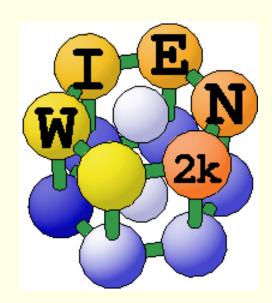


Magnetism (FM, AFM, FSM)



Karlheinz Schwarz

Institute of Materials Chemistry **TU Wien**





Localized vs. itinerant systems



- In localized systems (e.g. some rare earth) the magnetism is mainly governed by the atom (Hund's rule)
- In itinerant (delocalized) systems (many transition metals) magnetism comes from partial occupation of states, which differ between spin-up and spin-down.
- Boarderline cases (some f-electron systems)
 details of the structure (e.g. lattice spacing) determine whether or not some electrons are localized or itinerant.

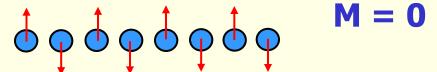


Ferro-, antiferro-, or ferri-magnetic



Ferromagnetic (FM) (e.g. bcc Fe)

Antiferromagnetic (AFM) (e.g. Cr)



Ferrimagnetic cases

the moments at different atoms are antiparallel but of different magnitude

Non-collinear magnetism (NCM)

the magnetic moments are not ligned up parallel.



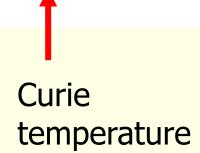


Itinerant electron magnetism



Experimental facts:

	$\sigma [{\rm emu/g}]$	$\sigma\left[\mu_{ m B} ight]$	$T_{ m c} \left[{ m K} ight]$	ρ at 298K [g/cm ³]
Fe (bcc)	221.7	2.22	1044	7.875
Co (fcc)	166.1	1.75	1388	8.793
Co (hcp)	163.1	1.72	1360	8.804
Ni (fcc)	58.6	0.62	627	8.912



Stoner theory of itinerant electron magnetism



- 1. The carriers of magnetism are the unsaturated spins in the d-band.
- 2. Effects of exchange are treated with a molecular field term.
- 3. One must conform to Fermi statistics.



Stoner model for itinerant electrons



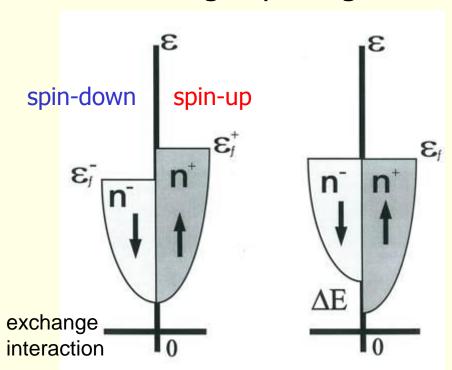
In a

- non magnetic (NM) case
 - $\mathbf{N}_{\uparrow} = \mathbf{N}_{\downarrow}$ (spin-up and spin-down)
- ferromagnetic (FM) case
 N_↑ > N_↓ (majority and minority spin)
 the moments at all sites are parallel
 (collinear)
- the (spin) magnetic moment m

 - its orientation with respect to the crystal axes is only defined by
 spin orbit coupling.
- there can also be an orbital moment it is often suppressed in 3d transition metals

$$\chi = \frac{\chi_{\mathrm{P}}}{1 - 2\mu_{\mathrm{B}}^2 I_{\mathrm{s}} \mathcal{N} \left(\varepsilon_{\mathrm{F}}\right)} = \chi_{\mathrm{P}} S$$

Exchange splitting



$$\begin{split} E_{\mathrm{b}} &= \int\limits_{0}^{\varepsilon_{\mathrm{F}}} \varepsilon \mathcal{N}\left(\varepsilon\right) \mathrm{d}\varepsilon - \int\limits_{\varepsilon^{-}}^{\varepsilon_{\mathrm{F}}} \varepsilon \mathcal{N}\left(\varepsilon\right) \mathrm{d}\varepsilon + \int\limits_{0}^{\varepsilon_{\mathrm{F}}} \varepsilon \mathcal{N}\left(\varepsilon\right) \mathrm{d}\varepsilon + \int\limits_{\varepsilon_{F}}^{\varepsilon^{+}} \varepsilon \mathcal{N}\left(\varepsilon\right) \mathrm{d}\varepsilon \\ &- \frac{I_{\mathrm{s}} M^{2}}{2} \quad . \end{split}$$

Stoner criterion

$$2\mu_{\mathrm{B}}^{2}I_{\mathrm{s}}\mathcal{N}\left(\varepsilon_{\mathrm{F}}\right)>1$$



Stoner model for itinerant electrons

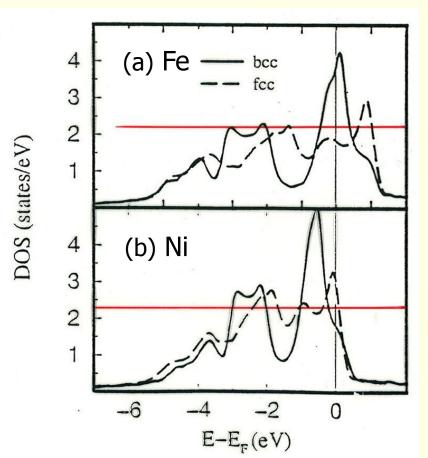


- The existence of ferromagnetism (FM) is governed by the
- Stoner criterion

$$I.N(E_F) > 1$$

 $N(E_F)$ DOS at E_F (of NM case) I Stoner parameter ~ independent of structure

 Ferromagnetism appears when the gain in exchange energy is larger than the loss in kinetic energy



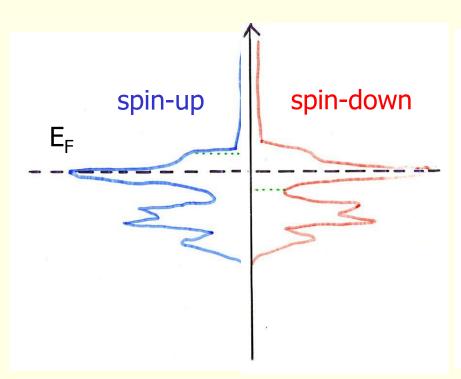
P.James, O.Eriksson, B.Johansson, I.A.Abrikosov, Phys.Rev.B **58**, ... (1998)

