

From “to_do_list.tex”:

1 From to-do list

Take out renegotiation

- Add more basic tradeoff
- (??) Draw inverted U for lobby
- Now my short punishments don’t rest on renegotiation
 - So now, for main analysis, must assume that we’re constraining attention to a certain class of punishments: symmetric, and “Punish for T periods then go back to cooperation”
 - * Go back to start if deviate should work for governments, but I think I need something else for lobbies since they would like that
 - Can I show that mine are optimal in this class?

2 Equilibrium overview

January 17, 2015

- Must show players are best responding in every subgame, on and off the eqm path
- I’m going to try to use reversion to the static nash, but this is not necessarily subgame perfect (deviations can trigger changes in future periods)
 - Basic intuition: lobby wants punishment to go longer, leg wants it to go shorter
 - Ideally, want each to choose static BR in each period of punishment: in non-cooperative state, you can pick whatever you want, but the other guy is doing whatever he wants; τ^{tw} is independent of what he does
 - * BUT it’s not independent of lobby’s effort

Equilibrium: Executives set trade agreement tariffs τ^A at $\tau^A = 0$. At $t \geq 1$, lobbies choose e , leg chooses applied τ

- $\forall t \geq 1$, leg applies τ^A if
 1. $\tau \leq \tau^A$ was applied last period
 2. There have been T periods of punishment: I think $\tau \geq \tau^N$ and $e \leq e^N$
- Not sure how to specify lobby in these cooperation periods: $e = 0$ if $\tau \geq \tau^A$ (in any period? how are they involved in punishment? they're not really)
- if $\tau > \tau^A$ within the last T periods, leg applies $\tau^N(e^N)$

January 19, 2015

- Think of punishment scheme being designed either by execs or by supranational body like WTO
- Then want to know whether it's an eqm for leg and lobbies to follow the rules

3 Classes of subgames

1. $\tau \leq \tau^A$ and $e < \bar{e}$ last period; if there had ever been a violation, it ended at least T periods previous.
 - Play $\tau = \tau^A$ and $e = e_a$
2. Conditions in (1) held in period $t - 2$, but there was a violation in period $t - 1$
 - Play static Nash this period and for $T - 1$ more periods before switching back to (1); more precisely, $\tau^D \geq \tau^N$ and $e^D \geq e^N$.
3. Static Nash punishment was initiated $i < T$ periods ago, and punishment has been followed since then, i.e. $\tau^D \geq \tau^N$ and $e^D \geq e^N \forall t \in$ (need to figure out indexing so I can say this precisely)
 - Punish this period and $T - i - 1$ more periods before switching back to (1)
4. In any punishment period (i.e. classes 2 and 3 above), legislature does not follow punishment: i.e. $\tau^D < \tau^N$

- Restart punishment at (2); lobby happy to do this
5. In any punishment period, lobby does not follow punishment: $e^D < e^N$
- Legislature chooses BR (make this precise: $\tau^D(e^D) = \dots$) to e^D , then restart at (1); if anything else, restart punishment from (2). BR + eqm, so okay
 - Lobby *must* pay in final period of punishment, or else IC for leg will not hold. That is why the equilibrium is being re-worked.
 - But, if leg is going to BR to lobby's payment and then restart cooperation, lobby should want to continue with punishment. This seems like a realistic set-up (your protection ends if you don't hold up your end of the deal with the promised payments).

4 Conditions for equilibrium

- Checking that punishment (2) is incentive compatible given (4) and (5)

– Legislature:

$$W(\gamma(e^N), \tau^N) + \frac{\delta - \delta^{T+1}}{1 - \delta} W(\gamma(e^N), \tau^N) + \delta^{T+1} W(\gamma(e^N), \tau^N) \geq W(\gamma(e^N), \cdot) + \frac{\delta - \delta^{T+1}}{1 - \delta} W(\gamma(e^N), \tau^N)$$

by definition, anything provides lower one-shot payoffs than τ^N , and Nash payoffs are lower than trade agreement payoffs (need to prove this—or is it just by assumption?)

- * Is this punishment IC for leg? Yes, condition is satisfied. Best responding in current period—would do the same in best deviation; future is trade agreement instead of restart of punishment for any other tariff.
 - * This conditions is always satisfied; the above equation is for the first period of the punishment. In later periods, there are more periods of the punishment that get repeated, so the constraint becomes looser
- Lobby [(2) is incentive compatible given (4) and (5)]:

$$\pi(\tau^N) - e^N + \frac{\delta - \delta^{T+1}}{1 - \delta} [\pi(\tau^N) - e^N] + \delta^{T+1} [\pi(\tau^a) - e_a] \geq \pi(\tau^D) - e^D + \frac{\delta - \delta^{T+1}}{1 - \delta} [\pi(\tau^a) - e_a]$$

best deviation, given that leg will one-shot best respond is also e^N ; given $\pi(\tau^N) - e^N \geq \tau^a - e_a$, which is necessary for any of this to be interesting, this condition holds.

