

1 Dixit, Grossman and Helpman analogy

DGH97 paper:

- Has to be a truthful contribution schedule

- Proposition 3: $G(a^0, e^T(a^0, u^0)) = \max_a G(a, 0)$
- $e^T(a^0, u^0)$ is essentially $\phi(a^0, u^0)$, which is defined implicitly in eqn3 (p. 760) as

$$U[a, \phi(a^0, u^0)] = u^0$$

- * Careful: truthful contribution schedule is not a best response function. But the lobby will still have to be best responding in equilibrium.
- * Truthful contribution schedule is a device for solving equilibrium in their model. Doesn't mean I have to follow it (I think; I hope)
- if $G = W + g(e)$ and $e = 0$ and $g(0) = 0$, then $a^* = \tau^{\text{opt}}$
- Then rewrite as

$$G(\tau^0, e^T(\tau^0, u^0)) = \max_a G(\tau^{\text{opt}}, 0)$$

- * Right hand side provides a number
- * Ignoring arguments of e^T function, LHS traces out (τ, e) pairs that satisfy the equation given $g(e)$.
- * For lobby to be best responding, it MUST pick the pair that maximizes $\pi(\tau) - e$. *This* concern must be what sets u^0 .
- Corollary to Prop 1 / Prop 3: Gov't gets utility equal to outside option. Is this true when there is just one lobby?
- Combining the two previous facts (if true in my case), then it must be that gov't getting outside option will set u^0 (eqm utility) and anchor contribution schedule (just have to be careful of zero contributions)

What editor proposes:

- Lobby offers contribution schedule (can be very simple: just one (e, τ) pair, $e = 0$ for everything else)

- Government maximizes $W + g(e)$

– Note that $CS_X + \gamma(e) \cdot PS_X + CS_Y + PS_Y + TR = W + (\gamma(e) - 1) PS_X$

- Sectioning from my paper:

3.1 Same (execs)

3.2 Trade war

- * Government chooses unilateral τ as $\frac{\partial W}{\partial \tau} + \frac{\partial g(e)}{\partial \tau} = 0$

- How to think about lobby's contribution schedule?
- DGH Proposition 1: principal (lobby) has to provide at least agent's (gov'ts) outside option; as long as this constraint is satisfied, lobby can propose τ and payment that maximizes his own utility
- DGH Proposition 3 (p. 760-61): simplifies so we don't need to look for contribution functions, only eqm values

Comparisons

- Note that in GH94, claim is that IN EQUILIBRIUM, government behaves as if it maximizes a weighted sum of the groups' utilities ($1 + a$ for those represented by lobbies; a for those not represented; pg. 10 of PDF). But this is in equilibrium: there's a lot going on out of equilibrium that leads us there!

– I haven't proved this to myself, but that must also depend on lobbies having all the bargaining power

- In DGH, $G(\tau^0, e^0) = \max_{\tau}(\tau, 0)$

– This is not generally true in my model

– I think the slippage is in bargaining power. DGH paradigm assumes lobby essentially make TIOLI offer.

– $\gamma(e)$ formulation in essence distributes bargaining power more generally

* Is it okay to characterize it this way?

* If so, does bargaining power vary with effort? Seems mixed up with diminishing returns to effort.

– $W + \Phi(e)$ of Limao and Tovar gives decreasing returns; then explicitly models bargaining power through Nash bargain instead of menu auction (as far as I can tell—I can't find it clearly specified).

- In DGH, essentially lobby chooses its favorite (τ, e) pair from among all the possible ones that make the Gov't indifferent.
 - Is it possible that this is equivalent to $\frac{\partial \pi}{\partial e} = 1$?
 - seems like the pair that satisfies that equation might not be available
 - When I calculate the various (τ, e) pairs to 'compare' government welfare levels, this comes from the government welfare function: each e induces an optimal τ and then I get an optimal value function
 - * Lobby doesn't care about these varying welfare levels. Chooses (τ, e) pair that maximizes $\pi - e$

Examples

- Use numeric example from BS2005 in R (DGH.r)
- Isomorphism I've already calculated: if $G = W + e$ then $\gamma(e) = 1 + \frac{e}{\pi_x}$
- Lobby's optimization:

$$W(\tau, e(\tau)) = W(0, 0)$$

$$W(\tau) + e = W(0)$$

$$e = W(0) - W(\tau)$$

- This forms a contribution schedule
- Lobby chooses the pair (τ, e) that maximizes $\pi(\tau) - e$
- Make sure these are unilateral changes in τ in the program
- Then compare to my old way: $\frac{\partial \pi}{\partial \tau} \frac{\partial \tau}{\partial \gamma} \frac{\partial \gamma}{\partial e} = 1$ (e changes with τ directly depending on shape of γ , then government maximizes w.r.t. τ)
 - NEXT: go into R program and sort it out