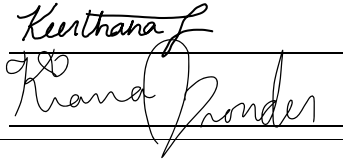


## Programming Assignments 3 and 4 – 601.455/655 Fall 2023

Score Sheet (hand in with report) Also, PLEASE INDICATE WHETHER YOU ARE IN 601.455 or 601.655

(one in each section is OK)

Name 1	Keerthana Thammanna
Email	lthamma1@jhu.edu
Other contact information (optional)	
Name 2	Kiana Bronder
Email	kbronde1@jhu.edu
Other contact information (optional)	
Signature (required)	<p>I (we) have followed the rules in completing this assignment</p> <div style="text-align: center;">  </div>

Grade Factor		
Program (40)		
Design and overall program structure	20	
Reusability and modularity	10	
Clarity of documentation and programming	10	
Results (20)		
Correctness and completeness	20	
Report (40)		
Description of formulation and algorithmic approach	15	
Overview of program	10	
Discussion of validation approach	5	
Discussion of results	10	
TOTAL	100	

# 1 Mathematical Approach

## 1.1 Registration and $d_k$ Calculation

We opted to implement a closed form solution for registration rather than an iterative method to have a quicker method. We used Arun's registration that we implemented in PA1, which we quickly describe below.

$$\begin{aligned}\bar{a} &= \frac{1}{N} \sum_{i=1}^N \vec{a}_i & \tilde{a}_i &= \vec{a}_i - \bar{a} \\ \bar{b} &= \frac{1}{N} \sum_{i=1}^N \vec{b}_i & \tilde{b}_i &= \vec{b}_i - \bar{b} \\ \mathbf{H} &= \sum_i \begin{bmatrix} \tilde{a}_{i,x} \tilde{b}_{i,x} & \tilde{a}_{i,x} \tilde{b}_{i,y} & \tilde{a}_{i,x} \tilde{b}_{i,z} \\ \tilde{a}_{i,y} \tilde{b}_{i,x} & \tilde{a}_{i,y} \tilde{b}_{i,y} & \tilde{a}_{i,y} \tilde{b}_{i,z} \\ \tilde{a}_{i,z} \tilde{b}_{i,x} & \tilde{a}_{i,z} \tilde{b}_{i,y} & \tilde{a}_{i,z} \tilde{b}_{i,z} \end{bmatrix}\end{aligned}$$

We then computed the singular value decomposition to get  $\mathbf{H} = \mathbf{U}\mathbf{S}\mathbf{V}^t$ , where the rotation matrix  $\mathbf{R} = \mathbf{V}\mathbf{U}^t$ . The translation was calculated using  $T = \bar{b} - \mathbf{R}\bar{a}$ . If the determinant of the rotation matrix is -1, the last column of  $\mathbf{V}$  was multiplied by -1 to make sure that the resulting rotation matrix has a determinant of 1. A determinant of -1 could be caused by having a very small rotation.

For each sample frame  $k$  of the marker bodies, the values  $a_{i,k}$  and  $b_{i,k}$ , the positions of the LED markers with respect to the optical tracker, were registered using Arun's method with  $A_i$  and  $B_i$ , the positions of the LED markers, giving  $F_{A,k}$  and  $F_{B,k}$ . The position of the pointer tip with respect to rigid body B was calculated using  $d_k = F_{B,k}^{-1} F_{A,k} A_{tip}$ .

## 1.2 Closest Point on Triangle

Since we are working with a surface mesh defined by triangles and we need to find the closest point on the surface to another point, we implemented a function that finds the closest point on a triangle to a given point.

If the vertices of a triangle are defined by  $p$ ,  $q$ , and  $r$ , and the given point is  $a$ , the closest point on the triangle to  $a$  can be found by the following steps:

$$\begin{aligned}a - p &= \lambda(q - p) + \mu(r - p) \\ \begin{bmatrix} q - p & r - p \end{bmatrix} \begin{bmatrix} \lambda \\ \mu \end{bmatrix} &= [a - p] \longrightarrow Ax = b \longrightarrow x = (A^T A)^{-1} A^T b\end{aligned}$$

After calculating  $\lambda$  and  $\mu$ ,

if  $\lambda \geq 0, \mu \geq 0, \lambda + \mu \leq 1$  :  $c = p + \lambda(q - p) + \mu(r - p)$

if  $\lambda < 0$  :  $\text{ProjectOnSegment}(c, r, p)$

if  $\mu < 0$  :  $\text{ProjectOnSegment}(c, p, q)$

if  $\lambda + \mu > 1$  :  $\text{ProjectOnSegment}(c, q, r)$

To project on a segment given  $c$ ,  $p$ , and  $q$ :

$$\begin{aligned}\lambda &= \frac{(c - p) \cdot (q - p)}{(q - p) \cdot (q - p)} \\ \lambda^{(seg)} &= \text{Max}(0, \text{Min}(\lambda, 1)) \\ c^* &= p + \lambda^{(seg)} \times (q - p)\end{aligned}$$

## 1.3 Iterative Closest Point

### 1.3.1 Optimized ("Binary") Search

We created a KD Tree\* from Nodes that store point, triangle, index, right child, and left child information, which makes searching for the closest point on the mesh surface much faster compared to a linear search. We used starter code from Geeksforgeeks.com (contributed by Prajwal Kandekar) and modified it as necessary for this assignment. We kept only the insert and search functions but modified search so that it returns the nearest node rather than check the tree for if that specific point already exists in the tree. We used our own Euclidean distance function to calculate distances, and updated this with each recursive search throughout the tree. Each depth level in the KD tree is oriented with respect to a specific dimension, looping from 0 to 2 and back to 0 again. This allows for as close to a binary search as is possible with 3-dimensional information.

The tree is constructed with respect to the information stored at point, which is the centroid of the triangle's vertices. This was calculated as:

$$x_c = \frac{x_1 + x_2 + x_3}{3}$$

Where  $x_c$  is the x-coordinate of the centroid, and  $x_i$  is the x-coordinate of vertex  $i$ . The same calculations were used for the  $y$  and  $z$  coordinates. This was necessary because it seemed the easiest way to reference each individual triangle, since the alternative required Nodes for each individual vertex (3 times as many Nodes!) and storing the information of all triangles it contributes to. The search(...) function traverses these centroid points to find the closest Node to the given query point, and this returned Node's triangle information is used to calculate the correct  $c_k$  value using Euclidean distance.

