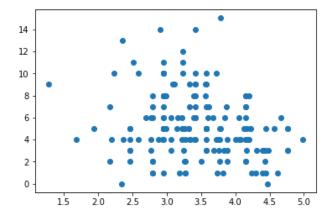
```
In [1]: import pandas as pd
         import numpy as np
In [2]: import matplotlib.pyplot as plt
         import seaborn as sns
         %matplotlib inline
In [3]:
        import statsmodels.formula.api as smf
         from sklearn.metrics import r2_score
In [4]: from sklearn.linear_model import LinearRegression
In [5]:
        from IPython.display import HTML
In [6]: import statsmodels.api as sm
        /Users/kcarnold/anaconda3/envs/py36/lib/python3.6/site-packages/statsmodels/comp
        at/pandas.py:56: FutureWarning: The pandas.core.datetools module is deprecated a
        nd will be removed in a future version. Please use the pandas.tseries module ins
        tead.
          from pandas.core import datetools
In [7]:
        from textrec.paths import paths
In [8]:
        dataset = pd.read csv(paths.data / 'num details training set.csv')
In [9]: sns.distplot(dataset.num_details)
        /Users/kcarnold/anaconda3/envs/py36/lib/python3.6/site-packages/scipy/stats/stat
        s.py:1706: FutureWarning: Using a non-tuple sequence for multidimensional indexi
        ng is deprecated; use `arr[tuple(seq)]` instead of `arr[seq]`. In the future thi
        s will be interpreted as an array index, `arr[np.array(seq)]`, which will result
        either in an error or a different result.
          return np.add.reduce(sorted[indexer] * weights, axis=axis) / sumval
Out[9]: <matplotlib.axes. subplots.AxesSubplot at 0x1c1afe02e8>
         0.200
         0.175
         0.150
         0.125
         0.100
         0.075
         0.050
         0.025
         0.000
                                      10
                              num details
```

## **Preprocessing**

Strip off punctuation; it just throws off token counts and probs. (We get a few percent boost in r^2 because of this.)

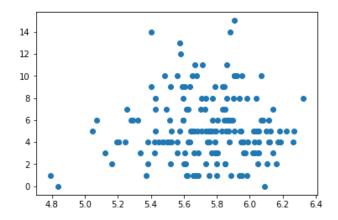
## **Word Frequencies**

```
In [18]: plt.scatter(dataset.min_freq, dataset.num_details)
Out[18]: <matplotlib.collections.PathCollection at 0x1c1de300f0>
```



```
In [19]: plt.scatter(dataset.mean_freq, dataset.num_details)
```

Out[19]: <matplotlib.collections.PathCollection at 0x1c1deae898>



# **Perplexity**

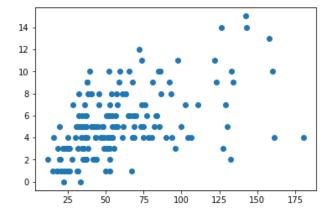
The perplexity of a language model is a rough proxy for the amout of information that a text contains. The more details included, the more uncertainty the LM has; and redundant text doesn't get counted. It's not quite right for a few reasons:

- Typos, grammar errors, etc. also increase perplexity
- Unusual wording of the same concepts increases perplexity
- Using a word that's more common than expected increases perplexity.

But we'll try it anyway.

```
In [20]: from textrec import automated analyses
         from textrec import onmt_model_2
         /Users/kcarnold/anaconda3/envs/py36/lib/python3.6/site-packages/h5py/ init
         :36: FutureWarning: Conversion of the second argument of issubdtype from `float`
         to `np.floating` is deprecated. In future, it will be treated as `np.float64 ==
         np.dtype(float).type`.
           from . conv import register converters as register converters
         Loading ONMT models...
         coco_lm_adam_acc_46.00_ppl_16.32_e10_nooptim.pt
         Loading model parameters.
         coco cap adam acc 48.73 ppl 12.56 e10 nooptim.pt
         Loading model parameters.
         Ready.
         Loading SpaCy...done
In [21]: | automated analyses.eval logprobs unconditional(dataset.text.iloc[0])
Out[21]: 3.3479643
         example text = dataset.text.iloc[0]
In [22]:
         example text
Out[22]: 'families stand around by the water flying kites on a sunny day'
In [23]:
         tokens = onmt_model_2.tokenize(example_text)
         logprobs = onmt_model_2.models['coco_lm'].eval_logprobs('.', tokens, use_eos=True)
         logprobs
Out[23]: array([1.0859766e+01, 4.1381788e+00, 2.3187706e+00, 7.0211720e+00,
                1.5096430e+00, 2.1149969e+00, 5.2354274e+00, 3.4142053e-01,
                5.1307883e+00, 1.5549884e+00, 1.9299134e+00, 3.4333759e-03,
                1.3650393e+00], dtype=float32)
In [24]: dataset['num tokens'] = dataset.text.apply(lambda text: len(onmt model 2.tokenize(
         text)))
         dataset['mean logprob uncond'] = dataset.text.apply(lambda text: automated analyse
         s.eval_logprobs_unconditional(text))
         dataset['total_logprob_uncond'] = dataset.mean_logprob_uncond * (dataset.num_token
         s + 1
In [27]: plt.scatter(dataset.num_tokens, dataset.num_details)
Out[27]: <matplotlib.collections.PathCollection at 0x1c432d8d30>
          14
          12
          10
           8
           6
           4
           2
           0
                     10
                          15
                               20
                                    25
                                         30
                                              35
```

```
In [28]: plt.scatter(dataset.total_logprob_uncond, dataset.num_details)
Out[28]: <matplotlib.collections.PathCollection at 0x1c34f0da90>
```



