

Self-enforcing Trade Agreements, Dispute Settlement and Separation of Powers

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Abstract

In an environment where international trade agreements must be enforced via promises of future cooperation, the presence of an import-competing lobby has important implications for optimal punishments, and therefore dispute resolution procedures. When lobbies work to disrupt trade agreements, the optimal punishment must balance two, conflicting objectives. Longer punishments help to enforce cooperation by increasing the government's costs of defecting, but because the lobby prefers the punishment outcome, this also incentivizes lobbying effort and with it political pressure to break the agreement. Thus the model generates new predictions for the design of mechanisms for resolving trade disputes: there is an optimal length for dispute resolutions procedures, and it depends directly on the political influence of the lobbies. Trade agreement tariffs are shown to be increasing in the political influence of the lobbies, as well as their patience levels.

Keywords:

trade agreements, lobbying, WTO, dispute settlement, repeated games, enforcement

1. Introduction

In the absence of strong external enforcement mechanisms for international trade agreements, we generally assume that cooperation is enforced by promises of future cooperation, or, equivalently, promises of future punishment for exploitative behavior.

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When repeated-game incentives are used to enforce cooperation and prevent players from defecting in a prisoner's dilemma-style stage game, the strongest punishment available is usually assumed to be the grim trigger strategy of defecting forever upon encountering a defection by one's partner.

Unfortunately, the ability of players to renegotiate out of punishment sequences can interfere with the efficacy of grim-trigger strategies for supporting cooperation; indeed, a variety of concerns about welfare and realism may lead us to explore alternative punishment sequences. Combining this with the observation that lobbies are not only relevant but critically-active players in the repeated game, I argue that we can derive optimal (non-grim-trigger) punishments directly from the players' incentive constraints. In the context of international trade agreements, these punishments can be interpreted as arising from the design and implementation of rules like those established in the World Trade Organization's Dispute Settlement Understanding.

Not only does adding lobbies suggest an optimal length for dispute settlement procedures; it also turns out that this optimal punishment length itself depends on how readily special interests are able to influence the political process. That is, the optimal length of the dispute settlement procedure is a function of the strength of the lobbies, reinforcing the idea that including lobbying in such analyses can be critically important for institutional design questions. We shall also see that, for a fixed dispute settlement procedure, as lobbies become more influential or more patient, the equilibrium trade agreement tariff that must be provided in order to overcome the ratification hurdle increases.

The structure of the model is similar to that of Bagwell and Staiger (2005) with two main changes: the political-economy weights are endogenously determined, and in place of a unitary government that has different preferences before and after signing a trade agreement, this model has two branches of government with differing preferences who share policy-making power as in Milner and Rosendorff (1997), Song (2008) and Buzard (2014*b*).

This paper incorporates such a separation-of-powers policy-making process with endogenous lobbying along the lines of Grossman and Helpman (1994, 1995) into a repeated-game setting with a dispute settlement institution (DSI) to take account of

the threat to cooperation posed by renegotiation. This DSI is patterned on that of Klimenko, Ramey and Watson (2008), who propose a notion of *recurrent agreement* that takes into account the possibility of renegotiation via such a DSI loosely patterned on the Dispute Settlement Body of the World Trade Organization. The DSI helps trading partners to credibly condition their negotiations on the state of their relationship and avoid the problems created by renegotiation.

Here, welfare-maximizing executives use their control over trade-agreement tariffs as a kind of political commitment device:¹ by setting tariffs to optimally reduce lobbying incentives, they reduce the political pressure on the legislatures. This changes the legislatures's incentives, so that they do not break the agreement as they would have if they had faced more intense political pressure.²

Given that all actors have perfect information about the effect of lobbying effort on the outcome of the political process, the executives maximize social welfare by choosing the lowest tariffs that make it unattractive for the lobbies to provoke the legislature to initiate a trade dispute.³ So even when there are no disputes in equilibrium, the out-of-equilibrium threat that a lobby might provoke a trade war is crucial in determining the equilibrium trade agreement structure.

Thus the problem with the lobby has an extra constraint relative to the standard problem. The constraint on the key repeated-game player, which here is the legislature, is loosened by increasing the punishment length because defections become relatively more unattractive. However, the new constraint due to the presence of lobbying be-

¹This is a different kind of domestic commitment role for trade agreements than that identified by Maggi and Rodríguez-Clare (2007), who show that trade agreements can be useful for helping governments commit vis-à-vis private firms in their investment decisions.

²This is not to say that the legislature itself is made better off by the reduction in political pressure, although Buzard (2014a) demonstrates that this is possible. It only means that the executive can use the commitment power of the trade agreement to improve its welfare, which is assumed to differ from that of the legislature. The commonly-made assumption that the executive is less protectionist than the legislature is a special case of the finding that susceptibility to special interests generally declines with the size of one's constituency. One simple illustration from the realm of trade policy is the following: a legislator whose district has a large concentration of a particular industry does not take into account the impact of tariffs on the welfare of consumers in other districts, while the executive, whose constituency encompasses the whole country, will internalize these diffuse consumption effects. For a detailed argument, see Lohmann and O'Halloran (1994).

³With no uncertainty of any kind, there will be no trade disputes in equilibrium. Political uncertainty can be easily added to the model, in which case lobbying effort is typically non-zero and there is a positive probability of dispute in equilibrium.

comes tighter as the punishment becomes more severe because the lobby *prefers* punishment periods. Because the tariffs during punishment, and thus the lobby's profits, are higher compared to those they receive during a cooperative period, the lobby has increased incentive to exert effort as the punishment lengthens.

The optimal punishment length must balance these two competing forces. Where the balance falls depends in large part on how influential the lobby is in the legislative process. If the lobby has very little power, the optimal punishment converges to that of the model without a lobby: longer punishments are better because the key constraint is the legislature's. As the lobby becomes stronger, the optimal punishment becomes shorter because the lobby's incentive becomes more important.

Quite intuitively, it is also shown that, for a given punishment length, increases in the lobby's strength lead to lower required payments to provoke trade dispute and therefore higher equilibrium trade agreement tariffs to avoid those disputes. Increases in the lobby's patience have the same qualitative effects, while increases in the patience of the legislature work in the opposite direction: the lobby must pay more to induce the legislature to endure the punishment and the executive can accordingly reduce trade agreement tariffs without fear that they will be broken.

The recurrent agreement approach to renegotiation in a WTO-like environment following Klimenko, Ramey and Watson (2008) (hereafter KRW) complements contributions by Cotter and Mitchell (1997), Ludema (2001) and Beshkar (2010a) that study *renegotiation-proof* trade agreements. Whereas the *renegotiation-proof* concept of Bernheim and Ray (1989) and Farrell and Maskin (1989) assumes that joint-value punishments are infeasible, the recurrent agreement approach argues that joint-value punishments can be made feasible by an institution such as the DSI.

Related is also a growing literature on renegotiation in one-shot models of trade agreements, ranging from the limited forms of renegotiation in Bagwell and Staiger (1999) and Beshkar (2010b) to the richer models of renegotiation in Beshkar (2013) and Maggi and Staiger (2013, 2014). These consider a substantively different question: instead of being concerned with the undermining of cooperation due to the renegotiation of punishments, they assume perfect external enforcement and ask questions about the optimality of various agreement and institutional designs given that the parties have

some ability to change the terms of their agreement within the one-shot interaction. Ethier (2005) and Maggi and Staiger (2011) study the role of dispute settlement procedures where there is perfect external enforcement and no possibility of renegotiation.

Repeated non-cooperative game models of trade agreements without renegotiation have been considered by McMillan (1986, 1989), Dixit (1987), Bagwell and Staiger (1990, 1997*a,b*, 2002), Kovenock and Thursby (1992), Maggi (1999), Ederington (2001), Rosendorff (2005), Bagwell (2009), and Park (2011). In particular, Hungerford (1991), Riezman (1991), and Martin and Vergote (2008) consider the impact of different assumptions about reactions and timing of punishments for deviations from agreements. Here, I assume the simplest case—that the trading partners remain in a symmetric trade war until the dispute resolution process has concluded. Although officially-sanctioned retaliation is not often imposed, and if it is, it is with delay, this timing is consistent with the idea that trading partners exact ‘vigilante justice’ through various means such as imposing unrelated anti-dumping duties.⁴

I begin in the next section by describing in detail the stage game, which is closely related to the model in Buzard (2014*b*). Both papers employ the separation-of-powers government structure with endogenous lobbying. While the current paper focuses on the implications of the self-enforcement and renegotiation constraints for the optimal design of trade agreements and dispute-settlement institutions, Buzard (2014*b*) abstracts from enforcement issues and demonstrates that taking into account the separation-of-powers structure can resolve the empirical puzzle surrounding the Grossman and Helpman (1994) model, highlights the importance of the threat of ratification failures on the formation of trade agreements and develops new results about the role of political uncertainty in the policy-making process.

Section 3 then sets out the dispute settlement institution and the set-up of the repeated game. I describe the structure and properties of optimal trade agreements in Section 4 and explore the forces shaping optimal dispute resolution procedures in Section 5 before concluding in Section 7.

⁴See the discussions in Bown (2005) and Martin and Vergote (2008) for evidence on informal versus formal retaliation.

2. Stage Game

I employ a two good partial equilibrium model with two countries: home (no asterisk) and foreign (asterisk). The countries trade two goods, X and Y , where P_i denotes the home price of good $i \in \{X, Y\}$ and P_i^* denotes the foreign price of good i . In each country, the demand functions are taken to be identical for both traded goods, respectively $D(P_i)$ in home and $D(P_i^*)$ in foreign and are assumed strictly decreasing and twice continuously differentiable.