\* K = number of dimensions = 3

### 1.3.2 Iterative Refinement of Points

We first started with an initial guess of  $F_{reg} = I$  such that  $s_k = F_{reg}d_k$ . We then found the closest point  $c_k$  on the mesh surface to  $s_k$  using the KD tree search algorithm and closest point on triangle. We then updated  $F_{reg}$  by registering the  $c_k$ s to  $d_k$ s. After calculating the distance from  $s_k$ s calculated using the new  $F_{reg}$  to the  $c_k$ s found, we compared the average distance between all the points to a  $d_{max}$  that we defined to determine if the iterative closest point algorithm converged.

## 2 Algorithms

### 2.1 Registration

Take in input vectors  $a$  (size:  $N \times 3$ ) and  $b$  (size:  $N \times 3$ ), where the registration algorithm will find a transform such that  $F^*a = b$ . Transpose vectors. Calculate averages for  $a$  and  $b$  and detract from vectors  $a$  and  $b$ . Implement Arun's method by creating the  $H$  matrix using the calculated vectors. Calculate the registration frame using SVD least squares. The output of the registration function is a Frame object, with a rotation ( $3 \times 3$  matrix) and translation part (Point 3D object). After reading in  $a_{i,k}$  and  $b_{i,k}$ , use a for loop for each  $k$  to find a transformation to  $A_i$  and  $B_i$  detailed in the Mathematical Approach section using Arun's method, and use those to calculate  $d_k$ .

### 2.2 Closest Point on Triangle

Take in an input consisting of a point ( $1 \times 3$ ) and an array of 3 point vectors that stored the vertex locations of a triangle. Transpose the point vectors as necessary to make sure that the matrices are the correct dimensions. Create the 2 known matrices shown in the mathematical approach and use least squares to find the unknowns. Using if-else statements on the calculated values to see if the closest point is on the edge of the triangle, calculate the final center point based on the conditions of the location. The output is  $c$ , the center point which is a  $1 \times 3$  vector.

## 2.3 Iterative Closest Point

### 2.3.1 Optimized ("Binary") Search

Take in the point to find the closest point for, a  $1 \times 3$  array, and a Node object that represents the root of the tree (which is found when creating and inserting nodes into the tree). Iterate over all triangle vertices in the mesh

and calculate their centroids. Create Nodes from these centroids and store their corresponding triangle vertices and triangle indices. Add each Node to the same tree. The output of the search function returns a Node class object, that consists of the triangle index, vertex locations of the triangle, and its centroid.

### 2.3.2 Iterative Refinement of Points

Take in an input of  $d_k$ s ( $N \times 3$ ) and the mesh model triangles loaded into the KD tree. Start with  $F_{reg} = I$ . For each  $d_k$ , calculate  $s_k = F_{reg}d_k$ . Iterate over each  $s_k$  and search the tree for its nearest Node. Use the Node's triangle information to find the closest point on the triangle. Return this  $c_k$  for each point. Update  $F_{reg}$  by registering  $d_k$  and  $c_k$  for all points, and use this  $F_{reg}$  to update  $s_k$ . Calculate the average distance between  $s_k$ s and  $c_k$ s. If the average distance is less than  $d_{max}$  or the number of iterations has exceeded the max number of iterations, then the algorithm has converged. If the algorithm has not converged, repeat the process of finding  $c_k$ s and updating  $F_{reg}$ . The output is the iteratively improved  $F_{reg}$ , a Frame object.

## 3 Overview of Program

Important Files for PA4:

File Directory	
File	Description
FileIO.py	functions to read input and output1 files
GenerateOutput4.py	functions to read the unknown dataset files and generate an output4 txt file
Point3d.py	class to create 3d point objects and perform cartesian math functions
Frame.py	class to do frame transformations, save frame data, and transform points.
Registration.py	an implementation of the Arun's registration method
ClosestPointOnTriangle.py	functions to find the closest location of a triangle to a given point
Mesh.py	class to store the surface mesh, and functions for KD-tree
ICP.py	function to run the ICP algorithm
testing.py	testing functions we used to test and debug our functions

### 3.1 Code Structure

GenerateOutput4.py is the main file that should be run on input data to get output 4 files.

This file includes functions to read the unknown dataset files and generate the desired output files. The output includes our calculated  $s_k$ ,  $c_k$ , and  $\|s_k - c_k\|$  values.

testing.py is a script that takes an input debugging data set and outputs the error of our calculated variables compared to those given in out "-output1.txt" and "-output2.txt" files. It also includes a few component tests that we did in addition to the debugging tests.

testKDTree() checks to make sure that the insert and search functions work correctly given a tree that we designed.

testClosestPointToTriangle() checks to make sure that the correct closest point to a triangle is found given different conditions.

printPA4OutputErrors() prints the average  $s_k$  error,  $c_k$  error, and magnitude error, and the number of iterations it takes to reach convergence.

FileIO.py includes functions to read the body, mesh, samplereadings, and output3 files.

For each type of file, the exact dimensions of the output arrays are specified in the python file, so that users can look at the description and understand how the array is formatted.

Point3d.py and Frame.py include classes to create 3d point objects, do transformations, save frame data, and other Cartesian math functions.

Each Point3d object stores the name of the frame it resides in in addition to its  $x, y, z$  coordinates. The base code for this class was taken off Github (cited in code) though we added several additional features (e.g., frame variable and error() function) as necessary for this scenario. Each Frame object

object stores its 3D rotation matrix  $\mathbf{R}$  and 3D position vector  $\vec{p}$ , as well as its neighboring Frames so that the whole system may be traversed from one Frame object.

Registration.py has an implementation of the Arun's registration, following the algorithm detailed above.

registrationArunMethod() takes in 2 point clouds and finds a transformation  $\mathbf{F}$  such that  $\mathbf{F} \cdot a = b$

Mesh.py creates a mesh object given the points of the vertices, indices of the vertices for each triangles, and each triangles' neighbors, along with functions to easy get the centroid of triangles and the vertices of triangles in array form. This file also contains the implementation of the KD-tree.

insert() inserts new nodes into the KD-tree and search() returns the triangle closest to a point based on Euclidean distance.

ClosestPointOnTriangle.py includes functions that take in a point and a triangle's vertices points, and returns the closest point on the triangle to the given point.

findClosestPointOnTriangle() is the main function that is called.

ICP.py includes a function to run iterative closest point registration between a set of points and a surface, which is defined by a KD tree

ICP() takes in  $d_k$ , the root of the KD tree,  $d_{max}$ , max number of iterations, and the initial transformation prediction, and returns the point-to-surface transformation found using ICP.

