

Exam 2 Review Key

① $y = 3x^2 - 12x + 1$

$y = 3(x^2 - 4x + 4) + 1$

$12 + y = 3x^2 - 12x + 12 + 1$

$y = 3(x-2)^2 - 11$

③ $y = 3x^2 - 12x + 1$

$y = 3(x-2)^2 - 11$

minimum
pt (2, -11)

↑ moved right 2 and down 11

83 $f(x) = x^2 - x - 2$

x-intercept

$y = 0$

$0 = x^2 - x - 2$

$0 = (x-2)(x+1)$

$x = 2 \quad x = -1$

$(2, 0) \quad (-1, 0)$

y-intercept

$x = 0$

$y = (0)^2 - (0) - 2$

$y = -2$

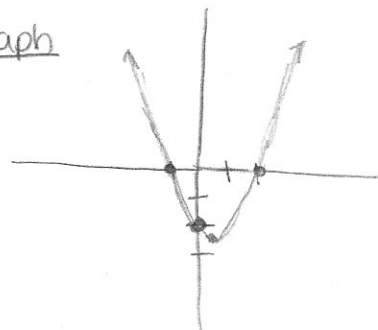
$(0, -2)$

asymptotes

* There are no

asymptotes

Graph



102 $x^2 + 2x < 63$

$x^2 + 2x - 63 < 0$

$(x+9)(x-7) < 0$

$x = -9 \quad x = 7$

$-9 < x < 7$

115 $S = -16t^2 + 156t$

t-intercept

$9.75/2 = 4.875$

$s = 0$

$t = 4.875$

$0 = -16t^2 + 156t$

$-380.25 + 760.5 = 380.5$

$0 = t(-16t + 156)$

$t = 0 \quad t = 9.75$

Max: 380.5 ft at 4.875 secs

② ⑦ $f(x) = 3x - 1$

$0 = 3x - 1$

$x = 1/3$

⑨ $h(x) = x^2 - 8$

$0 = x^2 - 8$

$8 = x^2$

$x = \pm\sqrt{8} \approx \pm 2\sqrt{2}$

⑪ $n(x) = 8x^3 - 1$

$0 = 8x^3 - 1$

$1/8 = x^3$

$x = \sqrt[3]{1/8} = 1/2$

$$\frac{1}{2} \begin{vmatrix} 8 & 0 & 0 & -1 \\ & 4 & 2 & 1 \\ & 8 & 4 & 2 & 0 \end{vmatrix}$$

↓

$8x^2 + 4x + 2$

$2(4x^2 + 2x + 1)$

$-2 \pm \sqrt{4 - 4(4)(1)}$

$2(4)$

$\frac{-2 \pm \sqrt{12}}{8} = \frac{-2 \pm 2i\sqrt{3}}{8}$

$\frac{-1 \pm i\sqrt{3}}{4}$

⑬ $P(t) = t^4 - 100$

$(t^2 - 10)(t^2 + 10)$

$t = \pm\sqrt{10} \quad t = \pm\sqrt{-10}$

$t = \sqrt{10}, -\sqrt{10}, -i\sqrt{10}, i\sqrt{10}$

$$16) R(s) = 8s^3 - 4s^2 - 2s + 1$$

$$\frac{1}{8} = \frac{\pm 1}{\pm 1, 2, 4, 8} = \pm 1, \pm \frac{1}{2}, \pm \frac{1}{4}, \pm \frac{1}{8}$$

$$\begin{array}{r|rrrr} 1/2 & 8 & -4 & -2 & 1 \\ & & 4 & 0 & -1 \\ \hline & 8 & 0 & -2 & 0 \end{array}$$

$$\rightarrow 8x^2 - 2 \Rightarrow 2(4x^2 - 1) \Rightarrow x = \sqrt{1/4} = \pm 1/2$$

$$x = \frac{1}{2}, -\frac{1}{2}$$

$$17) f(x) = x^3 + 2x^2 - 6x$$

$$= x(x^2 + 2x - 6)$$

$$\frac{-2 \pm \sqrt{4 - 4(1)(-6)}}{2} = \frac{-2 \pm \sqrt{28}}{2} = \frac{-2 \pm 2\sqrt{7}}{2} = -1 \pm \sqrt{7}$$