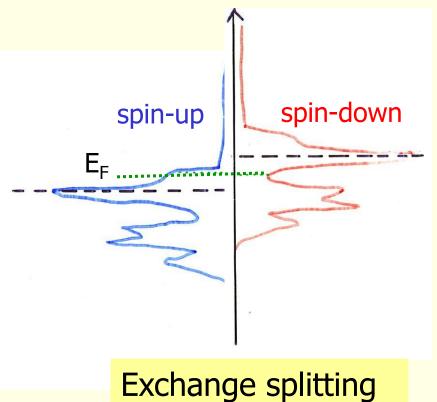




ferromagnetic case

Non magnetic case



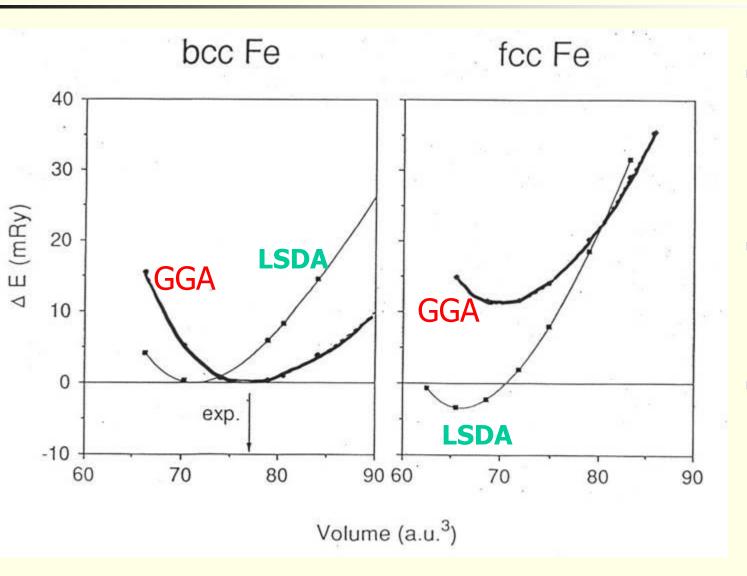


E_F at high DOS



DFT ground state of iron





LSDA

- NM
- fcc
- in contrast to experiment

GGA

- FM
- bcc
- Correct lattice constant

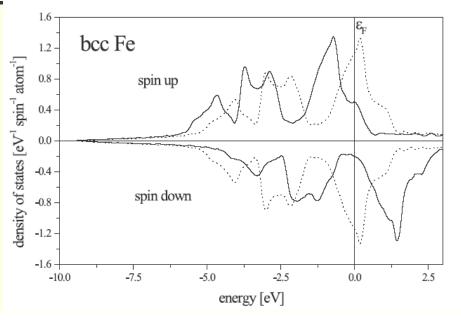
Experiment

- FM
- bcc

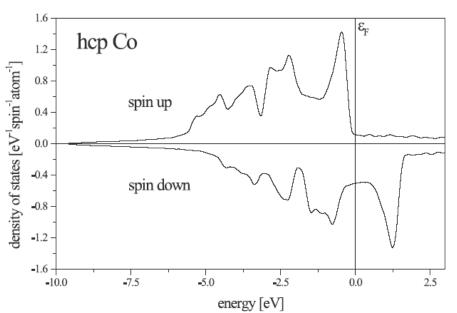


Iron and its alloys





Fe: weak ferromagnet (almost)

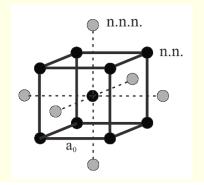


Co: strong ferromagnet

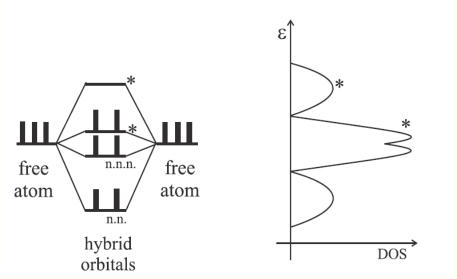


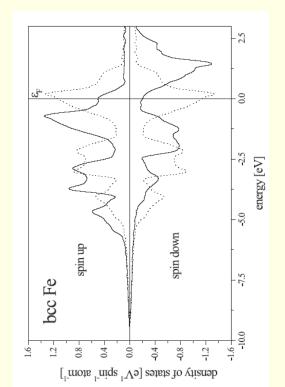
Magnetism and crystal structure





V. Heine: "metals are systems with unsaturated covalent bonds"







Covalent magnetism Fe-Co alloys



e.g. Fe-Co alloys

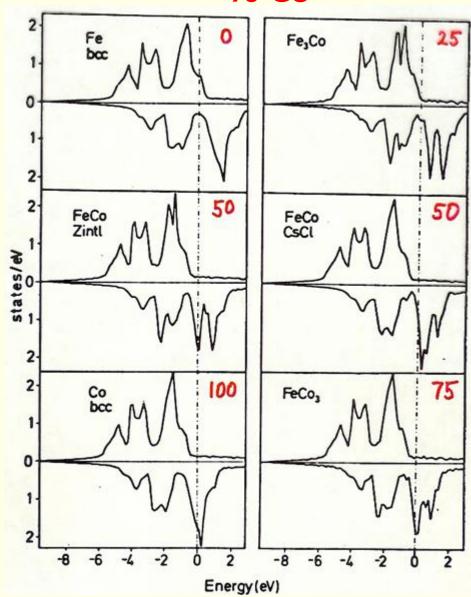
Wigner delay times



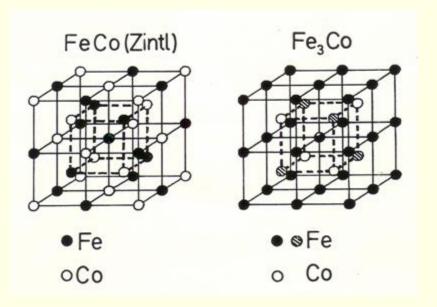
Spin projected DOS of Fe-Co alloys







- The alloy is represented by ordered structures
 - Fe₃Co and FeCo₃ (Heusler)
 - FeCo Zintl or CsCl
 - Fe, Co bcc

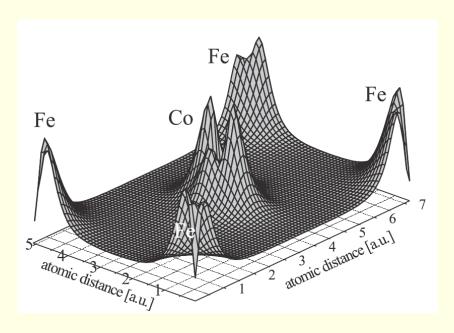


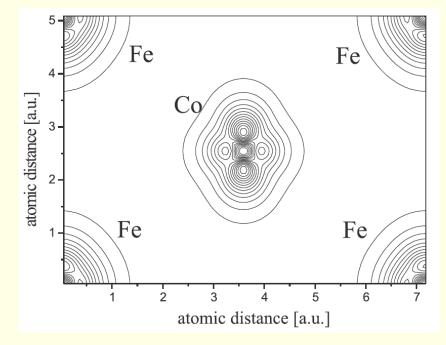


Iron and its alloys



Itinerant or localized?







Magnetization density in FeCo

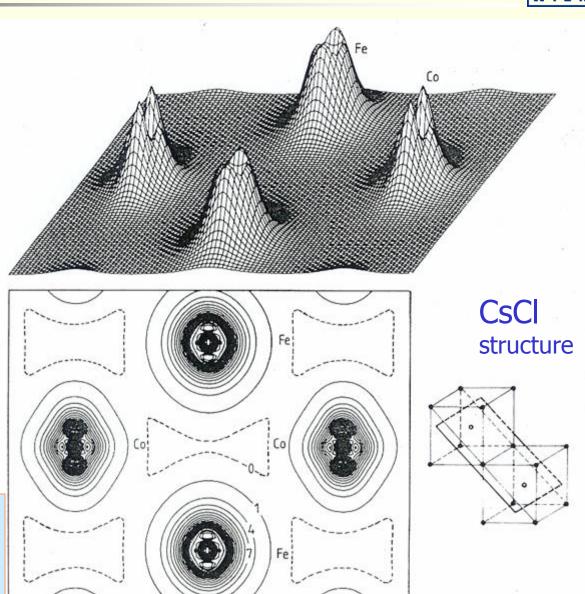


- Magnetization density difference between
 - Majoity spin
 - Minority spin

$$m(r) = \rho^{\dagger}(r) - \rho^{\dagger}(r)$$

- Localized around
 - Fe and Co
 - slightly negative between the atoms
- Itinerant electrons