### **Models**

```
In [29]: dataset.info()
         <class 'pandas.core.frame.DataFrame'>
         RangeIndex: 168 entries, 0 to 167
         Data columns (total 9 columns):
         image_id
                                  168 non-null int64
                                  168 non-null object
         text
         num_details
                                  168 non-null int64
                                  168 non-null int64
         num words
         min freq
                                  168 non-null float64
         mean_freq
                                  168 non-null float64
         num_tokens
                                  168 non-null int64
         mean logprob uncond
                                  168 non-null float64
         total_logprob_uncond
                                  168 non-null float64
         dtypes: float64(4), int64(4), object(1)
         memory usage: 11.9+ KB
```

In [50]: dataset[dataset.num\_words != dataset.num\_tokens][['text', 'num\_words', 'num\_tokens ']]

Out[50]:

|     | text   | num_words | num_tokens |
|-----|--|-----------|------------|
| 14  | a man in a red shirt with two children are on a beach holding a multi-colored kite while other people fly kites in the background                  | 26        | 25         |
| 19  | a man in a red shirt is helping his children fly a large rainbow-colored kite  | 16        | 15         |
| 22  | the image shows a railroad track with a train on it further out in the distance. multiple white buildings hug the side if the track, with some woo | 30        | 31         |
| 35  | a train passing a few small buildings, perhaps the station   | 10        | 11         |
| 41  | a landscape of a train stop with an old-looking brownish train and a few brightly colored buildings to one side                                    | 21        | 20         |
| 43  | a black-and-white picture of a young couple cutting the wedding cake with the help of a young photographer at the wedding event                    | 24        | 22         |
| 45  | a woman is standing next to a couple in front of a cake with a knife in it and holding the other woman's hands                                     | 24        | 25         |
| 56  | a husband, bride and female all stand in front of a table holding a knife cutting a cake   | 18        | 19         |
| 80  | a man-woman gracefully riding a wave using a surfboard   | 10        | 9          |
| 81  | a surfer is riding a wave the water looks so refreshing it's a beautiful day   | 15        | 16         |
| 86  | a double-decker bus drives through a busy city street in london  | 12        | 11         |
| 89  | a busy city street with cars, a large red bus and pedestrians going about their day  | 16        | 17         |
| 91  | the photo shows a downtown scene of a city. there are old buildings everywhere, and a red bus is prominent in the middle of the road. many people  | 32        | 33         |
| 97  | a busy city street with cars and people along the streets with high-rise buildings on both sides   | 18        | 17         |
| 99  | a red double-decker bus driving down a street next to tall buildings and a cloudy sky in london  | 19        | 18         |
| 101 | a red double-decker bus passes a group of people to its left while a black car looks to pass   | 20        | 19         |
| 111 | a curious cat sits perched upon a table, next to a glass of wine   | 14        | 15         |
| 118 | a brownish-orange cat with yellow eyes is look to his left past a glass of red wine  | 18        | 17         |
| 128 | sliding glass, frosted, shower doors with a tan towel hanging on the handle and a white toilet with a blue floor rug                               | 22        | 24         |
| 141 | someone is using a shower but it's hard to see due to the opaque glass   | 15        | 16         |
| 147 | a toilet paper sits on top of a toilet next to the sink, in a plain bathroom   | 17        | 18         |
| 153 | a toilet has a roll of toilet paper on it, and there is a sink that matches it to the right  | 21        | 22         |
| 155 | a sink, mirror and toilet, all in white with a roll of toilet paper on the toilet  | 17        | 19         |

```
In [30]: dataset.mean_freq.describe()
```

```
Out[30]: count 168.000000
                   5.738019
         mean
         std
                    0.283893
         min
                    4.790000
         25%
                    5.579911
         50%
                    5.764444
         75%
                    5.942990
                    6.323333
         max
         Name: mean_freq, dtype: float64
```