The supply functions for good X are $Q_X(P_X)$ and $Q_X^*(P_X^*)$ and are assumed strictly increasing and twice continuously differentiable for all prices that elicit positive supply. I also assume $Q_X^*(P_X) > Q_X(P_X)$ for any such P_X so that the home country is a net importer of good X . The production structure for good Y is taken to be symmetric, with both demand and supply such that the economy is separable in goods X and Y . As is standard, it is assumed that the production of each good requires the possession of a sector-specific factor that is available in inelastic supply and is non-tradable so that the income of owners of the specific factors is tied to the price of the good in whose production their factor is used.

For simplicity, I assume each government's only trade policy instrument is a specific tariff on its import-competing good: the home country levies a tariff τ on good X while the foreign country applies a tariff τ^* to good Y . Local prices are then $P_X = P_X^W + \tau$, $P_X^* = P_X^W$, $P_Y = P_Y^W$ and $P_Y^* = P_Y^W + \tau^*$ where a W superscript indicates world prices and equilibrium prices are determined by the market clearing conditions

$$M_X(P_X) = D(P_X) - Q_X(P_X) = Q_X^*(P_X^*) - D(P_X^*) = E_X^*(P_X^*)$$

$$E_Y(P_Y) = Q_Y(P_Y) - D(P_Y) = D(P_Y^*) - Q_Y^*(P_Y) = M_Y^*(P_Y^*)$$

where M_X are home-county imports and E_X^* are foreign exports of good X and E_Y are home-county exports and M_Y^* are foreign imports of good Y .

It follows that P_X^W and P_Y^W are decreasing in τ and τ^* respectively, while P_X and P_Y^* are increasing in the respective domestic tariff. This gives rise to a standard terms-of-trade externality. As profits and producer surplus (identical in this model) in a sector

are increasing in the price of its good, profits in the import-competing sector are also increasing in the domestic tariff. This economic fact, combined with the assumptions on specific factor ownership, is what motivates political activity.

I next describe the politically-relevant actors. In order to focus attention on protectionist political forces, I assume that only the import-competing industry in each country is politically-organized and able to lobby and that it is represented by a single lobbying organization.⁵ Each country's government is composed of two branches: an executive who can conclude trade agreements and a legislature that has final say on trade policy. In summary, the political process is modeled as involving three players in each country: the lobby, the executive, and the legislature.

The stage-game timing is as follows. First, the executives set trade policy cooperatively in an international agreement. In the context of the repeated game, this can be construed as concluding an agreement in the first period and then potentially renegotiating at the beginning of each subsequent period, or as forming a new agreement each period. After the trade agreement is concluded in each period, the lobbies attempt to persuade the legislatures in their respective countries to break the trade agreement. Next, the legislatures decide whether to abide by the agreement or to provoke a trade war. In the event that the trade agreement does not remain in force, there is a final stage of lobbying and voting to set the trade-war tariffs. Once all political decisions are taken, producers and consumers make their decisions.

We are in an environment of complete information, so the appropriate solution concept is subgame perfect Nash equilibrium. Whenever this is a possibility of multiple equilibria, I will focus on the one that maximizes the welfare of the executives. As this game is solved by backward induction, it is intuitive to start by describing the incentives of the legislatures, whose decisions I model as being taken by a median legislator. As the economy is fully separable and the economic and political structures are symmetric, I focus here on the home country and the X -sector. The details are analogous for Y and foreign.

⁵ Adding a pro-trade lobby for the exporting industry would modify the magnitude of the effects and make free trade attainable for a range of parameter values, but it would not modify the essential dynamic.

The per-period welfare function of the home legislature is

$$W_{ML} = CS_X(\tau) + \gamma(e) \cdot PS_X(\tau) + CS_Y(\tau^*) + PS_Y(\tau^*) + TR(\tau) \quad (1)$$

where CS is consumer surplus, PS is producer surplus, $\gamma(e)$ is the weight placed on producer surplus (profits) in the import-competing industry, e is lobbying effort, and TR is tariff revenue. Here, the weight the median legislator places on the profits of the import-competing industry, $\gamma(e)$ is affected by the level of lobbying effort.⁶

Notice that, aside from the endogeneity of the weight the legislature places on the lobbying industry's profits, this is precisely the *deus ex machina* government objective function popularized by Baldwin (1987) that is commonly employed in the literature on the political economy of trade agreements. Since trade policies are overwhelmingly determined within the context of trade agreements, it is useful to have a framework to bring together the endogenous political pressure of PFS-style modeling with the trade agreements approach; the formulation in Equation 1 is intended to be a bridge between the two. Modeling the objective function so closely on the standard in the trade agreements literature allows for direct comparisons to the large extant body of work that studies exogenous shocks only, revealing cleanly the effects of the addition of endogenous lobbying.

Assumption 1. $\gamma(e)$ is continuously differentiable, strictly increasing and concave in e .

Assumption 1 formalizes the intuition that the legislature favors the import-competing industry more the higher is its lobbying effort, but that there are diminishing returns to lobbying activity.⁷ The assumption of diminishing returns to lobbying effort has been present in the literature going back at least to Findlay and Wellisz (1982). Dixit, Grossman and Helpman (1997) point out the linearity in contributions assumed in the Protection for Sale model prevents complete analysis of distributional questions and

⁶The standard PFS modeling would specify $W_{ML} = C + aW$, but as will be seen when we come to the preferences of the executive, this is not sufficiently general for the purposes of this model. Although complex, an isomorphism can be made between the two forms in a special case as discussed in Buzard (2014b).

⁷The diminishing returns here take the form of declining increments to the lobby's influence as effort increases; Ethier (2012) has an alternate form in which the returns to lobbying decline with higher levels of protection.

restricts the returns to lobbying activity to be constant. They generalize the functional form as $G(a, c)$ where a is the policy vector in a general policy-setting environment and show that the PFS equilibrium analysis can be extended to this more general setting.

Lobbying affects only the weight the legislature places on the profits of the import-competing industry. These profits are higher in a trade war than under a trade agreement, so given Assumption 1, the legislature becomes more favorably inclined toward the high trade-war tariff and associated profits as lobbying increases and therefore more likely to break the trade agreement.

Given the legislature's preferences, the home lobby chooses its lobbying effort (e_b to influence the break decision, e_a to influence the applied tariff under the trade agreement, and e_p to influence the punishment tariff) to maximize the welfare function:

$$U_L = [\pi(\tau^{tw}) - e_{tw}] \mathbb{I}[\text{Trade War}] + \pi(\tau^a) \mathbb{I}[\text{Trade Agreement}] - e_b \quad (2)$$

where $\pi(\cdot)$ is the current-period profit and τ^a (τ^{tw}) is the home country's tariff on the import good under a trade agreement (war). I use the convention throughout of representing a vector of tariffs for both countries (τ, τ^*) as a single bold τ .

I assume the lobby's contribution is not observable to the foreign legislature. The implication is that the lobby can directly influence only the home legislature, and so the influence of one country's lobby on the other country's legislature occurs only through the tariffs selected.⁸

In the first stage, the executives choose the trade agreement tariffs $\tau^a = (\tau^a, \tau^{*a})$ via a negotiating process that I assume to be efficient. In this symmetric environment, this process maximizes the joint payoffs of the trade agreement:⁹

$$W_E(\tau^a) = W_E(\tau^a) + W_E^*(\tau^a) \quad (3)$$

I model the executives' choice via the Nash bargaining solution where the disagreement point is the executives' welfare resulting from the Nash equilibrium in the

⁸cfr. Grossman and Helpman (1995), page 685-686.

⁹If political uncertainty is present, the joint payoffs must take into account the possibility that the trade agreement will be broken. In the case of certainty, agreement will always be maintained on the equilibrium path and so this specification is sufficient.

non-cooperative game (i.e. in the absence of a trade agreement) between the legislatures.

The executives are assumed, for simplicity, to be social-welfare maximizers who can make transfers between them.¹⁰ Therefore the home executive's welfare is specified as follows:

$$W_E = CS_X(\tau) + PS_X(\tau) + CS_Y(\tau^*) + PS_Y(\tau^*) + TR(\tau)$$

Note that this is identical to the welfare function for the legislature aside from the weight on the profits of the import industry, which is not a function of lobbying effort and here is assumed to be 1 for simplicity. This assumption does *not* require that the executives are not lobbied; only that their preferences are not directly altered in a significant way by lobbying over trade—that they do not sell protection in order to finance their re-election campaigns. In the case of the post-war United States, where the Congress has consistently been significantly more protectionist than the President, this seems to reasonably reflect the political reality. For trade policy, where there are concentrated benefits but harm is diffuse, there are good reasons for this to be the case. Because the President has the largest constituency possible, delegating authority to the executive branch may simply be a mechanism for “concentrating” the benefits since consumers seem unable to overcome the free-riding problem. In fact, a strong argument can be made that power over trade policy has been delegated to the executive branch precisely *because* it is less susceptible to the influence of special interests Destler (2005).

Therefore, in line with both the theoretical and empirical literature, I will assume that $\gamma(e) \geq 1$ for all e . That is, even for the least favorable outcome of the lobbying process, the legislature will be at least weakly more protectionist than the executive.

Assumption 2. $\gamma(e) \geq 1 \forall e$.

Assumption 2 ensures that $\tau^a < \tau^{tw}$, and more generally, that the legislature's incentives are more closely aligned with the lobby's than are those of the executive.

¹⁰It is trivial to relax the assumption of social-welfare maximizing executives; in the present symmetric environment with no disputes, the same is true of the assumption about transfers.

This is not essential but simplifies the analysis and matches well the empirical findings that politicians with larger constituencies are less sensitive to special interests (See Destler (2005) and footnote 2 above).