$$x = 0, -1 + \sqrt{7}, -1 - \sqrt{7}$$

$$23) f(x) = -3x^3 + 6x^2 + 5x - 2$$

$$\frac{-2}{-3} = \frac{2}{3} = \frac{\pm 2, 1}{\pm 3, 1} = 1, -1, 2, -2, \frac{2}{3}, -\frac{2}{3}, \frac{1}{3}, -\frac{1}{3}$$

$$27) -\frac{1}{2}, 3$$

$$(2x+1)(x-3) = 2x^2 - 6x + x - 3 = 2x^2 - 5x - 3$$

$$29) 3 - 2i = 3 - \sqrt{-4} \quad x = 3 - \sqrt{-4} \Rightarrow 3 - x = \sqrt{-4} \Rightarrow (3-x)^2 = -4 \Rightarrow (3-x)^2 + 4$$

$$(3-x)(3-x) = 9 - 3x - 3x + x^2 + 4 = x^2 - 6x + 13$$

$$4) x^3 - 6x^2 + 11x - 6 = 0$$

$$\frac{1}{6} = \frac{\pm 1}{\pm 1, 2, 3, 6} = \pm 1, \pm \frac{1}{2}, \pm \frac{1}{3}, \pm \frac{1}{6}$$

$$1) \begin{array}{r|rrrr} & 1 & -6 & 11 & -6 \\ & & 1 & -5 & 6 \\ \hline & 1 & -5 & 6 & 0 \end{array}$$

$$x^2 - 5x + 6$$

$$(x-6)(x+1)$$

$$x = 6, -1, 1$$

$$49) 6x^4 - 5x^3 + 7x^2 - 5x + 1 = 0$$

$$\frac{1}{6} = \frac{\pm 1}{\pm 1, 2, 3, 6}$$

$$\begin{array}{r|rrrrr} 1/2 & 6 & -5 & 7 & -5 & 1 \\ & & 3 & -1 & 3 & -1 \\ \hline & 6 & -2 & 6 & -2 & 0 \end{array}$$

$$x = \frac{1}{2}, \frac{1}{3}, 1, -1$$

$$\begin{array}{r|rrrr} 1/3 & 6 & -2 & 6 & -2 & 0 \\ & & 2 & 0 & 2 & \\ \hline & 6 & 0 & 6 & 0 & \end{array}$$

$$6x^2 + 6 = 6(x^2 + 1)$$

$$51) x^3 - 9x^2 + 28x - 30 = 0$$

$$\frac{-30}{1} = \pm 1, 2, 3, 5, 6, 10, 15, 30$$

$$\begin{array}{r|rrrr} 3 & 1 & -9 & 28 & -30 \\ & & 3 & -18 & 30 \\ \hline & 1 & -6 & 10 & 0 \end{array}$$

$$x = 3, 3+i, 3-i$$

$$x^2 - 6x + 10$$

$$\frac{6 \pm \sqrt{36 - 4(1)(10)}}{2} = \frac{6 \pm \sqrt{36 - 40}}{2} = \frac{6 \pm \sqrt{-4}}{2} = \frac{6 \pm 2i}{2} = 3 \pm i$$

$$53) x^3 - 4x^2 + 7x - 6$$

$$\frac{-6}{1} = \pm 1, 2, 3, 6$$

$$\begin{array}{r|rrrr} 2 & 1 & -4 & 7 & -6 \\ & & 2 & -4 & 6 \\ \hline & 1 & -2 & 3 & 0 \end{array}$$

$$x = -1, 2, 3$$

$$x^2 - 2x + 3$$

$$(x-3)(x+1)$$

$$55) 2x^4 - 5x^3 - 2x^2 + 2x = 0 \Rightarrow x(2x^3 - 5x^2 - 2x + 2)$$

$$\frac{2}{2} = \frac{\pm 1, 2}{\pm 1, 2} = \pm 1, \pm 2, \pm \frac{1}{2}$$

$$\begin{array}{r|rrrrr} 1/2 & 2 & -5 & -2 & 2 \\ & & 1 & -2 & -2 \\ \hline & 2 & -4 & -4 & 0 \end{array}$$

$$\frac{2 \pm \sqrt{4 - 4(1)(-2)}}{2} = \frac{2 \pm \sqrt{4 + 8}}{2} = \frac{2 \pm \sqrt{12}}{2} = \frac{2 \pm 2\sqrt{3}}{2} = 1 \pm \sqrt{3}$$

