

SO FAR...

$$\hat{y}_i = b_0 + b_1 x_i$$

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↑
dependent
variable

↑
single
regressor



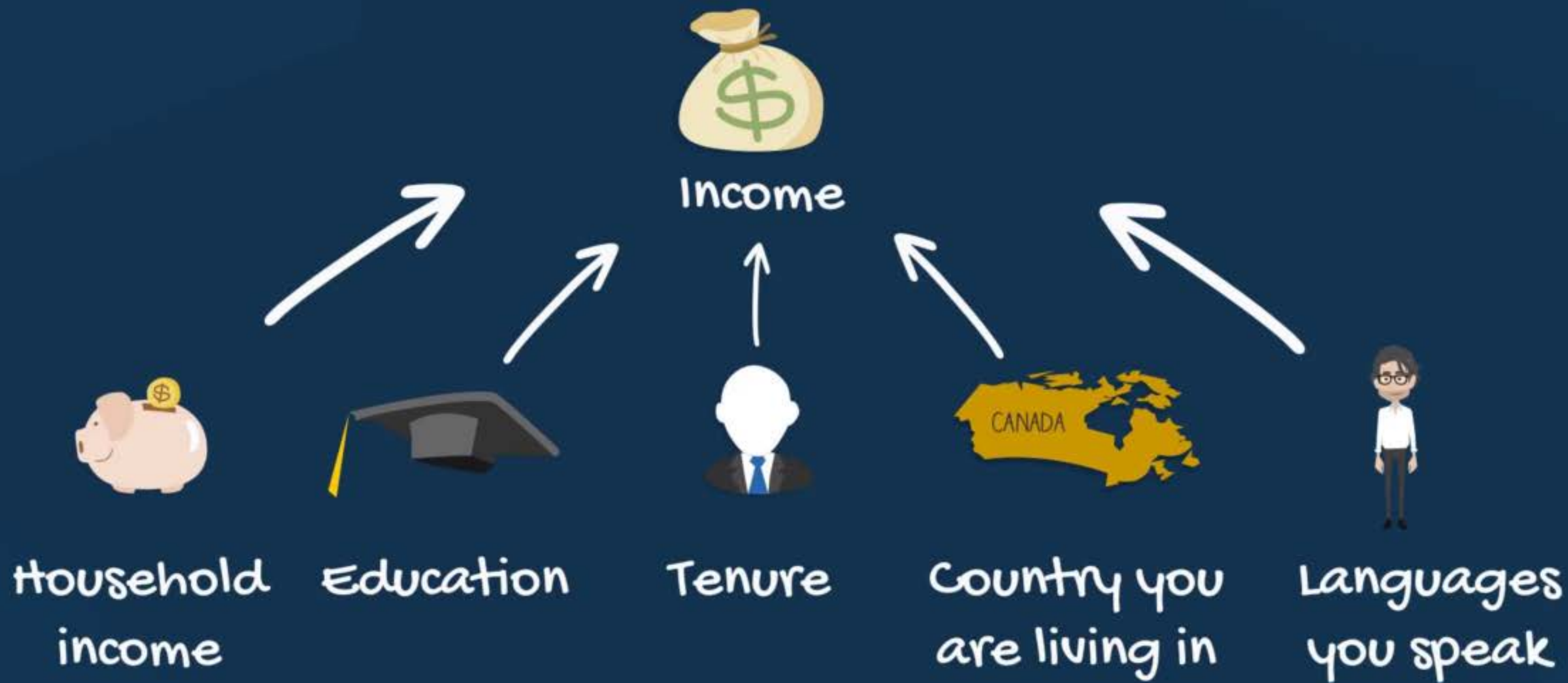
Income



Income



Education





house price



House price



Size



House price



Location



Size



Year

$$\text{College GPA} = 0.275 + 0.0017 * \text{SAT}$$

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Good models require multiple regressions, in order to address the higher complexity of problems



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POPULATION MODEL

$$\gamma = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \cdots + \beta_k x_k + \varepsilon$$

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MULTIPLE REGRESSION EQUATION

$$\hat{y} = b_0 + b_1x_1 + b_2x_2 + \cdots + b_kx_k$$

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$$\hat{y} = b_0 + b_1x_1 + b_2x_2 + \cdots + b_kx_k$$