Although the political process here matches most closely that of the United States in the post-war era, I believe the model or one of its extensions is applicable for a broad range of countries for which authority over the formation and maintenance of trade policy is diffuse and subject to political pressure either at home or in a trading partner.¹¹

3. Repeated Game

This trade policy environment has many features of a standard prisoner's dilemma. Most importantly, the legislatures face unilateral incentives to violate the terms of the agreement under pressure from the lobbies. When the legislatures and lobbies set tariffs at the higher stage-game Nash equilibrium level, payoffs for the social-welfare conscious executives is reduced. In order to maintain the trade agreement without external enforcement, we turn to repeated game incentives.

Precise conditions for supporting the trade agreement in equilibrium depend on the punishments that are specified, and the details for several possibilities are given in Section 6. For the results in Sections 4 and 5, deviations from the trade agreement are punished by reverting to the stage game Nash equilibrium for a specified number of periods before returning to cooperation. This represents a trade war that is limited in duration and therefore more realistic than infinite Nash reversion. I show in Section 5 that infinite Nash reversion punishments are dominated by shorter lengths of Nash reversion when lobbies are non-trivial political actors.

For Nash reversion punishments of length T , the timing of actions is the following. If neither country defects from the agreement in period t , each enters into the applied tariff stage of period t in which the lobby exerts effort in order to keep the tariff from falling below the tariff cap. If one or both countries defect from the agreement in period

¹¹In particular, the binary decision by the legislature about whether to abide by or break the trade agreement is modeled on the "Fast Track Authority" that the U.S. Congress granted to the Executive branch almost continuously from 1974-1994 and then again as "Trade Promotion Authority" from 2002-2007.

t , a dispute arises. In this case, each enters directly into an applied tariff stage for the T periods beginning in period $t+1$. In each of these periods, the punishment specifies that the lobbies and legislatures in both countries play their stage-game Nash equilibrium strategies. In period $t+T+1$, the trade agreement is reinstated.

In order to determine the repeated-game incentives in each state, we must fully specify the punishments for both on- and off-equilibrium path actions. We can think of the punishment scheme being designed either by the executives or by a supranational body like the WTO. The executives will jointly maximize social welfare given the state. After the punishment scheme is designed, they have no opportunity to affect the state other than to choose tariffs that are supportable. Thus the executives maximize joint welfare subject to the incentive constraints of the other players.

We assume that the trade agreement will be designed so that the legislatures and lobbies behave in such a way in equilibrium so that the trade agreement remains in force. In Section 5, the question of how to optimally design the punishment scheme within this class of punishments is addressed.

Again, because of symmetry and separability, it suffices to restrict attention to the home country. An overview of the punishment scheme is given here; for details and a precise description of equilibrium strategies, see Section 6.

On the equilibrium path, the lobby chooses effort level e_b less than a cut-off effort level \bar{e} that would cause the legislature to break the trade agreement. The determination of \bar{e} is described in the next section. The legislature never breaks the trade agreement, with an applied tariff less than or equal to the trade agreement tariff τ^a . These choices are made as long as any violation of the agreement was at least T periods in the past.

Whenever there is a violation of the agreement—that is, a tariff higher than the trade agreement level—the lobby and the legislature play their static Nash strategies for T periods.

For the legislature, this is the tariff that unilaterally maximizes Equation 1 given τ^* and the lobby's choice e_p . The separability of the economy implies that there are no interactions between the decision problems of the legislatures and the lobbies respectively, so the home and foreign best response tariffs are independent and the home country's tariff in a punishment period maximizes weighted home-country welfare in

the X -sector only. The foreign legislature's decision problem is analogous, and unilateral optimization leads to what I refer to as the trade war tariffs τ^{tw} as the solution to the following first order condition:

$$\frac{\partial CS_X(\tau)}{\partial \tau^p} + \gamma(e_p) \cdot \frac{\partial PS_X(\tau)}{\partial \tau^p} + \frac{\partial TR(\tau)}{\partial \tau^p} = 0$$

The lobby chooses its effort e_p given the above best response tariff-setting behavior denoted by τ^R by maximizing its profits net of effort: $\pi(\tau^R(\gamma(e_p))) - e_p$. (Note this is Equation 2 simplified by the resolution of uncertainty over the legislature's decision on the trade agreement). This implies a first order condition of

$$\frac{\partial \pi(\tau^R(\gamma(e_p)))}{\partial e_p} = 1 \quad (4)$$

That is, at this stage, the lobby chooses the level of effort that equates its expected marginal increase in profits with its marginal payment. I label this effort level e_{tw} .

Unlike with infinite Nash reversion punishments, these T -period Nash reversion punishments are not necessarily subgame perfect since the players may want to influence the future path of play during punishment periods. Subgame perfection can be ensured by punishing any deviations *from the punishment* by restarting either the punishment for the legislature or the trade agreement for the lobby. This works because the legislature prefers the trade agreement to the punishment while the lobby's preferences are the reverse. These details do not affect the main results and so are postponed to Section 6.1.

Here we focus on the key issue of the conditions under which the legislature decides to adhere to the trade agreement instead of violating it and triggering a punishment sequence. The trade agreement is broken when the legislature chooses a tariff that is higher than the trade agreement level, τ^a . The level of the break tariff is chosen in the same manner as the trade war tariff, that is, according to Equation 3, but with the lobby's effort at the break stage replacing e_p .

The legislature will, however, only choose the break tariff over the trade agreement tariff if its continuation value from breaking the agreement is higher than the continuation value it receives from abiding by the agreement. The incentive constraint for the median legislator is essentially a condition on the trade agreement tariffs τ^a . It can be

written as

$$W_{\text{ML}}(\gamma(e_b), \tau^a) + \delta_{\text{ML}} V_{\text{ML}}^A \geq W_{\text{ML}}(\gamma(e_b), \tau^b(e_b), \tau^{*a}) + \delta_{\text{ML}} V_{\text{ML}}^P$$

where V_{ML}^A is the continuation value of the median legislator when it abides by the trade agreement V_{ML}^P is the continuation value when it defects and is punished. δ_{ML} is the discount factor of the median legislator, while δ_L will be used to represent the discount factor of the lobby and δ_E that of the executive branch.

If the Nash reversion punishment lasts for T periods, then the only part of the continuation values that need be considered are the next T periods: after those T periods, the trade agreement will be in force so the continuation value will be the same from period $T+1$ on. The executives will choose the same trade-agreement tariffs because they will maximize welfare subject to the same conditions in any non-punishment period. Therefore we have¹²

$$W_{\text{ML}}(\gamma(e_b), \tau^a) + \frac{\delta_{\text{ML}} - \delta_{\text{ML}}^{T+1}}{1 - \delta_{\text{ML}}} W_{\text{ML}}(\gamma(e_b), \tau^a) \geq W_{\text{ML}}(\gamma(e_b), \tau^b(e_b), \tau^{*a}) + \frac{\delta_{\text{ML}} - \delta_{\text{ML}}^{T+1}}{1 - \delta_{\text{ML}}} W_{\text{ML}}(\gamma(e_b), \tau^{tw}). \quad (5)$$

The condition for the lobby is similar. Under the trade agreement, a break in the trade agreement, and punishment period, the lobby receives its profits at the chosen tariff level net of the effort level it exerts:

$$\pi(\tau^a) - e_a + \frac{\delta_L - \delta_L^{T+1}}{1 - \delta_L} [\pi(\tau^a) - e_a] \geq \pi(\tau^b(e_b)) - e_b + \frac{\delta_L - \delta_L^{T+1}}{1 - \delta_L} [\pi(\tau^{tw}) - e_{tw}]. \quad (6)$$

The next section explores the implications of these incentive constraints for the structure of the equilibrium trade agreement.

4. Trade Agreement Structure

We can write the executives' joint problem as

$$\max_{\tau^a} \frac{W_E(\tau^a)}{1 - \delta_E} \quad \text{subject to} \quad (7)$$

¹²Note that $\delta + \delta^2 + \dots + \delta^l = \sum_{k=1}^l \delta^k = \sum_{k=1}^{\infty} \delta^k - \sum_{k=l+1}^{\infty} \delta^k = \frac{\delta}{1-\delta} - \frac{\delta^{l+1}}{1-\delta} = \frac{\delta - \delta^{l+1}}{1-\delta}$.

$$\frac{\delta_{ML} - \delta_{ML}^{T+1}}{1 - \delta_{ML}} [W_{ML}(\gamma(e_b), \tau^a) - W_{ML}(\gamma(e_b), \tau^{tw})] \geq W_{ML}(\gamma(e_b), \tau^b(e_b), \tau^{*a}) - W_{ML}(\gamma(e_b), \tau^a) \quad (8)$$

and

$$e_b \geq \pi(\tau^b(e_b)) - \pi(\tau^a) + \frac{\delta_L - \delta_L^{T+1}}{1 - \delta_L} [\pi(\tau^{tw}) - e_{tw} - \pi(\tau^a)] \quad (9)$$

where Inequalities 8 and 9 are simple rearrangements of 5 and 6.

To understand how the executives optimally structure trade agreements, we must first examine the incentives of the lobbies and how the legislatures make decisions regarding breach of the trade agreement. The symmetric structure of the model permits restriction of attention to the home country.

I will consider the economically interesting case in which, for a given $\delta = (\delta_E, \delta_{ML}, \delta_L)$ and T , there exists a non-trivial trade agreement in the absence of lobbying, that is, one in which the lowest supportable cooperative tariffs are strictly lower than the trade-war (i.e. non-cooperative) level. Call the trade-agreement tariffs in the absence of lobbies τ_{NL}^a . If $\tau_{NL}^a = \tau^{tw}$, the lobby has no incentive to be active and the extra constraint implied by the presence of the lobby does not bind.

