generic HMM for multi-parent populations

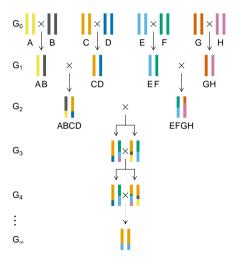
Karl Broman

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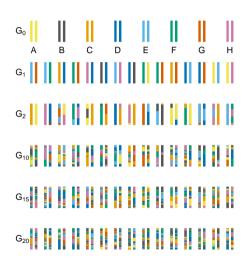
@kwbroman
 kbroman.org
 github.com/kbroman
kbroman.org/Talk_GenericHMM



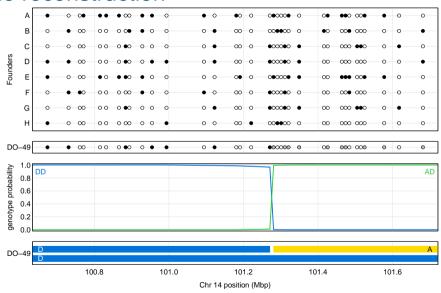
Recombinant Inbred Lines



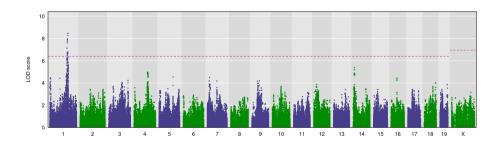
Advanced Intercross Population



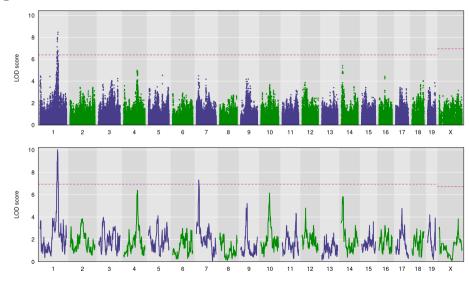
Genome reconstruction



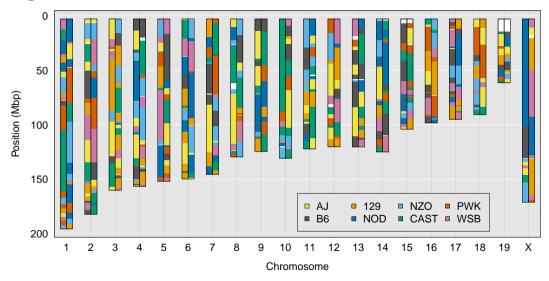
QTL genome scan



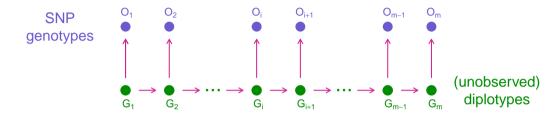
QTL genome scan



DO genome



Hidden Markov model



Initial
$$\Pr(G_1 = g)$$

$$\Pr(G_{i+1} = g' \mid G_i = g)$$
 Emission $\Pr(O_i \mid G_i = g)$

Exact probabilities

The Genomes of Recombinant Inbred Lines

Karl W. Broman¹

Department of Biostatistics, Johns Hopkins University, Baltimore, Maryland 21205

Manuscript received August 20, 2004

Accepted for publication November 5, 2004

ABSTRACT

Recombinant inbred lines (RILs) can serve as powerful tools for genetic mapping. Recently, members of the Complex Trait Consortium proposed the development of a large panel of eight-way RILs in the mouse, derived from eight genetically diverse parental strains. Such a panel would be a valuable community resource. The use of such eight-way RILs will require a detailed understanding of the relationship between alleles at linked loci on an RI chromosome. We extend the work of Haldane and Waddington on two-way RILs and describe the map expansion, clustering of breakpoints, and other features of the genomes of multiple-strain RILs as a function of the level of crossover interference in meiosis.

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Haplotype Probabilities for Multiple-Strain Recombinant Inbred Lines

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> Manuscript received July 28, 2006 Accepted for publication November 26, 2006

ABSTRACT

Recombiant inherd lines (BIL) derived from multiple inherd strains can serve as a powerful resource for the genetic dissection of complex rains. The use of such multiple-strain file, requires a detailed knowledge of the haplotype structure in such lines. Boostax (2005) derived the now and three-point haplotype probabilities for 2-way RIL to fromer required hely computation in one first whysholist results, and the latter were strictly numerical. We describe a simpler approach for the calculation of these probabilities, which allowed us to derive the symbolic form on the three-point haplotype probabilities which allowed us to derive the symbolic form of the three-point haplotype probabilities, which allowed us to derive populations (RIP).