Let's try including the interaction of mean\_freq and tokens. That's sorta like the total word frequency.. if we invert frequency to make rarity, then it's total rarity, or something proportional to unigram perplexity.

```
In [31]: dataset['mean_rarity'] = (7 - dataset.mean_freq) / 7
    dataset['max_rarity'] = (7 - dataset.min_freq) / 7
    dataset['total_rarity'] = dataset['mean_rarity'] * dataset['num_words']
```

```
In [32]: | formulas = '''
         C(image_id) + min_freq + mean_freq
         C(image_id) + total_rarity
         C(image_id) + num_tokens + total_rarity
         C(image_id) + num_tokens + total_rarity + total_logprob_uncond + mean_logprob_unco
         nd
         C(image_id) + num_tokens + mean_rarity + max_rarity + total_rarity + total_logprob
          _uncond + mean_logprob_uncond + max_rarity*num_tokens
         C(image_id) + num_tokens + mean_rarity + max_rarity + total_rarity + max_rarity*nu
         m_tokens
         '''.split('\n')
         models = \{\}
         for formula in formulas:
             formula = formula.strip()
             if not formula:
                 continue
             formula_full = 'num_details ~ ' + formula
             models[formula] = model = smf.ols(formula_full, dataset).fit()
             display(HTML(f'<h1>r^2=\{model.rsquared:.3f\}: \{formula\}</h1>'))
             display(model.summary())
```

# r^2=0.385: C(image\_id) + min\_freq + mean\_freq

**OLS Regression Results** 

| Dep. Variable:    |       | num_d          | etails |        | R-se   | quared:   | 0.38   | B5     |
|-------------------|-------|----------------|--------|--------|--------|-----------|--------|--------|
| Model:            |       |                | OLS    | Adj    | . R-sc | quared:   | 0.3    | 50     |
| Method:           |       | Least Sq       | uares  |        | F-st   | tatistic: | 10.9   | 98     |
| Date:             | We    | d, 10 Oct      | 2018   | Prob   | (F-st  | atistic): | 3.40e- | 13     |
| Time:             |       | 09:4           | 49:30  | Log    | g-Like | lihood:   | -378.  | 74     |
| No. Observations: |       |                | 168    |        |        | AIC:      | 777    | .5     |
| Df Residuals:     |       |                | 158    |        |        | BIC:      | 808    | 3.7    |
| Df Model:         |       |                | 9      |        |        |           |        |        |
| Covariance Type:  |       | nonre          | obust  |        |        |           |        |        |
|                   |       | coef           | std e  | rr     | t      | P> t      | [0.025 | 0.975] |
| Interd            | cept  | 3.2883         | 3.93   | 9 0    | .835   | 0.405     | -4.492 | 11.068 |
| C(image_id)[T.223 | 777]  | -2.3113        | 0.80   | 2 -2   | .882   | 0.005     | -3.896 | -0.727 |
| C(image_id)[T.227 | 326]  | -2.1374        | 0.75   | 2 -2   | .841   | 0.005     | -3.624 | -0.651 |
| C(image_id)[T.240 | 275]  | -4.3229        | 0.73   | 6 -5   | .877   | 0.000     | -5.776 | -2.870 |
| C(image_id)[T.247 | 576]  | 1.4757         | 0.75   | 4 1    | .956   | 0.052     | -0.014 | 2.966  |
| C(image_id)[T.275 | 449]  | -1.2033        | 0.74   | .9 -1  | .607   | 0.110     | -2.682 | 0.276  |
| C(image_id)[T.396 | 295]  | -1.1903        | 0.75   | 7 -1   | .572   | 0.118     | -2.686 | 0.305  |
| C(image_id)[T.431 | 140]  | 0.1770         | 0.77   | 2 0    | .229   | 0.819     | -1.349 | 1.703  |
| min_              | freq  | -1.5700        | 0.34   | .2 -4  | .595   | 0.000     | -2.245 | -0.895 |
| mean_             | freq  | 1.4900         | 0.74   | 0 2    | .015   | 0.046     | 0.029  | 2.951  |
| Omnibus:          | 17.29 | 4 <b>Dur</b> l | bin-Wa | tson:  | ;      | 2.051     |        |        |
| Prob(Omnibus):    | 0.00  | 0 <b>Jarqu</b> | e-Bera | (JB):  | 2      | 3.230     |        |        |
| Skew:             | 0.62  | 8              | Prol   | o(JB): | 9.03   | 3e-06     |        |        |
| Kurtosis:         | 4.32  | 0              | Cond   | d. No. |        | 148.      |        |        |
|                   |       |                |        |        |        |           |        |        |