## 3.2 Citations and Packages

Packages used:

- NumPy==1.26.0 (important functions include matrix functions and np.linalg.svd)
- Math (used math.comb, comes with python==3.11.0)
- Time (comes with python)

References:

- Point3D: <https://github.com/SplinterFM/Point3d>
- KD Tree: <https://www.geeksforgeeks.org/search-and-insertion-in-k-dimensional-tree/>

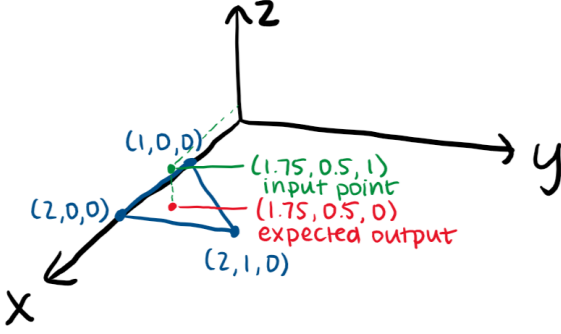
## 4 Verification of Code

### 4.1 Registration

We verified our Arun registration function by testing  $\mathbf{F}_D$  against the first frame's  $D$  coordinates (using debugging file "a") and confirmed that  $\mathbf{F}_D^{-1} \cdot \vec{D}_0 = \vec{d}_0$  on MATLAB.

### 4.2 Closest Point on Triangle

Since there are multiple checks in the function that calculates the closest point on triangle, multiple tests that satisfy the different conditions were written. There are tests where the closest point should lie in the middle of the triangle, on the first edge, on the second edge, and on the third edge. These tests compared against expected results. An example of a test is shown below:



### 4.3 KD Tree

Following the example given on the Geeksforgeeks page, We changed it to include a third dimension since it was given for a 2D tree rather than a 3D one. `testKDTree()` in `testing.py` checks both the insert and search function by looking for the closest node to a given point. Comparison of the two outputs reveals that the correct answer is reached, validating our KD tree implementation. A more detailed analysis and testing of the KD tree as well as its comparison to linear search in terms of accuracy and runtime can be found in our PA3 report.

### 4.4 Iterative Closest Point

After coding the step of each iterations, we tested our algorithm to make sure that the ICP algorithm updates  $F_{reg}$  in each iteration. To verify our ICP algorithm works as expected, we calculated the squared error between  $c_k$  found in the last iteration and the expected  $c_k$ , and  $s_k$  calculated using our final  $F_{reg}$  and the expected  $s_k$  of the debugging datasets. The error of the magnitudes between the two were also found. These results are shown below:

Table 1: Comparison of Errors

Dataset	$s_k$ Error	$c_k$ Error	Magnitude Error
A	0.009555	0.008653	0.006690
B	0.422691	0.393646	0.145841
C	0.240907	0.271679	0.121285
D	0.338191	0.355969	0.129926
E	0.236451	0.214759	0.095905
F	0.852592	0.716775	0.332576

Table 2: Comparison of Number of Iterations

Dataset	A	B	C	D	E	F	
Iterations	1	4	6	10	7	100	$d_{max} = 0.3$
	1	9	11	13	11	100	$d_{max} = 0.15$

Looking at the error between our generated outputs and the expected outputs for the debug datasets shown in Table 1, our ICP algorithm performs well. The error increases as more noise is added to the datasets. In addition, the number of iterations for the first 5 datasets was pretty low, showcasing the efficiency of our algorithm. Dataset F hit the maximum number of iterations limit at 100, which makes sense as our convergence criteria was  $d_{max} = 0.15$ .

We picked  $d_{max}$  by looking at how much the number of iterations would increase if  $d_{max}$  in increased. We used  $d_{max} = 0.15$  because the results from values just a bit higher, such as 0.2 or 0.3 had similar number of iterations (as seen in Table 2), but anything lower than 0.15 would cause multiple datasets to run until they reach the maximum number of iterations. The max number of iterations was picked by looking at how much the accuracy changes at the cutoff. For example, a max number of 100 vs 200 didn't have much of a difference in accuracy, but 100 is much more efficient. To summarize,  $d_{max}$  and maximum number of iterations were picked to balance accuracy and efficiency. However, we made sure that these numbers can be easily changed through the function parameters.

## 5 Results

### 5.1 Discussion

For all datasets A-F, the errors in  $s_k$  and  $c_k$  are greater than the errors associated with  $\|s_k - c_k\|$ , as shown in Table 1. This suggests that the their individual positional errors perhaps mitigate each other's when calculating the magnitude difference. The lowest error is seen in Dataset A, with an average error of 0.009 mm between  $s_k$  and  $c_k$ , implying this is likely a noise-free dataset. This assumption is further validated by dataset A's results in Table 2 as it did not need to iterate to reach convergence. From this, we conclude our code has high accuracy in ideal conditions.

Datasets B-E have similar error magnitudes for  $s_k$  and  $c_k$ , averaging at 0.3 mm across these 4 datasets. Assuming these datasets have similar noise additions to previous programming assignments, these likely have one type of additive noise each, such as varying amounts of Gaussian noise added to one marker (e.g., body A coordinates) or all markers. Our code is shown to be not very robust against these errors as there is a greater than 25x increase in the error magnitudes of  $s_k$ ,  $c_k$ , and  $\|s_k - c_k\|$ . Even so,  $d_{max}$  is achieved as the numbers of iterations in Table 2 never reach the maximum threshold (100).

The opposite is seen in the large errors of dataset F, approximately 0.77 mm between  $s_k$  and  $c_k$ . I assume this dataset to be the noisiest of the six, likely containing multiple types and/or large amounts of noise. Our results for this dataset likely do not meet our  $d_{max}$  requirements, as the maximum number of iterations is reached for both values (shown in Table 2). Even so, our errors do not ever exceed 0.9 mm, meaning we achieved a reliable error of  $< 1$  mm for noisy conditions.