When deciding whether to exert effort to derail a trade agreement, the lobby has a two-stage problem. First, for the given τ^a , δ and T , it calculates the minimum e_b required to induce the legislature to break the trade agreement. Call this minimum effort level $\bar{e}(\tau^a)$. It induces the minimum tariff that will break the agreement, $\tau^b(\bar{e})$.¹³

The following equation defines \bar{e} :

$$\frac{\delta_{ML} - \delta_{ML}^{T+1}}{1 - \delta_{ML}} [W_{ML}(\gamma(\bar{e}), \tau^a) - W_{ML}(\gamma(\bar{e}), \tau^{tw})] - [W_{ML}(\gamma(\bar{e}), \tau^b(\bar{e}), \tau^{*a}) - W_{ML}(\gamma(\bar{e}), \tau^a)] = 0 \quad (10)$$

This calculation of precise indifference is possible because it is assumed here that the political process is certain—that is, all actors know precisely how lobbying effort affects the identity of the median legislator through $\gamma(e_b)$.

¹³It is assumed that only tariffs strictly greater than τ^a serve to break the agreement.

Given the effort level required to break the agreement, the lobby will then compare its current and future payoffs from inducing a dispute net of lobbying effort (that is, $\pi(\tau^b(\bar{e})) - \bar{e} + \frac{\delta_L - \delta_L^{T+1}}{1 - \delta_L} [\pi(\tau^{tw}) - e_{tw}]$) to the profit stream from the trade agreement with no lobbying effort $\left(\pi(\tau^a) + \frac{\delta_L - \delta_L^{T+1}}{1 - \delta_L} \pi(\tau^a)\right)$. With the appropriate substitutions and rearrangements, this is just Condition (9) evaluated at \bar{e} . If the latter is larger, the lobby chooses to be inactive and the agreement remains in force. On the other hand, if the former is larger, the lobby induces the most profitable possible break.¹⁴

Anticipating this decision-making process of the lobby, the executives maximize social welfare by choosing the lowest tariffs such that the trade agreement they negotiate remains in force. They raise tariffs to the point that makes the lobby indifferent between exerting effort $\bar{e}(\tau^a)$ and disengaging completely.¹⁵ That is, they choose tariffs so that the following equation holds:

$$\bar{e}(\tau^a) - [\pi(\tau^b(\bar{e})) - \pi(\tau^a)] - \frac{\delta_L - \delta_L^{T+1}}{1 - \delta_L} [\pi(\tau^{tw}) - e_{tw} - \pi(\tau^a)] = 0 \quad (11)$$

This is simply the lobby's constraint in terms of the net gain to exerting effort when evaluated at \bar{e} at the indifference point.¹⁶

To understand the dynamics governing the solution to this problem, begin by considering the legislature's constraint at equality, Equation 10. This traces out a function from the trade agreement tariff into the minimum effort level required to break the trade agreement. The relationship between the home tariff and \bar{e} is straightforward.

Lemma 1. *The minimum lobbying effort required to break the trade agreement (\bar{e}) is increasing in the home trade agreement tariff τ^a .*

Proof: See the Appendix.

¹⁴Recall that the lobby's myopic profits are maximized at e_{tw} . This implies that if $\bar{e} < e_{tw}$, the lobby will break the agreement by exerting effort level e_{tw} since its net profits are higher than if it only exerted effort level \bar{e} in this case.

¹⁵Here I assume that the lobby does not exert effort when indifferent; if the opposite assumption were made, tariffs would have to be raised by an additional ε .

¹⁶By construction, the legislative constraint will always be slack in equilibrium because the $\bar{e}(\tau^a)$ schedule is calculated to make the median legislator indifferent between cooperating and initiating a dispute but then in equilibrium, τ^a is chosen so that the lobby disengages. When the lobby is disengaged ($e_b = 0$), the median legislator cannot prefer to break the agreement since her preferred tariff is lower when $e_b = 0$ than when $e_b = \bar{e}(\tau^a) \geq 0$.

The intuition is as follows: \bar{e} must be at least as large as e_{tw} in equilibrium because the lobby's net profits are maximized at e_{tw} . If $\bar{e} < e_{tw}$, the lobby's constraint will not be satisfied since the lobby will exert effort level e_{tw} . Since the trade agreement tariff is weakly less than the trade war tariff, the median legislator's most preferred tariff when $e_b = \bar{e}$ —that is, $\tau^b(\bar{e})$ —must be higher than the trade agreement tariff.¹⁷ Raising τ^a brings the trade agreement tariff closer to the legislature's ideal point, requiring the lobby to pay more to make the legislature willing to break the agreement.

The relationship between the foreign trade agreement tariff and \bar{e} is the opposite. This occurs because raising τ^{*a} make the agreement less attractive to the legislature and therefore requires less effort from the lobby to break.

Lemma 2. *The minimum lobbying effort required to break the trade agreement (\bar{e}) is decreasing in the foreign trade agreement tariff τ^{*a} .*

Proof: See the Appendix.

When the trade agreement is symmetric, $\tau^a = \tau^{*a}$. In this case, \bar{e} is concave in the trade agreement tariffs since the legislature's optimum in terms of τ^a is at τ^{tw} while its optimum in terms of τ^{*a} is at zero.

The concavity of this $\bar{e}(\tau^a)$ function implies that there may not be a truly interior solution to the problem. Of course whenever the solution to the problem in the absence of lobbies cannot be satisfied for any $\tau^a < \tau^{tw}$, then the solution to (7) will also be τ^{tw} . If the legislative constraint can be satisfied, then the lobby's constraint will always be satisfied when $\pi(\tau^{tw}) - e_{tw} - \pi(\tau^a) = 0$. Most of the results of this paper do not apply to this kind of solution, but it does exist. Call it τ_{NF}^a since the essential reason this tariff is a solution is that it implies that there are no future gain for the lobby. Since the highest net profits in one period are also achieved at the trade war tariff, there can be no contemporaneous gain either, so the lobby has no incentive to exert effort.

To see when an equilibrium of interest exists, recall that we need $\bar{e} \geq e_{tw}$ in order for the lobby's constraint to be truly satisfied. Even though it may appear at first sight that the constraint could be satisfied at a τ^a for which $\bar{e} < e_{tw}$, in fact the lobby would

¹⁷Note as well that whenever non-trivial cooperation is sustainable, $\tau^b(\bar{e})$ is also necessarily less than the trade war tariff. If \bar{e} were so high as to make $\tau^b \geq \tau^{tw}$, the legislature would not experience the trade war as a punishment.

choose the higher level of effort e_{tw} at which its net profits are maximized, breaking this incentive constraint. For some parameters, there may not exist a $\tau^a < \tau_{NF}^a$ for which $\bar{e} \geq e_{tw}$.

If there does exist $\tau^a < \tau^{tw}$ for which $\bar{e} \geq e_{tw}$, there *may* be another solution. What is required is that $\bar{e}(\tau^a)$ does not begin to decrease too quickly before it can satisfy the lobby's constraint. The more easily the lobby can exert influence, the harder it is to satisfy this constraint: this causes \bar{e} to rise slowly with tariffs and keeps the price of a break low in comparison to the profits.

Whether an interesting solution of the type we go on to examine in the next two sections exists or not, as long as there is a non-trivial trade agreement in the absence of lobbies, a trade agreement always exists and has the same form.

Result 1. *In the case of political certainty, the equilibrium trade agreement induces zero lobbying effort and is never subject to dispute. The executives choose the minimum tariff level that induces the lobby to choose $e_b = 0$.*

At the equilibrium tariffs, the lobby's constraint binds, while the legislature's does not. The amount of effort the lobby would have to exert to provoke a dispute, however, is derived from the legislature's constraint. This cost is then used in the lobby's constraint to calculate the lowest tariff level that will induce the lobby to disengage (that is, choose $e_b = 0$ over $e_b = \bar{e}(\tau^a)$) and therefore make the median legislator's constraint slack and induce *her* to choose the internationally-agreed-upon τ^a over τ^b and the implied dispute.¹⁸

Although in this simple model we do not see disputes in equilibrium, the lobby's out-of-equilibrium incentives to exert effort to provoke a dispute are essential in determining the tariff-setting behavior of the executives.

4.1. Trade Agreement Properties

Following Result 1, we know that the lobby first uses Expression 8 at equality to determine $\bar{e}(\tau^a)$: that is, it determines how much effort it has to exert for the given τ^a

¹⁸The results would be altered in magnitude but not in spirit by assuming that the trade agreement tariffs are weak bindings—that is, tariff caps—instead of strong bindings. The most important implication is that there would be positive lobbying in equilibrium as the lobby would need to put forth effort to bid protection levels up to the cap. There would still be no trade disputes in equilibrium.

in order to induce the legislature to choose noncooperation. This it accomplishes using Condition 10 above.

With $\bar{e}(\tau^a)$ determined, the executives use Expression 11 at equality to determine the required τ^a :¹⁹ that is, the trade agreement tariff that is just high enough to induce the lobby to disengage, causing the equilibrium outcome to be $e_b = 0$ and the trade agreement tariff to remain in place.

Although one cannot arrive at explicit expressions for the solution functions $\bar{e}(\cdot)$ and $\tau^a(\cdot)$ without imposing further assumptions, significant intuition can be derived implicitly. An overview of the results will be provided here, while the mathematical details are in the Appendix. It's important to keep in mind that these results apply to solutions that are truly interior in the sense that the lobby has been disengaged by making it too costly to exert effort.

We begin with the comparative static question of how changes in the patience level of the lobby affect the equilibrium trade agreement tariffs.

Corollary 1. *As the lobby becomes more patient (δ_L increases), the trade agreement tariff also increases, ceteris paribus.*

Proof: See the Appendix.