$$x = 0, 1/2, 1+\sqrt{3}, 1-\sqrt{3}$$

$$2x^2 - 4x - 4 \Rightarrow 2(x^2 - 2x - 2)$$

$$57) |2v-1| = 3v$$

$$59) x^4 + 7x^2 = 18$$

$$61) \sqrt{x+6} - \sqrt{x-5} = 1$$

$$x^4 + 7x^2 - 18 = 0$$

$$(\sqrt{x+6})^2 = (1 + \sqrt{x-5})^2 (1 + \sqrt{x-5})$$

$$(x^2 - 2)(x^2 + 9)$$

$$x+6 = 1 + 2\sqrt{x-5} + x+5$$

$$x = \pm 2$$

imaginary

$$x+6 = 6+x+2\sqrt{x-5}$$

$$2\sqrt{x-5} = 0$$

$$x = -5$$

$$60) x^4 - 3x^2 - 4 = 0$$

$$(x^2 - 4)(x^2 + 1)$$

$$x = \pm 2$$

imaginary

$$66) (y-1)^2 - (y-1) = 2$$

$$67) (x-1)^{2/3} = 4$$

$$(y-1)^2 = y+1$$

$$y^2 - 2y + 1 = y + 1$$

$$y^2 - 3y = 0$$

$$y(y-3) = 0$$

$$y = 0, 3$$

69 $(x+3)^{-3/4} = -8$

$\frac{1}{(x+3)^{3/4}} = -8$

5 85 $f(x) = x^3 - 3x - 2$

x-intercepts

when $y=0$

$0 = x^3 - 3x - 2 \quad \frac{2}{1} = \frac{\pm 1, 2}{\pm 1} = \pm 1, 2$

2 | 1 0 -3 -2
2 4 2

1 2 1 0

$x^2 + 2x + 1$

$(x+1)(x+1)$

$x = -2, -1$

y-intercept

when $x=0$

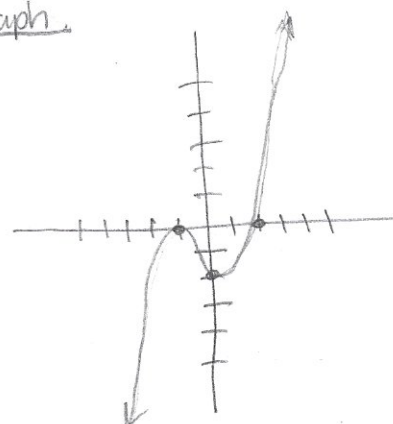
$y = (0)^3 - 3(0) - 2$

$y = -2$

asymptotes

*none

Graph



87 $f(x) = \frac{1}{2}x^3 - \frac{1}{2}x^2 - 2x + 2$

x-intercepts

when $y=0$

$0 = \frac{1}{2}x^3 - \frac{1}{2}x^2 - 2x + 2$

$0 = \frac{1}{2}(x^3 - x^2 - 4x + 4) \quad \frac{4}{1} = \frac{\pm 1, 2, 4}{\pm 1} = \pm 1, 2, 4$

2 | 1 -1 -4 4
2 2 -4

1 1 -2 0

$x^2 + x - 2$

$(x+2)(x-1)$

$x = -2, 1, 2$

y-intercept

when $x=0$

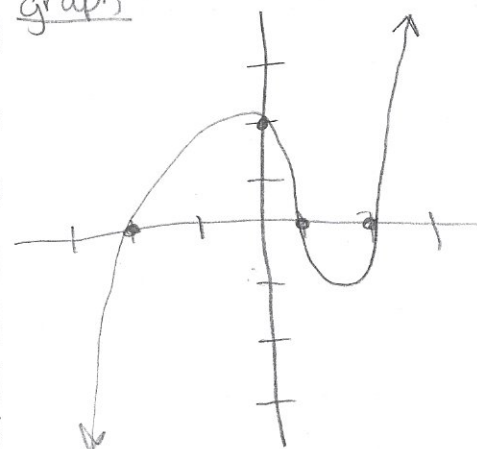
$y = \frac{1}{2}(0)^3 - \frac{1}{2}(0)^2 - 2(0) + 2$