The similarity in errors between  $s_k$  and  $c_k$  (largest difference is 0.14 mm in the very noisy dataset F) makes sense since  $s_k$  is calculated using frame  $\mathbf{F}_{reg}$  that is registered between  $d_k$  and  $c_k$ . Overall, this code would need to be further refined to operate in noisy conditions as errors in the 0.5 – 1 mm magnitude can make a large difference during surgery, especially when operating in areas with lots of important structures near the target region. Potential improvements to our code include switching to a different approach once a threshold number of iterations is reached (e.g., 50). The different approach could be switching to a convergence function that looks at the distance from previous iteration rather than a number (risks a long runtime), or improving the KD tree implementation to look at neighboring triangles if the closest point is in a neighboring triangle. Specific improvements to the KD tree include additional point variables that better represent its size or a bounding sphere implementation, since our code currently only utilizes the centroid of the triangle, which may be misleading if the centroid is far from the current point but the triangle has a large area.

### 5.2 Unknown outputs

#### 5.2.1 Dataset G

200 PA4-G-Unknown-Output.txt	18.78 -8.55 10.38 18.73 -8.46 10.32 0.123
-4.51 -18.59 -39.31 -4.49 -18.59 -39.39 0.082	-4.81 24.51 28.92 -4.81 24.36 28.86 0.160
-6.95 7.05 51.03 -6.95 7.05 51.00 0.026	21.18 3.44 56.35 21.18 3.40 56.31 0.051
12.56 21.68 49.28 12.58 21.69 49.26 0.036	22.24 9.99 51.71 22.19 9.94 51.67 0.082
-11.94 -13.57 -47.16 -11.99 -13.53 -47.12 0.080	28.08 -3.46 16.89 27.99 -3.42 16.83 0.115
7.37 25.11 10.36 7.35 25.25 10.34 0.138	35.55 -1.89 -18.99 35.43 -1.91 -18.99 0.116
-5.02 20.38 13.28 -4.93 20.28 13.36 0.156	16.73 -4.70 45.30 16.73 -4.74 45.27 0.053
-41.48 -15.70 -30.79 -41.21 -15.73 -30.59 0.343	11.81 -6.29 42.05 11.80 -6.33 42.02 0.046
-19.04 -31.80 -21.57 -19.06 -32.03 -21.58 0.230	-29.38 -26.51 -39.81 -29.44 -26.48 -39.86 0.084
17.29 -10.42 -20.77 17.35 -10.19 -20.52 0.352	-10.05 7.59 4.00 -9.99 7.53 3.99 0.090
30.39 7.25 -28.66 30.37 7.39 -28.44 0.268	19.67 -8.97 7.97 19.62 -8.87 7.90 0.135
-6.59 -6.32 -43.47 -6.52 -6.40 -43.42 0.116	-13.41 -5.15 5.50 -13.49 -5.17 5.51 0.080
37.57 10.31 -8.92 37.65 10.30 -8.96 0.090	-2.20 15.79 57.77 -2.17 15.74 57.76 0.056
18.53 -1.28 58.89 18.56 -1.34 58.86 0.074	-13.55 10.93 23.14 -13.72 10.80 23.09 0.217
-6.94 7.28 58.83 -6.99 7.28 58.80 0.053	21.68 25.34 2.88 21.77 25.49 2.87 0.174
0.40 -14.79 -3.47 0.38 -14.84 -3.48 0.060	2.85 -18.06 -12.43 2.87 -18.16 -12.42 0.096
38.30 5.00 -11.95 38.37 4.99 -12.03 0.109	-33.75 -28.00 -21.54 -33.85 -28.02 -21.55 0.103
-9.26 7.22 28.57 -9.45 7.15 28.61 0.207	19.12 -15.07 -17.07 19.13 -14.82 -16.83 0.345
5.45 23.09 26.72 5.47 23.10 26.70 0.035	-31.09 -11.49 -47.06 -31.05 -11.41 -46.89 0.185

-4.19	-13.60	-0.67	-4.23	-13.67	-0.67	0.085	-23.11	2.93	-44.43	-23.13	2.83	-44.25	0.206
21.11	1.89	53.38	21.11	1.85	53.35	0.054	1.39	-6.12	-26.92	1.40	-6.11	-26.98	0.063
0.21	-17.07	-28.76	0.37	-17.10	-28.87	0.191	-15.75	-11.06	-2.12	-15.87	-11.23	-2.22	0.234
-13.85	-29.47	-35.61	-13.87	-29.54	-35.70	0.120	9.61	22.77	-6.67	9.53	22.84	-6.76	0.138
-26.72	-29.66	-16.33	-26.90	-29.76	-16.27	0.208	-8.07	-23.02	-39.85	-8.03	-23.09	-39.97	0.141
0.39	-1.88	-26.00	0.38	-1.87	-26.04	0.041	-6.63	8.67	47.42	-6.69	8.68	47.40	0.069
22.38	-6.46	15.03	22.32	-6.30	14.96	0.179	-35.16	6.99	-29.53	-34.99	6.81	-29.50	0.251
10.06	20.82	56.22	10.09	20.72	56.20	0.106	11.74	-6.47	-22.09	11.73	-6.44	-21.88	0.212
26.83	10.47	26.40	26.87	10.44	26.37	0.059	14.88	25.57	-8.27	14.84	25.77	-8.34	0.224
-29.64	-29.63	-34.21	-29.71	-29.60	-34.25	0.083	-35.54	-19.16	-41.61	-35.50	-19.03	-41.55	0.142
-15.57	20.14	23.66	-15.61	20.22	23.63	0.096	35.45	15.27	2.41	35.56	15.29	2.37	0.115
-0.27	-12.68	-33.32	-0.12	-12.58	-33.42	0.206	-24.32	12.18	-26.39	-24.29	12.04	-26.43	0.154
-23.06	9.44	-18.14	-23.06	9.50	-18.12	0.064	14.88	18.37	-31.24	14.96	18.41	-31.00	0.258
1.30	8.52	-15.17	1.30	8.50	-15.19	0.024	-6.45	11.63	44.72	-6.54	11.64	44.71	0.101
-11.59	-4.13	9.79	-11.68	-4.16	9.81	0.098	8.29	20.50	55.90	8.32	20.47	55.88	0.047
6.51	-8.40	19.59	6.51	-8.49	19.58	0.086	9.60	-14.49	-17.21	9.53	-14.32	-17.16	0.194
-3.63	9.05	-11.12	-3.63	9.04	-11.14	0.028	-38.68	2.97	-31.83	-38.45	2.79	-31.74	0.303
-41.63	-7.24	-16.47	-41.49	-7.21	-16.57	0.177	-28.41	-1.56	-11.22	-28.58	-1.27	-11.41	0.383
-42.39	-17.37	-24.01	-42.50	-16.91	-24.26	0.532	28.42	-7.81	-24.31	28.31	-7.66	-24.04	0.331
33.05	17.21	-4.70	33.20	17.28	-4.72	0.169	-9.42	7.14	28.02	-9.61	7.07	28.06	0.205
18.65	16.13	55.92	18.57	16.02	55.89	0.143	27.32	22.85	-5.95	27.35	23.02	-6.05	0.201
-19.37	-4.07	-48.05	-19.45	-4.09	-47.95	0.130	18.40	0.64	62.19	18.48	0.53	62.26	0.152
16.39	-6.70	21.66	16.36	-6.61	21.61	0.103	21.40	-13.80	-19.84	21.56	-13.45	-19.93	0.400
18.09	-6.08	24.99	18.05	-6.03	24.94	0.075	-37.04	-2.30	-41.12	-36.83	-2.35	-40.96	0.263
9.52	26.04	3.97	9.51	26.22	3.95	0.175	34.47	-2.85	-20.76	34.29	-2.83	-20.72	0.189
-39.30	-17.77	-37.46	-39.12	-17.65	-37.44	0.218	-28.42	-3.20	-10.14	-28.44	-3.17	-10.19	0.058
-36.44	-26.48	-26.67	-36.51	-26.44	-26.70	0.086	15.48	8.60	62.94	15.48	8.57	63.17	0.228
-21.56	-17.97	-47.75	-21.59	-17.90	-47.66	0.117	28.20	21.67	6.77	28.31	21.86	6.76	0.220
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16.53	24.72	-15.62	16.37	25.02	-15.68	0.347	-41.01	0.70	-24.22	-40.81	0.64	-24.28	0.214
-6.23	-1.31	36.37	-6.26	-1.31	36.35	0.037	32.38	-5.22	10.59	32.27	-5.06	10.48	0.228
-8.36	8.26	-23.51	-8.40	8.20	-23.52	0.071	-19.21	-31.62	-19.89	-19.23	-31.86	-19.90	0.234
29.70	16.12	13.73	29.85	16.19	13.80	0.185	-6.76	-25.15	-35.25	-6.66	-25.29	-35.35	0.193
0.60	-19.13	-19.35	0.70	-19.25	-19.35	0.160	3.53	-12.19	7.78	3.51	-12.16	7.75	0.053
7.48	16.00	62.95	7.50	15.98	63.20	0.256	16.56	17.99	57.57	16.54	17.89	57.53	0.107
20.73	0.32	-25.65	20.93	0.38	-25.51	0.248	-5.39	11.97	58.89	-5.35	11.95	58.87	0.044
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### 5.2.2 Dataset H

