

# \* Power Transformers:- (Day - 31)

"A Power Transformer is a preprocessing technique that applies power-based mathematical transformations to make data more normally distributed, reduce skewness, and stabilize variance."

⇒ Why it used:-

- To reduce high skewness in data.
- To make distribution more Gaussian-like.
- To improve model performance for algo. sensitive to non-normal data.
- To handle heteroscedasticity (unequal variance)

→ Power Transformers data ne more normal banava mate power-based math function apply kare che

⇒ Types of Power-Transformers:- [Complex Math. Trans.]

(1) Box - Cox Transform:-

"Box-Cox is a power transformation method that transforms strictly positive data into a more normal distribution using an optimized lambda parameter ( $\lambda$ )."

→ Box-Cox only positive data par kaam kare che  
ane skewness ghatavi ne distribution ne smooth  
banave che

⇒ Why it is used.

- To reduce positive skewness.
- To stabilize variance.
- To make data more normal for statistical / machine learning models.
- Works well when all values are  $> 0$ .

⇒ Formula:-

$$x_i^\lambda = \begin{cases} \frac{x_i^\lambda - 1}{\lambda} & \text{if } \lambda \neq 0 \\ \ln(x_i) & \text{if } \lambda = 0 \end{cases}$$

⇒ When to use Box-Cox:-

- when all values are strictly positive.
- when your data shows right / positive skewness.
- when you want a transformation similar to log or sqrt but optimized automatically.
- Best for continuous, positive-only features.

→ The exponent here is a variable called lambda ( $\lambda$ ) that varies over the range of  $-5$  to  $5$ , and in the process of searching, we examine all values of  $\lambda$ . Finally, we choose the optimal value (resulting in the best approximation to a normal distribution) for your variable.

→ Aana j special case thi che Log and sq/sqrt.

## (2) Yeo-Johnson Transformation :-

"Yeo-Johnson is an extended version of Box-Cox that can transform positive, zero, and negative values without needing to shift the data."

→ Yeo-Johnson positive and negative banne values par kam kare che one data ne normal shape ma lai \$ jai che.

⇒ Why it is used:-

- To reduce skewness in data that has both positive and negative values.
- To automatically estimate the best power parameter.
- To stabilize variance when the dataset contains zeros or negative.

⇒ Formulas:-

$$x_i^{(\lambda)} = \begin{cases} [(x_i + 1)^\lambda - 1] / \lambda & \text{if } \lambda \neq 0, x_i \geq 0 \\ \ln(x_i) + 1 & \text{if } \lambda = 0 ; x_i \geq 0 \\ -[(-x_i + 1)^{2-\lambda} - 1] / (2-\lambda) & \text{if } \lambda \neq 2, x_i < 0 \\ -\ln(-x_i + 1) & \text{if } \lambda = 2, x_i < 0. \end{cases}$$

## ⇒ When to use :-

- When data contains zero or negative values.
- When you want a Box-Cox-like transformation but without positivity restrictions.
- When your data distribution is heavily skewed in either direction.
- Works for both positive and negative continuous feature.

→ This transformation is somewhat of an adjustment to the Box-Cox transformation, by which we can apply it to negative numbers.