```
MÉTODOS ESTADÍSTICOS
Nombre(s): Equipo 4:

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     José Juan García Romero
Nº 20
         Descripción:
         La base de datos UsingR::brightness cuenta con el registro de la brillantez
         de 966 estrellas. Aplicando el concepto BootStrap, inferir la media de la
         población realizando:
a) 3 muestras simples de tamaño 50, 300, 600
   Actividad 20.R >
   🛑 🖈 📗 🔚 💼 Source on Save 🛚 🥄 🥕 🗸 📳
        # Diana Zepeda Martinez
# José Juan García Romero
         library(boot)
      5
         library(dplyr)
      6
      9
        brillo = UsingR::brightness
     10 mediaP = mean(brillo)
     11
     12
         muestra1 = sample(brillo,replace = T,size = 50)
        media1 = mean(muestra1)
     13
     14
     15
         muestra2 = sample(brillo,replace = T,size = 300)
     16
        media2 = mean(muestra2)
     17
     18 muestra3 = sample(brillo,replace = T,size = 600)
     19
        media3 = mean(muestra3)
     20
         medias = rbind(mediaP, media1, media2, media3)
     21
     22
         medias
     23
   Console
            Terminal ×
                        Jobs
   R 4.1.3 ~/Universidad/Métodos Estadisticos/R/ 
   > # Diana Zepeda Martinez
   > # José Juan García Romero
     # INCISO A
     library(boot)
   > library(dplyr)
   > brillo = UsingR::brightness
   > mediaP = mean(brillo)
   > muestra1 = sample(brillo,replace = T,size = 50)
   > media1 = mean(muestra1)
   > muestra2 = sample(brillo,replace = T,size = 300)
   > media2 = mean(muestra2)
   > muestra3 = sample(brillo,replace = T,size = 600)
   > media3 = mean(muestra3)
> medias = rbind(mediaP, media1, media2, media3)
   > medias
                 [,1]
   mediaP 8.417743
   media1 8.508200
   media2 8.378333
```

media3 8.373267

```
medias
                                    num [1:4, 1] 8.42 8.37 8.4 8.39
Values
                                     num [1:966] 9.1 9.27 6.61 8.06 8.55 ...
  media1
                                    8.3702
                                    8.40246666666667
  media2
  mediaP
                                    8.41774327122153
                                    num [1:50] 5.78 7.09 8.01 9.99 9.06 8.24 8.27 8.31 8.11 7.46 ... num [1:300] 9.77 6.18 9.05 8.56 8.75 ...
  muestra1
  muestra2
  muestra3
                                    num [1:600] 8.33 9.37 8.77 10.82 7.91 ...
```

b) Implementando una función obtener 200 muestras

```
24
    # Diana Zepeda Martinez
25
26
   # INCISO B
27
    medias = NULL
28
29 v for(i in 1:200){
      muestra = sample(brillo, replace = T)
30
      medias[i] = mean(muestra)
31
32 - }
33
34 mediaP
35 muestra200 = mean(medias)
36
   muestra200
37
Console
         Terminal \times
                    \mathsf{Jobs} \times
```

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```
> # Diana Zepeda Martinez
> # José Juan García Romero
```

> # INCISO B

```
> medias = NULL
> for(i in 1:200){
```

```
muestra = sample(brillo, replace = T)
```

medias[i] = mean(muestra)

> mediaP

```
[1] 8.417743
```

> muestra200 = mean(medias)

> muestra200

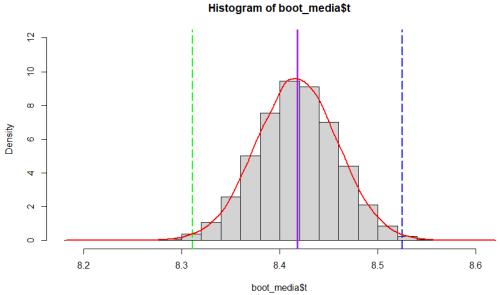
[1] 8.413804

```
Values
 brillo.
                                   num [1:966] 9.1 9.27 6.61 8.06 8.55 ...
                                   200L
  media1
                                   8.3702
                                   8.4024666666667
                                   8.3886
  media3
  mediaP
                                   8.41774327122153
                                  num [1:200] 8.43 8.5 8.47 8.38 8.4 ...
num [1:966] 9.16 7.96 8.3 8.76 8.55 8.8 7.78 8.34 8.27 8.95 ...
  medias
  muestra
                                  num [1:50] 5.78 7.09 8.01 9.99 9.06 8.24 8.27 8.31 8.11 7.46 ...
  muestra1
  muestra2
                                   num [1:300] 9.77 6.18 9.05 8.56 8.75 ...
  muestra200
                                   8.41309922360248
                                   num [1:600] 8.33 9.37 8.77 10.82 7.91 ...
  muestra3
```

c) Con la función boot:
 c.1) obtener 100,000 réplicas
 c.2) obtener sus intervalos de confianza al 99%
 c.3) graficar las medias de las réplicas obtenidas en el c.1 y los
intervalos del c.3