# r^2=0.713: C(image\_id) + total\_rarity

#### **OLS Regression Results**

| Dep. Variable:     |                  | num_de  | etails |        | R-sc   | quared:   | 0.7      | 13     |  |
|--------------------|------------------|---------|--------|--------|--------|-----------|----------|--------|--|
| Model:             | OLS              |         |        | Adj    | R-sc   | quared:   | 0.699    |        |  |
| Method:            | Least Squares    |         |        |        | F-st   | atistic:  | 49.49    |        |  |
| Date:              | Wed, 10 Oct 2018 |         |        | Prob   | (F-sta | atistic): | 2.32e-39 |        |  |
| Time:              |                  | 09:4    | 19:30  | Log    | -Like  | lihood:   | -314.5   | 55     |  |
| No. Observations:  |                  |         | 168    |        |        | AIC:      | 647      | .1     |  |
| Df Residuals:      |                  |         | 159    |        |        | BIC:      | 675      | .2     |  |
| Df Model:          |                  |         | 8      |        |        |           |          |        |  |
| Covariance Type:   |                  | nonro   | bust   |        |        |           |          |        |  |
| ••                 |                  |         |        |        |        |           |          |        |  |
|                    |                  | coef    | std e  | rr     | t      | P> t      | [0.025   | 0.975] |  |
| Interc             | ept              | 2.2352  | 0.47   | '3 4   | .722   | 0.000     | 1.300    | 3.170  |  |
| C(image_id)[T.2237 | 77]              | -3.6844 | 0.49   | 99 -7  | .381   | 0.000     | -4.670   | -2.698 |  |
| C(image_id)[T.2273 | 26]              | -3.6428 | 0.50   | 3 -7   | .243   | 0.000     | -4.636   | -2.649 |  |
| C(image_id)[T.2402 | 75]              | -3.6986 | 0.50   | 00 -7  | .399   | 0.000     | -4.686   | -2.711 |  |
| C(image_id)[T.2475 | 76]              | -0.1979 | 0.50   | )3 -0  | .393   | 0.695     | -1.192   | 0.796  |  |
| C(image_id)[T.2754 | 49]              | -1.7292 | 0.49   | 9 -3   | .464   | 0.001     | -2.715   | -0.743 |  |
| C(image_id)[T.3962 | 95]              | -1.9313 | 0.49   | 99 -3  | .868   | 0.000     | -2.917   | -0.945 |  |
| C(image_id)[T.4311 | 40]              | -0.9063 | 0.50   | 00 -1  | .813   | 0.072     | -1.893   | 0.081  |  |
| total_ra           | rity             | 1.9068  | 0.12   | 26 15  | .109   | 0.000     | 1.658    | 2.156  |  |
|                    |                  |         |        |        |        |           |          |        |  |
| Omnibus:           | 1.608            | Durb    | in-Wa  | tson:  | 1.87   | 7         |          |        |  |
| Prob(Omnibus):     | 0.447            | Jarque  | e-Bera | (JB):  | 1.22   | 7         |          |        |  |
| Skew: -            | 0.183            |         | Prob   | o(JB): | 0.54   | 1         |          |        |  |
| Kurtosis:          | 3.204            |         | Cond   | l. No. | 25.    | 2         |          |        |  |

r^2=0.736: C(image\_id) + num\_tokens + total\_rarity

| OLS Regression Result | OLS | Regression | Result |
|-----------------------|-----|------------|--------|
|-----------------------|-----|------------|--------|

| Dep. Variable:        | num_d         | etails          | R-s             | quared:   | 0.7    | 36     |
|-----------------------|---------------|-----------------|-----------------|-----------|--------|--------|
| Model:                |               | OLS             | Adj. R-s        | quared:   | 0.7    | 21     |
| Method:               | Least Squares |                 | F-s             | tatistic: | 48.90  |        |
| Date: We              | ed, 10 Oct    | 2018 <b>P</b> i | rob (F-st       | atistic): | 3.07e- | 41     |
| Time:                 | 09:4          | 49:30           | Log-Like        | elihood:  | -307.  | 73     |
| No. Observations:     |               | 168             |                 | AIC:      | 635    | 5.5    |
| Df Residuals:         |               | 158             |                 | BIC:      | 666    | 5.7    |
| Df Model:             |               | 9               |                 |           |        |        |
| Covariance Type:      | nonro         | obust           |                 |           |        |        |
|                       | coef          | std err         | t               | P> t      | [0.025 | 0.975] |
| Intercept             | 2.0451        | 0.459           | 4.457           | 0.000     | 1.139  | 2.951  |
| C(image_id)[T.223777] | -3.9423       | 0.486           | -8.112          | 0.000     | -4.902 | -2.982 |
| C(image_id)[T.227326] | -4.0243       | 0.496           | -8.120          | 0.000     | -5.003 | -3.045 |
| C(image_id)[T.240275] | -3.6838       | 0.482           | -7.650          | 0.000     | -4.635 | -2.733 |
| C(image_id)[T.247576] | -0.4408       | 0.489           | -0.901          | 0.369     | -1.407 | 0.526  |
| C(image_id)[T.275449] | -1.8718       | 0.482           | -3.880          | 0.000     | -2.825 | -0.919 |
| C(image_id)[T.396295] | -1.9181       | 0.481           | -3.988          | 0.000     | -2.868 | -0.968 |
| C(image_id)[T.431140] | -1.3426       | 0.496           | -2.707          | 0.008     | -2.322 | -0.363 |
| num_tokens            | 0.1481        | 0.041           | 3.656           | 0.000     | 0.068  | 0.228  |
| total_rarity          | 1.1980        | 0.229           | 5.236           | 0.000     | 0.746  | 1.650  |
| Omnibus: 5.04         | 5 <b>Durt</b> | oin-Watso       | on: 1.7         | 760       |        |        |
| Prob(Omnibus): 0.08   | 30 Jarque     | e-Bera (J       | <b>B):</b> 5.0  | 034       |        |        |
| <b>Skew:</b> -0.28    | 31            | Prob(J          | <b>B):</b> 0.08 | 307       |        |        |
| Kurtosis: 3.63        | 35            | Cond. N         | <b>No.</b> 1    | 40.       |        |        |

r^2=0.743: C(image\_id) + num\_tokens + total\_rarity + total\_logprob\_uncond + mean\_logprob\_uncond