inferred
value



intercept

MULTIPLE REGRESSION EQUATION

$$\hat{y} = b_0 + b_1x_1 + b_2x_2 + \cdots + b_kx_k$$



independent
variable



independent
variable



independent
variable

MULTIPLE REGRESSION EQUATION

$$\hat{y} = b_0 + b_1x_1 + b_2x_2 + \cdots + b_kx_k$$



coefficient



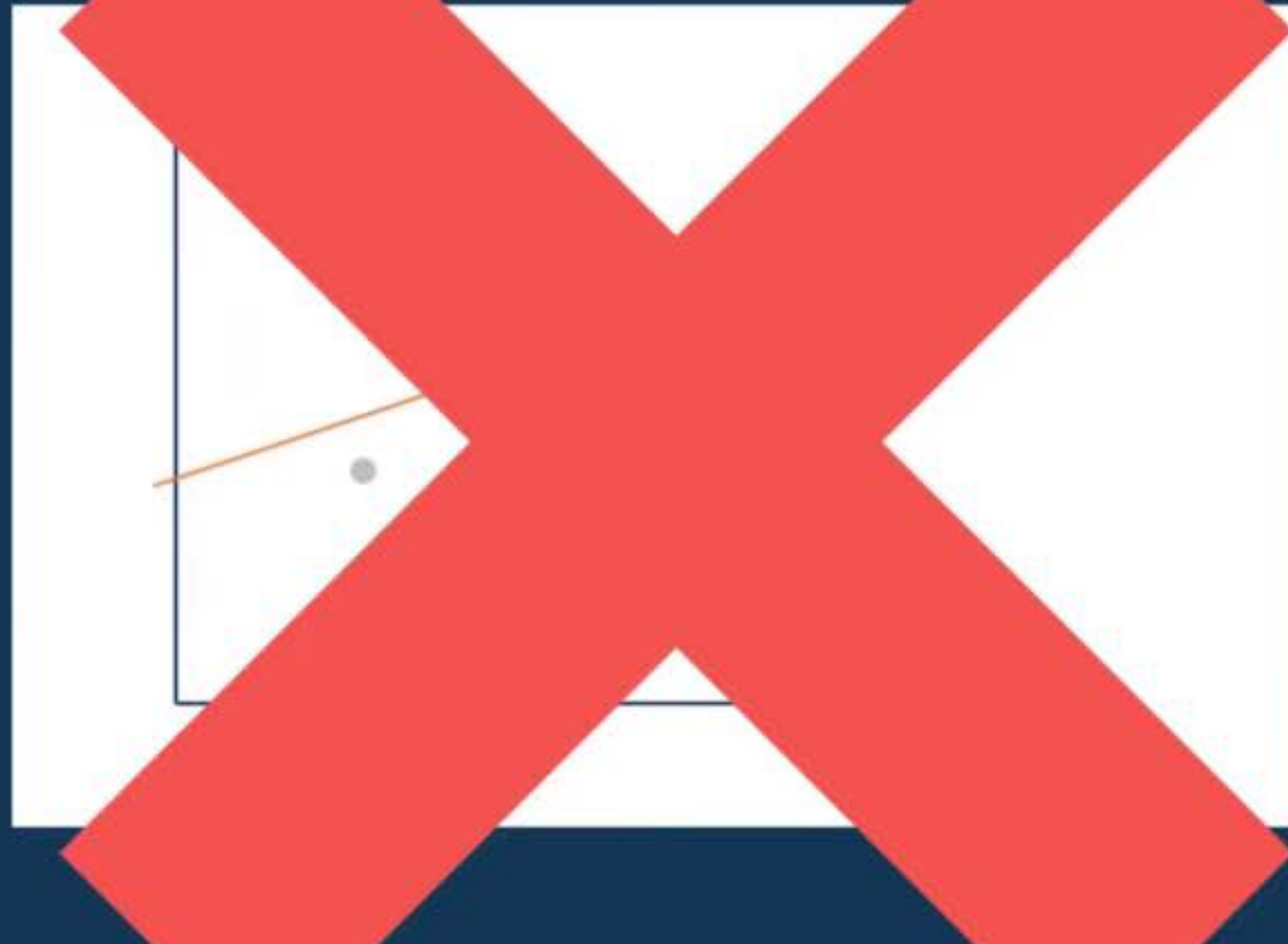
coefficient



coefficient

MULTIPLE REGRESSION EQUATION

$$\hat{y} = b_0 + b_1x_1 + b_2x_2 + \cdots + b_kx_k$$



MULTIPLE REGRESSION EQUATION

$$\hat{y} = b_0 + b_1x_1 + b_2x_2 + \cdots + b_kx_k$$

After 3 dimensions, there is no visual way to represent the data

MULTIPLE REGRESSION EQUATION

$$\hat{y} = b_0 + b_1x_1 + b_2x_2 + \cdots + b_kx_k$$

IT'S ABOUT THE BEST FITTING

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MULTIPLE REGRESSION EQUATION

$$\hat{y} = b_0 + b_1x_1 + b_2x_2 + \cdots + b_kx_k$$

IT'S ABOUT THE BEST FITTING MODEL

After 3 dimensions, there is no visual way to represent the data

MULTIPLE REGRESSION EQUATION

$$\hat{y} = b_0 + b_1x_1 + b_2x_2 + \cdots + b_kx_k$$

min *SSE*

MULTIPLE REGRESSION EQUATION

$$\hat{y} = b_0 + b_1x_1 + b_2x_2 + \cdots + b_kx_k$$

min *SSE*

SSE



SSR



MULTIPLE REGRESSION EQUATION

$$\hat{y} = b_0 + b_1x_1 + b_2x_2 + \cdots + b_kx_k$$

min ***SSE***

SSE ↓



SSR ↑



MULTIPLE REGRESSION EQUATION

$$\hat{y} = b_0 + b_1x_1 + b_2x_2 + \cdots + b_kx_k$$



min ***SSE***

SSE ↓



SSR ↑