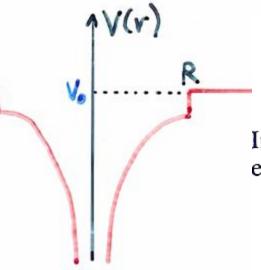
K.Schwarz, P.Mohn, P.Blaha, J.Kübler,
Electronic and magnetic structure of bcc Fe-Co alloys from band theory,
J.Phys.F:Met.Phys. 14, 2659 (1984)





Bonding by Wigner delay time





$$V(r) = \begin{cases} V(r) & r \leq b, \\ 0 & r > b. \end{cases}$$
 (1)

Inside such a sphere of radius b the radial Schrödinger equation (in Rydberg atomic units)

$$\left[-\frac{d^2}{dr^2} - \frac{2}{r}\frac{d}{dr} + \frac{l(l+1)}{r^2} + V(r) - \varepsilon\right]R_l(\varepsilon, r) = 0,$$
(2)

single scatterer (Friedel)

$$V(r)=0$$
 solution:

R_I joined in value and slope defines phase shift :

Friedel sum

Wigner delay time

Bessel Neumann
$$S_{l}(r) = A_{l}[j_{l}(kr)\cos\eta_{l}(\varepsilon) - n_{l}(kr)\sin\eta_{l}(\varepsilon)], \quad (3)$$

$$\tan \eta_l(\varepsilon) = \frac{R_l(\varepsilon, b)j'_l(kb) - j_l(kb)R'_l(\varepsilon, b)}{R_l(\varepsilon, b)n'_l(kb) - n_l(kb)R'_l(\varepsilon, b)}, \quad (4)$$

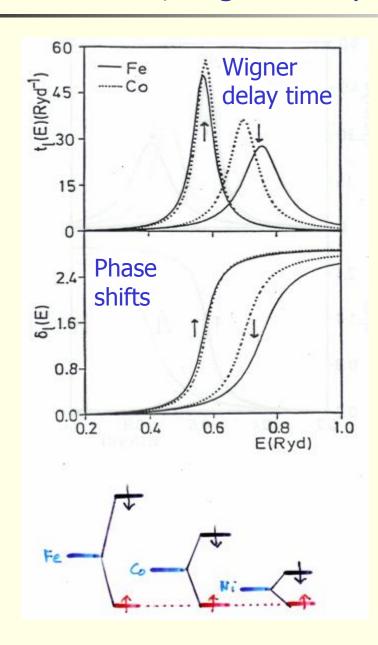
$$N(\varepsilon) = \frac{2}{\pi} \sum_{l=0}^{\infty} (2l+1) \eta_l(\varepsilon),$$

$$n(\varepsilon) = \frac{dN(\varepsilon)}{d\varepsilon} = \frac{1}{\pi} \sum_{l=0}^{\infty} (2l+1)t_l^{\mathrm{D}}(\varepsilon). \tag{6}$$

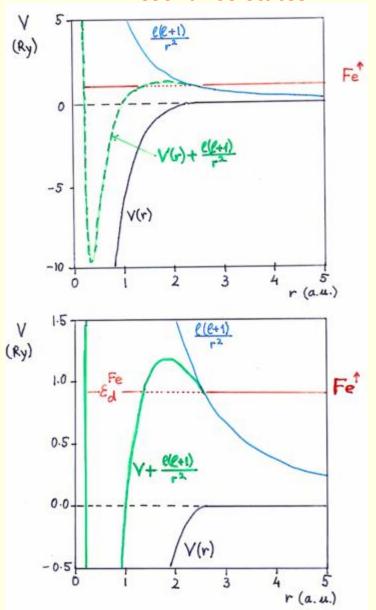


Phase shifts, Wigner delay times of Fe, Co, Ni





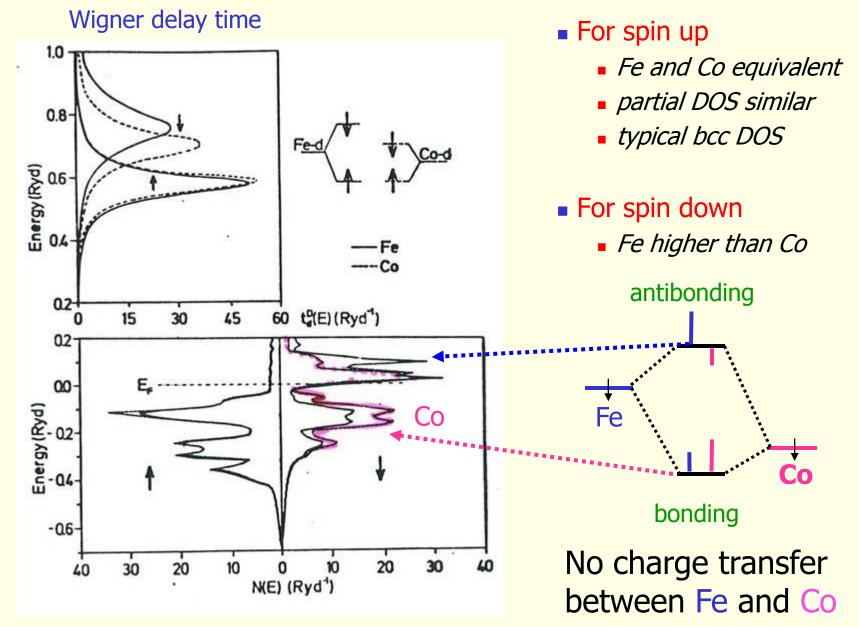
resonance states





Covalent magnetism in FeCo



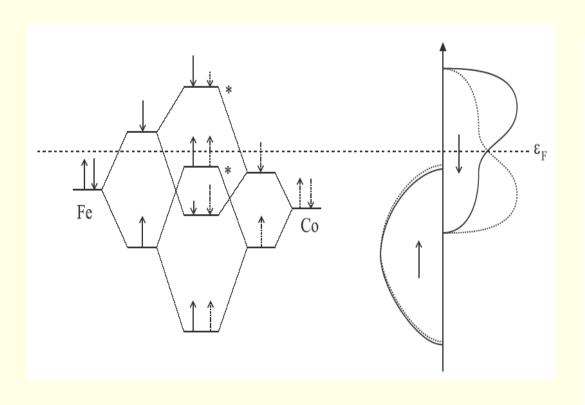


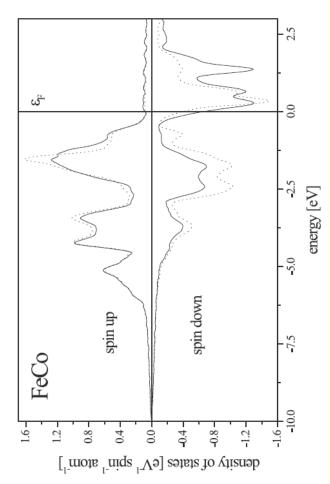


Magnetism and crystal structure



Covalent magnetism, FeCo:



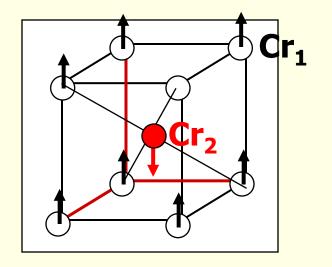


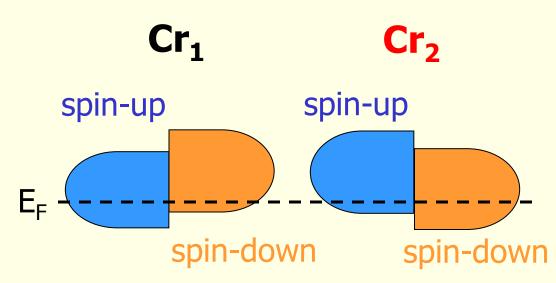


Antiferromagnetic (AFM) Cr



Cr has AFM bcc structure





There is a symmetry
 it is enough to do the spin-up
 calculation
 spin-down can be copied

