# SO5012 Analysising Data in the Real World Ordinal regression Solutions and commentary

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# Introduction

str(cricket)

This seminar sheet is intended as a introduction to multinomial regression and is a combination of code and interpretation for the worksheet  $SO5012\_semX\_ordinal\_regression.docx$ .

As with all the previous weeks, first we need to: 1. Set the working directory 2. Load the packages we'll be using 3. Load the data

Here we'll use the results='hide', message=FALSE command on the r chunk so that our output is not filled up by this set up code, although the code will be visible.

```
# setwd(whereeveryousavestuff)
# Note to RP - this isnt needed for a project, but you'll need to change if just posting rmd

if (!require(MASS)) install.packages("MASS")
library(MASS)

if (!require(tidyverse)) install.packages("tidyverse")
library(tidyverse)

if (!require(reshape2)) install.packages("reshape2")
library(reshape2)
cricket <- read.csv("data/cricket.csv")
```

As with each work sheet, and all analysis, we need to do basic checks on the data before starting any analysis proper.

```
## 'data.frame': 389 obs. of 17 variables:
## $ X : int 1 2 3 4 5 6 7 8 9 10 ...
```

```
: int 123 124 125 127 128 129 130 131 133 134 ...
## $ year
             : int 1960 1960 1960 1961 1961 1961 1962 1962 1962 1962 ...
              : chr "Pak" "Ind" "WI" "Ind" ...
## $ visitor : chr "Aus" "Aus" "Eng" "Pak" ...
## $ matches : int 3 5 5 5 5 5 5 5 5 5 ...
## $ winner : chr "Aus" "Aus" "Eng" "Draw" ...
## $ hrating : num -2.72 -33.33 4.07 -26.33 47.54 ...
   $ vrating : num 50.09 53.95 17.55 5.83 6.71 ...
##
   $ drating : num -52.8 -87.3 -13.5 -32.2 40.8 ...
## $ result : chr "Visitor" "Visitor" "Visitor" "Draw" ...
## $ period : chr "1960-69" "1960-69" "1960-69" "1960-69" ...
## $ per_60_69: int 1 1 1 1 1 1 1 1 1 1 ...
## $ per_70_79: int 0 0 0 0 0 0 0 0 0 ...
## $ per_80_89: int 0 0 0 0 0 0 0 0 0 ...
## $ per_90_02: int 0 0 0 0 0 0 0 0 0 ...
## $ per_02on : int 0 0 0 0 0 0 0 0 0 ...
# we see that home, visitor, winner, result and period are character vectors.
# Lets convert them into factors.
factorvars <- c("home", "visitor", "winner", "result", "period")</pre>
for (v in factorvars) {
 cricket[[v]] <- as.factor(cricket[[v]])</pre>
 print(levels(cricket[[v]])) # this simply report the resulting levels
## [1] "Aus" "Eng" "Ind" "NZ" "Pak" "SA"
                                          "SL"
                                                "WI"
## [1] "Aus" "Eng" "Ind" "NZ" "Pak" "SA"
                                          "SL"
                                               "WI"
                                                      "Zim"
## [1] "Aus" "Draw" "Eng" "Ind" "NZ"
                                          "Pak" "SA"
                                                        "SL"
                                                               "WI"
                                                                      "Zim"
                          "Visitor"
## [1] "Draw"
                "Home"
## [1] "1960-69"
                    "1970-79"
                                  "1980-89"
                                                "1990-3.2002" "4.2002-"
# the result variable is currently in the wrong order, running "Draw", "Home", "Visitor"
# this needs re-levelling.
cricket$result <- factor(cricket$result, levels = c("Visitor", "Draw", "Home"))</pre>
levels(cricket$result)
```

## [1] "Visitor" "Draw" "Home"

Only now are we ready to start the questions!