```
38
    # José Juan García Romero
# INCISO C
39
40
    library(boot)
41
42
43 • func_media <- function(m,d){ # v:datos d:indice
44
       (mean(m[d]))
45 -
46
   boot_media <- boot(brillo, func_media, R = 100000)</pre>
47
48 media_boot <- mean(boot_media$t)
49 media_pob <- boot_media$t0
50
    tabla = rbind(media_pob,media_boot)
     tabla
51
52
53
54
     IC <- boot.ci(boot_media,conf = 0.99,type = "norm")</pre>
55
56
     IC
57
58
    # INCISO C3
59
60
    hist(boot_media\$t,freq = F,ylim = c(0,12))
    abline(v = boot_media$t0,col = "purple",lwd = 3)
abline(v = IC$normal[2],col = "green",lwd = 2,lty = 5)
abline(v = IC$normal[3],col = "blue",lwd = 2,lty = 5)
61
62
63
     lines(density(boot_media$t),col = "red",lwd = 2)
64
65
66
```

```
Console Terminal ×
                       Jobs
🕟 R 4.1.3 - ~/Universidad/Métodos Estadisticos/R/ 🖈
   # Diana Zepeda Martinez
> # José Juan García Romero
> # INCISO C
> # INCISO C1
> # Diana Zepeda Martinez
  # José Juan García Romero
> # INCISO C
> library(boot)
> func_media <- function(m,d){ # v:datos d:indice
      (mean(m[d]))
> boot_media <- boot(brillo, func_media, R = 100000)
> media_boot <- mean(boot_media$t)</pre>
> media_pob <- boot_media$t0
> tabla = rbind(media_pob,media_boot)
> tabla
[,1]
media_pob 8.417743
media_boot 8.417947
> # INCISO C2
> IC <- boot.ci(boot_media,conf = 0.99,type = "norm")</pre>
BOOTSTRAP CONFIDENCE INTERVAL CALCULATIONS
Based on 100000 bootstrap replicates
boot.ci(boot.out = boot_media, conf = 0.99, type = "norm")
Intervals:
               Normal
99% (8.310, 8.525)
Calculations and Intervals on Original Scale
> # INCISO C3
> hist(boot_media$t,freq = F,ylim = c(0,12))
> abline(v = boot_media$t0,col = "purple",lwd = 3)
> abline(v = IC$normal[2],col = "green",lwd = 2,lty = 5)
> abline(v = IC$normal[3],col = "blue",lwd = 2,lty = 5)
> lines(density(boot_media$t),col = "red",lwd = 2)
```



```
Large boot (11 elements, 839.1 kB)
boot_media
① IC
                                      List of 4
 tabla
  brillo
                                      num [1:966] 9.1 9.27 6.61 8.06 8.55 ...
  media_boot
                                      8.41777374171843
  media_pob
                                      8.41774327122153
  media1
                                      8.3702
                                      8.4024666666667
  media2
  media3
                                      8.3886
  mediaP
  medias
                                      num [1:200] 8.43 8.5 8.47 8.38 8.4 ...
                                      num [1:966] 9.16 7.96 8.3 8.76 8.55 8.8 7.78 8.34 8.27 8.95 ...
num [1:50] 5.78 7.09 8.01 9.99 9.06 8.24 8.27 8.31 8.11 7.46 ...
num [1:300] 9.77 6.18 9.05 8.56 8.75 ...
  muestra
  muestra1
  muestra2
  muestra200
                                      8.41309922360248
                                      num [1:600] 8.33 9.37 8.77 10.82 7.91 ...
  muestra3
Functions
  func_media
                                      function (m, d)
```

d) Con la función bootstrap obtener 100,000 réplicas

```
67
68
   library(bootstrap)
69
70
   function <- function(x){mean(x)}
71
72
73
   replicas_bootstrap <- bootstrap(brillo,100000,funcion)</pre>
74
   mediaP
75
   media_bootstap <- mean(replicas_bootstrap$thetastar)</pre>
76
   media_bootstap
77
Console Terminal × Jobs ×
R 4.1.3 ~/Universidad/Métodos Estadisticos/R/ 
> # Diana Zepeda Martinez
> # José Juan García Romero
> # INCISO D
> # Diana Zepeda Martinez
> # José Juan García Romero
> # INCISO D
> library(bootstrap)
> funcion <- function(x){mean(x)}
> replicas_bootstrap <- bootstrap(brillo,100000,funcion)
> mediaP
[1] 8.417743
> media_bootstap <- mean(replicas_bootstrap$thetastar)
> media_bootstap
[1] 8.417823
```