| OLS Regression Result | OLS | Regression | Result |
|-----------------------|-----|------------|--------|
|-----------------------|-----|------------|--------|

| Dep. Variable:             |        | num_de     | tails          | R-sq            | uared:   | 0.743    |        |
|----------------------------|--------|------------|----------------|-----------------|----------|----------|--------|
| Model:                     |        | (          | OLS            | Adj. R-sq       | uared:   | 0.725    |        |
| Method:                    | L      | east Squ   | ares           | F-sta           | atistic: | 41.00    |        |
| Date:                      | Wed    | , 10 Oct 2 | 018 <b>P</b> i | rob (F-sta      | tistic): | 1.84e-40 |        |
| Time:                      |        | 09:49      | 9:30           | Log-Likel       | ihood:   | -305.41  |        |
| No. Observations:          |        |            | 168            |                 | AIC:     | 634.8    |        |
| Df Residuals:              |        |            | 156            |                 | BIC:     | 672.     | 3      |
| Df Model:                  |        |            | 11             |                 |          |          |        |
| Covariance Type:           |        | nonrol     | oust           |                 |          |          |        |
|                            |        | coef       | std err        | t               | P> t     | [0.025   | 0.975] |
| Inte                       | rcept  | 0.7258     | 1.160          | 0.625           | 0.533    | -1.566   | 3.018  |
| C(image_id)[T.22           | 3777]  | -3.7699    | 0.490          | -7.699          | 0.000    | -4.737   | -2.803 |
| C(image_id)[T.227          | 7326]  | -4.0356    | 0.493          | -8.182          | 0.000    | -5.010   | -3.061 |
| C(image_id)[T.240          | 0275]  | -3.6715    | 0.478          | -7.674          | 0.000    | -4.617   | -2.726 |
| C(image_id)[T.247576]      |        | -0.4646    | 0.486          | -0.956          | 0.340    | -1.424   | 0.495  |
| C(image_id)[T.27           | 5449]  | -1.8630    | 0.480          | -3.878          | 0.000    | -2.812   | -0.914 |
| C(image_id)[T.396          | 6295]  | -1.7238    | 0.492          | -3.502          | 0.001    | -2.696   | -0.751 |
| C(image_id)[T.43           | 1140]  | -1.3638    | 0.493          | -2.768          | 0.006    | -2.337   | -0.391 |
| num_to                     | kens   | 0.2491     | 0.081          | 3.091           | 0.002    | 0.090    | 0.408  |
| total_i                    | rarity | 1.3737     | 0.246          | 5.574           | 0.000    | 0.887    | 1.861  |
| total_logprob_un           | cond   | -0.0292    | 0.018          | -1.637          | 0.104    | -0.064   | 0.006  |
| mean_logprob_uncond 0.2810 |        | 0.2810     | 0.277          | 1.014           | 0.312    | -0.266   | 0.828  |
| Omnibus:                   | 3.726  | Durbi      | n-Watso        | on: 1.83        | 7        |          |        |
| Prob(Omnibus):             | 0.155  | Jarque-    | Bera (J        | <b>B):</b> 3.77 | 4        |          |        |
| Skew:                      | -0.180 |            | Prob(J         | <b>B):</b> 0.15 | 2        |          |        |
| Kurtosis:                  | 3.640  |            | Cond. N        | <b>lo.</b> 731  |          |          |        |

r^2=0.745: C(image\_id) + num\_tokens + mean\_rarity + max\_rarity + total\_rarity + total\_logprob\_uncond + mean\_logprob\_uncond + max\_rarity\*num\_tokens

| OLS | Regres | sion | Results |
|-----|--------|------|---------|
|-----|--------|------|---------|