$y = 2$

asymptotes

*none

graph



105 $4x^3 - 400x^2 - x + 100 \geq 0$

$$\begin{array}{r|rrrr} 100 & 4 & -400 & -1 & 100 \\ & & 400 & 0 & -100 \\ \hline & 4 & 0 & -1 & 0 \end{array}$$

$$4x^2 - 1$$

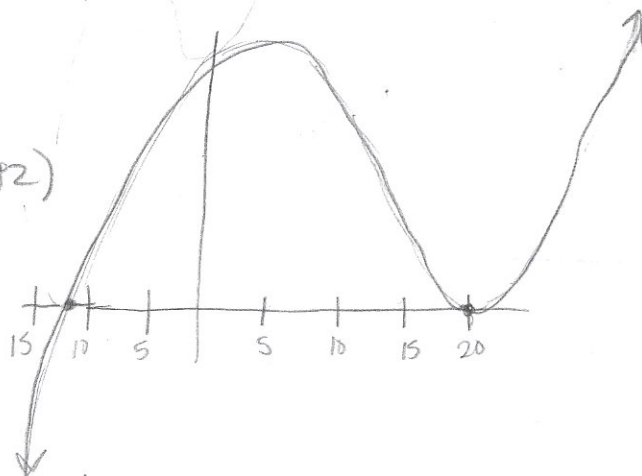
$$(2x+1)(2x-1)$$

$$x = -1/2, 1/2, 100$$

$$\frac{100}{4} = \frac{\pm 1, 2, 4, 5, 10, 20, 25, 50, 100}{\pm 1, 2, 4} = \pm 1, 2, 4, 5, 10, 20, 25, 50, 100$$

$$-1/2 \leq x \leq 1/2 \cup x \leq 100$$

6 Graph $f(x) = (x-20)^2 (x+12)$
 $0 = (x-20)(x-20)(x+12)$
 $x = 20^{1/2}, -12$



7 q1. $f(x) = \frac{2}{x+3}$

x-intercepts

$$0 = \frac{2}{x+3}$$

does not exist

you cannot divide by 0

y-intercepts

$$y = \frac{2}{0+3}$$

$$y = 2/3$$

$$(0, 2/3)$$

Asymptotes

when $x = -3$

there is a vertical asymptotes.