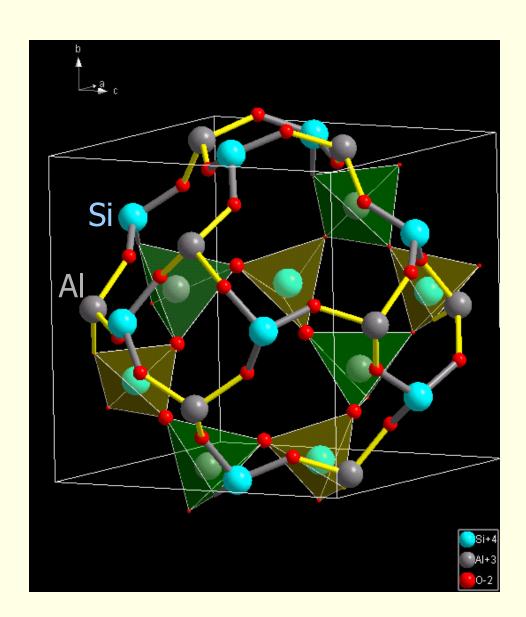
$$Cr_1 = Cr_2$$



Zeolite, sodalite



- Al-silicate
- corner shared
 - SiO₄ tetrahedra
 - AlO₄ tetrahedra
- β cage
- Al / Si ratio 1
- alternating
- ordered (cubic)
- 3 e⁻ per cage

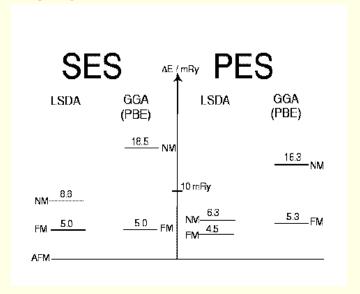




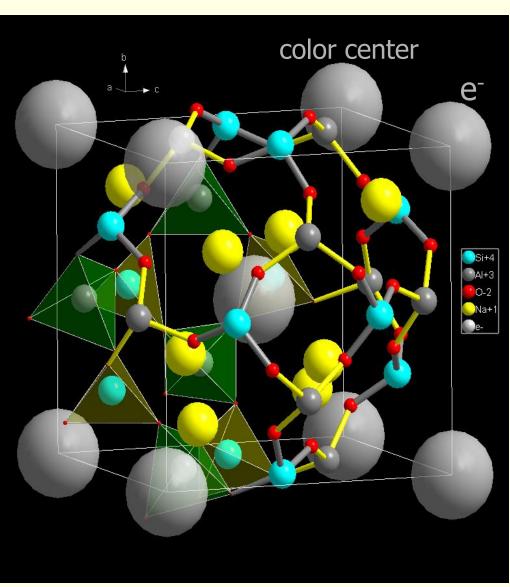
SES Sodium electro sodalite

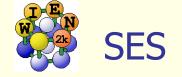


- Si-Al zeolite (sodalite)
 - Formed by corner-shared SiO₄
 and AlO₄ tetrahedra
- Charge compensated by doping with
 - 4 Na⁺
 - one e (color center)
- antiferromagnetic (AFM) order of e⁻



Energy (relative stability)

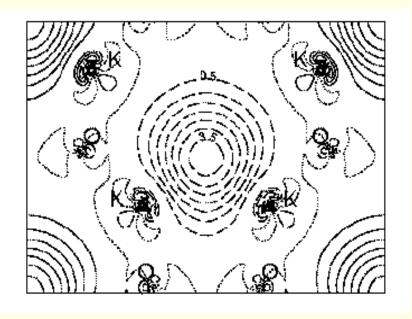


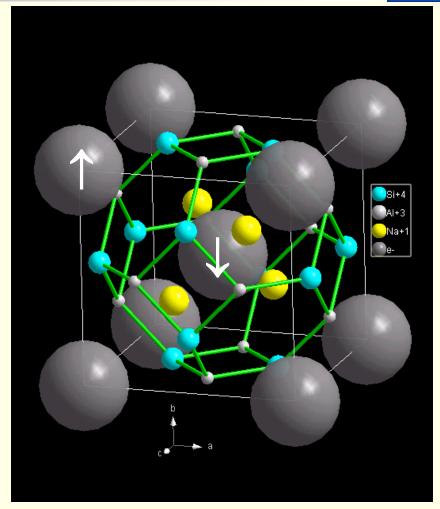




AFM order between color centers (e⁻)

Spin density ρ^{\uparrow} - ρ^{\downarrow}





G.K.H. Madsen, Bo B. Iversen, P. Blaha, K. Schwarz, Phys. Rev. B 64, 195102 (2001)



INVAR alloys (invariant)

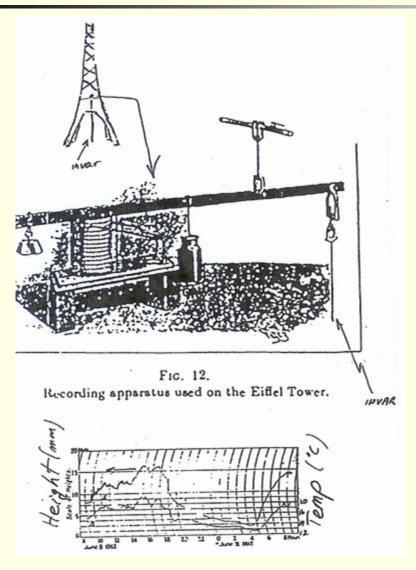


- e.g. Fe-Ni
- Such systems essentially show no thermal expansion around room temperature



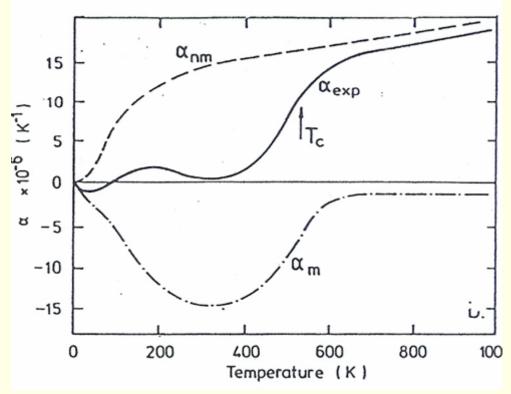
INVAR (invariant) of Fe-Ni alloys





Ch.E.Guillaume (1897)

- The thermal expansion of the Eifel tower
- Measured with a rigid Fe-Ni INVAR wire
- The length of the tower correlates with the temperature
- Fe₆₅Ni₃₅ alloy has vanishing thermal expansion around room temperature





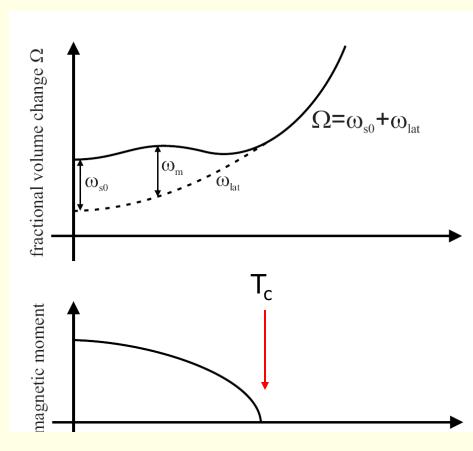
Magnetostriction and Invar behaviour



What is magnetostriction?