| Dep. Variable:    |        | num_det    | ails         | R-squared:          |          |        | 0.745    |        |
|-------------------|--------|------------|--------------|---------------------|----------|--------|----------|--------|
| Model:            |        | C          | DLS          | Adj                 | . R-squ  | ıared: | 0.722    |        |
| Method:           | L      | east Squa  | ares         | F-statistic:        |          |        | 31.92    |        |
| Date:             | Wed,   | , 10 Oct 2 | 018 <b>P</b> | Prob (F-statistic): |          |        | 2.57e-38 |        |
| Time:             |        | 09:49:30   |              |                     | g-Likeli | hood:  | -304.77  |        |
| No. Observations: |        |            | 168          |                     |          | AIC:   | 639.5    |        |
| Df Residuals:     |        |            | 153          |                     |          | BIC:   | 686.4    |        |
| Df Model:         |        |            | 14           |                     |          |        |          |        |
| Covariance Type:  |        | nonrob     | oust         |                     |          |        |          |        |
|                   |        | coef       | std ei       | r                   | t        | P> t   | [0.025   | 0.975] |
| Inte              | rcept  | 1.8745     | 2.09         | 6                   | 0.894    | 0.372  | -2.266   | 6.015  |
| C(image_id)[T.223 | 3777]  | -3.7092    | 0.55         | 1 -                 | -6.738   | 0.000  | -4.797   | -2.622 |
| C(image_id)[T.22] | 7326]  | -4.0110    | 0.51         | 4 -                 | -7.803   | 0.000  | -5.026   | -2.996 |
| C(image_id)[T.240 | 0275]  | -3.6637    | 0.48         | 5 -                 | -7.551   | 0.000  | -4.622   | -2.705 |
| C(image_id)[T.24] | 7576]  | -0.4367    | 0.51         | 3 -                 | -0.852   | 0.396  | -1.450   | 0.576  |
| C(image_id)[T.27  | 5449]  | -1.8771    | 0.49         | 6 -                 | -3.784   | 0.000  | -2.857   | -0.897 |
| C(image_id)[T.396 | 6295]  | -1.7201    | 0.52         | 0 -                 | -3.308   | 0.001  | -2.748   | -0.693 |
| C(image_id)[T.43  | 1140]  | -1.3342    | 0.51         | 6 -                 | -2.584   | 0.011  | -2.354   | -0.314 |
| num_to            | kens   | 0.1609     | 0.12         | 6                   | 1.274    | 0.204  | -0.089   | 0.410  |
| mean_i            | rarity | -3.8772    | 8.36         | 1 -                 | -0.464   | 0.643  | -20.394  | 12.640 |
| max_i             | rarity | -1.5791    | 3.46         | 3 -                 | -0.456   | 0.649  | -8.421   | 5.263  |
| total_ı           | rarity | 1.5233     | 0.54         | 5                   | 2.796    | 0.006  | 0.447    | 2.600  |
| total_logprob_un  | cond   | -0.0360    | 0.02         | 0 -                 | -1.797   | 0.074  | -0.076   | 0.004  |
| mean_logprob_un   | cond   | 0.3996     | 0.33         | 2                   | 1.205    | 0.230  | -0.256   | 1.055  |
| max_rarity:num_to | kens   | 0.1615     | 0.20         | 4                   | 0.792    | 0.430  | -0.241   | 0.564  |
| Omnibus:          | 4.007  | Durbir     | า-Wats       | on:                 | 1.       | 867    |          |        |
| Prob(Omnibus):    | 0.135  | Jarque-    | Bera (J      | JB):                | 4.       | 201    |          |        |
| Skew: -           | 0.183  |            | Prob(        | JB):                | 0.       | 122    |          |        |
| Kurtosis:         | 3.683  | •          | Cond.        | No.                 | 4.92e    | +03    |          |        |

r^2=0.737: C(image\_id) + num\_tokens + mean\_rarity + max\_rarity + total\_rarity + max\_rarity\*num\_tokens

#### **OLS Regression Results**

| Dep. Variable:    |        | num_det               | ails         | R-squared:   |          |         | 0.737    |        |
|-------------------|--------|-----------------------|--------------|--------------|----------|---------|----------|--------|
| Model:            |        | (                     | DLS          | Adj          | j. R-squ | ıared:  | 0.716    |        |
| Method:           | L      | east Squa             | ares         | F-statistic: |          |         | 36.13    |        |
| Date:             | Wed    | , 10 Oct 2            | 018 <b>P</b> | rob          | (F-stat  | istic): | 7.70e-39 |        |
| Time:             |        | 09:49:30 <b>Log</b> - |              |              | g-Likeli | hood:   | -307.47  |        |
| No. Observations: |        |                       | 168          |              |          | AIC:    | 640.9    |        |
| Df Residuals:     |        |                       | 155          |              |          | BIC:    | 681.5    |        |
| Df Model:         |        |                       | 12           |              |          |         |          |        |
| Covariance Type:  |        | nonrobust             |              |              |          |         |          |        |
|                   |        | coef                  | std er       | r            | t        | P> t    | [0.025   | 0.975] |
| Inte              | rcept  | 3.1419                | 2.03         | 0            | 1.548    | 0.124   | -0.868   | 7.152  |
| C(image_id)[T.22  | 3777]  | -3.9445               | 0.54         | 5 -          | -7.241   | 0.000   | -5.021   | -2.868 |
| C(image_id)[T.22  | 7326]  | -4.0215               | 0.51         | 9 -          | -7.756   | 0.000   | -5.046   | -2.997 |
| C(image_id)[T.24  | 0275]  | -3.6782               | 0.48         | 9 -          | -7.529   | 0.000   | -4.643   | -2.713 |
| C(image_id)[T.24  | 7576]  | -0.4441               | 0.51         | 8 -          | -0.858   | 0.392   | -1.467   | 0.578  |
| C(image_id)[T.27  | 5449]  | -1.9017               | 0.50         | 1 -          | -3.799   | 0.000   | -2.891   | -0.913 |
| C(image_id)[T.39  | 6295]  | -1.9284               | 0.50         | 6 -          | -3.813   | 0.000   | -2.928   | -0.929 |
| C(image_id)[T.43  | 1140]  | -1.3438               | 0.52         | 1 -          | -2.578   | 0.011   | -2.373   | -0.314 |
| num_to            | kens   | 0.0734                | 0.12         | 1            | 0.608    | 0.544   | -0.165   | 0.312  |
| mean_             | rarity | -1.7638               | 6.95         | 2 -          | -0.254   | 0.800   | -15.498  | 11.970 |
| max_              | rarity | -1.4324               | 3.49         | 2 -          | -0.410   | 0.682   | -8.331   | 5.466  |
| total_            | rarity | 1.2691                | 0.49         | 2            | 2.581    | 0.011   | 0.298    | 2.241  |
| max_rarity:num_to | kens   | 0.1159                | 0.20         | 5            | 0.567    | 0.572   | -0.288   | 0.520  |
| Omnibus:          | 4.893  | Durbii                | n-Wats       | on:          | 1.       | 774     |          |        |
| Prob(Omnibus):    | 0.087  | Jarque-               | Bera (J      | B):          | 4.       | 818     |          |        |
| Skew:             | -0.279 |                       | Prob(J       | B):          | 0.0      | 899     |          |        |
| Kurtosis:         | 3.614  |                       | Cond. I      | No.          | 1.08e    | +03     |          |        |