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33.05	-6.42	-0.80	32.86	-6.36	-0.74	0.217	-34.83	1.84	-13.25	-34.70	1.84	-13.36	0.169
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12.76	15.70	-23.14	12.68	15.60	-23.09	0.138	37.27	12.67	4.37	37.31	12.76	4.37	0.104
-4.56	13.78	7.16	-4.63	13.86	7.14	0.102	-15.93	-31.75	-24.39	-15.92	-31.97	-24.36	0.223
-8.05	-26.69	-34.55	-7.89	-26.87	-34.62	0.243	-8.80	8.23	-14.20	-8.77	8.15	-14.18	0.083
10.41	24.23	-5.30	10.23	24.45	-5.42	0.307	4.27	23.67	22.77	4.32	23.67	22.80	0.066
7.46	10.76	-11.30	7.47	10.89	-11.37	0.144	-28.51	1.32	-12.63	-28.47	1.31	-12.77	0.146
14.59	-5.79	38.99	14.54	-5.73	39.03	0.088	-11.00	-28.79	-34.09	-10.94	-28.98	-34.18	0.220
-22.19	11.45	-32.88	-22.12	11.34	-32.80	0.150	-4.50	-11.90	3.70	-4.52	-11.91	3.72	0.035
21.57	10.15	57.52	21.46	10.06	57.62	0.176	-42.41	-12.86	-18.68	-42.40	-12.77	-18.67	0.096
27.14	10.35	25.80	27.09	10.25	25.81	0.110	36.16	13.33	7.26	36.30	13.34	7.34	0.165
9.50	6.25	-15.80	9.54	6.29	-15.89	0.109	-16.29	16.77	23.02	-16.41	16.87	23.03	0.159

22.17 -2.24 34.69 22.02 -2.17 34.67 0.165  
 -34.40 3.81 -15.09 -34.27 3.78 -15.26 0.220  
 36.91 5.69 -15.46 36.88 5.61 -15.42 0.096  
 -4.13 2.67 -27.75 -4.12 2.67 -27.72 0.034  
 -15.64 8.93 -37.84 -15.63 8.88 -37.74 0.108  
 -0.11 -10.73 -30.20 0.01 -10.71 -30.20 0.118  
 -12.01 -18.06 -7.17 -12.04 -18.06 -7.13 0.053  
 -39.89 -15.60 -14.59 -39.81 -15.51 -14.65 0.136  
 22.45 3.46 48.15 22.35 3.41 48.17 0.116  
 18.97 -6.64 18.98 18.91 -6.45 18.98 0.201  
 -2.45 23.78 18.54 -2.39 23.74 18.58 0.079  
 21.16 13.18 52.15 21.08 13.07 52.16 0.138  
 -34.36 5.35 -35.59 -34.21 5.27 -35.49 0.192  
 15.09 23.11 23.25 15.17 23.21 23.30 0.130  
 -37.93 -10.03 -10.60 -37.88 -9.94 -10.63 0.100  
 -7.26 5.73 -29.49 -7.30 5.66 -29.45 0.088  
 -6.84 16.96 41.00 -6.95 16.98 41.09 0.151  
 -26.66 -25.79 -10.77 -26.71 -25.84 -10.63 0.154

-23.01 -32.48 -24.89 -23.05 -32.74 -24.87 0.267  
 -2.81 15.23 6.30 -2.89 15.33 6.27 0.135  
 3.93 -7.01 50.09 3.91 -7.02 50.12 0.034  
 25.68 8.43 32.58 25.58 8.35 32.58 0.135  
 -30.23 3.92 -40.81 -30.17 3.91 -40.68 0.145  
 16.94 -3.47 56.74 16.87 -3.47 56.77 0.078  
 38.05 -0.66 -12.73 37.82 -0.61 -12.62 0.268  
 -0.12 -15.67 -4.92 -0.15 -15.64 -4.92 0.045  
 21.67 -11.10 -21.59 21.66 -11.14 -21.53 0.075  
 -6.18 -23.38 -15.16 -6.15 -23.48 -15.09 0.122  
 0.50 -8.44 -28.49 0.59 -8.42 -28.54 0.112  
 -35.94 5.37 -20.61 -35.74 5.26 -20.67 0.232  
 -20.79 5.71 -41.63 -20.77 5.66 -41.52 0.120  
 6.64 -12.66 5.56 6.63 -12.54 5.55 0.118  
 13.42 11.53 -13.63 13.22 11.57 -13.71 0.227  
 9.93 3.04 -18.54 9.91 3.15 -18.65 0.160  
 8.18 16.16 63.23 8.21 16.12 63.21 0.059