Magnetostriction ω_{s0} is the difference in volume between the volume in the magnetic ground state and the volume in a hypothetical non-magnetic state.

Above the Curie temperature the magnetic contribution ω_{m} vanishes.

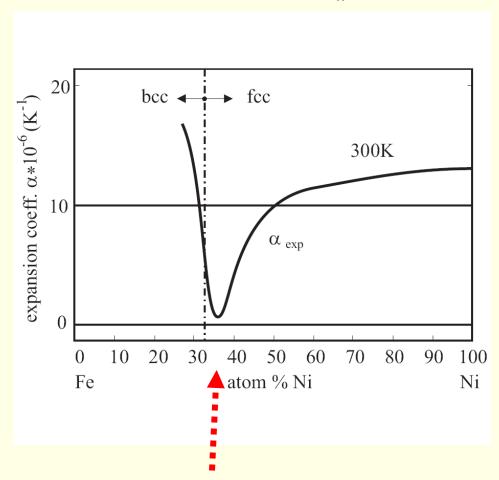




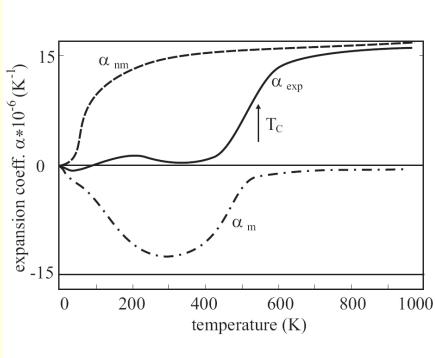
Fe-Ni Invar alloys



"classical" Fe-Ni Invar



■ Fe₆₅Ni₃₅ alloy has vanishing thermal expansion around room temperature





Early explanations of INVAR



R.J.Weiss

Proc.Roy.Phys.Soc (London) **32**, 281 (1963)

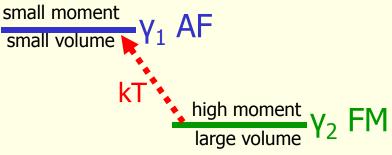
fcc Fe

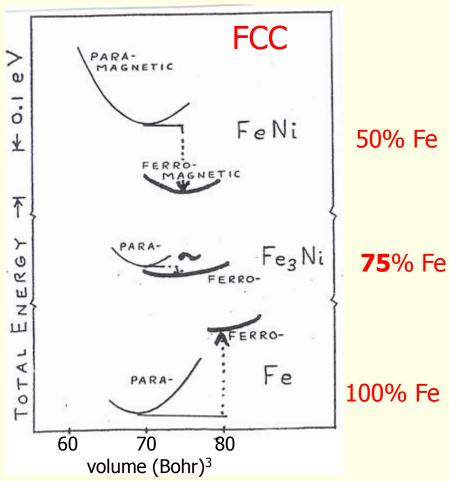
low spin

 $m=0.5 \mu_B AF$ a = 3.57 Å

high spin

 $m=2.8 \mu_B FM$ a = 3.64 Å





A.R.Williams, V.L.Moruzzi, G.D.Gelatt Jr., J.Kübler, K.Schwarz, *Aspects of transition metal magnetism,* J.Appl.Phys. **53**, 2019 (1982)

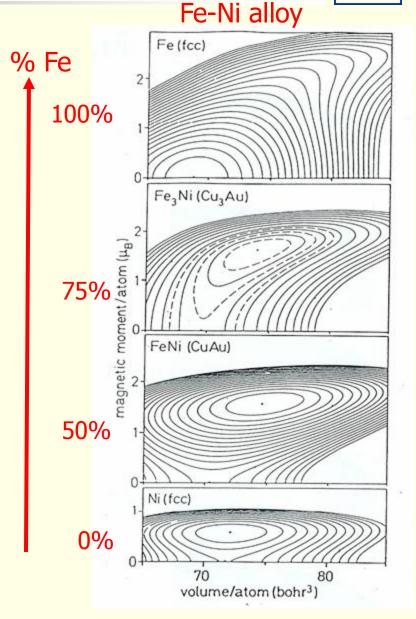


Energy surfaces of Fe-Ni alloys



This fcc structure

- from non magnetic Fe (fcc)
- to ferromagnetic Ni
- as the composition changes
- At the INVAR composition
 - There is a flat energy surface
 - as function of volume and moment





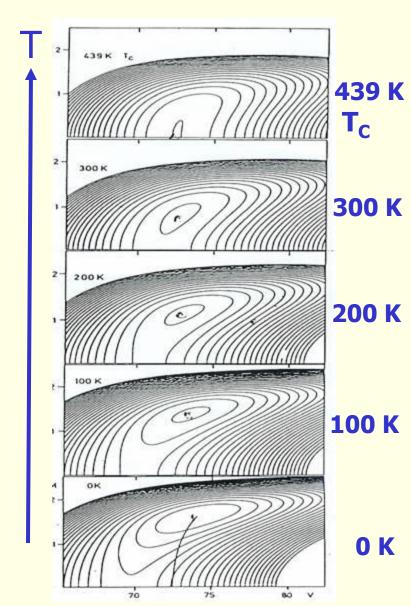
Finite temperature



Energy surface at T=0 (DFT)

- as a function of volume and moment
- using fixed spin moment (FSM) calculations
- Finite temperature
 - Spin and volume fluctuations
 - Ginzburg-Landau model

$$H = V^{-1} \int d^3r \left(E(M + \underline{m(r)}), V + \underline{v(r)} \right)$$
$$+ \frac{C}{2} \sum_{i,j} \left(\nabla_j m_i \right)^2 + \frac{D}{2} (\nabla v(r))^2 \right)$$





fixed spin moment (FSM)
 e.g. Fe-Ni alloy

- allows to explore energy surface E(V,M)
 as function of
 - volume
 - magnetic moment M



Fixed spin moment (FSM) method

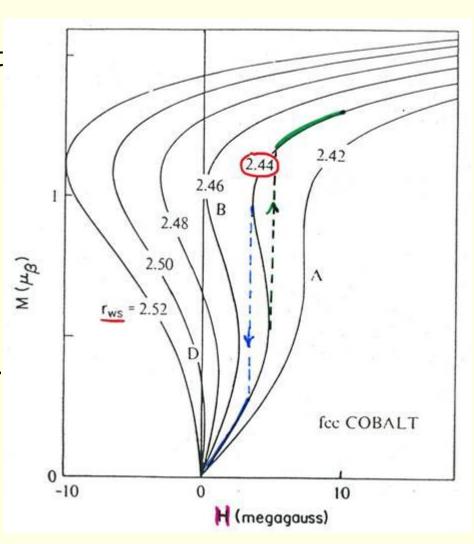


- There are systems (e.g. like fcc Fe or fcc Co), for which the magnetization shows a hysteresis, when a magnetic field is applied (at a volume V).
- The volume of the unit cell defines the Wigner-Seitz radius r_{ws}

$$V = \frac{4\pi r_{WS}^3}{3}$$

- The hysteresis causes numerical difficulties, since there are several solutions (in the present case 3 for a certain field H).
- In order to solve this problem the FSM method was invented