93. $f(x) = \frac{2x}{x^2-4}$

x-intercepts

$$0 = \frac{2x}{x^2-4}$$

when $x=0$ then you get

$$0/-4 = 0$$

$$(0, 0)$$

y-intercept

$$y = \frac{2(0)}{0-4} = 0$$

$(0, 0)$ is the

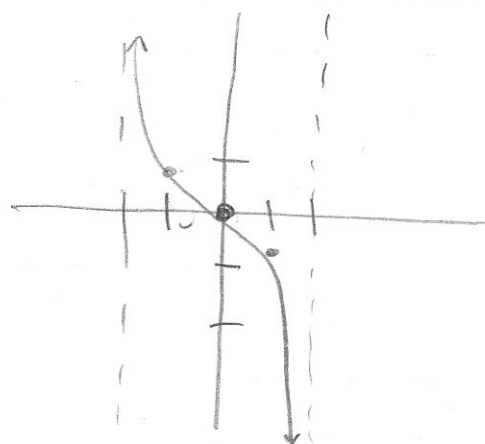
y-intercept as

well,

Asymptotes

when $x = 2, -2$

you have a vertical asymptote



95. $f(x) = \frac{x^2-2x+1}{x-2} = \frac{(x-1)(x-1)}{x-2}$

x-intercepts

$$0 = \frac{x^2-2x+1}{x-2}$$

$$0 = (x-1)(x-1)$$

$$x = 1$$

$$(1, 0)$$

y-intercepts

$$y = \frac{0^2-2(0)+1}{0-2}$$

$$y = -1/2$$

$$(0, -1/2)$$

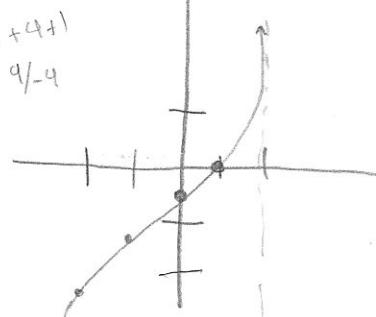
Asymptotes

when $x = 2$

there is a vertical asymptote

vertical asymptote

$$\frac{4+4+1}{4-4}$$



97. $f(x) = \frac{2x-1}{2-x}$

x-intercept

$$0 = \frac{2x-1}{2-x}$$

$$0 = 2x - 1$$

$$x = 1/2$$

$$(1/2, 0)$$

y-intercept

$$y = \frac{2(0)-1}{2-(0)}$$

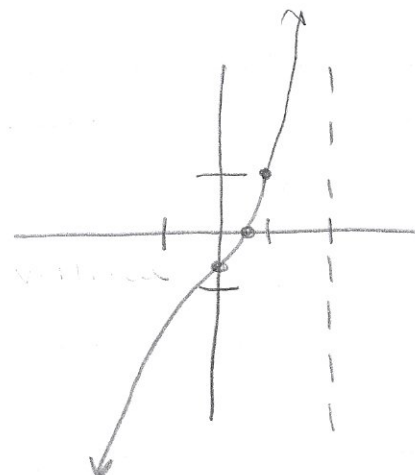
$$y = -1/2$$

$$(0, -1/2)$$

asymptotes

$$2-x=0$$

$x=2$ there is a vertical asymptote



107. $\frac{x+10}{x+2} < 5$

$$x+10 < 5x+10$$

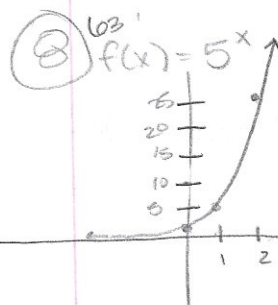
$$0 < 4x$$

$$x > 0$$

check

$$x = -1$$

$$9/1 \neq 5$$

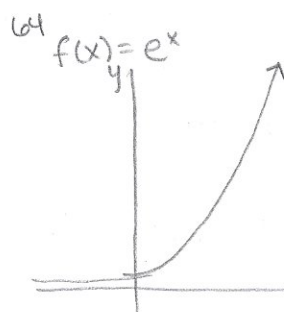


domain: $(-\infty, \infty)$

range: $(0, \infty)$

it is an increasing fxn

Asymptote at $y=0$



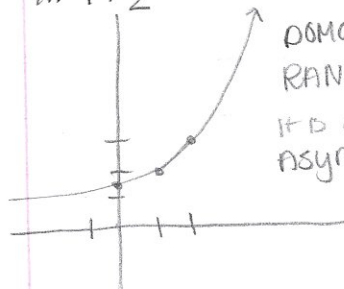
domain: $(-\infty, \infty)$

range: $(0, \infty)$

it is an increasing fxn

Asymptote at $y=0$

71. $1+2^{x-1}$



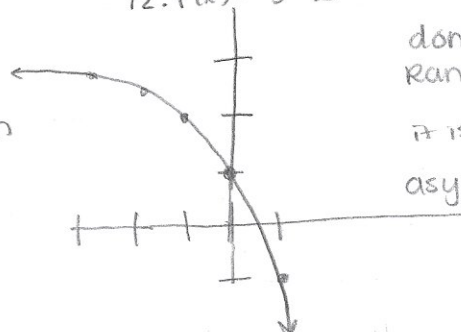
domain: $(-\infty, \infty)$

range: $(1, \infty)$

it is an increasing fxn

asymptote at $y=1$

72. $f(x) = 3-2^{x+1}$



domain: $(-\infty, \infty)$

range: $(-\infty, 3)$

it is a decreasing fxn

asymptote at $y=3$

105. 50,000, 5% compounded quarterly, at the end of 18 years?

$$A = P(1 + \frac{r}{n})^{nt} \Rightarrow A = 50000(1 + \frac{.05}{4})^{4 \cdot 18} \Rightarrow A = 50000(\frac{4.05}{4})^{76}$$

106. 30,000, 6.18% compounded continuously, after 12 yr \approx 3 months

$$A = Pe^{rt} \Rightarrow A = 30000e^{.0618 \cdot 12.25} = 63959.328$$

9 33. $\log(x) = 10 \Rightarrow 10^{10} = x$

35. $\log_x(81) = 4 \Rightarrow x^4 = 81 \Rightarrow x = \pm 3$

37. $\log_{1/3}(27) = x+2 \Rightarrow \frac{1}{3}^{x+2} = 27$

$$\frac{1}{3}^x \cdot \frac{1}{3}^2 = 27 \Rightarrow \frac{1}{9}(\frac{1}{3})^x = 27 \Rightarrow (\frac{1}{3})^x = 243$$