When the lobby becomes more patient, the equilibrium trade agreement tariff must be raised because the lobby now places relatively less weight on the lower net profits it gains during the break period relative to the benefits it attains during the trade war in future periods. The lobby's incentives to exert effort must be reduced by increasing the trade agreement tariff, thus reducing the profit gap between the trade war and the trade agreement.

A change in δ_L might reflect a change in firms' planning horizons, or even their operational horizons—although it is not entirely clear in which direction this might work for firms who are facing extinction without sufficient protection. The lobby's patience level might also change with a change in the administrative leadership of the lobby, or as a reduced form for changes in risk aversion in a model with political uncertainty—a more risk-averse lobby would effectively weigh the future, uncertain

¹⁹There are analogous expression for τ^{*a} throughout that can be ignored by symmetry.

gains less relative to the current, certain cost.

Turning to the patience of the median legislator, we start with the effect on the minimum lobbying effort level.

Corollary 2. *As the median legislator becomes more patient (δ_{ML} increases), the minimum lobbying effort (\bar{e}) required to break the trade agreement increases ceteris paribus.*

Proof: See the Appendix.

For any given level of effort, a more patient median legislator weighs the future punishment for deviating more heavily relative to the gain from the cheater's payoff in the current period. The lobby must compensate by putting forth more effort in the current period to bend the median legislator's preferences toward higher tariffs.

What does an increase in δ_{ML} , leading to an increase in \bar{e} , imply for the optimal trade agreement tariff? The math is in the Appendix, but the intuition is straightforward.

Corollary 3. *As the median legislator becomes more patient (δ_{ML} increases), the trade agreement tariff decreases ceteris paribus.*

Proof: See the Appendix.

This result contrasts with Corollary 1. When the median legislator becomes more patient, the executives are able to decrease the trade agreement tariff *because* the cutoff lobbying expenditure increases. This is because the lobby must now pay more to convince the legislature to choose short-run gains in the face of future punishment, so a wider profit gap between the trade war and trade agreement tariffs is consistent with disengaging the lobby.

Here the result comes through the legislature's indifference condition instead of directly from the lobby's indifference condition, but the intuition is the same: the trade agreement tariff is determined as whatever it takes to quell the lobby's willingness to exert effort to break the agreement.

The median legislator's patience level will increase with any change that makes her less susceptible to challenges from incumbents and therefore more likely to remain in office into the future. Changes to electoral rules, the strength of her party and similar

political environment variables are influential here. Also influencing δ_{ML} are electoral timing issues and individual decisions about seeking re-election.

Let's turn to another variable that impacts the equilibrium trade agreement in important ways: the weight the median legislator places on the profits of the import-competing sector. This political weighting function, $\gamma(e)$, is endogenous to many of the decisions underpinning the equilibrium, but here we examine the effect of an exogenous change in γ . First, on the cutoff effort level:

Corollary 4. *Exogenous positive shifts in the political weighting function $\gamma(e)$ reduce the minimum lobbying effort (\bar{e}) required to break the trade agreement, ceteris paribus.*

Proof: See the Appendix.

In accordance with intuition, if there is a shift in the political weighting function so that the legislature weights the profits of the import-competing sector more heavily for a given amount of lobbying effort, the lobby will have to exert less effort in order to induce a trade disruption.

This translates in a straightforward way to an impact on the trade agreement tariff.

Corollary 5. *Exogenous positive shifts in the political weighting function $\gamma(e)$ lead to higher trade agreement tariffs, ceteris paribus.*

Proof: See the Appendix.

This makes sense given that an upward shift in the political weighting function in effect means that the lobby becomes more powerful, that is, it has a larger impact on the median legislator for a given level of effort. This is why the minimum effort level required to break the trade agreement is reduced, and therefore why the trade agreement tariff must be increased: when the lobby has to pay less to break the agreement for any given tariff level, the agreement must be made more agreeable to the lobby.

Examples of phenomena that would shift $\gamma(\cdot)$ abound: the lobby becoming more effectively organized, a national news story that makes the industry more sympathetic in the eyes of voters, or the appointment of an individual who is particularly supportive to a key leadership role in the legislature would all shift the political weighting function upward.

5. Optimal Dispute Resolution

In an environment without lobbying, KRW show that social welfare increases (that is, trade-agreement tariffs can be reduced) as punishments are made stronger. This can be seen here if we restrict attention to the legislature's constraint:

$$\frac{\delta_{\text{ML}} - \delta_{\text{ML}}^{T+1}}{1 - \delta_{\text{ML}}} [W_{\text{ML}}(\gamma(e_b), \tau^a) - W_{\text{ML}}(\gamma(e_b), \tau^{tw})] \geq W_{\text{ML}}(\gamma(e_b), \tau^b(e_b), \tau^{*a}) - W_{\text{ML}}(\gamma(e_b), \tau^a)$$

This constraint is made less binding as T increases—that is, as we increase the number of periods of punishment. The intuition is straightforward: the per-period punishment is felt for more periods as the one period of gain from defecting remains the same. Thus larger deviation payoffs remain consistent with equilibrium cooperation as T increases.

Lemma 3. *The slackness of the legislative constraint is increasing in T .*

This is why the standard environment with no lobby gives no model-based prediction about the optimal length of punishment. Longer is better, although there are renegotiation constraints that must be taken into account that are typically outside of the model as well as other concerns.

The lobby's constraint

$$e_b \geq \pi(\tau^b(e_b)) - \pi(\tau^a) + \frac{\delta_L - \delta_L^{T+1}}{1 - \delta_L} [\pi(\tau^{tw}) - e_{tw} - \pi(\tau^a)]$$

works in the opposite direction in relation to T . Here, the lobby benefits in each dispute period, and so the total profit from a dispute is increasing in T . Thus we have

Lemma 4. *The slackness of the lobbying constraint is decreasing in T .*

Although the interaction of the impact of the length of the punishment on these two constraints is quite nuanced, in many cases, adding the lobbying constraint provides a prediction for the optimal T .

As the executives choose the smallest τ^a that makes the lobby indifferent at $\bar{e}(\tau^a)$, we must analyze the lobby's constraint evaluated at $\bar{e}(\tau^a)$ (Expression 11) to determine the optimal length of punishment T . Obtaining the derivative of $\bar{e}(\tau^a)$ from

Equation 10 via the Implicit Function Theorem, the derivative of the lobby's constraint with respect to T is

$$\left(1 - \frac{\partial \pi}{\partial \bar{e}}\right) \frac{-\frac{\delta_{ML}^{T+1} \ln \delta_{ML}}{1-\delta_{ML}} [W_{ML}(\gamma(\bar{e}), \tau^a) - W_{ML}(\gamma(\bar{e}), \tau^{tw})]}{\frac{\partial \gamma}{\partial e} [\pi(\tau^b(\bar{e})) - \pi(\tau^a)] + \frac{\delta_{ML} - \delta_{ML}^{T+1}}{1-\delta_{ML}} \frac{\partial \gamma}{\partial e} [\pi(\tau^{tw}) - \pi(\tau^a)]} + \frac{\delta_L^{T+1} \ln \delta_L}{1-\delta_L} [\pi(\tau^{tw}) - e_{tw} - \pi(\tau^a)] \quad (12)$$

If this expression is negative for all T , the lobby's constraint is most slack at $T = 0$. The optimal punishment length cannot be zero, however, because the median legislator's constraint cannot be satisfied with a punishment period of length zero. In this case, which occurs only when the lobby is extraordinarily strong relative to the legislature, we must invoke an ad-hoc constraint on the minimum feasible length.

On the other hand, if this expression is positive for all T , the constraint is most slack as T approaches infinity and so we are in a case similar to that of the model without lobbying where a ad-hoc renegotiation constraint determines the upper bound on the punishment length. Here, the legislative constraint outweighs concerns about provoking lobbying effort. Perhaps of most interest are intermediate cases where the optimal T is interior—that is, the punishment length optimally balances the need to punish legislators for deviating with that of not rewarding lobbies too much for provoking a dispute.

The intuition is clearest if we examine the case of perfectly patient actors, that is, let δ_L and $\delta_{ML} \rightarrow 1$. In essence, this removes the influence of the period of cheater's payoffs in which the interests of the legislature and the lobby are aligned (both do better in the defection stage) and exposes the differences between them in the dispute phase. In the limit, the derivative of the constraint with respect to T becomes

$$\left(1 - \frac{\partial \pi}{\partial \bar{e}}\right) \frac{W_{ML}(\gamma(\bar{e}), \tau^a) - W_{ML}(\gamma(\bar{e}), \tau^{tw})}{\frac{\partial \gamma}{\partial e} \{[\pi(\tau^b(\bar{e})) - \pi(\tau^a)] + T [\pi(\tau^{tw}) - \pi(\tau^a)]\}} - [\pi(\tau^{tw}) - e_{tw} - \pi(\tau^a)] \quad (13)$$

The proof of Corollary 3 shows that $(1 - \frac{\partial \pi}{\partial \bar{e}})$ is positive. \bar{e} is determined so that $W_{ML}(\gamma(\bar{e}), \tau^a) - W_{ML}(\gamma(\bar{e}), \tau^{tw})$ is always positive,²⁰ so the numerator of the first

²⁰See the discussion in the proof of Corollary 2 for a full treatment.

fraction is positive. The trade-agreement tariff is always lower than both the trade war tariff and the cheater's tariff ($\tau^b(\bar{e})$) and $\frac{\partial \gamma}{\partial e}$ is positive by Assumption 1, so the denominator is always positive. Note that the only influence of T on the entire expression is through this denominator, so the value of the expression is decreasing in T .