Hysteresis





Fixed spin moment (FSM) method



Conventional scheme

$$E_F^{\uparrow} = E_F^{\downarrow}$$
 $Z_v = N^{\uparrow} + N^{\downarrow}$

output

Fe₃Ni

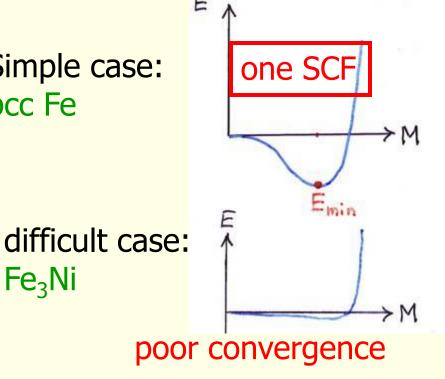
$$M=N^{\uparrow}-N^{\downarrow}$$

constrained (FSM) method

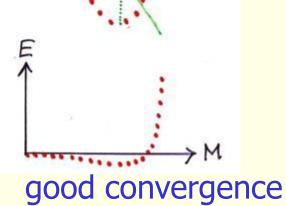
$$E_F^{\uparrow} \neq E_F^{\downarrow}$$
 output $Z_v = N^{\uparrow} + N^{\downarrow}$

$$M = N^{\uparrow} - N^{\downarrow}$$
 input

Simple case: bcc Fe



AEF. many calculations

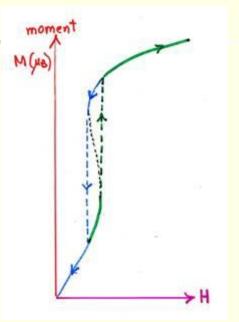






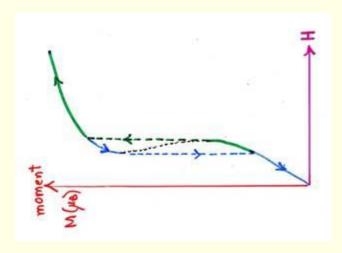
Physical situation:

- One applies a field H and obtains M
- but this functions can be multivalued



Computational trick (unphysical):

- One interchanges the dependent and independent variable
- this function is single valued (unique)
- i.e. one chooses M and calculates
 H afterwards





FSM key references



A.R.Williams, V.L.Moruzzi, J.Kübler, K.Schwarz, Bull.Am.Phys.Soc. **29**, 278 (1984)

K.Schwarz, P.Mohn J.Phys.F **14**, L129 (1984)

P.H.Dederichs, S.Blügel, R.Zoller, H.Akai, Phys. Rev, Lett. **53**,2512 (1984)

Unusual magnetic systems



GMR (Giant Magneto Resistance)

half-metallic systemse.g. CrO₂

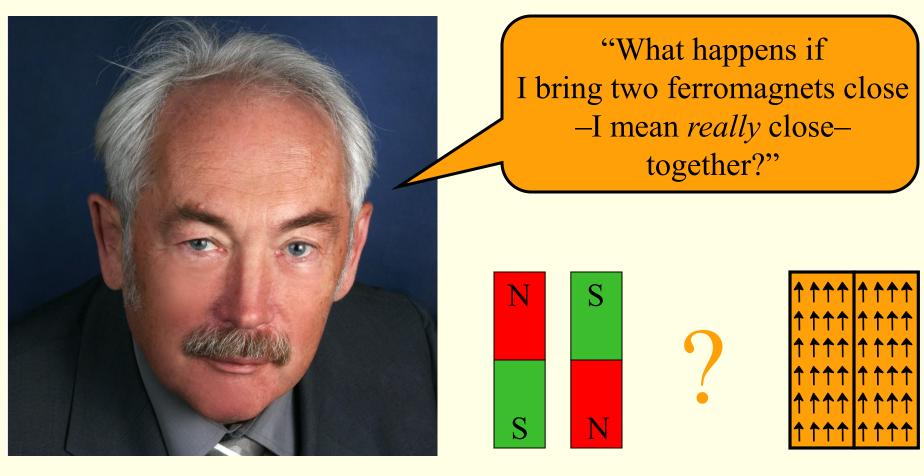
important for spintronics



Once upon a time, ...



Once upon a time, in the early 1980's ...

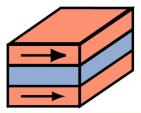


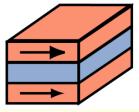
Peter Grünberg

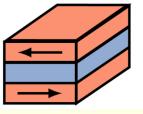


Giant magnetoresistance (GMR)









Ferromagnet

Electrical resistance:

 R_{P}

The electrical resistance depends on the relative magnetic alignment of the ferromagnetic layers

$$GMR = \frac{R_{AP} - R_P}{R_P}$$

19% for trilayers @RT

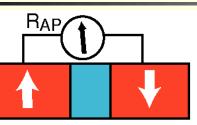
80% for multilayers @ RT

GMR is much larger than the anisotropic magnetoresistance (AMR)

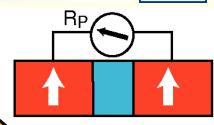


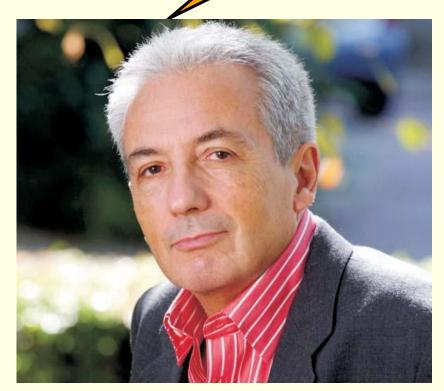
1988: ... simultaneously, but independent ...





"Does the electrical resistance depend on the magnetization alignment?"





Albert Fert



Peter Grünberg







The Nobel Prize in Physics 2007



This year's Nobel Prize in Physics is awarded to Albert Fert and Peter Grünberg for their discovery of Giant Magnetoresistance. Applications of this phenomenon have revolutionized

techniques for retrieving data from hard disks.

Scientific Background on the Nobel Prize in Physics 2007

http://www.kva.se/

Scientific background

The Discovery of Giant Magnetoresistance

compiled by the Class for Physics of the Royal Swedish Academy of Sciences

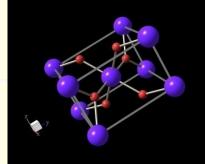
4. Half-metals

Since magnetoresistance deals with electrical conductivity it is obvious that it is the behaviour of the electrons at the Femi surface (defined by the Fermi energy) which is of primary interest. The more spin-polarized the density of states (DOS) at the Fermi energy, i.e., the more N_{\uparrow} (E_F) deviates from N_{\downarrow} (E_F), the more pronounced one expects the efficiency of the magnetoelectronic effects to be. In this respect a very interesting class of materials consists of what are called half-metals, a concept introduced by de Groot and co-workers (23). Such a property was then predicted theoretically for CrO₂ by Schwarz in 1986 (24). The name half-metal originates from the particular feature that the spin down band is metallic while the spin up band is an insulator.

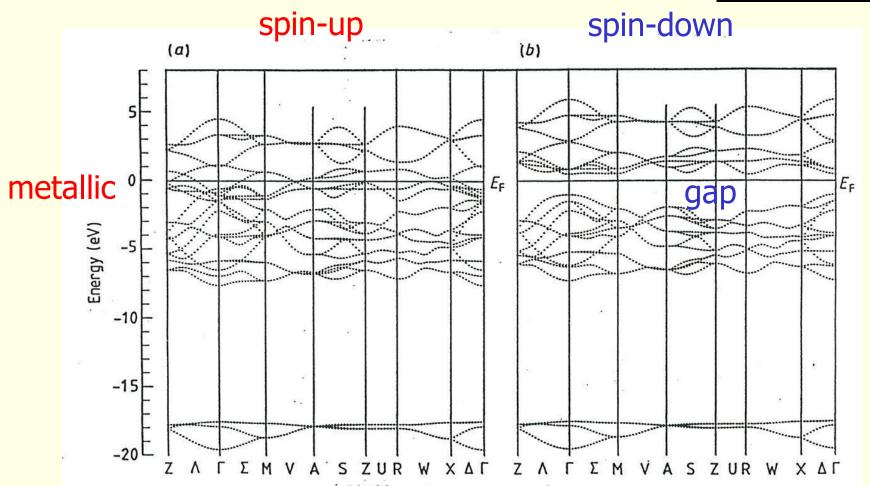
24. K. Schwarz, "CrO₂ predicted as a half-metallic ferromagnet", J. Phys. F, 16, L211 (1986).