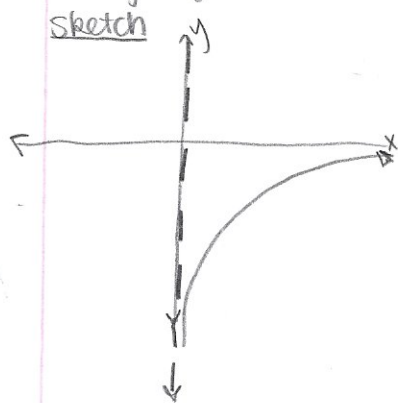
39. $3^{x+2} = \frac{1}{9} - 4 \Rightarrow (x+2)\log(3) = \log(\frac{1}{9} - 4) \Rightarrow x+2 = \frac{\log(\frac{1}{9} - 4)}{\log(3)}$
 $\Rightarrow x = \frac{\log(\frac{1}{9} - 4)}{\log(3)} - 2$

41. $e^{x-2} = 9 \Rightarrow (x-2)\ln(e) = \ln 9 \Rightarrow x-2 = \ln 9 \Rightarrow x = \ln 9 + 2 \approx 4.197$

43. $4^{x+3} = \frac{1}{2^x} \Rightarrow 4^x \cdot 4^3 = \frac{1}{2^x} \Rightarrow 64 \cdot 4^x = \frac{1}{2^x} \Rightarrow 4^x \cdot 2^x = \frac{1}{64}$

67. $y = \log_3(x)$

Sketch



Domain: $(0, \infty)$

Range: $(-\infty, \infty)$

Increasing/Decreasing:

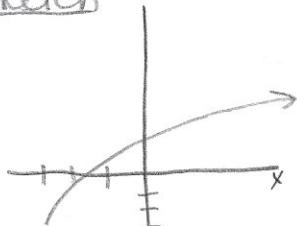
Increasing

Asymptotes:

Vertical at $x=0$

69. $y = 1 + \ln(x+3)$

Sketch



DOMAIN:

$(-3, \infty)$

RANGE:

$(-\infty, \infty)$

Increasing/decreasing:

increasing

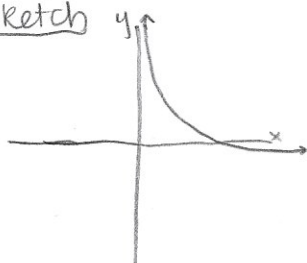
Asymptotes:

vertical asymptote at $x = -3$

horizontal asymptote at $y = -3$

70. $y = 3 - \log_2(x)$

Sketch



DOMAIN:

$(0, \infty)$

RANGE:

$(-\infty, \infty)$

Increasing/decreasing:

decreasing

Asymptotes

vertical asymptote at $x = 0$

10

21. $\log(x-3) + \log(x) \Rightarrow \log(x(x-3)) \Rightarrow \log(x^2 - 3x)$

23. $2 \cdot \ln(x) + \ln(y) + \ln(3) \Rightarrow \ln(x^2) + \ln(3y) \Rightarrow \ln(3x^2y)$

24. $3 \cdot \log_2(x) - 2 \cdot \log_2(y) + \log_2(z) \Rightarrow \log_2(x^3) - \log_2(y^2) + \log_2(z) = \log_2(x^3y^2z)$

25. $\log(3x^4) = \log(3) + \log(x^4) = \log(3) + 4 \cdot \log(x)$

27. $\log_3\left(\frac{5\sqrt{x}}{y^4}\right) = \log_3(5\sqrt{x}) - \log_3(y^4) \Rightarrow (\log_3(5) + \log_3(x^{1/2})) - 4\log_3(y)$
 $\Rightarrow (\log_3(5) + 1/2 \cdot \log(x)) - 4\log_3(y)$

41. $e^{x-2} = 9 \Rightarrow (x-2)\ln(e) = \ln 9 \Rightarrow x = \ln(9) + 2 = 4.197$

43. $\log_4 4^{x+3} = \log_4 \frac{1}{2^x} \Rightarrow (x+3)\log(4) = \log\left(\frac{1}{2^x}\right) \Rightarrow (x+3)\log(4) = \log(1) - x\log(2)$
 $\Rightarrow x\log 4 + 3\log 4 = -x\log 2$