### 5.2.3 Dataset J

200 PA4-J-Unknown-Output.txt  
 13.53 22.55 32.00 13.53 22.55 32.00 0.001  
 8.32 12.50 -9.80 8.32 12.51 -9.82 0.017  
 -11.08 6.39 -37.38 -11.08 6.39 -37.38 0.007  
 -21.48 11.24 -35.30 -21.42 10.80 -35.13 0.474  
 -5.45 -19.87 -11.16 -5.27 -20.27 -10.89 0.515  
 -2.79 3.33 -24.74 -2.65 3.46 -24.84 0.220  
 33.36 15.93 -10.21 34.10 16.66 -10.39 1.059  
 -23.86 -13.14 -5.60 -23.81 -13.05 -5.76 0.193  
 0.52 -4.21 50.88 -0.28 -6.11 50.90 2.063  
 -16.71 2.58 -2.55 -16.38 2.18 -2.57 0.518  
 16.73 -3.86 51.21 16.90 -4.05 51.23 0.260  
 22.57 -15.59 -4.11 22.14 -14.56 -4.88 1.353  
 -30.33 -26.43 -13.32 -30.16 -26.24 -13.46 0.288  
 -16.18 -16.75 -46.93 -16.15 -16.86 -47.35 0.431  
 26.88 14.97 23.42 26.25 14.63 23.19 0.750  
 -17.31 -1.55 -47.05 -17.32 -1.51 -47.15 0.103  
 -42.74 -14.02 -18.16 -42.05 -13.86 -18.37 0.741  
 20.63 22.07 16.67 20.96 22.71 16.79 0.730  
 7.27 24.64 14.65 7.31 24.82 14.55 0.213  
 34.59 4.16 -22.78 34.17 4.15 -22.54 0.481  
 -41.64 -19.41 -29.63 -41.17 -19.26 -29.34 0.576  
 19.77 3.46 -27.44 20.56 3.86 -27.04 0.974  
 16.59 22.10 31.35 16.61 22.19 31.35 0.095  
 32.65 14.42 10.18 33.16 14.81 10.47 0.700  
 -10.21 8.07 3.37 -9.80 7.61 3.44 0.627  
 -6.63 -25.07 -19.11 -6.25 -25.59 -18.84 0.701  
 40.14 5.25 -0.60 40.09 5.25 -0.60 0.050  
 3.15 20.86 50.09 3.51 19.41 49.96 1.499  
 -30.51 8.93 -17.00 -30.32 7.98 -17.47 1.076  
 -23.56 11.32 -34.05 -23.41 10.69 -33.84 0.684  
 -25.28 -16.35 -5.65 -25.03 -16.32 -6.32 0.717  
 20.69 -9.62 8.23 20.43 -8.64 7.97 1.055  
 -7.90 -17.63 -6.57 -7.89 -17.56 -6.63 0.095  
 14.63 16.09 62.09 14.92 16.42 62.89 0.907

11.70 25.34 7.08 11.47 26.54 7.20 1.223  
 -33.02 3.38 -40.81 -32.59 2.72 -40.29 0.939  
 8.51 -12.00 -21.66 8.25 -11.81 -21.40 0.413  
 11.53 -9.18 14.95 11.39 -8.69 14.77 0.537  
 -7.22 17.65 37.63 -8.19 18.55 38.81 1.777  
 10.43 -12.17 7.68 10.31 -11.76 7.52 0.465  
 1.45 -5.75 -25.93 1.79 -5.58 -26.37 0.582  
 15.10 -0.44 62.76 15.10 -0.44 62.98 0.222  
 -0.68 -10.46 -29.03 0.24 -10.25 -29.67 1.134  
 23.13 5.09 52.04 22.20 5.25 51.90 0.958  
 -0.87 -2.89 -26.94 -0.54 -2.78 -27.33 0.522  
 -32.01 -29.02 -30.52 -32.16 -29.24 -30.55 0.275  
 -23.25 -18.55 -46.69 -23.24 -18.80 -47.34 0.691  
 1.61 19.67 52.31 1.90 18.67 52.14 1.060  
 40.52 1.30 -1.28 39.47 2.07 -1.44 1.315  
 -7.50 10.12 3.98 -7.47 10.09 3.99 0.044  
 -17.05 0.72 -45.84 -17.06 0.78 -45.92 0.106  
 3.27 20.99 47.01 3.54 19.73 46.84 1.299  
 -25.38 10.48 -35.42 -25.07 9.75 -35.14 0.836  
 1.80 -4.78 54.25 1.07 -6.81 54.10 2.167  
 -14.66 19.35 21.66 -15.11 19.59 21.45 0.552  
 -9.15 -0.90 20.14 -9.35 -0.93 20.18 0.199  
 -7.62 -25.10 -33.51 -6.84 -25.94 -34.17 1.320  
 -4.72 -4.17 30.30 -5.81 -4.72 30.84 1.336  
 18.73 20.04 -28.63 18.89 20.22 -28.88 0.346  
 -39.90 0.29 -35.52 -39.25 -0.15 -35.23 0.841  
 11.06 -18.51 -7.30 11.75 -16.83 -7.17 1.815  
 -21.77 8.72 -38.58 -21.75 8.38 -38.38 0.396  
 15.10 -5.22 42.30 15.22 -5.57 42.32 0.370  
 9.43 -14.89 2.94 9.44 -13.98 2.59 0.975  
 -6.19 7.01 50.05 -6.93 7.15 50.05 0.751  
 -27.88 -19.98 -6.67 -27.85 -19.97 -7.17 0.498  
 -27.83 -8.99 -6.25 -27.89 -9.33 -7.18 0.989  
 -8.50 25.47 19.80 -8.45 24.04 20.32 1.524  
 -3.76 -3.18 36.58 -4.79 -4.13 36.59 1.399