CrO₂ half-metallic ferromagnet



CrO₂ (rutile structure)



important for spintronics



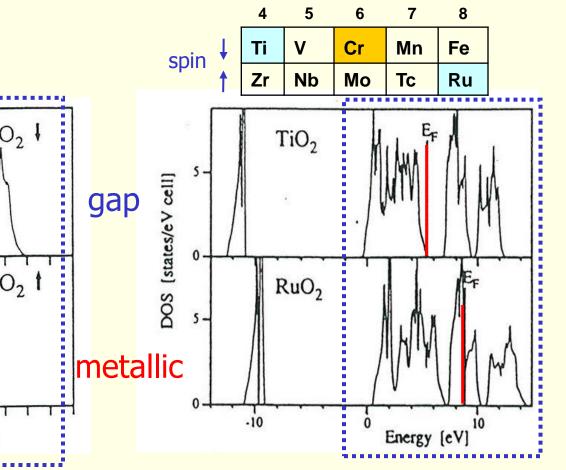
K.Schwarz,

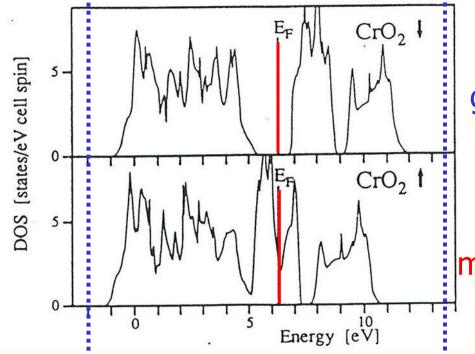


■ The DOS features of CrO₂ are qualitatively like

- *TiO*₂ (for spin-down)
- RuO₂ (for spin-up)

CrO₂ predicted as a half-metallic ferromagnet, J.Phys.F:Met.Phys. **16**, L211 (1986)





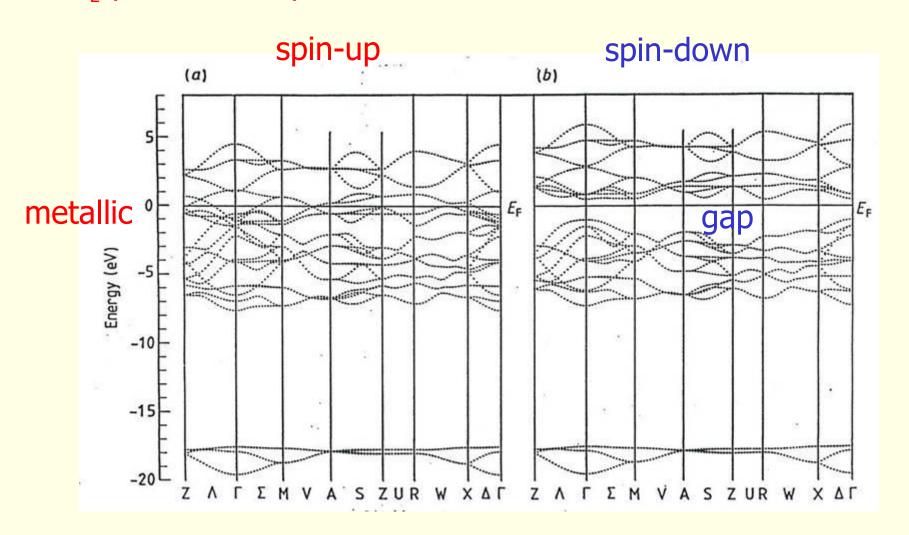
all three compound crystallize in the rutile structure



Half-metallic ferromagnet



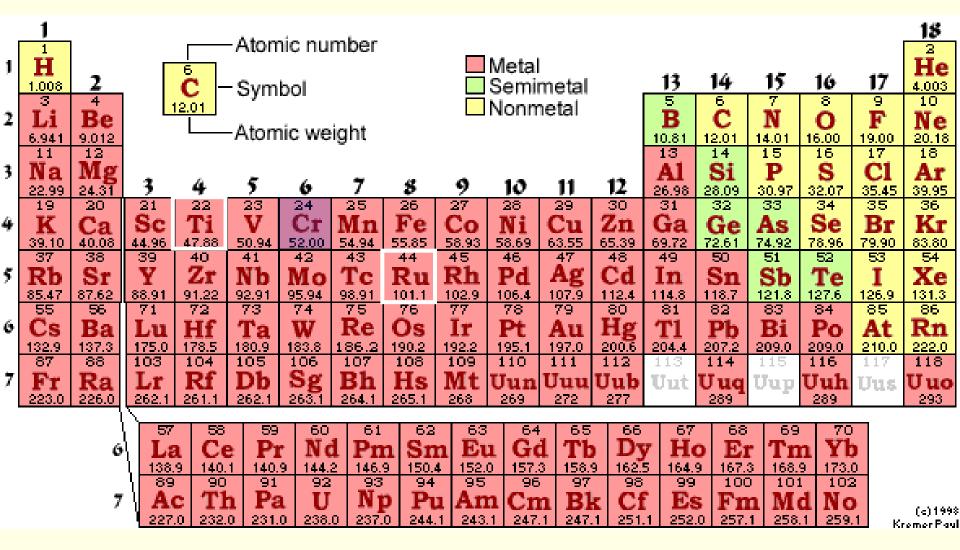
CrO₂ (rutile structure)





CrO₂ spin-down (**TiO₂**) spin-up (**RuO₂**)







Magnetic structure of uranium dioxide UO₂



- R.Laskowski
- G.K.H.Madsen
- P.Blaha
- K.Schwarz



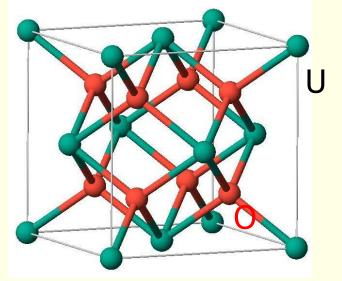






topics

- non-collinear magnetism
- spin-orbit coupling
- LDA+U (correlation of U-5f electrons)
- Structure relaxations
- electric field gradient (EFG)



R.Laskowski, G.K.H.Madsen, P.Blaha, K.Schwarz: *Magnetic structure and electric-field gradients of uranium dioxide: An ab initio study* Phys.Rev.B **69**, 140408-1-4 (2004)



Atomic configuration of uranium (Z=92)



[Rn]