The second term, the lobby's gain from a break in the trade agreement, can in principle be negative for very large values of τ^a . As discussed in Section 4, the lobby's incentive constraint is satisfied as soon as τ^a is large enough to make this term zero. Since the executives have no incentive to raise τ^a above this level, this term must be at least weakly positive. Note that whenever the lobby's constraint must be satisfied by choosing τ^a such that $\pi(\tau^{tw}) - e_{tw} - \pi(\tau^a) = 0$, Expression 13 is always positive so that the optimal T is the largest possible value. Essentially, only the legislature's incentives are of concern in this case.

In the case of interest where the lobby potentially has an interest in breaking the agreement, the right-hand term is strictly positive. Here where we've taken $\delta_L \rightarrow 1$, the rate of change of the lobby's gain is constant.

Depending on the relative magnitudes, the overall expression may be positive for small T and then become negative, or it may be negative throughout. In the former case, the optimal interior T can be determined, while in the latter we must choose the shortest feasible T . The expression cannot be positive for all values of T , so it cannot be optimal to have arbitrarily long punishments when the players approach perfect patience.

Result 2. *When both the legislature and lobby are perfectly patient, the optimal punishment scheme precisely balances the future incentives of the lobby and legislature. It always lasts a finite number of periods and may be of some minimum feasible length if the influence of lobbying on legislative preferences is extraordinarily strong (i.e. $\frac{\partial \gamma}{\partial e}$ is sufficiently high).*

The key intuition for distinguishing between the situations described in Result 2 comes from examining the properties of the political process. If $\frac{\partial \gamma}{\partial e}$ is moderate, the positive term in Expression 13 is more likely to dominate in the beginning and lead to an interior value for the optimal T , whereas extremely large values for $\frac{\partial \gamma}{\partial e}$ make it more likely that the boundary case occurs. For a given effort level, this derivative

will be smaller when the lobby is less influential; that is, when a marginal increase in e creates a smaller increase in the legislature's preferences. Thus when the lobby is less powerful ($\frac{\partial \gamma}{\partial e}$ is smaller), longer punishments are desirable. If the lobby is very influential, the same length of punishment will have a larger impact on the legislature's decisions (the impact on the gain accruing to the lobby does not change). This tips the balance in favor of shorter punishments.

This intuition generalizes for all (δ_{ML}, δ_L) as in Expression (12). Here the second-order condition is more complicated and can be positive if $\frac{\partial \gamma}{\partial e}$ is very small. That is, if the lobby has very little influence in the legislature, it is conceivable that welfare will be maximized by making T arbitrarily large (subject, of course, to other concerns about long punishments).

Result 3. *If non-trivial cooperation is possible in the presence of a lobby, the optimal punishment scheme is finite when the influence of lobbying on legislative preferences is sufficiently strong ($\frac{\partial \gamma}{\partial e}$ is sufficiently high).*

This helps to complete the comparison to the standard repeated-game model without lobbying. There, grim-trigger (i.e. infinite-period) punishments are most helpful for enforcing cooperation (cfr. KRW's Proposition 4). I have shown here that the addition of lobbies makes shorter punishments optimal in many cases. This is because long punishments incentivize the lobby to exert more effort to break trade agreements.

However, the model with no lobbies and one with very strong lobbies can be seen as two ends of a spectrum parameterized by the strength of the lobby. The optimal punishment will lengthen as the political influence of the lobby wanes and the desire to discipline the legislature becomes more important relative to the need to de-motivate the lobby.

6. Repeated Game Enforcement

6.1. Nash Reversion Punishments

I now turn to a full description of the strategies and incentives for the equilibrium that has been analyzed in the preceding sections—that is, when the punishment is Nash reversion for a limited number of periods. Again, this is a symmetric equilibrium, so

I describe strategies for the home country only; similar conditions hold for the foreign country.

In the first period of the game, in any period following a period when the trade agreement has been adhered to, after the successful completion of a punishment, or after a violation of the punishment by the lobby, the lobby chooses $e_b = 0$ and the legislature chooses to abide by the agreement. In the applied tariff stage, the lobby chooses e_a and the legislature chooses τ^a as the applied tariff.

In any period t in which a violation of the agreement occurred $j+1$ periods previous for $j \in [0, T-1]$ with Nash reversion punishments initiated $j < T$ periods previous and followed in every period until t , the lobby chooses $e_p \geq e_{tw}$ and the legislature chooses a tariff at least as large as its unilateral best response given e_p .

In any non-cooperative period in which the legislature does not follow its prescribed action, a new punishment phase is started. That is, the strategies prescribe that the lobby chooses $e_p \geq e_{tw}$ and the legislature chooses a tariff at least as large as its unilateral best response given e_p for T periods.

In any non-cooperative period in which the lobby does not follow its prescribed action, a new cooperative phase is started. That is, the lobby chooses $e_b = 0$ and the legislature chooses to abide by the agreement. In the applied tariff stage, the lobby chooses e_a and the legislature chooses τ^a as the applied tariff.

Having fully described the strategies accompanying this punishment scheme, it must be shown that they constitute a subgame perfect equilibrium equilibrium, i.e. that each player's strategy constitutes a best response in every subgame. Recall that payoffs are independent of the trading partner's tariff level, so while checking incentives in the home country it can be assumed that players in foreign play their equilibrium strategies.

Section 3 establishes that the cooperative-phase behavior is incentive compatible for both the lobby and legislature given T-period Nash reversion punishment. Thus here we must show that it is incentive compatible to play the Nash-reversion punishments given the rest of the scheme. This will be accomplished in two phases: first by showing that the punishments are incentive compatible, and then by demonstrating the same for the punishments for deviating from the punishments.

First examine the incentives for the legislature to adhere to the punishment. La-

being the best deviation tariff as τ^D , the incentive constraint in the first period of a punishment phase is

$$\begin{aligned} W(\gamma(e_{tw}), \tau^{tw}) + \frac{\delta_{ML} - \delta_{ML}^T}{1 - \delta_{ML}} W(\gamma(e_{tw}), \tau^{tw}) + \delta_{ML}^T W(\gamma(e_a), \tau^a) \geq \\ W(\gamma(e_{tw}), \tau^D, \tau^{*tw}) + \frac{\delta_{ML} - \delta_{ML}^T}{1 - \delta_{ML}} W(\gamma(e_{tw}), \tau^{tw}) + \delta_{ML}^T W(\gamma(e_{tw}), \tau^{tw}) \end{aligned} \quad (14)$$

In order to ensure that this condition holds, I assume that the median legislator prefers the trade agreement outcome to the trade war outcome:

Assumption 3. $W(\gamma(e_a), \tau^a) \geq W(\gamma(e_{tw}), \tau^{tw})$

If Assumption 3 is violated, both the lobby and the legislature prefer the punishment and it will not be possible to enforce cooperation. Since τ^{tw} is the legislature's one-shot best response to e_{tw} , there is no profitable deviation for the legislature given that it has no interest in creating a delay in completing the punishment. By the same logic, the legislature has no incentive to deviate in later portions of the punishment, as re-starting the punishment then would create a longer delay in returning to cooperation.

The lobby's condition for adhering to the punishment has the same structure:

$$\begin{aligned} \pi(\tau^{tw}) - e_{tw} + \frac{\delta_L - \delta_L^T}{1 - \delta_L} [\pi(\tau^{tw}) - e_{tw}] + \delta_L^T [\pi(\tau^a) - e_a] \geq \\ \pi(\tau^R(e_D)) - e_D + \frac{\delta_L - \delta_L^{T+1}}{1 - \delta_L} [\pi(\tau^a) - e_a] \end{aligned} \quad (15)$$

Since net profits are maximized at (e_{tw}, τ^{tw}) , this condition always holds. Any current period deviation creates a loss, and this only serves to create additional losses in the future. The size of the loss is the same in each period so the total loss grows with the number of periods in which the trade war tariff is replaced by the trade agreement tariff. This constraint is therefore tightest in the last period of the punishment but clearly holds for any T and at all points within a T -length punishment

There is a second type of subgame that must be checked: those in which one of the players has deviated from the prescribed punishments. If the legislature deviates from the punishment, that is, chooses a tariff that is less than its best response to e_{tw} , it must be incentive compatible for the lobby to exert e_{tw} in the next period to restart the punishment. The structure of incentives is exactly the same as in Expression 15.

Since it has been shown that Expression 15 holds for all $j \in [1, T]$, the abiding by the punishment is incentive compatible for the lobby.

Similarly, the legislature's constraint for abiding by the punishment is almost identical to Expression 14. Only the trade war effort level in the current period payoffs should be replaced by the deviation-from-the-punishment effort level. The logic is the same: the legislature can do no better than its instruction to best respond in the current period, and it would not want to deviate and take a loss in the present period because this only causes future losses. This condition also holds for all $j \in [1, T]$ so incentive compatibility for the legislature is ensured. Thus the posited equilibrium supported by T-length Nash reversion punishments is subgame perfect.

6.2. Alternative Punishments

The above-explored symmetric Nash-reversion punishments are of course not the only possible punishments. This section explores an asymmetric punishment scheme in which welfare is reduced for both the legislature and the lobby in the defecting country. Although this type of punishment is not hard to find in practice, it is shown here that it allows for increased cooperation in the form of lower trade agreement tariffs.