```
boot_media
                                        Large boot (11 elements, 839.1 kB)
① IC
                                       List of 4
                                       Large list (5 elements, 801.3 kB)
neplicas_bootstrap
  tabla
                                       num [1:2, 1] 8.42 8.42
Values
                                        num [1:966] 9.1 9.27 6.61 8.06 8.55 ...
  brillo.
                                       200L
  media_boot
                                       8.41777374171843
                                        8.41782250879917
  media_bootstap
  media_pob
  media1
                                       8.3702
                                       8.4024666666667
  media2
  media3
                                       8.3886
                                       num [1:200] 8.43 8.5 8.47 8.38 8.4 ...
num [1:966] 9.16 7.96 8.3 8.76 8.55 8.8 7.78 8.34 8.27 8.95 ...
num [1:50] 5.78 7.09 8.01 9.99 9.06 8.24 8.27 8.31 8.11 7.46 ...
num [1:300] 9.77 6.18 9.05 8.56 8.75 ...
  medias
  muestra
  muestra1
  muestra2
                                        8.41309922360248
  muestra200
  muestra3
                                       num [1:600] 8.33 9.37 8.77 10.82 7.91 ...
Functions
  func_media
                                        function (m, d)
  funcion
                                       function (x)
```

e) Realizar una tabla comparativa de medias y una conclusión sobre esta.

```
79
80
           82
84
86
             tabla_general
  Console Terminal × Jobs ×

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    * # Diana Zepeda Martinez
    * # José Juan García Romero
    * # INCISO E

      tabla_general = rbind(mediap,media1,media2,media3,muestra200,media_boot,media_bootstap)
rownames(tabla_general) = c("poblacion","muestra1","muestra2","muestra3","muestra200","media_boot","media_bootstap")
colnames(tabla_general) = c("medias")
tabla_general
 | medias | medias | medias | poblacion | 8.417743 | muestra1 | 8.370200 | muestra2 | 8.402467 | muestra3 | 8.388600 | muestra200 | 8.413099 | media_boot | 8.417784 | media_bootstap | 8.417823 | medi
 Data
                                                                                                      Large boot (11 elements, 839.1 kB)
boot media
① IC
oreplicas_bootstrap
                                                                                                       Large list (5 elements, 801.3 kB)
     tabla
                                                                                                      num [1:2, 1] 8.42 8.42
                                                                                                      num [1:7, 1] 8.42 8.37 8.4 8.39 8.41 ...
      tabla_general
Values
                                                                                                       num [1:966] 9.1 9.27 6.61 8.06 8.55 ...
      brillo
                                                                                                      200L
                                                                                                       8.41777374171843
      media_boot
                                                                                                       8.41782250879917
      media_bootstap
       media_pob
                                                                                                        8.41774327122153
       media1
      media2
                                                                                                       8.40246666666667
      media3
                                                                                                       8.3886
                                                                                                       8.41774327122153
      mediaP
                                                                                                      num [1:200] 8.43 8.5 8.47 8.38 8.4 ...
num [1:966] 9.16 7.96 8.3 8.76 8.55 8.8 7.78 8.34 8.27 8.95 ...
      medias
      muestra
                                                                                                       num [1:50] 5.78 7.09 8.01 9.99 9.06 8.24 8.27 8.31 8.11 7.46 ...
       muestra1
                                                                                                       num [1:300] 9.77 6.18 9.05 8.56 8.75 ...
       muestra200
                                                                                                        8.41309922360248
       muestra3
                                                                                                       num [1:600] 8.33 9.37 8.77 10.82 7.91 ...
 Functions
       func_media
       function
                                                                                                        function (x)
```

f) Describir las nuevas funciones

boot: Es la biblioteca de arranque y con esta se generan réplicas. **bootstrap:** Se obtiene la distribución del estadístico que se va a usar.

hist: Crea histogramas, gráficas, etc.

abline: Pinta líneas dentro de un histograma.

lines: pinta una línea de tendencia en el histograma.

rownames: Sirve para definir nombres de las filas de una tabla.

colnames: Sirve para definir los nombres de las columnas de una tabla. **UsingR:** Es para usar una colección de datos, en este caso brightness.

rbind: Sirve para unir varios arreglos de datos.