Genotype Probabilities at Intermediate Generations in the Construction of Recombinant Inbred Lines

Karl W. Broman¹

Department of Biostatistics and Medical Informatics, University of Wisconsin, Macison, Wisconsin 53706

ABSTRACT The mouse Collaborate Cross (CC) is a paire of eight-way recombinant inhed lines eight deven powerful strain are internated, followed by repealed stilling makes must present partial to crossal are next of the red lines whose general strain are internated, followed by repealed stilling makes present partial strain are required to much inherently, and so a number of meetings makes and the processing of the original eight strain. Many generations are required to much inherently, and so a number of meetings in the sound in the processing of the CC lines could not be a found to the processing of the CC lines incompletely informative general crowders (but his subject and control of the CC lines incompletely informative general crowders (but his subject acceptance) in the makes (but his subject and the processing ana

Haplotype Probabilities in Advanced Intercross Populations

Karl W. Broman¹

Department of Biostatistics and Medical Informatics, University of Wisconsin-Madison, Madison, Wisconsin 53706

ABSTRACT Advanced intercross populations, in which multiple inbred strains are mated at random for many generations, have the advantage of greater precision of genetic mapping because of the accumulation of recombination events across the multiple generations. Related designs include heterogeneous stock and the diversity outcross population. In this article, I derive the two-locus haplotype probabilities on the autosome and X chromosome with these designs. These haplotype probabilities provide the key quantities for developing hiddem Markov models for the treatment of missing genotype information. I further derive the map expansion in these populations, which is the frequency of recombination breakpoints on a random chromosome.

Generic model



k founders in proportions $\{\alpha_i\}$ *n* generations of random mating

Random chromosome:

$$\pi_i = \alpha_i$$

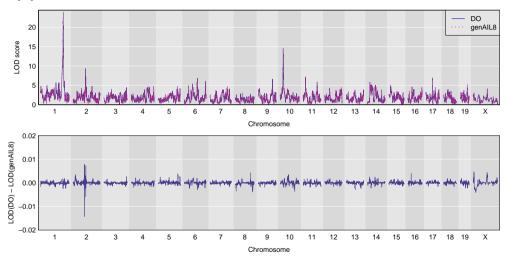
$$t_{ij} = \alpha_j \left[1 - (1 - r)^n \right] \quad \text{when } i \neq j$$

Map expansion:

$$n(1 - \sum_{i} \alpha_i^2)$$

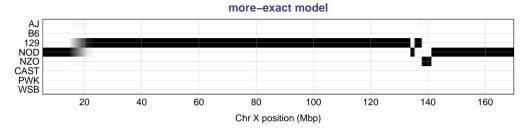
= $n(\frac{k-1}{k})$ if $\alpha_i \equiv 1/k$

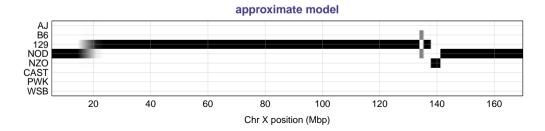
DO application



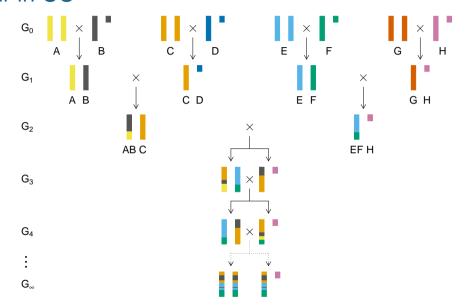
data from Al-Barghouthi et al (2021) doi.org/gkf64n

CC038 X chr





X chr in CC



Summary

- ► Generic model for genome reconstruction in multi-parent populations
- Specific relative proportions of founders + effective number of generations of random mating
- Basic conclusion: HAPPY is effective
- ► bioRxiv manuscript: doi.org/gswx

Slides: kbroman.org/Talk_GenericHMM



bioRxiv manuscript: doi.org/gswx

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