# Questions and answers

# Question 1

As always, spend some time playing with the data to understand how it works. In particular, answer these following questions (HINT: you may need to do some data manipulation):

```
a. How many series were played in each year, in total?
# Each row is a series, and there is a variable related to year - so simply tabulate it!
table(cricket$year)
##
## 1960 1961 1962 1963 1964 1965 1966 1967 1968 1969 1970 1971 1972 1973 1974 1975
      3
                      2
                           1
                                6
                                      2
                                           3
                                                4
                                                      3
                                                           2
                                                                4
                                                                      2
                                                                           4
## 1976 1977 1978 1979 1980 1981 1982 1983 1984 1985 1986 1987 1988 1989 1990 1991
                      6
                           7
                                6
                                      6
                                           5
                                                7
                                                      7
                                                           8
                                                                7
## 1992 1993 1994 1995 1996 1997 1998 1999 2000 2001 2002 2003 2004 2005 2006 2007
                     10
                               14
                                     16
                                          10
                                               14
                                                     17
                                                          15
                                                               12
                                                                     17
## 2008 2009 2010 2011
##
     14
          13
                11
  b. List each country by their number of series wins
# Again, each row is a series and the winner is identified
table(cricket$winner)
##
                                     SA
                                                    Zim
    Aus Draw
              Eng
                   Ind
                          ΝZ
                              Pak
                                          SL
                                               WI
                          19
                                     30
                                          22
                                               40
     67
                     40
                               34
                                                      1
  c. How many series have been played in each country, and how many series in total has each country
    played?
# The first is easy
table(cricket$home)
## Aus Eng Ind NZ Pak SA SL WI Zim
   59 69 52 47 44 30
                            31
                                 43
# The second requires us to sum the number of occurrences of each country across two columns
table(cricket$home) + table(cricket$visitor)
## Aus Eng Ind NZ Pak
                                WI Zim
                         SA
                            \operatorname{SL}
## 116 127 106 95 95 56
                            59
                                 96
# This only works as the two tables have the same countries, in the same order.
# If they don't - its more complicated...
# see https://stackoverflow.com/questions/26986363/adding-two-vectors-by-names
# first save each table:
v1 <- table(cricket$home)</pre>
v2 <- table(cricket$visitor)</pre>
```

# make them into one long table, with repeated countries

```
v3 <- c(v1, v2)
## Aus Eng Ind NZ Pak SA SL WI Zim Aus Eng Ind NZ Pak SA SL WI Zim
## 59 69 52 47 44 30 31 43 14 57 58 54 48 51
                                                          26 28 53
# then a little trick to compress it
# this means 'create a crosstab of v3, by the names of v3'
total_series <- xtabs(v3 ~ names(v3))</pre>
total_series
## names(v3)
## Aus Eng Ind NZ Pak SA SL WI Zim
## 116 127 106 95 95 56 59
                               96
  d. How many wins does each country have when they were a visitor? How many draws? And loses?
table(cricket$visitor[cricket$result == "Visitor"])
## Aus Eng Ind NZ Pak SA SL WI Zim
                6 14 11
## 26 19 11
                            5 17
table(cricket$visitor[cricket$result == "Draw"])
##
## Aus Eng Ind NZ Pak SA SL WI Zim
## 11 11 12
                7 16
                        6
# loses
table(cricket$visitor[cricket$result == "Home"])
## Aus Eng Ind NZ Pak SA SL WI Zim
## 20 28 31 35 21 9 17 25 12
  e. What is average difference between the home team's rating and the away team's rating? In which series
    was this largest?
summary(cricket$drating)
     Min. 1st Qu. Median
                             Mean 3rd Qu.
                                             Max.
## -87.288 -16.770 -2.757 -2.629 13.110 62.667
cricket[cricket$drating == (summary(cricket$drating))[6],]
        X series year home visitor matches winner hrating vrating drating
## 288 288
             494 2004 Aus
                               Zim
                                         2
                                              Aus 40.29146 -22.37519 62.66665
      result period per_60_69 per_70_79 per_80_89 per_90_02 per_02on
       Home 4.2002-
                             0
                                                 0
## 288
                                       0
# This looks confusing, but (summary(cricket$drating))[6] is simply returning
# the value of the summary that is the 6th entry in the summary table
# i.e. the maximum, and only returning the row of dataset where drating equals it.
```

#### Question 2

These question appear similar, but are harder and require some more detailed data manipulation.