- For now, even though it's not realistic, leave punisher at τ^{tw} so that previous analysis for symmetric case Nash reversion goes through
- Have cheater go to $\tau = 0$ in part (2) of equilibrium construction
 - It's not clear if there is an air-tight restriction on e_{tw} . Leg's condition would be easy if $e_{tw} = 0$, so going to go with that
- Before worrying about punishment for punishment, go back to TA structure
 - For legislature:

$$\frac{\delta_{ML} - \delta_{ML}^{T+1}}{1 - \delta_{ML}} \left[W_{ML}(\gamma(e_b), \tau^a) - W_{ML}(\gamma(e_b), 0, \tau^{*tw}) \right] \geq W_{ML}(\gamma(e_b), \tau^b(e_b), \tau^{*a}) - W_{ML}(\gamma(e_b), \tau^a) \quad (16)$$

- * Want to show whether or not this punishment can support lower τ^a
- * Only thing that changed from main construction is τ^{tw} to 0 in second term
- * For a given τ^a ,

$$\frac{\partial \bar{e}}{\partial \tau^p} = - \frac{\frac{\partial \Omega}{\partial \tau^p}}{\frac{\partial \Omega}{\partial \bar{e}}} = - \frac{- \frac{\delta_{ML} - \delta_{ML}^{T+1}}{1 - \delta_{ML}} \frac{\partial}{\partial \tau^p} W_{ML}(\gamma(e_b), \tau^p, \tau^{*tw})}{(-)} = \frac{\frac{\delta_{ML} - \delta_{ML}^{T+1}}{1 - \delta_{ML}} \frac{\partial}{\partial \tau^p} W_{ML}(\gamma(e_b), \tau^p, \tau^{*tw})}{(-)}$$

- \bar{e} is always \geq both τ^{tw} and 0, so reducing τ^p reduces this welfare term. Then overall, reducing τ^p raises \bar{e}
 - Intuition: punishment gets worse, so have to pay more for a break for any given τ^a
- Lobby no longer wants “trade war” (really, punishment period). Only thing they can want is break tariff for one period. Then punishment punishes lobby too

$$0 \geq [\pi(\tau^b(\bar{e})) - \bar{e}] - \pi(\tau^a) + \frac{\delta_L - \delta_L^{T+1}}{1 - \delta_L} [\pi(\tau^{tw}) - e_{tw} - \pi(\tau^a)] \quad (17)$$

becomes

$$0 \geq [\pi(\tau^b(\bar{e}')) - \bar{e}'] - \pi(\tau^{a'}) + \frac{\delta_L - \delta_L^{T+1}}{1 - \delta_L} [\pi(0) - \pi(\tau^{a'})] \quad (18)$$

- * We know from above that starting at the τ^a that's optimal when the punishment is τ^n , \bar{e} goes up when punishment tariff drops to 0. Then net profits (first bracketed term) goes down. The reasoning is as follows: net profits are largest at $\bar{e} = e_{tw}$. When $\tau^p = \tau^{tw}$, we know $\bar{e} \geq e_{tw}$. When $\tau^p = 0$, \bar{e} still $\geq e_{tw}$, but there is slack in the condition so that we could have a lower τ^a than the one that leads to e_{tw} . But this is talking about initial impact, and as long as $\bar{e} \geq e_{tw}$ and e goes up, net profits must decrease.
- * For now we're holding τ^a constant so the profit at τ^a term stays the same
- * The last bracketed term goes from positive in Expression 9 to negative in Expression ??

- * So the whole right side of Expression ?? becomes negative. There is thus slack that can be exploited to reduce τ^a .
- * Reducing τ^a will tighten up the condition via the last two terms. It's not clear what happens with net profits because the (τ^a, \bar{e}) correspondence is concave. It may give additional slack, or it may slow you down a little.
- To truly compare, have to assume we're at an interior for both (although entirely possible that whichever is higher may be on boundary and other is interior)
 - * **If the lobby's constraint loosens, does it do so everywhere?**
 - * $\frac{\partial \bar{e}}{\partial \tau^a}$ **concave seems to complicate the analysis**
 - I've verified that it remains concave for this punishment scheme: it looks like Lemmas 1 and 2 could reverse because the denominator could be positive, but this requires $f(\delta) [\pi(\tau^a) - \pi(0)] > \pi(\tau^b) - \pi(\tau^a)$. But since $\pi(\tau^b) - \pi(\tau^a) > \pi(\tau^b) - e_b - \pi(\tau^a)$, we can put the two together and see that in this case the lobby's constraint is violated. So Lemmas 1 and 2 hold as for the τ^{tw} punishment.
 - * If there is slack, can we for sure lower τ^a ?

- Punishment

- Lobby doesn't want to deviate
- Legislature would want to go to $\tau^D(0)$.
 - * Punish with $e = 0$, $\tau > \tau^D(0)$ (needs to be higher so that lobby likes it)
- **need to make sure payoffs for all of these are lower than eqm payoff for punisher**

7. Conclusion

I have integrated a separation-of-powers policy-making structure with lobbying into a theory of recurrent trade agreements. This theory takes seriously the idea that

the threat of renegotiation can undermine punishment when cooperation is meant to be enforced through repeated interaction alone. Assuming that countries can bind themselves to condition their negotiations on the state designation of a dispute settlement institution allows punishments to become incentive compatible.

I have shown here that, given no uncertainty about the outcome of the lobbying and political process, the executives maximize social welfare by choosing the lowest tariffs that make it unattractive for the lobbies to exert effort toward provoking a trade dispute. Although there are no disputes in equilibrium in this simple model, this extra constraint added by the lobby—apparently out-of-equilibrium—plays a key role in the determination of the optimal tariff levels and in the optimal dispute settlement procedure. While the constraint on the key repeated-game player, which here is the legislature, is loosened by increasing the punishment length, this new constraint due to the presence of lobbying becomes tighter as the punishment becomes more severe. This happens because the lobby *prefers* punishment periods in which tariffs, and thus its profits, are higher. It thus has increased incentive to exert effort as the punishment lengthens.

In a model with only the legislature, welfare increases with the punishment length. Here, this result only occurs if the lobby is sufficiently weak. As the lobby's political influence grows, the optimal punishment length becomes shorter—in the race between incentivizing the legislature and the lobby, the need to de-motivate the lobby begins to win. This suggests that a key consideration when designing the length of dispute settlement procedures is how to optimally balance the incentives of those capable of breaking trade agreements with the political forces who influence them, *given* the strength of that influence.

Future work is planned in at least two, related directions. In order for disputes to occur in equilibrium, I will add political uncertainty to the model as in Buzard (2014*b*) (alternatively, asymmetric information could be introduced, or possibly both). The model will then be able to address questions about the impact of political uncertainty on trade agreements and optimal dispute resolution mechanisms.

It will also be possible to explore whether accounting for the endogeneity of political pressure can explain the observed variation in the outcomes of dispute settlement

cases (Busch and Reinhardt (2006)) because, in this context, it becomes meaningful to ask when lobbies have the incentive to exert effort to perpetuate a dispute (hence removing the ad-hoc assumption imposed in the proof of Corollary 1 that the trade agreement tariff is always low enough to incentivize the lobby to exert effort during the trade war). Once political uncertainty has been added to the model, this is a completely natural extension that helps display the range and flexibility of the base model presented here.

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Appendix A. Mathematical Appendix

Proof of Lemma 1:

Labeling the left sides of Equations 10 and 11 as $\Omega(\cdot)$ and $\Pi(\cdot)$, for notational convenience, these equations can be represented as²¹

$$\Omega(\bar{e}(\delta_{ML}, \gamma, \tau^a), \delta_{ML}, \gamma, \tau^a) = 0 \quad (A.1)$$

$$\Pi(\tau^a(\delta_L, \delta_{ML}, \gamma), \bar{e}(\delta_{ML}, \gamma, \tau^a), \delta_L, \delta_{ML}, \gamma) = 0 \quad (A.2)$$

By the Implicit Function Theorem:

$$\frac{\partial \bar{e}}{\partial \tau^a} = -\frac{\frac{\partial \Omega}{\partial \tau^a}}{\frac{\partial \Omega}{\partial \bar{e}}} = -\frac{\left[1 + \frac{\delta_{ML} - \delta_{ML}^{T+1}}{1 - \delta_{ML}}\right] \frac{\partial}{\partial \tau^a} W_{ML}(\gamma(\bar{e}), \tau^a)}{\frac{\delta_{ML} - \delta_{ML}^{T+1}}{1 - \delta_{ML}} \frac{\partial \gamma}{\partial \bar{e}} [\pi(\tau^a) - \pi(\tau^{tw})] - \frac{\partial \gamma}{\partial \bar{e}} [\pi(\tau^b(\bar{e})) - \pi(\tau^a)]} \quad (A.3)$$

In order for the lobby's incentive constraint (Equation 11) to hold in equilibrium, \bar{e} must be at least as large as e_{tw} . Since the executives have no incentive to set the trade agreement tariff above the trade war tariff, this means that $\tau^a \leq \tau^{tw} \leq \tau^b$. Therefore \bar{e} will be set so that the median legislator's ideal point is (weakly) to the right of τ^a , implying that the numerator is (weakly) positive.

Turning to the denominator, γ is assumed increasing in e so $\frac{\partial \gamma}{\partial \bar{e}}$ is positive. Both profit differences are negative since $\tau^a \leq \tau^{tw} \leq \tau^b$. Therefore the denominator is negative.²² Combined with the positive numerator and the leading negative sign, the expression is positive. ■

Proof of Lemma 2:

By the Implicit Function Theorem:

$$\frac{\partial \bar{e}}{\partial \tau^a} = -\frac{\frac{\partial \Omega}{\partial \tau^a}}{\frac{\partial \Omega}{\partial \bar{e}}} = -\frac{\frac{\delta_{ML} - \delta_{ML}^{T+1}}{1 - \delta_{ML}} \frac{\partial}{\partial \tau^a} W_{ML}(\gamma(\bar{e}), \tau^a)}{\frac{\delta_{ML} - \delta_{ML}^{T+1}}{1 - \delta_{ML}} \frac{\partial \gamma}{\partial \bar{e}} [\pi(\tau^a) - \pi(\tau^{tw})] - \frac{\partial \gamma}{\partial \bar{e}} [\pi(\tau^b(\bar{e})) - \pi(\tau^a)]}$$

²¹Note that all expressions also depend on the fundamentals of the welfare function— D, Q_X, Q_Y —but these are suppressed for simplicity.