$x\log 4 + x\log 2 = -3\log 4$

$x = \frac{-3\log 4}{\log 4 + \log 2} = -2$

45. $\log(x) + \log(2x) = 5 \Rightarrow \log(x(2x)) = 5 \Rightarrow \log(2x^2) = 5 \Rightarrow 2x^2 = 10^5 \Rightarrow$

$x^2 = 50000$

$x = 100\sqrt{5} = 223.61$

$$47. \log_2(x) + \log_2(x-4) = \log_2(x+24)$$

$$\log(2) \left(\frac{\log(x)}{\log(2)} + \frac{\log(x-4)}{\log(2)} = \frac{\log(x+24)}{\log(2)} \right) \Rightarrow \log(x) + \log(x-4) = \log(x+24)$$

$$\log(x(x-4)) = \log(x+24)$$

$$\Rightarrow x^2 - 4x = x + 24$$

$$\Rightarrow x^2 - 5x - 24$$

$$(x-8)(x+3) \quad x = 8, -3$$

$$49. 2 \cdot \ln(x+2) = 3 \ln(4) \Rightarrow \ln((x+2)^2) = \ln(4^3) \Rightarrow x^2 + 4x + 4 = 64$$

$$\Rightarrow x^2 + 4x - 60$$

$$(x-6)(x+10) \quad x = 6, -10$$

$$51. \frac{x \cdot \log(4)}{x \log 4 + x \log 25} = \frac{6 - x \cdot \log(25)}{x \log 4 + x \log 25}$$

$$x \log 4 + x \log 25 = 6$$

$$x(\log 4 + \log 25) = 6$$

$$x = \frac{6}{\log 4 + \log 25} = 1.303$$

89. False, because $\log_3(81) = \log_3 9 + \log_3(9)$ it does not apply to multiplication

91. False: because $\ln(3^2)$ is $2\ln(3)$ while $(\ln(3))^2$ would be $\ln(3) \cdot \ln(3)$

93. True

$$4 \cdot \log_2 8 = 12 \Rightarrow 4 \cdot 3 = 12$$

95. False

$$\log(1006) = 3.002 \text{ while } 3 + \log(6) = 3.77$$

$$97. \frac{\log_2 8}{\log_2 16} \neq (\log_2(8) - \log_2(16)) \Rightarrow \log_2(8/16) \text{ not } \frac{\log_2 8}{\log_2 16}$$

83. $3^x = 10 \Rightarrow x \ln(3) = \ln(10) \Rightarrow x = \frac{\ln(10)}{\ln(3)} \approx 2.0959$

84. $4^{2x} = 12 \Rightarrow 2x \ln(4) = \ln(12) \Rightarrow 2x = \frac{\ln(12)}{\ln(4)} \Rightarrow \frac{\ln(12)}{2\ln(4)} = x \approx .8962$

85. $\log_3(x) = 1.876 \Rightarrow 3^{1.876} = x \approx 7.8538$

86. $\log_5(x+2) = 2.7 \Rightarrow 5^{2.7} - 2 = x \approx 75.1292$

$$87. 5^x = 8^{x+1} \Rightarrow x \ln(5) = (x+1) \ln(8) \Rightarrow \frac{\ln(5)}{\ln(8)} = \frac{x+1}{x} \Rightarrow \frac{\ln(5)}{\ln(8)} = 1 + 1/x$$

$$\Rightarrow (0.7739 - 1) = (x^{-1})^{-1} \Rightarrow x = -4.4243$$

$$88. 3^x = e^{x+1} \Rightarrow x \ln 3 = (x+1) \Rightarrow x \ln 3 - x = 1$$

$$x(\ln 3 - 1) = 1$$

$$x = \frac{1}{\ln 3 - 1} = 10.14$$

109

$$A = \# \text{ of grams} \quad A = 25e^{-0.00032t}$$

t = time (# of yrs from present)

a. How many grams are present initially? 25

b. How many grams are present after 1000 yrs? $A = 25e^{-0.00032(1000)} = 18.1537$

c. What is the half-life of this substance?

$$12.5 = 25e^{-0.00032t} \Rightarrow 1/2 = e^{-0.00032t} \Rightarrow \ln(1/2) = -0.00032t$$

$$\Rightarrow t = \frac{\ln(1/2)}{-0.00032} \approx 2166.0849 \text{ years}$$

111.