a. Which country has the highest win ratio?

```
# This isn't easy...
# first we need the total games of each country, from question 1c
total_series
## names(v3)
## Aus Eng Ind NZ Pak SA
                            \mathtt{SL}
                                 WI Zim
## 116 127 106 95 95
                         56
                             59
                                 96
# and then the total wins - i.e.
win_series <- table(cricket$winner)</pre>
win_series
##
##
    Aus Draw
              Eng
                    Ind
                          NZ
                              Pak
                                     SA
                                          SL
                                               WI
                                                   Zim
                               34
                                     30
                                          22
     67
               55
                     40
                          19
                                               40
                                                      1
          81
# then we need to divide one by the other, but the tables are different
# because of draws (look at both),
# so we need to create a little data frame of the two, using cbind (column bind)
wins_total <- data.frame(cbind(wins = win_series,</pre>
                                total = total_series[names(win_series)]))
# and now we can divide one column by the other
wins total$win ratio <- wins total$wins/wins total$total
# and then display it, ordering by win ratio descending
wins_total[order(-wins_total$win_ratio),]
##
        wins total win_ratio
## Aus
          67
               116 0.57758621
## SA
          30
                56 0.53571429
## Eng
               127 0.43307087
          55
## WI
          40
               96 0.41666667
               106 0.37735849
## Ind
          40
                59 0.37288136
## SL
          22
## Pak
                95 0.35789474
          34
                95 0.20000000
## NZ
          19
## Zim
                28 0.03571429
          1
## Draw
  b. Which country has the largest difference between the percentage of wins at home compared to away?
# No of wins at home per country
win_home <- table(cricket$winner[cricket$result == "Home"])</pre>
# Number of home series
home series <- table(cricket$home)</pre>
# and using the method from 2a
```

```
home_total <- data.frame(cbind(win_home = win_home,</pre>
                                  no_home = home_series[names(win_home)]))
home_total$home_ratio <- home_total$win_home / home_total$no_home
# and then the same for away series wins
win_away <- table(cricket$winner[cricket$result == "Visitor"])</pre>
visitor series <- table(cricket$visitor)</pre>
visitor_total <- data.frame(cbind(win_away = win_away,</pre>
                                   no visitor = visitor series[names(win away)]))
visitor_total$visit_ratio <- visitor_total$win_away/visitor_total$no_visitor</pre>
ratios_home_visit <- cbind(home_total, visitor_total)</pre>
ratios_home_visit$ratio_diff <- ratios_home_visit$home_ratio - ratios_home_visit$visit_ratio
ratios_home_visit[order(-ratios_home_visit$ratio_diff),]
##
        win_home no_home home_ratio win_away no_visitor visit_ratio ratio_diff
## SL
              17
                      31
                          0.5483871
                                            5
                                                      28 0.17857143 0.36981567
## Ind
              29
                      52
                          0.5576923
                                           11
                                                      54
                                                          0.20370370 0.35398860
## Aus
              41
                      59
                          0.6949153
                                           26
                                                      57
                                                          0.45614035 0.23877490
## WI
              23
                      43 0.5348837
                                           17
                                                      53
                                                          0.32075472 0.21412900
              19
                      30 0.6333333
                                                          0.42307692 0.21025641
## SA
                                           11
                                                       26
              36
                      69
                          0.5217391
                                           19
                                                      58
                                                          0.32758621
                                                                       0.19415292
## Eng
## Pak
              20
                      44
                          0.4545455
                                           14
                                                      51
                                                          0.27450980 0.18003565
              13
                                            6
## NZ
                      47 0.2765957
                                                       48 0.12500000 0.15159574
## Zim
               0
                      14 0.0000000
                                            1
                                                      14
                                                          0.07142857 -0.07142857
## Draw
               0
                      NA
                                  MΔ
                                            0
                                                      NΑ
                                                                   MΔ
```

c. Are there any occurrences when the home team had a higher rating but failed to win the series? List the teams involved by year. What about when the home team with a higher rating lost?

```
loss_high_rating <- cricket[cricket$drating > 0 & cricket$result != "Home",]
loss_high_rating[,3:4]
```

```
##
      year home
## 11 1963
## 13 1964
            Eng
## 15 1965
             SA
## 19
     1965 Eng
## 26
     1968
             WI
      1968
## 27
             NZ
## 28
      1968 Eng
## 35
     1971
             WI
## 37
      1971
            Eng
## 39 1972
            Eng
      1973
## 43
            Eng
## 48 1974
            Eng
     1975
## 49
            Ind
## 82 1980
            Eng
## 107 1985
            Pak
## 110 1985
            Ind
## 116 1986
            Aus
## 120 1986 Eng
```

```
## 124 1987
## 132 1988
              NZ
## 133 1988
              WI
## 141 1990
             Pak
## 156 1993
             Aus
## 178 1995
              WI
## 180 1996
             Pak
## 185 1996
              ΝZ
## 192 1997
             Pak
## 208 1998
             Ind
## 212 1998
              SA
## 222 1999
             Pak
## 228 1999
             Eng
## 243 2001
              SL
## 255 2001
             Eng
## 262 2002
             Aus
## 270 2002
              NZ
## 274 2002
             Eng
## 292 2004
             Aus
## 294 2004
              NZ
## 298 2004
             Pak
## 305 2005
## 311 2005
             Ind
## 330 2006
             Eng
## 340 2007
             Eng
## 341 2008
             Pak
## 359 2009
             Aus
## 371 2010
              SA
## 382 2011
              SL
\# and without the intermediate step for visitor wins
cricket[cricket$drating > 0 & cricket$result == "Visitor",3:4]
##
       year home
## 13
       1964
             Eng
```

```
## 15
      1965
               SA
       1965
             Eng
## 19
       1968
## 26
               WI
## 27
       1968
               ΝZ
## 35
      1971
               WI
## 37
       1971
             Eng
## 43
       1973
             Eng
## 49
       1975
             Ind
## 82
       1980
             Eng
## 110 1985
             Ind
## 120 1986
             Eng
## 124 1987
             Aus
## 156 1993
             Aus
## 178 1995
               WI
## 180 1996
             Pak
## 222 1999
             Pak
## 228 1999
             Eng
## 243 2001
               SL
## 294 2004
               ΝZ
## 298 2004 Pak
```

```
## 340 2007 Eng
## 341 2008 Pak
## 359 2009 Aus

# and just to see who did most often:

table(cricket[cricket$drating > 0 & cricket$result == "Visitor",]$home)

##
## Aus Eng Ind NZ Pak SA SL WI Zim
## 3 8 2 2 4 1 1 3 0
```

