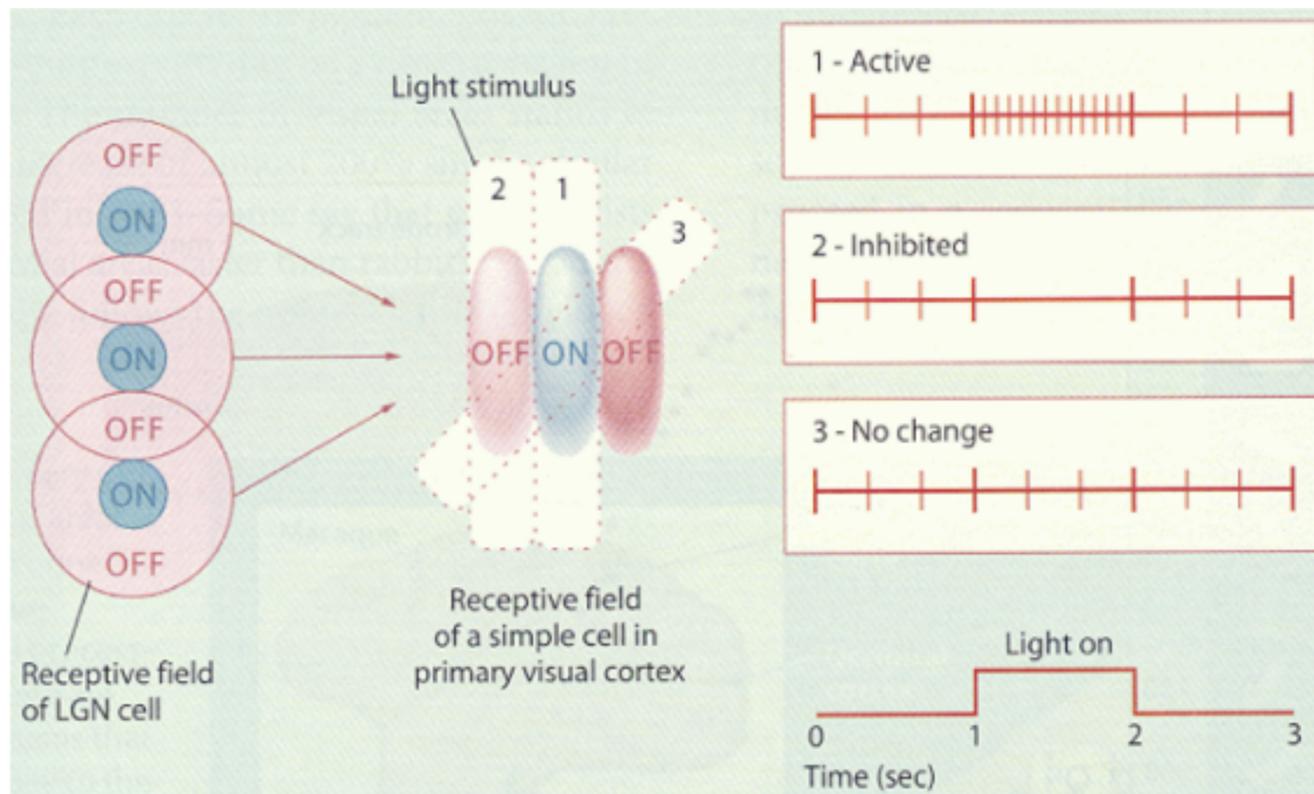
# Retinotopic Mapping in V1



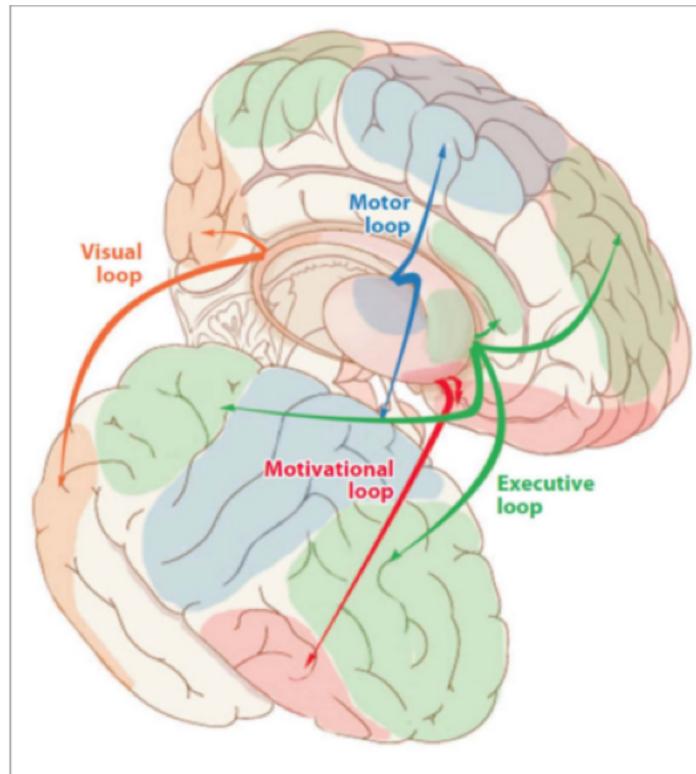
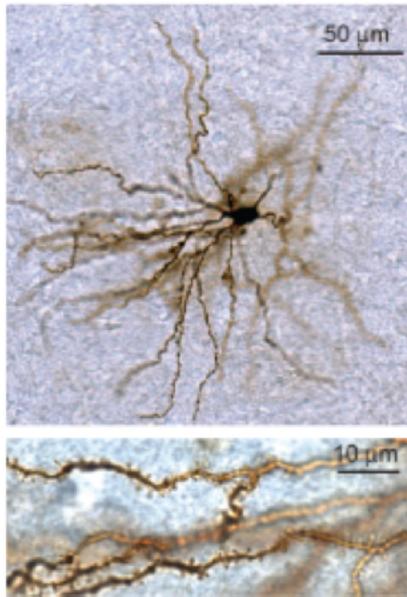
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