25.62	16.86	23.43	25.16	16.60	23.31	0.544	-7.73	-21.48	-38.92	-6.92	-22.11	-39.60	1.233
7.77	-14.51	-18.97	7.64	-14.22	-18.79	0.358	21.52	1.00	50.33	21.35	1.36	50.62	0.494
36.16	-5.86	-16.37	34.98	-5.05	-16.12	1.454	5.14	22.56	35.18	5.10	21.49	35.25	1.074
19.75	-1.94	-24.91	20.26	-1.84	-23.96	1.082	5.94	6.82	62.84	5.99	6.80	63.22	0.388
-43.32	-11.42	-27.73	-43.04	-11.29	-27.55	0.351	1.06	25.01	27.17	0.94	23.61	27.03	1.406
34.91	10.94	-17.48	35.07	11.01	-17.54	0.183	-31.18	-19.17	-7.46	-30.86	-19.03	-8.09	0.716
27.40	-15.06	-14.66	26.28	-13.50	-14.81	1.932	32.86	16.67	-13.40	33.31	17.03	-13.60	0.613
16.10	-17.75	-15.52	16.60	-15.80	-14.56	2.233	-26.96	-3.37	-8.30	-26.49	-3.96	-9.17	1.147
38.44	1.15	7.96	38.32	1.19	7.91	0.138	-3.31	-8.85	-37.37	-2.05	-8.43	-37.64	1.356
-27.05	7.74	-39.12	-26.80	7.11	-38.66	0.826	14.34	12.44	-23.44	14.45	12.55	-23.47	0.165
28.60	7.88	23.87	28.16	7.82	23.73	0.469	11.26	18.13	-10.94	10.78	17.92	-11.24	0.604
-40.29	-16.89	-37.49	-39.40	-16.66	-37.31	0.933	19.29	20.78	39.07	18.28	20.34	39.11	1.103
-15.07	11.37	-22.44	-15.12	11.14	-22.49	0.239	31.85	-9.68	1.05	30.82	-8.25	0.82	1.781
29.95	-6.68	-26.41	30.00	-5.64	-25.41	1.440	13.34	-18.57	-11.28	13.88	-16.73	-10.57	2.048
-28.43	-25.29	-10.97	-28.40	-25.27	-11.01	0.049	6.69	-5.74	42.27	6.78	-6.80	42.26	1.064
-5.91	-23.47	-17.21	-5.55	-24.02	-16.93	0.714	-42.35	-5.63	-15.86	-41.33	-5.63	-16.64	1.280
-0.84	-3.12	56.43	-2.72	-4.94	56.45	2.621	-42.55	-13.66	-30.13	-41.45	-14.07	-29.48	1.340
29.51	-8.54	-26.25	28.96	-7.26	-24.11	2.558	-8.01	6.02	-31.30	-8.02	6.01	-31.30	0.009
16.66	20.09	-28.92	16.96	20.55	-29.60	0.864	-5.46	1.72	42.06	-6.48	1.56	42.06	1.034
-33.58	-16.04	-7.86	-33.51	-15.99	-8.18	0.327	24.32	-16.21	-9.64	23.41	-15.14	-9.82	1.420
35.69	-5.55	8.21	34.64	-4.46	7.87	1.543	-3.53	14.75	52.80	-3.64	14.85	52.80	0.153
16.38	-18.85	-12.60	16.73	-16.90	-12.02	2.070	-2.71	-9.30	-35.83	-1.55	-9.38	-36.05	1.192
-34.00	-27.79	-31.58	-34.05	-27.86	-31.58	0.095	3.83	-7.85	22.78	3.94	-8.52	22.87	0.689
17.11	21.99	33.47	17.04	21.83	33.45	0.180	12.86	24.18	17.88	12.87	24.41	17.92	0.240
-4.09	18.13	10.88	-4.11	18.16	10.86	0.037	9.85	24.89	3.10	9.37	26.23	3.36	1.445
5.75	6.01	-16.76	5.79	6.13	-16.88	0.177	9.02	-5.32	62.65	9.04	-5.32	63.41	0.764
35.29	13.23	-4.99	36.13	13.84	-5.02	1.039	34.53	10.92	-18.93	34.67	10.97	-18.97	0.150
5.94	-7.61	22.37	6.07	-8.12	22.44	0.523	22.98	22.07	13.85	23.20	22.47	14.00	0.476
-30.79	-19.58	-7.37	-30.48	-19.44	-7.98	0.705	-33.87	-27.30	-19.58	-33.92	-27.36	-19.56	0.087
11.18	23.99	16.71	11.21	24.63	16.79	0.641	-41.77	1.61	-28.64	-40.63	0.82	-28.60	1.383
-23.61	8.89	-16.55	-23.73	8.45	-17.29	0.872	-21.03	-27.06	-40.09	-21.16	-27.70	-40.62	0.836
24.32	3.36	-31.04	24.43	3.70	-29.91	1.185	-1.74	-9.75	-31.10	-0.90	-9.29	-31.55	1.058
-40.00	-18.38	-36.21	-39.30	-18.19	-35.99	0.754	30.25	6.96	19.82	29.91	6.92	19.64	0.388
2.60	24.90	21.67	2.58	23.93	21.42	1.008	-30.39	-21.42	-43.79	-30.53	-21.56	-43.98	0.273
26.28	-11.10	3.95	26.21	-9.20	3.29	2.015	10.80	19.47	-9.65	9.68	19.72	-10.17	1.258
-34.97	3.63	-13.28	-34.38	2.60	-13.99	1.382	-10.95	-24.86	-14.20	-10.68	-25.46	-13.81	0.760
-4.37	26.92	26.71	-4.81	24.75	26.71	2.217	12.11	7.29	62.29	12.10	7.25	62.95	0.658
29.91	5.33	20.91	29.50	5.37	20.75	0.439	-1.03	-7.78	23.65	-1.04	-8.92	23.88	1.158
18.44	21.00	40.73	17.75	20.35	40.48	0.976	38.40	-0.88	7.84	37.74	-0.61	7.58	0.758
-12.91	19.08	31.76	-14.43	19.63	32.29	1.705	-8.89	-25.05	-16.37	-8.46	-25.55	-15.91	0.804
1.54	-16.70	-23.21	2.17	-17.12	-23.54	0.830	-38.74	-17.86	-13.17	-38.20	-17.60	-13.53	0.693
-4.58	0.85	56.29	-6.07	0.33	56.29	1.576	-34.49	-14.85	-8.19	-34.48	-14.85	-8.21	0.017
-4.01	-19.31	-35.94	-3.05	-19.96	-36.55	1.310	9.01	-9.04	15.78	8.99	-9.00	15.76	0.047
27.02	-13.61	-3.26	26.32	-12.07	-3.95	1.820	-12.76	6.36	-7.87	-12.53	5.91	-7.94	0.515
20.04	22.73	-19.96	21.08	24.90	-19.92	2.412	-15.74	-29.69	-33.85	-15.44	-30.69	-34.37	1.157
13.84	-14.60	-18.04	14.12	-13.45	-17.09	1.524	-14.28	18.10	28.96	-15.85	18.51	29.39	1.679
-0.28	25.15	28.25	-0.52	23.81	27.95	1.391	-32.79	3.91	-40.24	-32.39	3.28	-39.75	0.894
31.85	-9.42	-22.85	30.62	-8.02	-21.82	2.133	-4.12	14.06	57.86	-4.01	13.97	57.85	0.143
-2.45	-20.00	-32.90	-1.67	-20.72	-33.21	1.105	4.74	-5.10	49.23	4.51	-7.11	49.27	2.028
21.62	3.45	55.26	21.35	3.50	55.23	0.275	-4.57	12.28	3.91	-4.62	12.33	3.92	0.075
-11.43	9.58	-28.64	-11.56	9.10	-28.64	0.495	-26.72	-28.55	-36.70	-26.94	-29.26	-37.01	0.800
-12.70	7.78	-37.54	-13.00	7.94	-37.31	0.408	-26.55	-18.77	-6.10	-26.42	-18.81	-7.03	0.939
23.13	22.49	-19.00	24.08	24.00	-19.42	1.835	29.92	-4.21	-27.90	30.08	-4.28	-26.16	1.744
-1.90	3.53	-23.93	-1.73	3.50	-24.33	0.440	6.98	21.03	56.02	7.29	20.12	56.00	0.963
12.16	9.18	62.23	12.15	9.12	63.07	0.836	-17.15	-18.16	-6.62	-17.23	-18.34	-6.22	0.446
-2.98	18.00	9.80	-3.08	18.08	9.71	0.159	-11.08	7.29	-1.36	-10.77	6.73	-1.32	0.644