Overall, these questions should demonstrate that there are multiple ways to interrogate the dataset and, for anyone with an interest in cricket at least, there are numerous interesting findings within it. The issue is that one can quickly become lost just pulling our various statistics, which don't answer a fundamental and general questions such as (i) how well do the team ratings predict results of test series, and (ii) what is the extent of home advantage? Ordinal regression can be used here.

#### Question 3.

Fit an ordinal regression model for result, with drating as the only explanatory variable. Confirm that the effect of drating is statically significant.\*

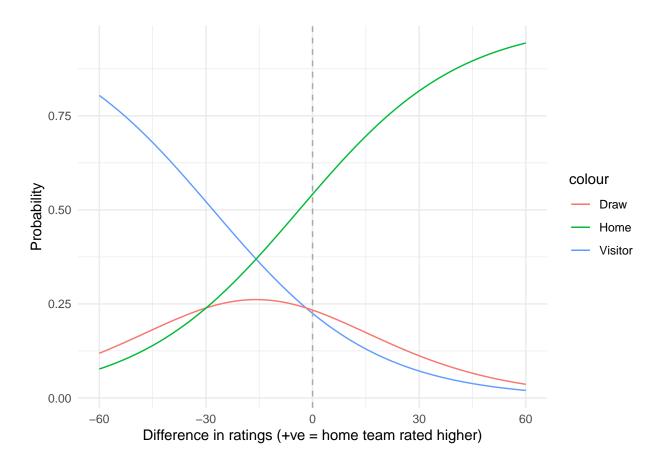
```
m1 <- polr(result ~ drating , data = cricket)</pre>
summary(m1)
##
## Re-fitting to get Hessian
## polr(formula = result ~ drating, data = cricket)
##
## Coefficients:
             Value Std. Error t value
## drating 0.04416
                     0.005327
                                  8.29
##
## Intercepts:
##
                 Value
                         Std. Error t value
## Visitor|Draw -1.2369
                          0.1295
                                     -9.5480
## Draw|Home
                -0.1659 0.1127
                                     -1.4721
##
## Residual Deviance: 715.1328
## AIC: 721.1328
# as with multinomial regression this table does not include p values which need
# to be calculated separately - see https://stats.oarc.ucla.edu/r/dae/ordinal-logistic-regression/
ctable1 <- coef(summary(m1))</pre>
##
## Re-fitting to get Hessian
p <- pnorm(abs(ctable1[, "t value"]), lower.tail = FALSE) * 2</pre>
ctable <- cbind(ctable1, "p value" = p)</pre>
round(ctable1,4)
                  Value Std. Error t value
                             0.0053 8.2896
## drating
                  0.0442
```

The P-value of the coefficient of drating is P < 0.001, so the coefficient is statistically significant. The estimated coefficient is 0.044, and its exponential is  $\exp(0.044) = 1.045$ . The interpretation of this is that a 1-point increase in the difference between home and visiting teams' ratings is associated with 4.5% increase in the odds of a more favourable outcome for the home team. This same increase applies to both the odds of home win, against draw or visitor winning, and the odds of home win or draw, against visitor winning.