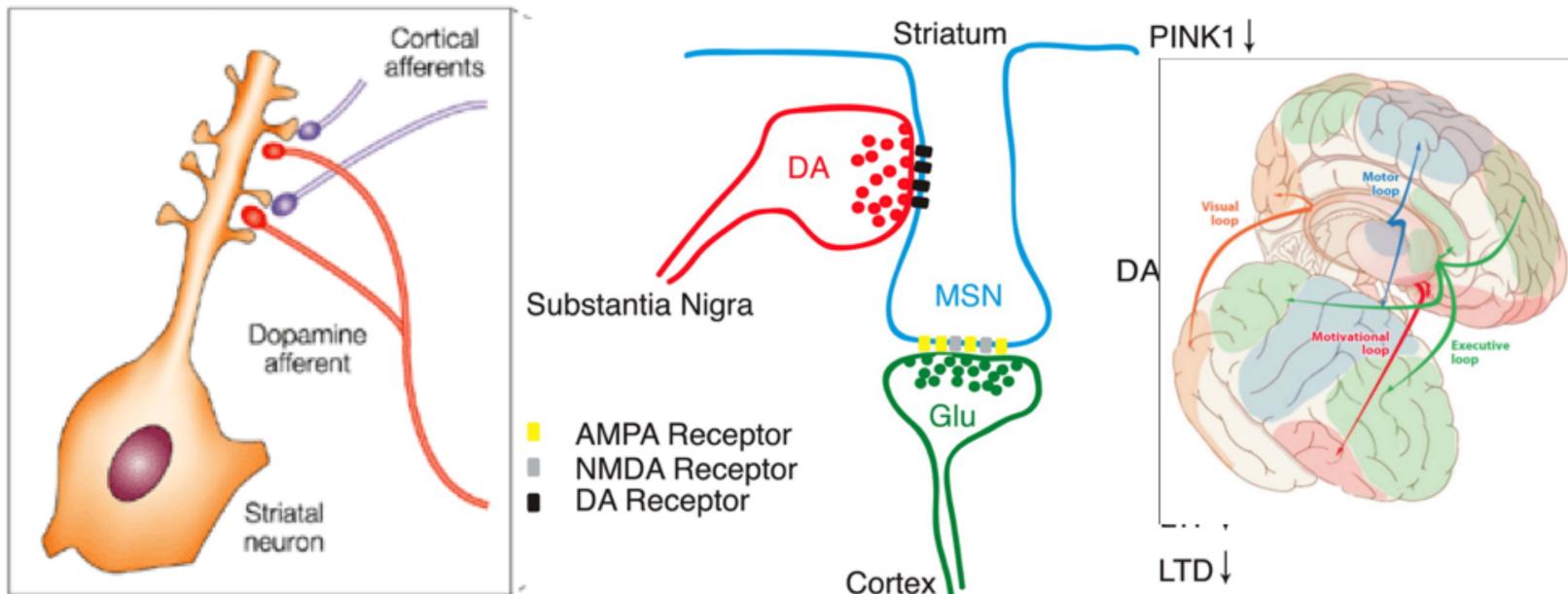
# Hierarchical Structure



# Corticostriatal Loops



# 3-Factor Hebbian Learning



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