Summary: num\_details increases by 1.4 for each additional token of rarity.

Let's look at resids.

```
In [33]: model = models['C(image_id) + num_tokens + total_rarity']
In [34]: predicted = model.predict(dataset)
```

```
In [35]: plt.scatter(predicted, model.resid)
plt.axhline(0, color='r')
plt.xlabel('$\hat{y}$')
plt.ylabel('residual');
```

10

12

14

Ok, let's have a look at captions for which length and frequency don't predict num\_details well.

ŷ

Ó

```
In [36]:
         dsr = dataset.copy()
In [37]: | dsr['resid'] = model.resid
         dsr['resid_mag'] = model.resid.abs()
         dsr['predicted'] = predicted
         dsr.info()
         <class 'pandas.core.frame.DataFrame'>
         RangeIndex: 168 entries, 0 to 167
         Data columns (total 15 columns):
         image id
                                  168 non-null int64
         text
                                  168 non-null object
         num_details
                                  168 non-null int64
         num_words
                                  168 non-null int64
         min_freq
                                  168 non-null float64
         mean_freq
                                  168 non-null float64
                                  168 non-null int64
         num_tokens
                                  168 non-null float64
         mean_logprob_uncond
         total_logprob_uncond
                                  168 non-null float64
         mean_rarity
                                  168 non-null float64
         max_rarity
                                  168 non-null float64
         total_rarity
                                  168 non-null float64
                                  168 non-null float64
         resid
                                  168 non-null float64
         resid mag
         predicted
                                  168 non-null float64
         dtypes: float64(10), int64(4), object(1)
         memory usage: 19.8+ KB
In [38]: pd.set_option('display.max_colwidth', 150)
```

In [39]: print("over-predicted:") dsr[dsr.predicted.between(4,8)]['image\_id text num\_tokens resid predicted total\_lo

gprob\_uncond num\_details'.split()].sort\_values('resid').iloc[:5]

over-predicted:

#### Out[39]:

|     | image_id | text   | num_tokens | resid     | predicted | total_logprob_uncond | num_details |
|-----|----------|--|------------|-----------|-----------|----------------------|-------------|
| 3   | 200451   | several multicolored kites<br>with streamers are seen<br>soaring above the heads<br>of people  | 13         | -3.965627 | 7.965627  | 54.609120            | 4           |
| 22  | 223777   | the image shows a railroad track with a train on it further out in the distance. multiple white buildings hug the side if the track, with some woo | 31         | -3.901685 | 7.901685  | 180.252899           | 4           |
| 9   | 200451   | one kite flying over four other kites on a blue sky  | 11         | -2.645860 | 6.645860  | 43.533666            | 4           |
| 103 | 247576   | a double decker bus<br>traveling down the middle<br>of the street in the city<br>streets   | 15         | -2.493046 | 6.493046  | 36.642353            | 4           |
| 164 | 431140   | toilet paper roll is on top<br>of the toilet in a mellow<br>yellow painted bathroom  | 15         | -2.422958 | 6.422958  | 75.009583            | 4           |

In [40]: | print("Under-predicted") dsr[dsr.predicted.between(4,8)]['image\_id text num\_tokens resid predicted total\_lo gprob uncond num details'.split()].sort values('resid').iloc[-5:]

Under-predicted

#### Out[40]:

|     | image_id | text  | num_tokens | resid    | predicted | total_logprob_uncond | num_details |
|-----|----------|---|------------|----------|-----------|----------------------|-------------|
| 120 | 275449   | a half full glass of red wine<br>on a table in front of a<br>calico cat                                   | 16         | 2.541694 | 5.458306  | 38.410653            | 8           |
| 145 | 396295   | a tan towel is hanging<br>from a chrome handle on a<br>textured glass shower<br>door                      | 15         | 2.543200 | 6.456800  | 81.209793            | 9           |
| 2   | 200451   | a man and his two children<br>are flying multicolored<br>kites on a sandy beach                           | 14         | 2.646132 | 7.353868  | 39.750552            | 10          |
| 7   | 200451   | a man flies a butterfly kite with his two daughters   | 10         | 3.061945 | 5.938055  | 37.889245            | 9           |
| 151 | 431140   | a bathroom with a white<br>sink and white toilet. a roll<br>of unwrapped toilet paper<br>sits on the bowl | 19         | 3.144114 | 7.855886  | 97.487974            | 11          |

#### I notice:

- We can generally do surprisingly well on this task using total rarity. We can explain about 74% of the variance in details.
- Some of the over-predicts actually have more details than I gave them credit for. Some of the under-predicts are less detailed.
- Some of the over-predicted just have extra words ("there is" one kite; "a view of" a bathroom, "in the city streets"); I went back and stripped them off and the above reflects that. (we get a boost of about 0.01 R^2.)