### Question 4.

## 1.045145

Plot the fitted values of the probabilities of the individual categories of Y (i.e. the three values of result options) against drating



#### Question 5

What does this show you in terms of who is likely to win? What can tou say about the probability of a draw? And is there a home advantage?

The plot of the probabilities of the individual outcomes shows that the probability of the home team winning is very high when drating is large and positive, i.e. when the home team is much stronger than the visiting team. Similarly, the probability of the visitors winning is high when drating is large and negative. The ratings of the teams before a series are thus strongly predictive of the result of the series. A draw is never the likeliest outcome, and has probabilities of roughly 0.2 for most of the values of drating.

As to whether there is a home advantage: the probability curves for wins by home and visiting teams are quite clearly not mirror images of each other - at each value of the ratings difference between the same two teams, a team has a much higher predicted probability of winning if it plays at home than if it plays away. In particular, in a series of two equally strong teams the probability that the home team wins is around 0.55, and the probability that the visiting team wins is about 0.22. This shows evidence of a substantial home advantage in test cricket.

#### Question 6.

It has been argued that the rating system has become less relevant since the mid 90s, and particularly after 2002. Similarly, the effect of rating is thought to be less pronounced when there are few matches in series. Can you test these hypotheses? \*

```
m2 <- polr(result ~ drating + matches + period, data = cricket)
summary(m2)</pre>
```

##

```
## Re-fitting to get Hessian
## Call:
## polr(formula = result ~ drating + matches + period, data = cricket)
##
## Coefficients:
##
                        Value Std. Error t value
## drating
                      0.04479 0.005397 8.3001
## matches
                     -0.04791 0.097320 -0.4922
## period1970-79
                      0.22963 0.474503 0.4839
## period1980-89
                      0.74614   0.448677   1.6630
                                0.422565 1.0558
## period1990-3.2002 0.44616
## period4.2002-
                      0.43070
                                0.433761 0.9930
##
## Intercepts:
##
                        Std. Error t value
                Value
## Visitor|Draw -0.9710 0.5551
                                   -1.7493
## Draw|Home
                 0.1098 0.5524
                                    0.1987
## Residual Deviance: 711.2552
## AIC: 727.2552
# as with multinomial regression this table does not include p values which need
# to be calculated separately - see https://stats.oarc.ucla.edu/r/dae/ordinal-logistic-regression/
ctable2 <- coef(summary(m2))</pre>
##
## Re-fitting to get Hessian
p2 <- pnorm(abs(ctable2[, "t value"]), lower.tail = FALSE) * 2
ctable2 <- cbind(ctable2, "p value" = p2)</pre>
round(ctable2,4)
                       Value Std. Error t value p value
##
## drating
                      0.0448
                                 0.0054 8.3001 0.0000
## matches
                     -0.0479
                                 0.0973 -0.4922 0.6225
## period1970-79
                      0.2296
                                 0.4745 0.4839
                                                 0.6284
## period1980-89
                                 0.4487 1.6630
                      0.7461
                                                0.0963
## period1990-3.2002 0.4462
                                 0.4226 1.0558 0.2910
## period4.2002-
                      0.4307
                                 0.4338 0.9930 0.3207
## Visitor|Draw
                     -0.9710
                                 0.5551 -1.7493 0.0802
## Draw|Home
                      0.1098
                                 0.5524 0.1987 0.8425
# and of course we need to exponential of the coeff to interpret
exp(coef(m2))
##
                                           period1970-79
                                                              period1980-89
             drating
                               matches
##
           1.0458115
                             0.9532239
                                               1.2581299
                                                                  2.1088453
  period1990-3.2002
##
                         period4.2002-
           1.5623026
                             1.5383415
p2
##
                                           period1970-79
                                                             period1980-89
             drating
                               matches
##
        1.040588e-16
                          6.225450e-01
                                            6.284350e-01
                                                               9.631671e-02
## period1990-3.2002
                         period4.2002-
                                            Visitor|Draw
                                                                  Draw | Home
        2.910413e-01
                          3.207325e-01
                                            8.024443e-02
                                                              8.424790e-01
```

We can see from this output that neither the number of matches nor the time period in which the game was played are significant. Similarly the value of drating coefficient does not change much so we can say that in all likelihood, that the rating of teams is important regardless of the number of matches and is as relevent now as it was in the 1960s.

Note: we have used here period as a categorical variable here to see if there are non-liner changes over the time period. We could have added the raw year value if our hypothesis was that the outcomes had changed the probability of occuring over over time