Since the best deviation is to the Nash tariff, it reduces to

$$\frac{\delta - \delta^{T+1}}{1 - \delta} [\pi(\tau^N) - e^N] \geq \frac{\delta - \delta^{T+1}}{1 - \delta} [\pi(\tau^a) - e_a]$$

$$\frac{\delta - \delta^{T+1}}{1 - \delta} [\pi(\tau^N) - e^N - \pi(\tau^a) + e_a] \geq 0 \quad (1)$$

This is always true.

Note that Expression 1 will hold for all T (or, alternatively, i).

- * In last period of punishment, will hold with equality. Is tightest at the end of the punishment, looser at beginning. Holds for all T , i.e. always holds.
- * Note that if a deviation were to occur (off eqm path), leg would apply a “punishment” tariff that is too low, which would normally cause the punishment to reset; but here, it’s because the lobby deviated, so we re-start cooperation to punish the lobby further after giving the reduced tariff in the period in which the lobby deviates
- Legislature’s constraint holds $\forall T$ (but is tighter for large T)
- Lobby’s constraint also holds $\forall T$ (but is tighter for small T)
 - * $\frac{\delta - \delta^{T+1}}{1 - \delta}$ is increasing in T , which means it gets smaller as you move toward the end of the punishment (there are fewer periods of punishment payoffs left)

4.1 Conditions for punishment

- Legislature’s condition (for class 4 above):

$$\frac{1 - \delta^T}{1 - \delta} W(\gamma(e^N), \tau^N) + \delta^T W(\gamma(e_a), \tau^a) \geq W(\gamma(e^N), \cdot) + \frac{\delta - \delta^{T+1}}{1 - \delta} W(\gamma(e^N), \tau^N) + \delta^{T+1} W(\gamma(e_a), \tau^a)$$

- The \cdot on the right hand side is where we fill in the best deviation. Given that this deviation can’t affect the future path of play (any deviation triggers the resetting of the punishment phase), this should be a unilateral best response.
- The unilateral best response is τ^N , so this “deviation” could not even be detected as a deviation. There is no incentive to deviate from the punishment given the strategy for punishing deviations from the punishment
- This same logic holds at any point during the punishment (replace T with $r < T$). Logic stays the same.
- Lobby’s condition (for class 5 above)

$$\frac{1 - \delta^T}{1 - \delta} [\pi(\tau^N) - e^N] + \frac{\delta^T}{1 - \delta} [\pi(\tau^a) - e_a] \geq \pi(\tau^D) - e^D + \frac{\delta}{1 - \delta} [\pi(\tau^a) - e_a]$$

- What is best deviation? Would lobby want to choose $e^D = 0$ and get $\tau(\gamma(0))$?
- Given that the lobby can't affect the future path and that the legislature will provide the unilateral tariff that is its best response to $e^D = 0$, the lobby's best deviation payoff is the unilateral best choice, i.e. the trade war lobbying effort / tariff.
- If the lobby deviates to something lower, it both gets a lower tariff in return (less than what is optimal for it in the one-shot game, which is what it was doing before) and gets stuck with the trade agreement tariff ever after
- NOTE: EVERYTHING hinges on whether this is a valid punishment, this two-stage, dynamic punishment

5 Giovanni's asymmetric punishment suggestion

- For now, even though it's not realistic, leave punisher at τ^{tw} so that previous analysis for symmetric case Nash reversion goes through
- Have cheater go to $\tau = 0$ in part (2) of equilibrium construction
 - It's not clear if there is an air-tight restriction on e_{tw} . Leg's condition would be easy if $e_{tw} = 0$, so going to go with that
- Before worrying about punishment for punishment, go back to TA structure
 - If $\tau < \tau^a$, lobby's constraint becomes much easier to satisfy
 - * Lobby no longer wants "trade war." Only thing they can want is break tariff for one period. Then punishment punishes lobby too
 - For legislature:

$$\frac{\delta_{ML} - \delta_{ML}^{T+1}}{1 - \delta_{ML}} [W_{ML}(\gamma(e_a), \tau^a) - W_{ML}(\gamma(?), 0, \tau^{*tw})] \geq W_{ML}(\gamma(e_b), \tau^b(e_b), \tau^{*a}) - W_{ML}(\gamma(e_b), \tau^a) \quad (2)$$

- * Not clear what's needed to make the LHS positive (RHS is always positive). If $e > e_a$, it should be at least somewhat positive. Not obvious that LHS is positive if $e = 0$.
 - * Maybe should focus on legislature...Not necessarily on this level of punishment; maybe go to deviation punishment
- Punishment
 - Lobby doesn't want to deviate
 - Legislature would want to go to $\tau^D(0)$.
 - * Punish with $e = 0$, $\tau > \tau^D(0)$ (needs to be higher so that lobby likes it)
 - **need to make sure payoffs for all of these are lower than eqm payoff for punisher**