Since this model has image only as a slope (should be random but alas I'm lazy), we can still get relative details measures.

### Aside: random-effects model.

```
In [41]:
            md = smf.mixedlm("num_details ~ mean_rarity + num_tokens + total_rarity", dataset,
            groups=dataset["image_id"])
            md.fit().summary()
Out[41]:
                      Model: MixedLM
                                       Dependent Variable:
                                                         num_details
             No. Observations:
                                                 Method:
                                                               REML
                                  168
                 No. Groups:
                                    8
                                                   Scale:
                                                              2.4408
                                               Likelihood:
              Min. group size:
                                   21
                                                           -323.9069
              Max. group size:
                                   21
                                              Converged:
                                                                 Yes
             Mean group size:
                                 21.0
                          Coef. Std.Err.
                                                P>|z|
                                                        [0.025
                                                               0.975]
                          0.371
                                  1.431
                                          0.259
                                                0.795
                                                        -2.434
                                                                3.177
               Intercept
                         -2.535
                                  6.720
                                         -0.377 0.706
                                                       -15.707 10.636
             mean_rarity
             num_tokens
                          0.118
                                  0.085
                                         1.392
                                                0.164
                                                        -0.048
                                                                0.285
              total_rarity
                          1.360
                                  0.465
                                         2.924 0.003
                                                        0.449
                                                                2.272
              groups RE 2.372
                                  0.870
```

```
In [42]:
           md = smf.mixedlm("num details ~ total rarity", dataset, groups=dataset["image id"]
           mdf = md.fit()
           mdf.summary()
Out[42]:
                    Model: MixedLM Dependent Variable: num_details
            No. Observations:
                                168
                                              Method:
                                                           REML
                No. Groups:
                                                          2.6164
                                 8
                                               Scale:
             Min. group size:
                                            Likelihood:
                                                       -330.8710
                                 21
             Max. group size:
                                           Converged:
                                 21
                                                            Yes
            Mean group size:
                      Coef. Std.Err.
                                         z P>|z| [0.025 0.975]
             Intercept 0.251
                              0.641
                                     0.392
                                          0.695
                                                 -1.006
                                                         1.508
            total_rarity 1.911
                              0.126 15.161 0.000
                                                 1.664 2.158
            groups RE 2.295
                              0.817
In [43]: r2_score(dataset['num_details'], mdf.predict(dataset))
Out[43]: 0.4685851105546911
```

I don't understand why that R^2 score is much smaller than the fixed-effects version. Probably we have different parameters.

```
In [44]:
         model.params
Out[44]: Intercept
                                   2.045098
         C(image id)[T.223777]
                                  -3.942306
         C(image_id)[T.227326]
                                  -4.024281
         C(image_id)[T.240275]
                                  -3.683757
         C(image id)[T.247576]
                                  -0.440750
         C(image_id)[T.275449]
                                  -1.871804
         C(image_id)[T.396295]
                                  -1.918077
         C(image_id)[T.431140]
                                  -1.342626
         num_tokens
                                   0.148146
         total_rarity
                                   1.198048
         dtype: float64
In [45]: mdf.params
Out[45]: Intercept
                         0.251184
         total rarity
                          1.910701
                          0.877341
         groups RE
         dtype: float64
```

```
In [46]: re_params = pd.Series({k: v.iloc[0] for k, v in mdf.random_effects.items()})
         re_params
Out[46]: 200451
                 1.872634
                -1.622234
         223777
         227326 -1.584410
         240275
                -1.634757
         247576
                 1.683106
         275449
                0.232425
         396295
                0.041020
         431140
                  1.012215
         dtype: float64
In [47]: fixed_params = pd.Series({int(k[14:-1]): v for k, v in model.params.items() if k.s
         tartswith('C')})
         fixed_params
Out[47]: 223777 -3.942306
         227326 -4.024281
         240275 -3.683757
         247576 -0.440750
         275449
                -1.871804
         396295
                -1.918077
         431140 -1.342626
         dtype: float64
In [48]: d = pd.DataFrame(dict(fixed=fixed params + model.params['Intercept'], random=re pa
         rams + mdf.params['Intercept']))
         d['diff'] = d['fixed'] - d['random']
         d['absdiff'] = d['fixed'].abs() - d['random'].abs()
         d.mean(axis=0)
Out[48]: fixed
                 -0.415417
         random
                  0.251184
         diff
                  -0.399082
         absdiff
                  0.008690
         dtype: float64
```

The random-effects estimates are generally smaller.