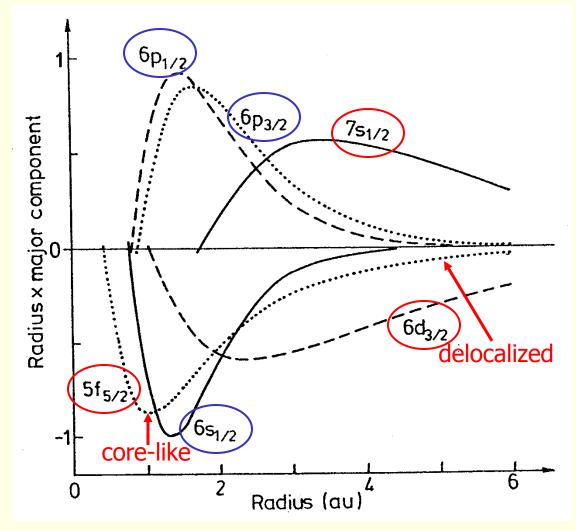
core

U [Xe] 4f¹⁴ 5d¹⁰ 6s² 6p⁶ semi-core

5f³ 6d¹ 7s² valence

E_i (Ryd)

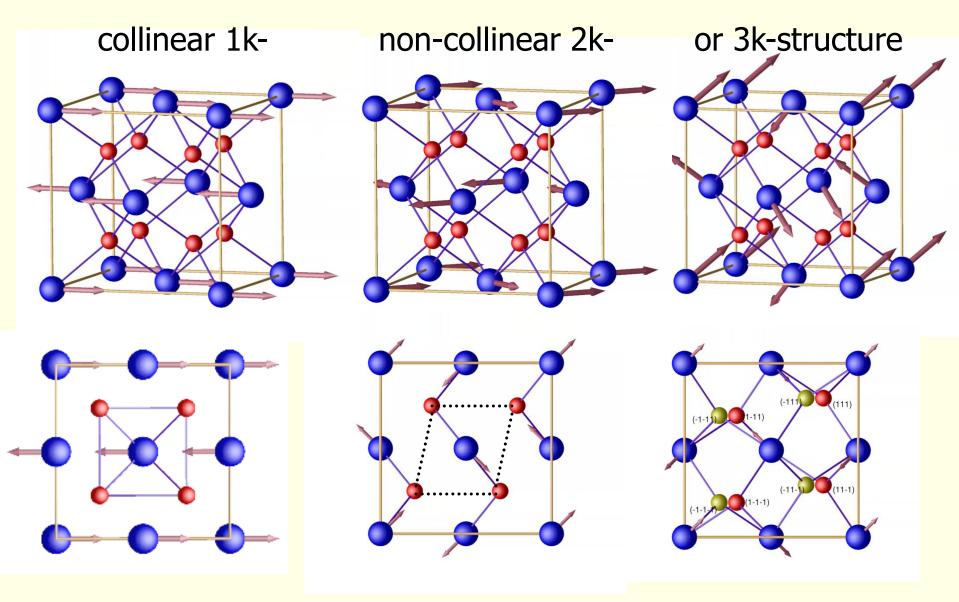
nrel	j (relativ.)	
n l	{-s	ℓ+s
7s		-0.25
6d	-0.29	-0.25
5f	-0.17	-0.11
6р	-1.46	-2.10
6s		-3.40
5d	-7.48	-6.89
5p	-18.05	-14.06
5s		-22.57
4f	-27.58	-26.77
1s		-8513.38





non-collinear magnetism in UO₂

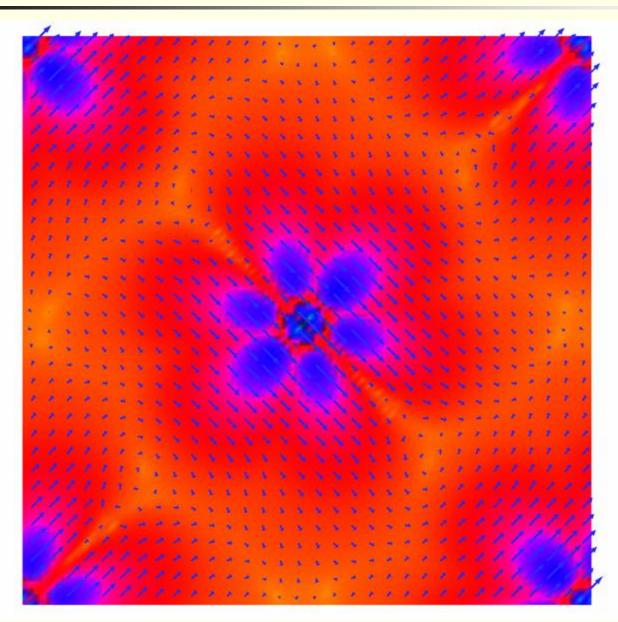




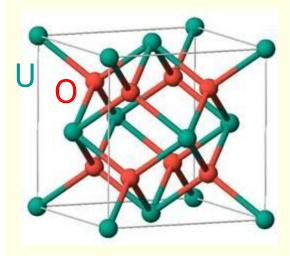


UO₂ 2k structure, LDA+SO+U





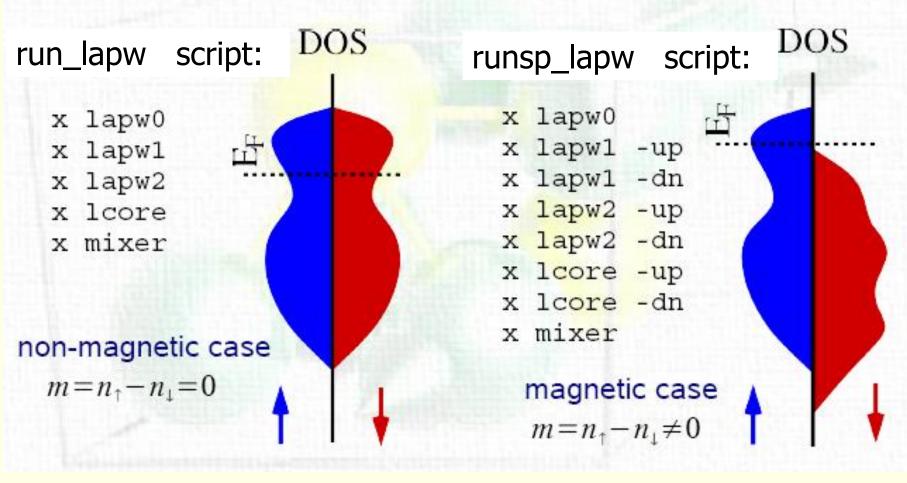
- Magnetisation direction
 perpenticular at the two U sites (arrows)
- Magnetisation density (color)



Magnetism with WIEN2k



Wien2k can only handle collinear or non-magnetic cases





Spin polarized calculations



- runsp_lapw script (unconstrained magnetic calc.)
 - runs lapw1/2 for both spins independently
 - case.scf contains extra information:

```
    grep : MMT case.scf (for total moment)
```

grep :MMI case.scf (for atomic moments)

• grep : HFF case.scf (for hyperfine fields)



Run spin-polarized, FSM or AFM calculations



- runsp_lapw script (unconstrained magnetic calc.)
 - runs lapw1/2 for both spins independently
 - case.scf contains extra information:
 - grep :MMT case.scf (for total moment)
 - grep :MMI case.scf (for atomic moments)
 - grep : HFF case.scf (for hyperfine fields)
- runfsm_lapw -m value (constrained moment calc.)
 - for difficult to converge magnetic cases or simply to constrain a moment (→ 2 Fermi-energies → external magnetic field)
- runafm lapw (anti-ferromagnetic calculation)
 - calculates only spin-up, uses symmetry to generate spin-dn



Various magnetism cases



- runsp_lapw script (unconstrained magnetic calc.)
- runfsm_lapw -m value (constrained moment calc.)
- runafm_lapw (anti-ferromagnetic calculation)

- spin-orbit coupling can be included in second variational step
- never mix polarized and non-polarized calculations in one case directory !!!



Thank you for your attention