²²Note that when $\tau^a = \tau^{tw} = \tau^b$, only the trivial trade agreement is possible and so this result and those that build upon it are not of interest.

The numerator is negative since the median legislator's welfare decreases in the foreign tariff (note that two other terms in the numerator cancel each other). The denominator is shown to be negative in the proof of Lemma 1. Combined with the negative numerator and the leading negative sign, the expression is negative. ■

Proof of Corollary 1:

By the Implicit Function Theorem:

$$\frac{\partial \tau^a}{\partial \delta_L} = - \frac{\frac{\partial \Pi}{\partial \delta_L}}{\frac{\partial \Pi}{\partial \tau^a}} = \frac{\frac{1-(T+1)\delta_L^T + T\delta_L^{T+1}}{(1-\delta_L)^2} [\pi(\tau^{tw}) - e_{tw} - \pi(\tau^a)]}{\frac{\partial \bar{e}(\tau^a)}{\partial \tau^a} + \frac{\partial \pi(\tau^a)}{\partial \tau^a} + \frac{\delta_L - \delta_L^{T+1}}{1-\delta_L} \frac{\partial \pi(\tau^a)}{\partial \tau^a}} \quad (\text{A.4})$$

First I will show that $\frac{1-(T+1)\delta_L^T + T\delta_L^{T+1}}{(1-\delta_L)^2}$ is positive. Focusing on the numerator and rearranging, we have

$$\begin{aligned} 1 - (T+1)\delta_L^T + T\delta_L^{T+1} &= (1 - \delta_L^T) - T\delta_L^T(1 - \delta_L) = (1 - \delta_L) \sum_{i=0}^{T-1} \delta_L^i - T\delta_L^T(1 - \delta_L) \\ &= (1 - \delta_L) \left[\left(\sum_{i=0}^{T-1} \delta_L^i \right) - T\delta_L^T \right] = (1 - \delta_L) \left[\sum_{i=0}^{T-1} \delta_L^i - \delta_L^T \right] > 0 \text{ for all } \delta_L < 1. \end{aligned}$$

Therefore $\frac{1-(T+1)\delta_L^T + T\delta_L^{T+1}}{(1-\delta_L)^2}$ is positive.

The bracketed term must be positive in order for the lobby to have the incentive to lobby in the trade-war phase. I assume that this is the case, as all the results of this section are not interesting for any trade agreement for which it is violated. See the conclusion for discussion of a planned extension that more fully explores the trade-war phase.

Lemma 1 established that $\frac{\partial \bar{e}(\tau^a)}{\partial \tau^a}$ is positive, and profits are increasing in τ^a , so the other two terms in the denominator are positive. The denominator is the sum of three positive terms and so positive itself. Since both terms in the numerator have already been shown to be positive, $\frac{\partial \tau^a}{\partial \delta_L}$ is positive. ■

Proof of Corollary 2:

By the Implicit Function Theorem:

$$\frac{\partial \bar{e}}{\partial \delta_{ML}} = -\frac{\frac{\partial \Omega}{\partial \delta_{ML}}}{\frac{\partial \Omega}{\partial \bar{e}}} = -\frac{\frac{1-(T+1)\delta_{ML}^T + T\delta_{ML}^{T+1}}{(1-\delta_{ML})^2} [W_{ML}(\gamma(\bar{e}), \tau^a) - W_{ML}(\gamma(\bar{e}), \tau^{tw})]}{\frac{\delta_{ML}-\delta_{ML}^{T+1}}{1-\delta_{ML}} \frac{\partial \gamma}{\partial \bar{e}} [\pi(\tau^a) - \pi(\tau^{tw})] - \frac{\partial \gamma}{\partial \bar{e}} [\pi(\tau^b(\bar{e})) - \pi(\tau^a)]} \quad (\text{A.5})$$

I have shown in the proof of Corollary 1 that the first term in the numerator is positive. The bracketed term is positive because \bar{e} is always determined via Equation 10 so that $W_{ML}(\gamma(\bar{e}), \tau^a) - W_{ML}(\gamma(\bar{e}), \tau^{tw})$ is positive: the trade-war tariff is the punishment relative to the trade agreement tariff. Therefore the numerator of the fraction is positive. The denominator is shown to be negative in the proof of Lemma 1. Therefore $\frac{\partial \bar{e}}{\partial \delta_{ML}}$ is positive. ■

Proof of Corollary 3:

Differentiating Equation A.2 with respect to δ_{ML} , we have

$$\frac{\partial \Pi}{\partial \tau^a} \frac{\partial \tau^a}{\partial \delta_{ML}} + \frac{\partial \Pi}{\partial \bar{e}} \frac{\partial \bar{e}}{\partial \delta_{ML}} + \frac{\partial \Pi}{\partial \delta_{ML}} = 0$$

There is no direct effect of δ_{ML} on this equation, so $\frac{\partial \Pi}{\partial \delta_{ML}} = 0$. Thus

$$\frac{\partial \tau^a}{\partial \delta_{ML}} = -\frac{\frac{\partial \Pi}{\partial \bar{e}} \frac{\partial \bar{e}}{\partial \delta_{ML}}}{\frac{\partial \Pi}{\partial \tau^a}} = -\frac{\left(1 - \frac{\partial \pi}{\partial \bar{e}}\right) \cdot \frac{\partial \bar{e}}{\partial \delta_{ML}}}{\frac{\partial \bar{e}(\tau^a)}{\partial \tau^a} + \frac{\partial \pi(\tau^a)}{\partial \tau^a} + \frac{\delta_L - \delta_L^{T+1}}{1 - \delta_L} \frac{\partial \pi(\tau^a)}{\partial \tau^a}} \quad (\text{A.6})$$

The total effect of \bar{e} on Π is the negative of the lobby's FOC, that is

$$\frac{\partial}{\partial \bar{e}} [\bar{e} - \pi(\tau^b(\bar{e}))] = 1 - \frac{\partial \pi}{\partial \bar{e}} = -\left(\frac{\partial \pi}{\partial \bar{e}} - 1\right).$$

The lobby's FOC decreases to the right of e_{tw} since e_{tw} is the optimum ($\frac{\partial \pi}{\partial \bar{e}} = 1$ at $e = e_{tw}$). Since we must have $\bar{e} \geq e_{tw}$ in equilibrium in order for the lobby's constraint to bind, the effect of \bar{e} on Π is positive. In addition, $\frac{\partial \bar{e}}{\partial \delta_{ML}}$ is positive by Corollary 2, so the numerator is positive.

By the same argument as in the proof of Corollary 1, the denominator is positive. Since there is a leading negative sign, $\frac{\partial \tau^a}{\partial \bar{e}(\delta_{ML})}$ is negative. ■

Proof of Corollary 4:

By the Implicit Function Theorem:

$$\frac{\partial \bar{e}}{\partial \gamma} = -\frac{\frac{\partial \Omega}{\partial \gamma}}{\frac{\partial \Omega}{\partial \bar{e}}} = -\frac{\frac{\delta_{ML}-\delta_{ML}^{T+1}}{1-\delta_{ML}}[\pi(\tau^a)-\pi(\tau^{tw})]-[\pi(\tau^b(e_b))-\pi(\tau^a)]}{\frac{\delta_{ML}-\delta_{ML}^{T+1}}{1-\delta_{ML}}\frac{\partial \gamma}{\partial \bar{e}}[\pi(\tau^a)-\pi(\tau^{tw})]-\frac{\partial \gamma}{\partial \bar{e}}[\pi(\tau^b(e_b))-\pi(\tau^a)]} \quad (A.7)$$

keeping in mind that the numerator is simplified by the envelope theorem. We can factor $\frac{\partial \gamma}{\partial \bar{e}}$ out of the denominator and cancel the rest, leaving $-\frac{1}{\frac{\partial \gamma}{\partial \bar{e}}} < 0$. ■

Proof of Corollary 5:

Differentiating the lobby's condition, Equation A.2 with respect to γ , we have

$$\frac{\partial \Pi}{\partial \tau^a} \frac{\partial \tau^a}{\partial \gamma} + \frac{\partial \Pi}{\partial \bar{e}} \frac{\partial \bar{e}}{\partial \gamma} + \frac{\partial \Pi}{\partial \gamma} = 0$$

Because $\frac{\partial \Pi}{\partial \gamma} = 0$, we are looking for

$$\frac{\partial \tau^a}{\partial \gamma} = -\frac{\frac{\partial \Pi}{\partial \bar{e}} \frac{\partial \bar{e}}{\partial \gamma}}{\frac{\partial \Pi}{\partial \tau^a}} = -\frac{\left(1 - \frac{\partial \pi}{\partial \bar{e}}\right) \cdot \frac{\partial \bar{e}}{\partial \gamma}}{\frac{\partial \bar{e}(\tau^a)}{\partial \tau^a} + \frac{\partial \pi(\tau^a)}{\partial \tau^a} + \frac{\delta_L - \delta_L^{T+1}}{1 - \delta_L} \frac{\partial \pi(\tau^a)}{\partial \tau^a}} \quad (A.8)$$

As shown in Corollary 4, $\frac{\partial \bar{e}}{\partial \gamma}$ is negative, whereas Corollary 3 shows that $\left(1 - \frac{\partial \pi}{\partial \bar{e}}\right)$ is positive. The arguments given in the proof of Corollary 1 show that the denominator is positive. Therefore $\frac{\partial \tau^a}{\partial \gamma}$ is positive. ■