-5.86 -15.51 -40.44 -4.84 -15.67 -41.26 1.316  
 33.75 8.72 -23.04 33.65 8.72 -23.00 0.104  
 -2.98 -21.15 -31.12 -1.77 -21.81 -31.34 1.397  
 15.82 -18.55 -12.67 16.29 -16.78 -12.15 1.902  
 25.80 -11.14 3.40 25.74 -9.39 2.79 1.857  
 -31.26 -2.78 -45.25 -31.11 -2.90 -44.98 0.333  
 15.52 1.32 62.51 15.54 1.32 62.97 0.467  
 -12.37 5.48 7.07 -12.14 5.32 7.06 0.275  
 -39.12 5.02 -27.39 -38.18 4.24 -27.22 1.239  
 -34.70 -26.86 -20.24 -34.74 -26.92 -20.22 0.080

28.55 -12.39 -2.36 27.58 -11.05 -2.62 1.676  
 26.55 -14.60 -10.11 25.65 -13.44 -10.34 1.479  
 25.93 8.04 35.10 25.03 7.99 34.93 0.909  
 31.55 -1.17 15.79 31.30 -1.09 15.59 0.324  
 -4.53 1.14 60.37 -5.74 0.73 60.65 1.310  
 -1.68 0.17 -26.38 -1.59 0.21 -26.44 0.115  
 30.01 17.20 -21.75 30.15 17.30 -21.86 0.206  
 -4.96 12.86 46.13 -6.04 13.20 46.46 1.177  
 -14.98 -28.16 -16.55 -14.72 -28.75 -16.20 0.734

#### 5.2.4 Dataset K

200 PA4-K-Unknown-Output.txt  
 16.21 21.42 38.20 16.24 21.50 38.19 0.082  
 -32.35 7.13 -18.35 -32.36 7.09 -18.34 0.045  
 -22.93 2.52 -44.26 -22.96 2.62 -44.39 0.172  
 20.25 15.73 48.85 20.02 15.55 48.82 0.288  
 -2.55 -6.58 -35.05 -2.49 -6.54 -35.04 0.075  
 -37.35 -0.50 -38.96 -37.38 -0.52 -38.94 0.038  
 -19.75 -31.82 -34.21 -19.76 -31.73 -34.18 0.090  
 -35.17 1.22 -13.17 -35.07 1.12 -13.27 0.171  
 29.94 -7.53 5.26 30.02 -7.95 5.29 0.425  
 37.41 11.81 -6.52 37.32 11.82 -6.53 0.095  
 11.57 20.48 58.72 11.60 20.50 58.72 0.039  
 21.96 -15.54 -14.51 22.01 -15.69 -14.55 0.166  
 23.73 23.12 -22.27 23.71 23.20 -22.31 0.092  
 -6.05 -13.48 -42.92 -5.99 -13.49 -43.02 0.113  
 27.18 19.18 14.07 27.21 19.24 14.09 0.061  
 0.83 -18.53 -11.35 0.85 -18.55 -11.36 0.032  
 3.81 -7.52 60.88 3.82 -7.40 60.91 0.129  
 4.99 20.28 43.22 4.89 20.40 43.24 0.166  
 0.83 -18.53 -24.39 0.95 -18.56 -24.43 0.123  
 -9.64 7.29 -5.98 -9.66 7.37 -6.01 0.083  
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1.92	-7.02	53.71	1.97	-6.99	53.71	0.060	-24.28	0.20	-11.18	-24.34	0.12	-11.24	0.121
16.54	-10.54	-20.19	16.62	-10.41	-20.08	0.190	-19.73	0.13	-6.14	-19.62	0.04	-6.21	0.153
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38.34	11.05	-3.84	38.23	11.04	-3.85	0.111	-14.79	14.56	31.75	-14.77	14.53	31.76	0.039
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18.41	21.83	29.50	18.37	21.76	29.49	0.078	-14.22	13.52	32.13	-14.14	13.25	31.99	0.314
-0.17	-6.53	38.75	-0.14	-6.55	38.74	0.044	-8.33	13.56	11.56	-8.34	13.54	11.57	0.019
13.53	22.75	-27.80	13.71	22.54	-27.90	0.293	-39.42	-22.07	-21.36	-39.47	-22.14	-21.34	0.091
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## 6 Partner Work

Both Kiana and Keerthana worked on all the python files as well as the report.