t = hours

$$f(t) = 40,000(1 - e^{-0.0001t})$$

$f(t)$ = # of words learned

a. How many hours would it take to learn 10,000 words?

$$10,000 = 40,000(1 - e^{-0.0001t}) \Rightarrow 1/4 = 1 - e^{-0.0001t} \Rightarrow 3/4 = e^{-0.0001t}$$

$$\Rightarrow \ln(3/4) = -0.0001t \Rightarrow \frac{\ln(3/4)}{-0.0001} = t \approx 2876.8207 \text{ hours}$$

112.

i = thousands

$$P = 31.5(0.935)^i$$

P = % of pediatric TB cases

$$a. P = 31.5(0.935)^8 \Rightarrow P \approx 18.399$$

$$b. 2 = 31.5(0.935)^i \Rightarrow 2/31.5 = (0.935)^i \Rightarrow \log(.06349) = i \log(.935)$$

$$i = \frac{\log(.06349)}{\log(.935)} \approx 41.019 \text{ thousands}$$

$$12) 1. (x-3)^2 = 4 \rightarrow (x-3) = 2 \text{ or } (x-3) = -2$$

$$\boxed{x=5} \quad \boxed{x=1}$$

$$2. \log((x-3)^2) = \log 4$$

$$x^2 - 6x + 9 = 4 \Rightarrow x^2 - 6x + 5 = 0$$

$$(x-5)(x-1) \Rightarrow \boxed{x=1, 5}$$

$$3. \log_2(x-3) = 4 \Rightarrow \frac{\log(x-3)}{\log(2)} = 4 \Rightarrow \log(x-3) = 4 \cdot \log(2)$$

$$\log(x-3) = \log(2^4) \Rightarrow x-3 = 16 \Rightarrow \boxed{x=19}$$

$$4. 2^{x-3} = 4 \Rightarrow (x-3)\ln(2) = \ln(4) \Rightarrow (x-3) = \frac{\ln(4)}{\ln(2)} \Rightarrow x = \frac{\ln(4)}{\ln(2)} + 3$$

$$\boxed{x=5}$$

$$5. \sqrt{x-3} = 4 \Rightarrow x-3 = 16 \Rightarrow \boxed{x=19}$$

$$6. |x-3| = 4$$

$$(-x+3) = -4 \text{ and } (x-3) = 4$$

$$\boxed{x=-1} \quad \boxed{x=7}$$

$$7. x^2 - 4x = -2$$

$$x^2 - 4x + 2 = 0$$

$$\frac{4 \pm \sqrt{16 - 4(1)(2)}}{2} = \frac{4 \pm \sqrt{8}}{2} = \frac{4 \pm 2\sqrt{2}}{2} = 2 \pm \sqrt{2}$$

$$\boxed{2+\sqrt{2} = 3.414} \quad \boxed{2-\sqrt{2} = .585}$$

$$8. 2^{x-3} = 4^x \Rightarrow (x-3)\ln(2) = x\ln(4) \Rightarrow x\ln 2 - 3\ln 2 = x\ln 4$$

$$x\ln 2 - x\ln 4 = 3\ln 2$$

$$x(\ln 2 - \ln 4) = 3\ln 2$$

$$x = \frac{3\ln 2}{\ln 2 - \ln 4} = -3$$

$$9. \sqrt{x-5} = 5 \Rightarrow x-5 = 25 \Rightarrow \boxed{x=30}$$

$$10. 2^x = 3 \Rightarrow x\ln(2) = \ln(3) \Rightarrow x = \frac{\ln(3)}{\ln(2)} \approx 1.5849$$

$$11. \log(x-3) + \log(4) = \log(x) \Rightarrow \log(4(x-3)) = \log(x) = 4x - 12 = x$$

$$-3x = -12 \Rightarrow \boxed{x=4}$$

$$12. x^3 - 4x^2 + x + 6 = 0$$

$$\frac{6}{1} = \pm 1, \pm 2, \pm 3, \pm 6$$

$$-1 \mid \begin{array}{cccc} 1 & -4 & 1 & 6 \\ & -1 & 5 & -6 \\ \hline 1 & -5 & 6 & 0 \end{array}$$

$$x^2 - 5x + 6 = 0$$

$$(x-3)(x-2)$$

$$\boxed{x=-1, 3, 2}$$

